

k-best Spanning Tree Parsing

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Abstract

This paper introduces a Maximum Entropy dependency parser based on an efficient k -best Maximum Spanning Tree (MST) algorithm. Although recent work suggests that the edge-factored constraints of the MST algorithm significantly inhibit parsing accuracy, we show that generating the 50-best parses according to an edge-factored model has an oracle performance well above the 1-best performance of the best dependency parsers. This motivates our parsing approach, which is based on reranking the k -best parses generated by an edge-factored model. Oracle parse accuracy results are presented for the edge-factored model and 1-best results for the reranker on eight languages (seven from CoNLL-X and English).

1 Introduction

The Maximum Spanning Tree algorithm¹ was recently introduced as a viable solution for non-projective dependency parsing (McDonald et al., 2005b). The dependency parsing problem is naturally a spanning tree problem; however, efficient spanning-tree optimization algorithms assume a cost function which assigns scores independently to edges of the graph. In dependency parsing, this effectively constrains the set of models to those which independently generate parent-child pairs;

¹In this paper we deal only with MSTs on directed graphs. These are often referred to in the graph-theory literature as Maximum Spanning Arborescences.

these are known as edge-factored models. These models are limited to relatively simple features which exclude *linguistic* constructs such as verb sub-categorization/valency, lexical selectional preferences, etc.²

In order to explore a rich set of syntactic features in the MST framework, we can either approximate the optimal non-projective solution as in McDonald and Pereira (2006), or we can use the constrained MST model to select a subset of the set of dependency parses to which we then apply less-constrained models. An efficient algorithm for generating the k -best parse trees for a constituency-based parser was presented in Huang and Chiang (2005); a variation of that algorithm was used for generating projective dependency trees for parsing in Dreyer et al. (2006) and for training in McDonald et al. (2005a). However, prior to this paper, an efficient non-projective k -best MST dependency parser has not been proposed.³

In this paper we show that the naïve edge-factored models are effective at selecting sets of parses on which the oracle parse accuracy is high. The oracle parse accuracy for a set of parse trees is the highest accuracy for any individual tree in the set. We show that the 1-best accuracy and oracle accuracy can differ by as much as an absolute 9% when the oracle is computed over a small set generated by edge-factored models ($k = 50$).

²Labeled edge-factored models can capture selectional preference; however, the unlabeled models presented here are limited to modeling head-child relationships without predicting the *type* of relationship.

³The work of McDonald et al. (2005b) would also benefit from a k -best non-projective parser for training.

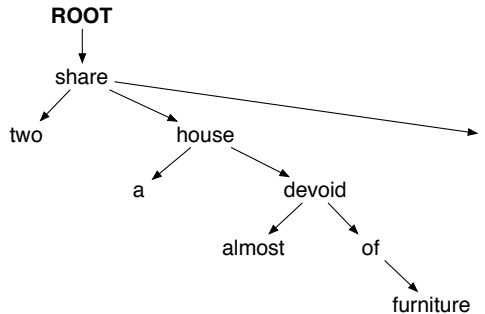


Figure 1: A dependency graph for an English sentence in our development set (Penn WSJ section 24): *Two share a house almost devoid of furniture.*

The combination of two discriminatively trained models, a k -best MST parser and a parse tree reranker, results in an efficient parser that includes complex tree-based features. In the remainder of the paper, we first describe the core of our parser, the k -best MST algorithm. We then introduce the features that we use to compute edge-factored scores as well as tree-based scores. Following, we outline the technical details of our training procedure and finally we present empirical results for the parser on seven languages from the CoNLL-X shared-task and a dependency version of the WSJ Penn Treebank.

2 MST in Dependency Parsing

Work on statistical dependency parsing has utilized either dynamic-programming (DP) algorithms or variants of the Edmonds/Chu-Liu MST algorithm (see Tarjan (1977)). The DP algorithms are generally variants of the CKY bottom-up chart parsing algorithm such as that proposed by Eisner (1996). The Eisner algorithm efficiently ($O(n^3)$) generates projective dependency trees by assembling structures over contiguous words in a clever way to minimize book-keeping. Other DP solutions use constituency-based parsers to produce phrase-structure trees, from which dependency structures are extracted (Collins et al., 1999). A shortcoming of the DP-based approaches is that they are unable to generate non-projective structures. However, non-projectivity is necessary to capture syntactic phenomena in many languages.

McDonald et al. (2005b) introduced a model for dependency parsing based on the Edmonds/Chu-Liu algorithm. The work we present here extends their work by exploring a k -best version of the MST algo-

algorithm. In particular, we consider an algorithm proposed by Camerini et al. (1980) which has a worst-case complexity of $O(km \log(n))$, where k is the number of parses we want, n is the number of words in the input sentence, and m is the number of edges in the hypothesis graph. This can be reduced to $O(kn^2)$ in dense graphs⁴ by choosing appropriate data structures (Tarjan, 1977). Under the models considered here, all pairs of words are considered as candidate parents (children) of another, resulting in a fully connected graph, thus $m = n^2$.

In order to incorporate second-order features (specifically, sibling features), McDonald et al. proposed a dependency parser based on the Eisner algorithm (McDonald and Pereira, 2006). The second-order features allow for more complex phrasal relationships than the edge-factored features which only include parent/child features. Their algorithm finds the best solution according to the Eisner algorithm and then searches for the single valid edge change that increases the tree score. The algorithm iterates until no better single edge substitution can improve the score of the tree. This greedy approximation allows for second-order constraints and non-projectivity. They found that applying this method to trees generated by the Eisner algorithm using second-order features performs better than applying it to the best tree produced by the MST algorithm with first-order (edge-factored) features.

In this paper we provide a new evaluation of the efficacy of edge-factored models, k -best oracle results. We show that even when k is small, the edge-factored models select k -best sets which contain good parses. Furthermore, these good parses are even better than the parses selected by the best dependency parsers.

2.1 k -best MST Algorithm

The k -best MST algorithm we introduce in this paper is the algorithm described in Camerini et al. (1980). For proofs of complexity and correctness, we defer to the original paper. This section is intended to provide the intuitions behind the algorithm and allow for an understanding of the key data-structures necessary to ensure the theoretical guarantees.

⁴A dense graph is one in which the number of edges is close to the number of edges in a fully connected graph (i.e., n^2).

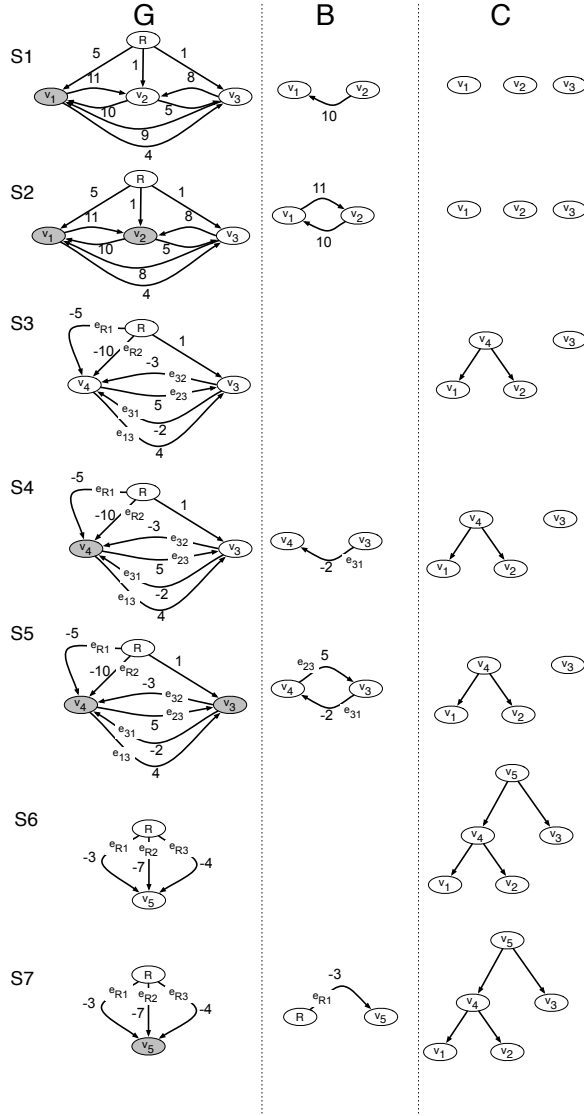


Figure 2: Simulated 1-best MST algorithm.

Let $G = \{V, E\}$ be a directed graph where $V = \{R, v_1, \dots, v_n\}$ and $E = \{e_{11}, e_{12}, \dots, e_{1n}, e_{21}, \dots, e_{nn}\}$. We refer to edge e_{ij} as the edge that is directed from v_i into v_j in the graph. The initial dependency graph in Figure 2 (column **G**) contains three regular nodes and a root node.

Algorithm 1 is a version of the MST algorithm as presented by Camerini et al. (1980); subtleties of the algorithm have been omitted. Arguments Y (a branching⁵) and Z (a set of edges) are constraints on the edges that can be part of the solution, A . Edges in Y are required to be in the solution and edges in

⁵A branching is a subgraph that contains no cycles and no more than one edge directed into each node.

Algorithm 1 Sketch of 1-best MST algorithm

```

procedure BEST( $G, Y, Z$ )
   $G = (G \cup Y) - Z$ 
   $B = \emptyset$ 
   $C = V$ 
5:   for unvisited vertex  $v_i \in V$  do
      mark  $v_i$  as visited
      get best in-edge  $b \in \{e_{jk} : k = i\}$  for  $v_i$ 
       $B = B \cup b$ 
       $\beta(v_i) = b$ 
10:  if  $B$  contains a cycle  $\mathcal{C}$  then
      create a new node  $v_{n+1}$ 
       $C = C \cup v_{n+1}$ 
      make all nodes of  $\mathcal{C}$  children of  $v_{n+1}$  in  $C$ 
      COLLAPSE all nodes of  $\mathcal{C}$  into  $v_{n+1}$ 
15:  ADD  $v_{n+1}$  to list of unvisited vertices
       $n = n + 1$ 
       $B = B - \mathcal{C}$ 
      end if
end for
20:  EXPAND  $C$  choosing best way to break cycles
      Return best  $A = \{b \in E \mid \exists v \in V : \beta(v) = b\}$ 
      and  $C$ 
end procedure

```

Z cannot be part of the solution. The branching C stores a hierarchical history of cycle collapses, encapsulating embedded cycles and allowing for an *expanding* procedure, which breaks cycles while maintaining an optimal solution.

Figure 2 presents a view of the algorithm when run on a three node graphs (plus a specified root node). Steps S1, S2, S4, and S5 depict the processing of lines 5 to 8, recording in β the best input edges for each vertex. Steps S3 and S6 show the process of *collapsing* a cycle into a new node (lines 10 to 16).

The main loop of the algorithm processes each vertex that has not yet been visited. We look up the best incoming edge (which is stored in a priority-queue). This value is recorded in β and the edge is added to the current *best* graph B . We then check to see if adding this new edge would create a cycle in B . If so, we create a new node and *collapse* the cycle into it. This can be seen in Step S3 in Figure 2.

The process of collapsing a cycle into a node involves removing the edges in the cycle from B , and adjusting the weights of all edges directed into any node in the cycle. The weights are adjusted so that they reflect the relative difference of choosing the new in-edge rather than the edge in the cycle. In step S3, observe that edge e_{R1} had a weight of 5, but now that it points into the new node v_4 , we subtract the weight of the edge e_{21} that also pointed into v_1 ,

which was 10. Additionally, we record in C the relationship between the new node v_4 and the original nodes v_1 and v_2 .

This process continues until we have visited all original and newly created nodes. At that point, we *expand* the cycles encoded in C . For each node not originally in G (e.g., v_5, v_4), we retrieve the edge e_r pointing into this node, recorded in β . We identify the node v_s to which e_r pointed in the original graph G and set $\beta(v_s) = e_r$.

Algorithm 2 Sketch of next-best MST algorithm

```

procedure NEXT( $G, Y, Z, A, C$ )
   $\delta \leftarrow +\infty$ 
  for unvisited vertex  $v$  do
    get best in-edge  $b$  for  $v$ 
  5:   if  $b \in A - Y$  then
      $f \leftarrow$  alternate edge into  $v$ 
     if swapping  $f$  with  $b$  results in smaller  $\delta$  then
       update  $\delta$ , let  $e \leftarrow f$ 
     end if
  10:  end if
     if  $b$  forms a cycle then
       Resolve as in 1-best
     end if
  end for
  15:  Return edge  $e$  and  $\delta$ 
end procedure

```

Algorithm 2 returns the single edge, e , of the 1-best solution A that, when removed from the graph, results in a graph for which the best solution is the next best solution after A . Additionally, it returns δ , the difference in score between A and the next best tree. The branching C is passed in from Algorithm 1 and is used here to efficiently identify alternate edges, f , for edge e .

Y and Z in Algorithms 1 and 2 are used to construct the next best solutions efficiently. We call $G_{Y,Z}$ a constrained graph; the constraints being that Y restricts the in-edges for a subset of nodes: for each vertex with an in-edge in Y , only the edge of Y can be an in-edge of the vertex. Also, edges in Z are removed from the graph. A constrained spanning tree for $G_{Y,Z}$ (a tree covering all nodes in the graph) must satisfy: $Y \subseteq A \subseteq E - Z$.

Let A be the (constrained) solution to a (constrained) graph and let e be the edge that leads to the next best solution. The third-best solution is either the second-best solution to $G_{Y,\{Z \cup e\}}$ or the second-best solution to $G_{\{Y \cup e\},Z}$. The k -best ranking algorithm uses this fact to incrementally partition the

solution space: for each solution, the next best either will include e or will not include e .

Algorithm 3 k -best MST ranking algorithm

```

procedure RANK( $G, k$ )
   $A, C \leftarrow$  best( $E, V, \emptyset, \emptyset$ )
   $(e, \delta) \leftarrow$  next( $E, V, \emptyset, \emptyset, A, C$ )
  bestList  $\leftarrow A$ 
  5:   $Q \leftarrow$  enqueue( $s(A) - \delta, e, A, C, \emptyset, \emptyset$ )
     for  $j \leftarrow 2$  to  $k$  do
        $(s, e, A, C, Y, Z) =$  dequeue( $Q$ )
        $Y' = Y \cup e$ 
        $Z' = Z \cup e$ 
  10:   $A', C' \leftarrow$  best( $E, V, Y', Z', A', C'$ )
       bestList  $\leftarrow A'$ 
        $e', \delta' \leftarrow$  next( $E, V, Y', Z', A', C'$ )
        $Q \leftarrow$  enqueue( $s(A) - \delta', e', A', C', Y', Z'$ )
        $e', \delta' \leftarrow$  next( $E, V, Y, Z', A', C'$ )
  15:   $Q \leftarrow$  enqueue( $s(A) - \delta', e', A', C', Y, Z'$ )
     end for
  Return bestList
end procedure

```

The k -best ranking procedure described in Algorithm 3 uses a priority queue, Q , keyed on the first parameter to *enqueue* to keep track of the horizon of next best solutions. The function $s(A)$ returns the score associated with the tree A . Note that in each iteration there are two new elements enqueued representing the sets $G_{Y,\{Z \cup e\}}$ and $G_{\{Y \cup e\},Z}$.

Both Algorithms 1 and 2 run in $O(m \log(n))$ time and can run in quadratic time for dense graphs with the use of an efficient priority-queue⁶ (i.e., based on a Fibonacci heap). Algorithm 3 runs in constant time, resulting in an $O(km \log n)$ algorithm (or $O(kn^2)$ for dense graphs).

3 Dependency Models

Each of the two stages of our parser is based on a discriminative training procedure. The edge-factored model is based on a conditional log-linear model trained using the Maximum Entropy constraints.

3.1 Edge-factored MST Model

One way in which dependency parsing differs from constituency parsing is that there is a fixed amount of structure in every tree. A dependency tree for a sentence of n words has exactly n edges,⁷ each repre-

⁶Each vertex keeps a priority queue of candidate parents. When a cycles is collapsed, the new vertex inherits the union of queues associated with the vertices of the cycle.

⁷We assume each tree has a *root* node.

senting a *syntactic* or *semantic* relationship, depending on the linguistic model assumed for annotation. A spanning tree (equivalently, a dependency parse) is a subgraph for which each node has one in-edge, the root node has zero in-edges, and there are no cycles.

Edge-factored features are defined over the edge and the input sentence. For each of the n^2 parent/child pairs, we extract the following features:

Node-type There are three basic node-type features: word *form*, morphologically reduced *lemma*, and part-of-speech (*POS*) tag. The CoNLL-X data format⁸ describes two part-of-speech tag types, we found that features derived from the coarse tags are more reliable. We consider both unigram (parent or child) and bigram (composite parent/child) features. We refer to parent features with the prefix p- and child feature with the prefix c-; for example: p-pos, p-form, c-pos, and c-form. In our model we use both word form and POS tag and include the composite form/POS features: p-form/c-pos and p-pos/c-form.

Branch A binary feature which indicates whether the child is to the left or right of the parent in the input string. Additionally, we provide composite features p-pos/branch and p-pos/c-pos/branch.

Distance The number of words occurring between the parent and child word. These distances are bucketed into 7 buckets (1 through 6 plus an additional single bucket for distances greater than 6). Additionally, this feature is combined with node-type features: p-pos/dist, c-pos/dist, p-pos/c-pos/dist.

Inside POS tags of the words between the parent and child. A count of each tag that occurs is recorded, the feature is identified by the tag and the feature value is defined by the count. Additional composite features are included combining the inside and node-type: for each type t_i the composite features are: p-pos/ t_i , c-pos/ t_i , p-pos/c-pos/ t_i .

Outside Exactly the same as the **Inside** feature except that it is defined over the features to the left and right of the span covered by this parent-child pair.

Extra-Feats Attribute-value pairs from the CoNLL *FEATS* field including combinations with parent/child node-types. These features represent word-level annotations provided in the tree-bank and include morphological and lexical-semantic features. These do not exist in the English data.

Inside Edge Similar to *Inside* features, but only includes nodes immediately to left and right within the span covered by the parent/child pair. We include the following features where i^l and i^r are the inside left and right POS tags and i^p is the inside POS tag closest to the parent: i^l/i^r , p-pos/ i^p , p-pos/ i^l/i^r /c-pos,

Outside Edge An *Outside* version of the *Inside Edge* feature type.

Many of the features above were introduced in McDonald et al. (2005a); specifically, the *node-type*, *inside*, and *edge* features. The number of features can grow quite large when form or lemma features are included. In order to handle large training sets with a large number of features we introduce a bagging-based approach, described in Section 4.2.

3.2 Tree-based Reranking Model

The second stage of our dependency parser is a reranker that operates on the output of the k -best MST parser. Features in this model are not constrained as in the edge-factored model. Many of the model features have been inspired by the constituency-based features presented in Charniak and Johnson (2005). We have also included features that exploit non-projectivity where possible. The node-type is the same as defined for the MST model.

MST score The score of this parse given by the first-stage MST model.

Sibling The POS-tag of immediate siblings. Intended to capture the preference for particular immediate siblings such as modifiers.

Valency Count of the number of children for each word (indexed by POS-tag of the word). These

⁸The 2006 CoNLL-X data format can be found on-line at: <http://nextens.uvt.nl/~conll/>.

counts are bucketed into 4 buckets. For example, a feature may look like p-pos=VB/v=4, meaning the POS tag of the parent is ‘VB’ and it had 4 dependents.

Sub-categorization A string representing the sequence of child POS tags for each parent POS-tag.

Ancestor Grandparent and great grandparent POS-tag for each word. Composite features are generated with the label c-pos/p-pos/gp-pos and c-pos/p-pos/ggp-pos (where gp is the grandparent and ggp is the great grandparent).

Edge POS-tag to the left and right of the subtree, both inside and outside the subtree. For example, say a subtree with parent POS-tag p-pos spans from i to j , we include composite *outside* features: p-pos/ n_{i-1} -pos/ n_{j+1} -pos, p-pos/ n_{i-1} -pos, p-pos/ n_{j+1} -pos; and composite *inside* features: p-pos/ n_{i+1} -pos/ n_{j-1} -pos, p-pos/ n_{i+1} -pos, p-pos/ n_{j-1} -pos.

Branching Factor Average number of left/right branching nodes per POS-tag. Additionally, we include a boolean feature indicating the overall left/right preference.

Depth Depth of the tree and depth normalized by sentence length.

Heavy Number of dominated nodes per POS-tag. We also include the average number of nodes dominated by each POS-tag.

4 MaxEnt Training

We have adopted the conditional Maximum Entropy (MaxEnt) modeling paradigm as outlined in Charniak and Johnson (2005) and Riezler et al. (2002). We can partition the training examples into independent subsets, Y_s : for the edge-factored MST models, each set represents a word and its candidate parents; for the reranker, each set represents the k -best trees for a particular sentence. We wish to estimate the conditional distribution over hypotheses in the set y_i , given the set: $p(y_i|Y_s) = \frac{\exp(\sum_k \lambda_k f_{ik})}{\sum_{j: y_j \in Y_s} \exp(\sum_{k'} \lambda_{k'} f_{jk'})}$, where f_{ik} is the k^{th} feature function in the model for example y_i .

4.1 MST Training

Our MST parser training procedure involves enumerating the n^2 potential tree edges (parent/child pairs). Unlike the training procedure employed by McDonald et al. (2005b) and McDonald and Pereira (2006), we provide positive and negative examples in the training data. A node can have at most one parent, providing a natural split of the n^2 training examples. For each node n_i , we wish to estimate a distribution over n nodes⁹ as potential parents, $p(v_i, e_{j_i}|e_{-i})$, the probability of the correct parent of v_i being v_j given the set of edges associated with its candidate parents e_{-i} . We call this the parent-prediction model.

4.2 MST Bagging

The complexity of the training procedure is a function of the number of features and the number of examples. For large datasets, we use an ensemble technique inspired by *Bagging* (Breiman, 1996). Bagging is generally used to mitigate high variance in datasets by sampling, with replacement, from the training set. Given that we wish to include some of the less frequent examples and therefore are not necessarily avoiding high variance, we partition the data into disjoint sets.

For each of the sets, we train a model independently. Furthermore, we only allow the parameters to be changed for those features observed in the training set. At inference time, we apply each model to the training data and then combine the prediction probabilities.

$$\tilde{p}_\theta(y_i|Y_s) = \max_m p_{\theta_m}(y_i|Y_s) \quad (1)$$

$$\tilde{p}_\theta(y_i|Y_s) = \frac{1}{M} \sum_m p_{\theta_m}(y_i|Y_s) \quad (2)$$

$$\tilde{p}_\theta(y_i|Y_s) = \left(\prod_m p_{\theta_m}(y_i|Y_s) \right)^{1/M} \quad (3)$$

$$\tilde{p}_\theta(y_i|Y_s) = \frac{M}{\sum_m \frac{1}{p_{\theta_m}(y_i|Y_s)}} \quad (4)$$

Equations 1, 2, 3, and 4 are the maximum, average, geometric mean, and harmonic mean, respectively. We performed an exploration of these on the

⁹Recall that in addition to the $n-1$ other nodes in the graph, there is a root node for which we know has no parents.

development data and found that the geometric mean produces the best results (Equation 3); however, we observed only very small differences in the accuracy among models where only the combination function differed.

4.3 Reranker Training

The second stage of parsing is performed by our tree-based reranker. The input to the reranker is a list of k parses generated by the k -best MST parser. For each input sentence, the hypothesis set is the k parses. At inference time, predictions are made independently for each hypothesis set Y_s and therefore the normalization factor can be ignored.

5 Empirical Evaluation

The CoNLL-X shared task on dependency parsing provided data for a number of languages in a common data format. We have selected seven of these languages for which the data is available to us. Additionally, we have automatically generated a dependency version of the Penn WSJ treebank.¹⁰ As we are only interested in the structural component of a parse in this paper, we present results for unlabeled dependency parsing. A second labeling stage can be applied to get labeled dependency structures as described in (McDonald et al., 2006).

In Table 1 we report the accuracy for seven of the CoNLL languages and English.¹¹ Already, at $k = 50$, we see the oracle rate climb as much as 9.25% over the 1-best result (Dutch). Continuing to increase the size of the k -best lists adds to the oracle accuracy, but the relative improvement appears to be increasing at a logarithmic rate. The k -best parser is used both to train the k -best reranker and, at inference time, to select a set of hypotheses to rerank. It is not necessary that training is done with the same size hypothesis set as test, we explore the matched and mismatched conditions in our reranking experiments.

¹⁰The Penn WSJ treebank was converted using the conversion program described in (Johansson and Nugues, 2007) and available on the web at: <http://nlp.cs.lth.se/pennconverter/>

¹¹The **Best Reported** results is from the CoNLL-X competition. The best result reported for English is the Charniak parser (without reranking) on Section 23 of the WSJ Treebank using the same head-finding rules as for the evaluation data.

Table 2 shows the reranking results for the set of languages. For each language, we select model parameters on a development set prior to running on the test data. These parameters include a feature count threshold (the minimum number of observations of a feature before it is included in a model) and a mixture weight controlling the contribution of a quadratic regularizer (used in MaxEnt training). For Czech, German, and English, we use the MST bagging technique with 10 bags. These test results are for the models which performed best on the development set (using 50-best parses).

We see minor improvements over the 1-best baseline MST output (repeated in this table for comparison). We believe this is due to the overwhelming number of parameters in the reranking models and the relatively small amount of training data. Interestingly, increasing the number of hypotheses helps for some languages and hurts the others.

6 Conclusion

Although the edge-factored constraints of MST parsers inhibit accuracy in 1-best parsing, edge-factored models are effective at selecting high accuracy k -best sets. We have introduced the Camerini et al. (1980) k -best MST algorithm and have shown how to efficiently train MaxEnt models for dependency parsing. Additionally, we presented a unified modeling and training setting for our two-stage parser; MaxEnt training is used to estimate the parameters in both models. We have introduced a particular ensemble technique to accommodate the large training sets generated by the first-stage edge-factored modeling paradigm. Finally, we have presented a reranker which attempts to select the best tree from the k -best set. In future work we wish to explore more robust feature sets and experiment with feature selection techniques to accommodate them.

Acknowledgments

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Language	Best Reported	Oracle Accuracy				
		$k = 1$	$k = 10$	$k = 50$	$k = 100$	$k = 500$
Arabic	79.34	77.92	80.72	82.18	83.03	84.47
Czech	87.30	83.56	88.50	90.88	91.80	93.50
Danish	90.58	89.12	92.89	94.79	95.29	96.59
Dutch	83.57	81.05	87.43	90.30	91.28	93.12
English	92.36	85.04	89.04	91.12	91.87	93.42
German	90.38	87.02	91.51	93.39	94.07	95.47
Portuguese	91.36	89.86	93.11	94.85	95.39	96.47
Swedish	89.54	86.50	91.20	93.37	93.83	95.42

Table 1: k -best MST oracle results. The 1-best results represent the performance of the parser in isolation. Results are reported for the CoNLL test set and for English, on Section 23 of the Penn WSJ Treebank.

Language	Best Reported	Reranked Accuracy				
		1-best	10-best	50-best	100-best	500-best
Arabic	79.34	77.61	78.06	78.02	77.94	77.76
Czech	87.30	83.56	83.94	84.14	84.48	84.46
Danish	90.58	89.12	89.48	89.76	89.68	89.74
Dutch	83.57	81.05	82.01	82.91	82.83	83.21
English	92.36	85.04	86.54	87.22	87.38	87.81
German	90.38	87.02	88.24	88.72	88.76	88.90
Portuguese	91.36	89.38	90.00	89.98	90.02	90.02
Swedish	89.54	86.50	87.87	88.21	88.26	88.53

Table 2: Second-stage results from the k -best parser and reranker. The **Best Reported** and 1-best fields are copied from table 1. Only non-lexical features were used for the reranking models.

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