

## A Computing supervision through tree hashing

In every decoding step  $t$ , we wish to compute for every tree  $z_{\text{new}}$  in the frontier  $F_{t+1}$  if  $z_{\text{new}} \in \mathcal{Z}_t^{\text{gold}}$ . This is achieved using tree hashing. First, during preprocessing, for every height  $t$ , we compute the gold hashes  $h_t^{\text{gold}}$ , the hash values of every sub-tree of  $z^{\text{gold}}$  of height  $t$ , in a recursive fashion using a Merkle tree hash (Merkle, 1987). Specifically, we define:

$$\text{hash}(z) = g(\text{label}(z), \text{hash}(z_l), \text{hash}(z_r))$$

Where  $g$  is a simple hash function,  $z_l, z_r$  are the left and right children of  $z$ , and  $\text{label}(\cdot)$  gives the node type (such as  $\sigma$  and  $\Pi$ ).

During training, in each decoding step  $t$ , since the hash function is defined recursively, we can compute the frontier hashes using the hash values of the current beam. Then, for every frontier hash we can perform a lookup to check if  $\text{hash}(z) \in h_t^{\text{gold}}$ . Both the hash computation and lookup are done in parallel for all frontier trees using the GPU.

## B Examples for Relational Algebra Trees

We show multiple examples of relation algebra trees along with the corresponding SQL query, for better understanding of the mapping between the two.

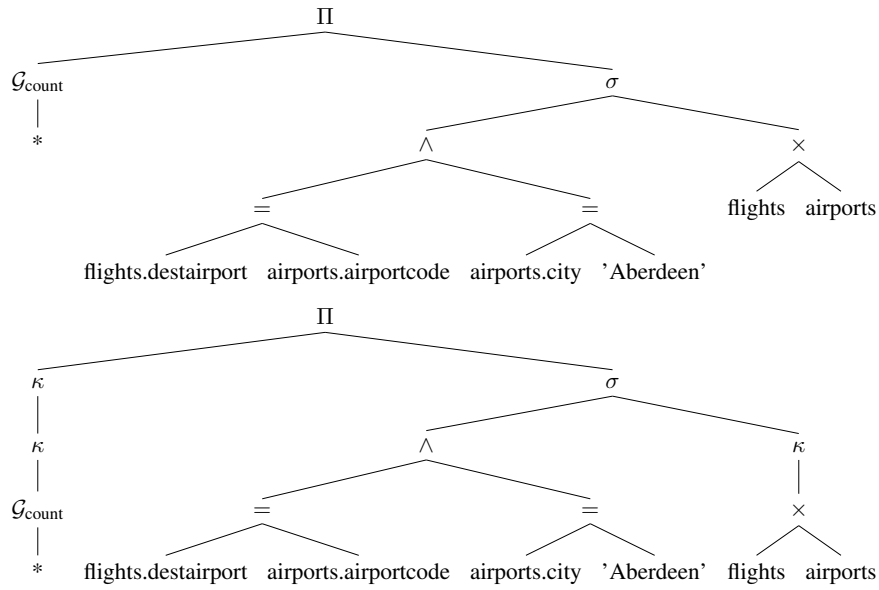


Figure 8: Unbalanced and balanced relational algebra trees for the utterance “How many flights arriving in Aberdeen city?”, where the corresponding SQL query is `SELECT COUNT(*) FROM flights JOIN airports ON flights.destairport = airports.airportcode WHERE airports.city = 'Aberdeen'`.

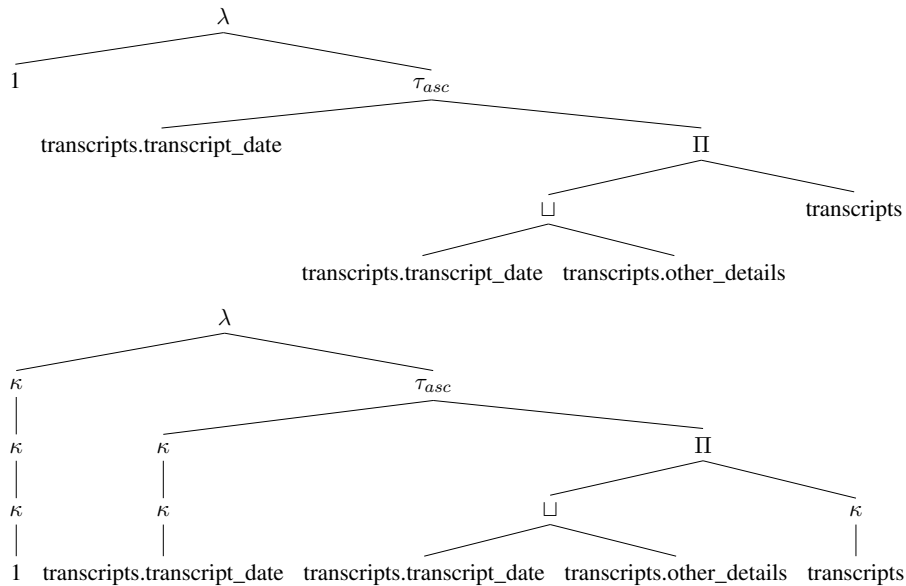


Figure 9: Unbalanced and balanced relational algebra trees for the utterance “When is the first transcript released? List the date and details.”, where the corresponding SQL query is `SELECT transcripts.transcript_date, transcripts.other_details FROM transcripts ORDER BY transcripts.transcript_date ASC LIMIT 1`.

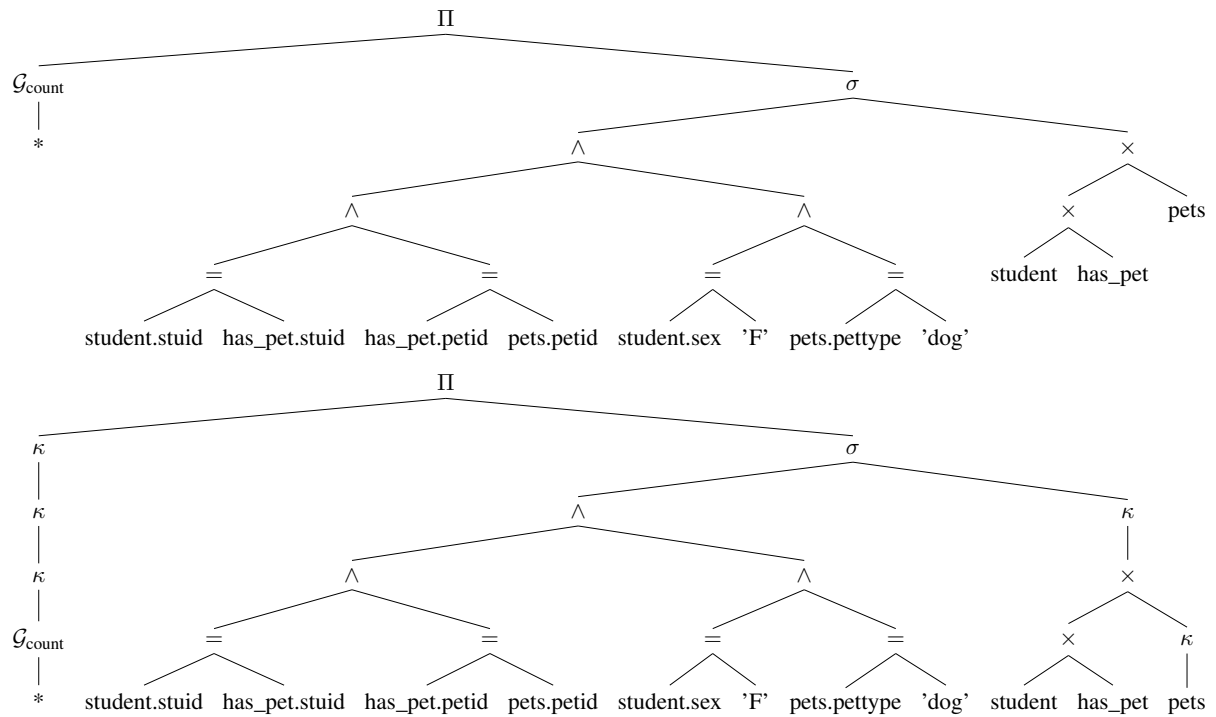


Figure 10: Unbalanced and balanced relational algebra trees for the utterance “How many dog pets are raised by female students?”, where the corresponding SQL query is `SELECT COUNT(*) FROM student JOIN has_pet ON student.stuid = has_pet.stuid JOIN pets ON has_pet.petid = pets.petid WHERE student.sex = 'F' AND pets.pettype = 'dog'.`

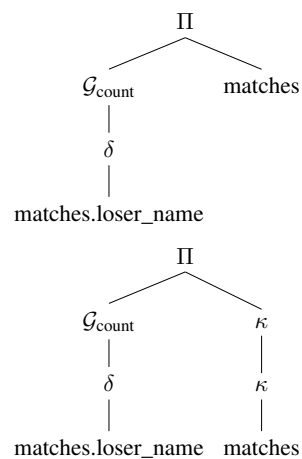


Figure 11: Unbalanced and balanced relational algebra trees for the utterance “Find the number of distinct name of losers.”, where the corresponding SQL query is `SELECT COUNT(DISTINCT matches.loser_name) FROM matches.`