

# Learning Topic Hierarchies for Wikipedia Categories

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## Abstract

Existing studies have utilized Wikipedia for various knowledge acquisition tasks. However, no attempts have been made to explore multi-level topic knowledge contained in Wikipedia articles' *Contents* tables. The articles with similar subjects are grouped together into Wikipedia *categories*. In this work, we propose novel methods to automatically construct *comprehensive* topic hierarchies for given categories based on the structured *Contents* tables as well as corresponding unstructured *text* descriptions. Such a hierarchy is important for information browsing, document organization and topic prediction. Experimental results show our proposed approach, incorporating both the structural and textual information, achieves high quality category topic hierarchies.

## 1 Introduction

As a free-access online encyclopedia, written collaboratively by people all over the world, Wikipedia (abbr. to Wiki) offers a surplus of rich information. Millions of articles cover various concepts and instances<sup>1</sup>. Wiki has been widely used for various knowledge discovery tasks. Some good examples include knowledge mining from Wiki infoboxes (Lin et al., 2011; Wang et al., 2013), and *taxonomy deriving* from Wiki category system (Zesch and Gurevych, 2007).

We observe that, in addition to Wiki's infoboxes and category system, Wiki articles' Contents tables (CT for short) also provide valuable structured topic knowledge with different levels of granularity. For example, in the article "2010 Haiti Earthquake", shown in Fig.1, the left Contents zone is a CT formed in a topic hierarchy for-

The image shows a screenshot of the Wikipedia article "2010 Haiti earthquake". On the left is the "Contents" table, which is a hierarchical list of sections. On the right are the corresponding text descriptions for several of these sections, each with a red box and a label indicating the topic tag. The "Contents" table includes sections like "Background", "Geology", "Damage to infrastructure", "Conditions in the aftermath", "Casualties", "Early response", "Rescue and relief efforts", "Recovery", "Status of the recovery", "See also", and "References". The text descriptions on the right include "Background" (describing the island of Hispaniola), "Geology" (describing the earthquake's magnitude and location), "Aftershocks" (listing recorded aftershocks), and "Tsunami" (reporting a tsunami warning).

Contents (hide)	Text description
1 Background	<b>Background</b> Tag: The island of Hispaniola, shared by Haiti and the Dominican Republic, is seismically active and has a history of destructive earthquakes. During Haiti's
2 Geology	<b>Geology</b> Tag: The magnitude 7.0 Mw earthquake occurred inland, on 12 January 2010 at 16:53 (UTC-05:00), approximately 25 km (16 mi) WSW from Port-au-Prince at a depth of 13 km (8.1 mi) [7] on blind thrust faults associated with the Enriquillo-Plantain
3 Damage to infrastructure	<b>Aftershocks</b> Tag: The United States Geological Survey (USGS) recorded eight aftershocks in the two hours after the main earthquake, with magnitudes between 4.3 and 5.9. [9] Within
4 Conditions in the aftermath	<b>Tsunami</b> Tag: The Pacific Tsunami Warning Center issued a tsunami warning immediately after the initial quake, [45] but quickly cancelled it. [46] Nearly two weeks later it
5 Casualties	
6 Early response	
7 Rescue and relief efforts	
8 Recovery	
9 See also	
10 References	

Figure 1: The Wiki article "2010 Haiti Earthquake" with structured *Contents* table and corresponding unstructured *text* descriptions.

mat. If we view "2010 Haiti earthquake" as the root topic, the first-level "Geology" and "Damage to infrastructure" tags can be viewed as its subtopics, and the second-level "Tsunami" and "Aftershocks" tags underneath "Geology" are the subtopics of "Geology". Clicking any of the tags in Contents, we can jump to the corresponding text description. Wiki articles contain a wealth of this kind of structured and unstructured information. However, to our best knowledge, little work has been done to leverage the knowledge in CT.

In Wiki, similar articles (each with their own CT) belonging to the same subject are grouped together into a *Wiki category*. We aim to integrate multiple topic hierarchies represented by C-T (from the articles under the same *Wiki category*) into a *comprehensive category topic hierarchy* (CTH). While there also exist manually built CTH represented by CT in corresponding Wiki articles, they are still too high-level and incomplete. Take the "Earthquake" category as an example, its corresponding Wiki article<sup>2</sup> only contains

<sup>1</sup><http://en.wikipedia.org/wiki/Encyclopedia>

<sup>2</sup><http://en.wikipedia.org/wiki/Earthquake>

some major and common topics. It does not include the subtopic “*nuclear power plant*”, which is an important subtopic of the “*2011 Japan earthquake*”. A comprehensive CTH is believed to be more useful for information browsing, document organization and topic extraction in new text corpus (Veeramachaneni et al., 2005). Thus, we propose to investigate the Wiki articles of the same category to *automatically* build a comprehensive CTH to enhance the manually built CTH.

Clearly, it is very challenging to learn a CTH from multiple topic hierarchies in different articles due to the following 3 reasons: 1) A topic can be denoted by a variety of tags in different articles (e.g., “*foreign aids*” and “*aids from other countries*”); 2) Structural/hierarchical information can be inconsistent (or even opposite) across different articles (e.g., “*response subtopicOf aftermath*” and “*aftermath subtopicOf response*” in different earthquake event articles); 3) Intuitively, text descriptions of the topics in Wiki articles are supposed to be able to help determine *subtopic* relations between topics. However, how can we model the textual correlation?

In this study, we propose a novel approach to build a high-quality CTH for any given Wiki category. We use a Bayesian network to model a CTH, and map the CTH learning problem as a structure learning problem. We leverage both structural and textual information of topics in the articles to induce the optimal tree structure. Experiments on 3 category data demonstrate the effectiveness of our approach for CTH learning.

## 2 Preliminaries

Our problem is to learn a CTH for a Wiki category from multiple topic hierarchies represented by CT in the Wiki articles of the category. For example, consider the category “*earthquake*”. There are a lot of Wikipedia articles about earthquake events which are manually created by human experts. In these articles, the CTs imply hierarchical topic knowledge in the events. However, due to crowdsourcing nature, these knowledge is heterogeneous across different articles. We want to integrate these knowledge represented by CTs in different earthquake event articles to form a comprehensive understanding of the category “*earthquake*” (CTH).

Specifically, our input consists of a set of Wiki articles  $A_c = \{a\}$ , belonging to a Wiki category

$c$ . As shown in Fig.1, each article  $a \in A_c$  contains a CT (topic tree hierarchy)  $H_a = \{T_a, R_a\}$ , where  $T_a$  is a set of topics, each denoted by a tag  $g$  and associated with a text description  $d_g$ , and  $R_a = \{(g_i, g_j)\}, g_i, g_j \in T_a$  is a set of subtopic relations ( $g_j$  is a subtopic of  $g_i$ ). The output is an integrated comprehensive CTH  $H_c = \{T_c, R_c\}$  where  $T_c = \{t\}$  is a set of topics, each denoted by a *set of tags*  $t = \{g\}$  and associated by a text description  $d_t$  aggregated by  $\{d_g\}_{g \in t}$ , and  $R_c = \{(t_i, t_j)\}, t_i, t_j \in T_c$  is a set of subtopic relations ( $t_j$  is a subtopic of  $t_i$ ).

We map the problem of learning the output  $H_c$  from the input  $\{H_a\}, a \in A_c$ , as a structure learning problem. We first find clusters of similar tags  $T_c$  (each cluster represents a topic) and then derive hierarchical relations  $R_c$  among these clusters.

Particularly, given a category  $c$ , we first collect relevant Wiki articles  $A_c = \{a\}$ . This can be done automatically since each Wiki article has links to its categories. We can also manually find the Wikipage which summarizes the links of  $A_c$  (e.g., [http://en.wikipedia.org/wiki/Lists\\_of\\_earthquakes](http://en.wikipedia.org/wiki/Lists_of_earthquakes)) and then collect  $A_c$  according to the links.

Then we can get a global tag set  $G = \{g\}$  containing all the tags including titles in the articles  $A_c$ . We cluster the same or similar tags from different articles using single-pass incremental clustering (Hammouda and Kamel, 2003) to construct the topic set  $T_c$ , with cosine similarity computed based on the names of tags  $g$  and their text descriptions  $d_g$ . Note that titles of all the articles belonging to the same cluster corresponds to a root topic.

Next, the issue is how to induce a CTH  $H_c = \{T_c, R_c\}$  from a set of topics  $T_c$ .

## 3 Topic Hierarchy Construction

We first present a basic method to learn  $H_c$  and then describe a principled probabilistic model incorporating both structural and textual information for CTH learning.

### 3.1 Basic Method

After replacing the tags in a CT (see Fig.1) with the topics they belong to, we can then get a topic hierarchy  $H_a = \{T_a, R_a\}$  for each article  $a$ . For each subtopic relation  $(t_i, t_j) \in R_a$ , we can calculate a count/weight  $n(t_i, t_j)$ , representing the number of articles in  $A_c$  containing the

relation. We then construct a directed complete graph with a weight  $w(t_i, t_j) = n(t_i, t_j)$  on each edge  $(t_i, t_j)$ . Finally, we apply the widely used Chu-Liu/Edmonds algorithm (Chu and Liu, 1965; Edmonds, 1967) to find an optimal tree with the largest sum of weights from our constructed graph, meaning that the overall subtopic relations in the tree is best supported by all the CT/articles. The Chu-Liu/Edmonds algorithm works as follows. First, it selects, for each node, the maximum-weight incoming edge. Next, it recursively breaks cycles with the following idea: nodes in a cycle are collapsed into a pseudo-node and the maximum-weight edge entering the pseudo-node is selected to replace the other incoming edge in the cycle. During backtracking, pseudo-nodes are expanded into an acyclic directed graph, i.e., our final category topic hierarchy  $H_c$ .

However, the basic method has a problem. Consider if  $n(\text{“earthquake”}, \text{“damages to hospitals”})=10$  and  $n(\text{“earthquake”}) =100$ , while  $n(\text{“damages”}, \text{“damages to hospitals”})=5$  and  $n(\text{“damages”})=5$ . We would prefer “damages” to be the parent topic of “damages to hospitals” with a higher *confidence* level ( $5/5=1$  vs  $10/100=0.1$ ). However, the above basic method will choose “earthquake” which maximizes the weight sum. An intuitive solution is to normalize the weights. In Subsection 3.2, we present our proposed principled probabilistic model which can derive normalized structure based weights. In addition, it can be easily used to incorporate and combine textual information of topics into CTH learning.

### 3.2 Probabilistic Model for CTH Learning

We first describe the principled probabilistic model for a CTH. Then we present how to encode structural dependency and textual correlation between topics. Last, we present our final approach combining both structural dependency and textual correlation for CTH construction.

#### 3.2.1 Modeling a Category Topic Hierarchy

In a topic hierarchy, each node represents a topic. We consider each node as a variable and the topic hierarchy as a Bayesian network. Then the joint probability distribution of nodes  $N$  given a particular tree  $H$  is

$$P(N|H) = P(\text{root}) \prod_{n \in N \setminus \text{root}} P(n|\text{par}_H(n)),$$

where  $P(n|\text{par}_H(n))$  is the conditional probability of node  $n$  given its parent node  $\text{par}_H(n)$  in  $H$ . Given the nodes, this is actually the likelihood of  $H$ . Maximizing the likelihood with respect to the tree structure gives the optimal tree:

$$\begin{aligned} H^* &= \operatorname{argmax}_H P(N|H) \\ &= \operatorname{argmax}_H P(\text{root}) \prod_{n \in N \setminus \text{root}} P(n|\text{par}_H(n)) \\ &= \operatorname{argmax}_H \sum_{n \in N} \log P(n|\text{par}_H(n)) \end{aligned} \quad (1)$$

**Encoding Structural Dependency.** Considering  $t_j$  is a subtopic of  $t_i$ , we define the structural conditional probability:

$$P_{\text{struc}}(t_j|t_i) = \frac{n(t_i, t_j) + \alpha}{n(t_i) + \alpha \cdot |T_c - 1|}, \quad (2)$$

where  $n(t_i, t_j)$  is the count of articles containing relation  $(t_i, t_j)$  and  $n(t_i)$  is the count of articles containing topic  $t_i$ . The parameter  $\alpha = 1.0$  is the Laplace smoothing factor, and  $|T_c - 1|$  is the total number of possible relations taking  $t_i$  as their parent topic.

**Encoding Textual Correlation.** Considering a topic text description  $d_t$  as a bag of words, we use the normalized word frequencies  $\phi_t = \{\phi_{t,w}\}_{w \in V}$  s.t.  $\sum_{w \in V} \phi_{t,w} = 1$  to represent a topic  $t$ . To capture the subtopic relationship  $(t_i, t_j)$ , we prefer a model where the expectation of the distribution for the child is exactly same with the distribution for its parent, i.e.,  $E(\phi_{t_j}) = \phi_{t_i}$ . This naturally leads to the hierarchical Dirichlet model (Wang et al., 2014; Veeramachaneni et al., 2005), formally,  $\phi_{t_j}|\phi_{t_i} \sim \text{Dir}(\beta\phi_{t_i})$  in which  $\beta$ <sup>3</sup> is the concentration parameter which determines how concentrated the probability density is likely to be. Thus we have:

$$P_{\text{text}}(t_j|t_i) = \frac{1}{Z} \prod_{w \in V} \phi_{t_j,w}^{\beta\phi_{t_i,w} - 1}, \quad (3)$$

where  $Z = \frac{\prod_{w \in V} \Gamma(\alpha\phi_{t_i,w})}{\Gamma(\sum_{w \in V} \alpha\phi_{t_i,w})}$  is a normalization factor and  $\Gamma(\cdot)$  is the standard Gamma distribution. We note that for the root node we have the uniform prior instead of the prior coming from the parent.

#### 3.2.2 Combining Structural and Textual Information

Substituting Eq.2 into Eq.1, we can solve the optimal tree structure by applying Chu-

<sup>3</sup>Experimental results are insensitive to  $\beta$ , we set  $\beta=5$

Liu/Edmonds algorithm to the directed complete graph with structure based weights  $w_{struc} = \log(P_{struc}(t_j|t_i)) = \log \frac{n(t_i, t_j) + \alpha}{n(t_i) + \alpha \cdot |T_c - 1|}$  on the edges  $(t_i, t_j)$ . While this solves the problem of the basic method, it only considers structural dependency and does not consider textual correlation which is supposed to be useful.

Therefore, we calculate text based weights  $w_{text} = \log(P_{text}(t_j|t_i)) = \sum_{w \in V} \log \phi_{t_j, v}^{\alpha \phi_{t_i, w} - 1} - \log Z$  similarly. Then we combine structural information and textual information by defining the weights  $w(t_i, t_j)$  of the edges  $(t_i, t_j)$  as a simple weighted average of  $w_{struc}(t_i, t_j)$  and  $w_{text}(t_i, t_j)$ . Specifically, we define:

$$w(t_i, t_j) = \lambda w_{text}(t_i, t_j) + (1 - \lambda) w_{struc}(t_i, t_j),$$

where  $\lambda$  controls the impacts of text correlation and structure dependency in optimal structure learning. Note that  $w_{text}$  and  $w_{struc}$  should be scaled<sup>4</sup> first before applying Chu-Liu/Edmonds algorithm to find an optimal topic hierarchy.

## 4 Experiments

We evaluate the CTH automatically generated by our proposed methods via comparing it with a manually constructed ground-truth CTH.

### 4.1 Data and Evaluation Metric

**Data.** We evaluate our methods on 3 categories, i.e., English “earthquake” and “election” categories containing 293 and 60 articles, and Chinese “earthquake” category containing 48 articles<sup>5</sup>. After removing noisy tags such as “references” and “see also”, they contain 463, 79 and 426 unique tags respectively. After tag clustering<sup>6</sup>, we can get 176, 57 and 112 topics for each category.

**Evaluation Metric.** We employ the *precision* measure to evaluate the performance of our methods. Let  $\mathbf{R}$  and  $\mathbf{R}_s$  be subtopic relation sets of our generated result and ground-truth result respectively, then  $precision = |\mathbf{R} \cap \mathbf{R}_s| / |\mathbf{R}|$ . Due to the number of relations  $|\mathbf{R}| = |\mathbf{R}_s| = |T_c - 1|$ , we have  $precision = recall = F1 = |\mathbf{R} \cap \mathbf{R}_s| / |\mathbf{R}|$ .

We compare three methods, including our basic method (Basic) which uses only non-normalized structural information, our proposed probabilistic method considering only structural information

( $\lambda = 0$ ) (Pro+S), and considering both structural and textual information ( $0 < \lambda < 1$ ) (Pro+ST).

## 4.2 Results and Analysis

**Quantitative Analysis.** From Table 1, we observe that our approach Pro+ST (with best  $\lambda$  values as shown in Fig.2) significantly outperforms Basic and Pro+S which only utilize the structural information (+24.3% and +5.1% on average,  $p < 0.025$  with *t-test*). Pro+S which normalizes structural information also achieves significant higher precision than Basic (+19.2% on average,  $p < 0.025$ ).

	Earth.(En)	Elect.(En)	Earth.(Ch)
Basic	0.5965	0.7719	0.7143
Pro+S	0.8971	0.8596	0.9017
Pro+ST	0.9543	0.9298	0.9286

Table 1: Precision of different methods on 3 categories

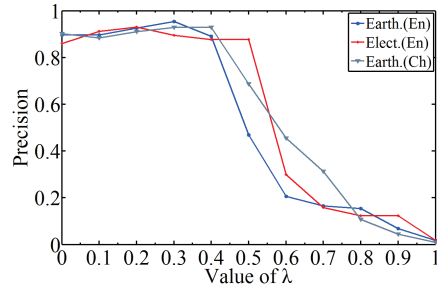


Figure 2: The precision of CTH with different  $\lambda$  values

To examine the influence of  $\lambda$ , we show the performance of our approach Pro+ST with different  $\lambda$  values on 3 categories in Fig.2. All the curves grow up first and then decrease dramatically as we emphasize more on textual information. They can always get consistent better results when  $0.2 \leq \lambda \leq 0.3$ . When  $\lambda$  approaches 1, the precision declines fast to near 0. The reason is that the topics with short (or null) text descriptions are likely to be a parent node of all other nodes and influence the results dramatically, but if we rely mostly on structural information and use the textual information as auxiliary for correcting minor errors in some ambiguous cases, we can improve the precision of the resultant topic hierarchy.

**Qualitative Analysis.** Due to space limitation, we only show the topic hierarchy for “Election” with smaller topic size in Fig.3. As we can see,

<sup>4</sup>We use min-max normalization  $x^* = \frac{x - \min}{\max - \min}$

<sup>5</sup>We filter articles with little information in Contents.

<sup>6</sup>We use an incremental clustering algorithm



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