Capacity Matters: a Proof-of-Concept for Transformer Memorization on Real-World Data *

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Abstract

This paper studies how the model architecture and data configurations influence the empirical memorization capacity of generative transformers. The models are trained using synthetic text datasets derived from the Systematized Nomenclature of Medicine (SNOMED) knowledge graph: triplets, representing static connections, and sequences, simulating complex relation patterns. The results show that embedding size is the primary determinant of learning speed and capacity, while additional layers provide limited benefits and may hinder performance on simpler datasets. Activation functions play a crucial role, and Softmax demonstrates greater stability and capacity. Furthermore, increasing the complexity of the data set seems to improve the final memorization. These insights improve our understanding of transformer memory mechanisms and provide a framework for optimizing model design with structured real-world data.

1 Introduction

Transformer-based Large Language Models (LLMs) have revolutionized natural language processing, excelling at tasks ranging from text generation and translation to question answering and summarization. Despite these advances, a fundamental understanding of how these models store and recall information, particularly factual or structured knowledge, remains limited. Clarifying these mechanisms is crucial for optimizing model performance and enabling efficient, real-world deployment. One impactful example is healthcare, where transformer-based models could assist clinicians through wearable devices such as smart glasses or watches (Gupta et al., 2024; Wu et al., 2024; Balloccu et al., 2024). Due to privacy and reliability, the preferred system would be a local

on-edge, requiring minimal computation but with the capacity to memorize all relevant facts in the specific healthcare area.

Recent theoretical and empirical studies have sought to quantify the memorization capacity of transformers. Kim et al. (2023) introduced mathematical bounds for memory capacity, demonstrating that transformers could memorize O(d + n + 1) \sqrt{nN}) parameters, where d, n, N correspond to embedding dimensions, dataset size, and model size, respectively. Additionally, Kajitsuka and Sato (2024) proved, that $\tilde{O}(\sqrt{nN})$ parameters are not only sufficient, but also necessary for some types of transformers. Mahdavi et al. (2024) extended this work by analyzing the effects of multi-head attention on memorization, revealing the interplay between architectural components and the model's ability to store and recall information. The experiments in Härmä et al. (2024) used randomly generated sequences of numbers to evaluate the memorization capabilities of the transformer models on unstructured data. Most capacity studies use synthetic datasets because accurate capacity measurement becomes very difficult in the case of uncontrolled free text content.

The experiments reported in the current paper use sequential data generated from the knowledge graph, which, while controlled, has some of the hierarchical and relational complexity of realworld text content. More specifically, small-scale decoder-only transformer models (Brown et al., 2020) were trained to memorize structured sentences derived from the Systematized Nomenclature of Medicine (SNOMED) knowledge graph (KG) (El-Sappagh et al., 2018), a comprehensive medical ontology, which encodes semantic relationships between medical concepts, offering a rich dataset to explore memory mechanisms under realistic conditions. Exact memorization of selected relations would be critical, for example, in the healthcare use cases described above. Our aim is not

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to generalize to all LLMs or domains, but rather to offer a practical, reproducible framework for measuring memorization on realistic KG data. The relative task simplicity is by design: more complex or less-controlled tasks would conflate memorization with generalization, making it difficult to draw clear, interpretable conclusions about model capacity.

To measure the memorization of the transformer models, the Maximum Attainable Capacity (MAC) method was used. It evaluates the practical limit of samples a model can retain when trained on a large dataset. Our approach leverages structured datasets consisting of static triplets and longer sequences simulating graph traversal paths, capturing relationship patterns between concepts. These datasets allowed us to empirically analyze how model architecture, training configurations, dataset size, and complexity influence training dynamics and final memorization performance.

This work serves as a proof-of-concept, showing that structured data in the real world can evaluate memorization in practice. Firstly, we introduce a reproducible pipeline for converting large ontologies into tokenized datasets suitable for memorization studies. Secondly, we evaluate how transformers' architecture influences capacity, building on prior theoretical insights. Lastly, we highlight cases where models fail to memorize all samples despite sufficient capacity, motivating future studies into training dynamics and error patterns.

Our findings do not aim to establish universal scaling laws or generalization behavior but to provide a reproducible framework for studying memory-limited models under realistic constraints.

2 Methods

2.1 Data

2.1.1 Data Source and Preprocessing

To evaluate transformer memorization and retrieval capabilities, we used SNOMED KG, which encodes medical concepts and their relationships as nodes and edges of a graph. It was accessed using the owlready2 library (Lamy, 2017), filtering out non-informative or overly specific properties to ensure meaningful relationships. Unlike graph transformers that use GNNs (Shehzad et al., 2024), we focus on a universal architecture, transforming the graph into (1) triplets (concept-property relationships, see 2.1.2), and (2) sequences, simulating graph traversal paths (see 2.1.3).

2.1.2 Triplets Generation

A dataset of the form (Concept, Property, Related Concept) was created, capturing semantic relationships in the SNOMED KG (see Figure 1A). It involves graph initialization and the exclusion of non-informative properties, followed by the triplets extraction: for each concept in the KG, all allowed properties and their associated related concepts are retrieved. If multiple related concepts existed for a (Concept, Property) pair, one was randomly chosen to ensure uniqueness.

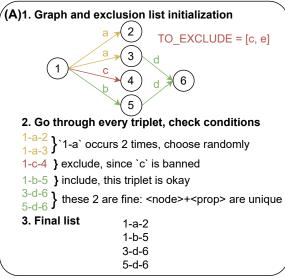
2.1.3 Sequences Generation

The sequence generation simulated graph traversal to encode both local and global structures (Figure 1B). The extended graph excluded banned properties and added reverse edges for bidirectional traversal; labels were standardized. Sequences of the form (node₁, edge₁, node₂, . . . , node_{n-1}, edge_{n-1}, node_n) were generated by selecting a random starting node, creating a subgraph by breadth-first search (BFS) with a set depth and randomly traversing unique edges. Every time, check that the same (node, edge) pair is not already visited before. The traversal stopped once it reached a pre-defined random edge limit or when no valid neighbors remained. This process was repeated for the desired number of sequences.

2.2 Transformers training

Decoder-only transformers with variations in architecture were implemented. Each unique element (node or edge) was assigned a unique integer (ensuring that repeated elements were consistently tokenized), followed by learned positional encoding. The architecture included an embedding layer to map tokenized inputs into continuous vector representations, transformer decoder layers with multihead attention mechanisms, and a linear output for token prediction.

For all experiments, the task was to predict a concept based on the previous concepts and relations. The accuracy was evaluated as:
\[\frac{#correct_predictions}{#total_predictions} - \]
\[\text{the proportion of correctly predicted related concepts to the total number of predictions. Additionally, Maximum Attainable Capacity (MAC) was used as a more suitable metric to measure the capacity of the model. MAC is a computationally efficient alternative to the Maximum Library Size (MLS) method. While MLS involves iteratively training models on progressively larger datasets to determine the largest library size that can be



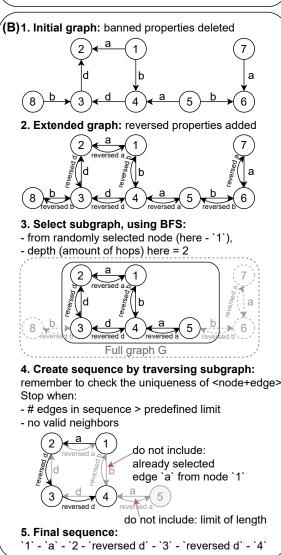


Figure 1: Algorithms of triplets (A) and sequences (B) data generation.

fully memorized, MAC is measuring the maximum number of samples that a model can memorize, provided with a large library. Previous research has shown a strong correlation between MLS and MAC (Härmä et al., 2024), making MAC an effective and time-efficient choice for this study.

To minimize the effect of randomness, each experiment was repeated 10 times for the first two setups and 3 times for the third and fourth setups, reporting the mean and double standard deviation. Training accuracy was evaluated at every other epoch for all configurations.

Models were implemented in PyTorch v1.13.1+cu117 (Paszke et al., 2017) and Transformers v4.30.2 (Wolf et al., 2019), trained with cross-entropy loss and Adam optimizer (learning rate 0.001) (Kingma and Ba, 2017). All other were default unless specified. In total, 546 models were trainded on NVIDIA A100 GPU with 16GB memory, totaling approximately 3, 100 hours of training time. Model sizes ranged from 2.9 to 44.5 million parameters, primarily varying with embedding size and layer count, but also influenced by vocabulary size.

2.3 Code availability

All code pertinent to the methods and results presented in this work is available at: https://github.com/um-dacs-nlp/capacity/.

2.3.1 Triplets memorization

Three experimental setups were designed for the triplets dataset. In all cases, the prediction of a related concept was based on a unique concept-relation pair, making correctness unambiguous.

In the first setup, dataset sizes ranged 50,000 to 100,000 samples. The model architecture consisted of a single transformer layer (embedding size 128, 4 attention heads, Rectified Linear Unit (ReLU) activation function (Agarap, 2019), batch size 64, 500 epochs). This setup focused on evaluating memorization performance under a fixed architecture while varying dataset sizes.

The second setup varied both architecture and activations: transformer layers (1, 2, or 4), and activation functions (ReLU, Gaussian Error Linear Unit (GELU) (Hendrycks and Gimpel, 2023), Randomized Leaky Rectified Linear Unit (RReLU) (Xu et al., 2015), and Softmax (Boltzmann, 1868)), with dataset sizes of 50,000, 70,000, or 100,000. To ensure fair comparisons, the total number of model parameters was kept constant across configurations by adjusting the embedding size (d_model parameter in PyTorch implementation of Transformers) proportionally to the number of

layers, using the formula: embedding_size = $\left\lfloor \frac{\text{base_number_of_parameters}}{\text{n_layers}} \right\rfloor$ with a base number of parameters of 128. This approach ensured that variations in performance could be attributed solely to architectural differences rather than changes in the total parameter count. For this setup, however, the batch size was increased to 128 and models were trained for 1000 epochs, since it was required for achieving a plateau.

The third setup examined the interplay between model depth and embedding size, while keeping other hyperparameters the same: number of layers was set to 1 or 2 and base numbers of parameters for embedding sizes varied in $\{16; 32; 64; 128\}$ (calculated as in the second experiment), with dataset sizes of 1,000, 10,000, 50,000, and 100,000. Only the Softmax activation function and 4 attention heads were used. To ensure fair comparisons, the configurations were designed to evaluate the impact of increasing the embedding sizes and depth of the model on the performance of the memory. The total parameter count was recalculated for each configuration using the same formula as in the second experiment. For this setup, the batch size was 128 and the training lasted 500 epochs.

2.3.2 Sequences memorization

The sequence memorization dataset used the same tokenization process as triplets, with additional steps for standardization: zero-padding at the end to a uniform length served both as a filler and a marker for sequence termination. A node mask was applied to distinguish the node from edge tokens for metric computation. Notably, each node was predicted based on all preceding tokens in the sequence, meaning the last node in a sequence benefited from the most context. This setup provided deeper insights into the transformer model's ability to handle more structured data and its patterns.

The experimental setup was consistent with the triplet setups: embedding size 64, 4 attention heads, batch size 128, and 400 training epochs. Models with 1, 2, or 4 layers were tested, using RReLU and Softmax activations. Dataset sizes were 20,000, 50,000, and 100,000 sequences, each containing 4–6 nodes (3–5 edges), built from subgraphs extracted via BFS with a depth of 5 hops.

For this experiment, accuracy and capacity were measured similarly to the triplet-based experiments, with slight adaptations to account for the sequential structure of the data. Accuracy was defined as the proportion of correctly predicted tokens at node positions to the total number of node predictions in the dataset and is equal to all nodes across all sequences, excluding starting points. The total correct predictions also represent the MAC.

3 Results

3.1 Dataset Size Influence

Figure 2 illustrates capacity and accuracy trends across dataset sizes in the first setup. Smaller datasets learn quickly, with both metrics rising rapidly in the first 5–6 epochs and reaching maximum capacity by epoch 20. Larger datasets improve little in the first 15 epochs but later reach higher final accuracy and capacity. This suggests a threshold existence ($\sim 70,000$ rows for this case), beyond which the training process changes and a lot more epochs are required for full memorization.

The final accuracy and capacity (Table 1) indicate that although smaller datasets initially achieve higher accuracy, their capacity remains well below the size of the dataset (e.g., 50,000 rows yield only 46,811 samples). In contrast, larger datasets, such as 100,000 rows, significantly improve memorization (86,776 samples), highlighting the model's ability to use more data. The progressive increase in capacity suggests that the size of the dataset plays a crucial role in optimizing memorization; however, the reasons behind the unlearned data, despite the available capacity, remain unclear.

data size	accuracy, %	capacity
50,000	93.62 ± 0.3	$46,811 \pm 149$
60,000	92.42 ± 0.2	$55{,}455 \pm 126$
70,000	91.1 ± 1.08	$63,773 \pm 756$
80,000	89.63 ± 1.66	$71,706 \pm 1326$
90,000	87.24 ± 1.66	$78,\!517 \pm 2173$
100,000	86.78 ± 2.42	$86,776 \pm 2484$

Table 1: Final results after the full training process for the first setup (data sizes, for triplets dataset).

3.2 Architectural Variations Influences

In the second setup, the batch size was increased from 64 to 128, Since larger batch sizes seem to reduce gradient noise and improve memorization. As a result, one-layer models converged faster and reached higher capacity than in the first setup.

Softmax consistently outperformed other activation functions, yielding the highest average capacity, fewer outliers, and more stable training. Notably, four-layer models with Softmax achieved

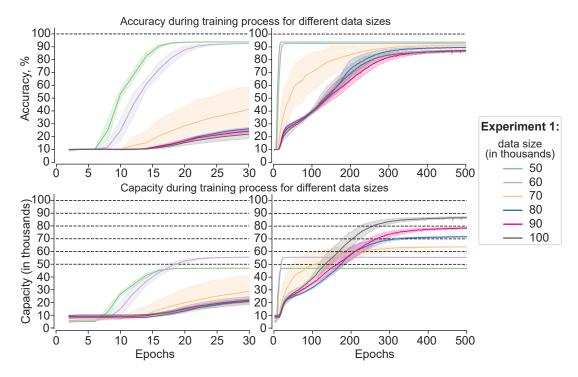


Figure 2: Trends in training accuracy (upper) and capacity (lower) for the first setup (different data sizes, for triplets dataset). Left: first 30 epochs; right: full training process of 500 epochs.

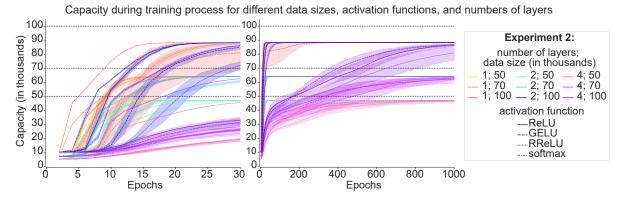


Figure 3: Trends in training capacity for the second setup (different data sizes, activation functions, and numbers of layers for triplets dataset). Left: first 30 epochs; right: full training process of 1000 epochs.

capacities comparable to one- or two-layer models without sacrificing convergence speed (Figure 3), suggesting its scalability with depth.

In contrast, ReLU and RReLU showed moderate performance, but suffered from increased variability and decreased capacity as the layers increased, aligning with the findings of Paik and Choi (2023) and Chen and Ge (2024). These activations exhibited inconsistent learning patterns, with unexpected slowdowns in capacity improvements (Fu et al., 2024). GELU followed a similar trend, though it performed better in the early training stages with larger datasets.

As previously, the size of the dataset significantly affected training: larger sets required longer warmup phases, initially achieving lower capacities than smaller datasets under the same conditions. This suggests the existence of distinct learning phases where improvements depend on architectural depth, dataset size, and activation function.

Furthermore, adding more layers did not improve performance; instead, it slowed training and reduced final capacity, likely due to the simplicity of the dataset, where additional layers do not provide any advantage in capturing patterns. Although deeper architectures benefit more complex datasets (He et al., 2024), their impact can be reduced for data with simple relationships.

3.3 Number of Parameters Influence

The third experiment further confirmed that, for simple datasets, learning dynamics depend on em-

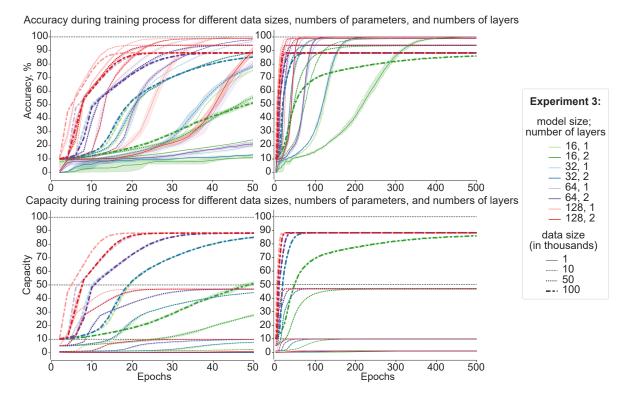


Figure 4: Trends in training accuracy (upper) and capacity (lower) for the third setup (different data sizes, numbers of parameters, and numbers of layers for triplets dataset). Left: first 50 epochs; right: full training process of 500 epochs. Light color corresponds to 1 layer, dark – to 2; number of parameters is a total number for all layers: green – 16, blue – 32, violet – 64, red – 128; embedding size can be computed by dividing it by layer count.

bedding size, not the number of layers. Models with the same embedding size but different layer counts exhibited nearly identical accuracy improvement. For instance, as shown in Figure 4, a one-layer model with 16 parameters (embedding size is 16, light green) converged at almost the same rate as a two-layer transformer with 32 parameters (embedding size is 16 per layer, dark blue). Similar trends were observed for models with embedding sizes of 32 and 64, regardless of layer count.

These results highlight that embedding size is the key factor influencing learning speed, while adding layers without increasing embedding size neither accelerates convergence nor improves final capacity. In fact, additional layers often slow the training, as evidenced by the faster growth of accuracy of one-layer models (Figure 4). Smaller embedding sizes further reduced the learning speed, consistent with previous experiments. However, all configurations ultimately reached similar accuracy, highlighting that the simplicity of the dataset allows embedding size to dominate training dynamics.

The final capacity values remained nearly identical across configurations, regardless of embedding size or layer count: with a dataset size of 1,000 samples, the capacities for the one- and two-layer

models were nearly accurate. Similarly, at 10,000 and 50,000 samples, one-layer models achieved $9,874\pm11$ and $46,939\pm105$, while two-layer models reached $9,875\pm7$ and $46,911\pm117$, respectively. However, at 100,000 samples, a capacity "barrier" emerged. Two-layer transformers with an embedding size of 8 (16 total parameters) showed the capacity drop to $85,935\pm153$, compared to $\sim88,200$ for other configurations, while one-layer models maintained a higher capacity of $88,240\pm62$. This suggests that larger datasets, smaller embeddings, and deeper architectures may introduce limitations due to slower convergence or suboptimal capacity utilization.

3.4 Insights from Sequence Datasets

In the fourth setup, model capacity was evaluated by testing its ability to memorize each node in a sequence using the full preceding sequence of nodes and edges (instead of triplets), involving 34,908, 85,972, and 167,965 predictions for datasets of 20, 50, and 100 thousand sequences, respectively.

Compared to triplet datasets, models trained on sequences achieved near-perfect memorization in significantly fewer epochs, plateauing within 150 epochs (Figure 5). The sequential structure likely

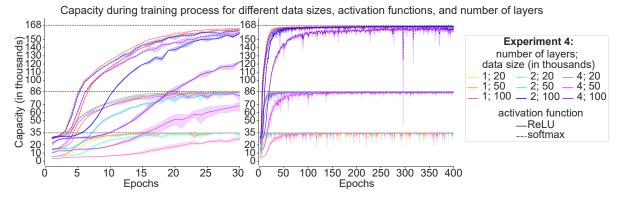


Figure 5: Trends in training capacity for the fourth setup (different data sizes, activation functions, and numbers of layers for sequences dataset). Left: first 30 epochs; right: full training process of 400 epochs.

sped up learning but increased training time because of more information per sequence. Training showed greater capacity fluctuations over epochs, probably reflecting the increased complexity of the dataset, as sequences encode more intricate patterns than triplets. Nonetheless, models demonstrated exceptional memorization, achieving 100% capacity for the 20 thousand sequence dataset and over 99.5% for 50 and 100 thousand sequences.

As before, RReLU converged more slowly than Softmax, however, the final capacities were nearly identical for one- and two-layer models: with 100 thousand sequences, RReLU achieved $166,934 \pm 243$ (one layer) and $166,995 \pm 118$ (two layers), while Softmax reached $166,992 \pm 110$ and $166,985 \pm 904$, respectively. In deeper models (4 layers), RReLU showed lower final capacities and greater fluctuations (165,271 \pm 1,068 vs. $166,825 \pm 319$ for Softmax). This contrasts with previous findings (Shen et al., 2023), which reported that ReLU outperformed Softmax. The discrepancy may suggest that the relative effectiveness of activation functions depends on the dataset structure and task, warranting further investigation. Nonetheless, even with increased sequence complexity, all models demonstrated rapid adaptation and strong memorization.

4 Discussion

This study examined how decoder-only transformer models memorize structured data derived from a real-world medical ontology. Our focus was not on generalization, but on a controlled analysis of memorization, presenting a proof-of-concept framework that bridges theoretical insights and practical evaluation. The complete SNOMED KG contains more than a million relations, integrating diverse fields of medicine (e.g., substances, diseases, and anatom-

ical structures). However, in mobile applications, e.g. small transformers in smart glasses or smartwatches, models must efficiently retain only targeted subsets of information. For example, smart glasses for a cardiac surgeon or a smartwatch with a personal dietary coach might require a domainspecific LLM that memorizes about 10 to 100,000 items. As discussed in Kajitsuka and Sato (2024); Härmä et al. (2024), isolating memorization is a valid objective that reveals how much a transformer can reliably store under different architectural configurations. Our methodology reflects this: we analyze how dataset characteristics and architectural choices affect convergence and memorization, independent of generalization ability or test-time reasoning.

To ensure clear capacity measurement, we deliberately focused on tasks where ground-truth memorization can be unambiguously defined. Increasing complexity would blur the line between memorization and generalization, making interpretation less fair and direct.

4.1 Effect of Dataset Structure

Smaller datasets led to faster convergence but lower capacity, whereas larger datasets required longer warm-up but achieved higher memorization. Beyond a certain size, the training slowed significantly, indicating optimization bottlenecks. The fact that some samples remain unlearned even with sufficient capacity points to possible optimization barriers or local minima (see Limitations).

Sequence-based datasets outperformed triplets, achieving near-perfect memorization with fewer epochs. Sequences improved learning by capturing relationships and patterns in the data, though they also led to increased training fluctuations, aligning with Ju et al. (2021). This suggests that longer

traversal sequences could further improve memorization in domain-specific medical applications.

The complexity of the sequence datasets was controlled through BFS depth and edge count, allowing capture of both local and global structures from the SNOMED graph (e.g., transitions between anatomical concepts and related procedures), while avoiding trivially linear or purely synthetic patterns. Randomness was balanced with structural constraints such as bidirectional edges and node uniqueness, reflecting how medical knowledge is typically reasoned over in practice (e.g., from symptom to diagnosis to treatment).

4.2 Architectural Influence

Embedding size was the main factor in learning speed and capacity, and adding layers often reduced performance, probably due to the data simplicity. This supports the findings that many transformer layers are redundant and can be pruned without loss He et al. (2024). Although we did not directly analyze redundancy, our results suggest that pruning could further optimize capacity.

For larger datasets, smaller embeddings struggled to reach full capacity, particularly in deeper architectures, suggesting that increasing embedding size is more beneficial than adding depth, at least for structured domain-specific memorization.

Softmax led to greater stability and capacity, while ReLU-based activations showed higher variability and performance drops in deeper models, which is consistent with, e.g., Paik and Choi (2023); Chen and Ge (2024). However, this contrasts with Shen et al. (2023), who found ReLU advantageous, emphasizing that activation effectiveness may be highly dependent on the structure of the dataset, the initialization of the model, or the formulation of the task.

For deployment in limited edge devices, our results suggest favoring shallow architectures (1 to 2 layers) with wider embeddings, which consistently demonstrated better memorization per parameter. This configuration offers a practical trade-off for applications where total parameter count and energy use are constrained, such as wearables or low-power clinical decision support tools.

5 Conclusions

This study investigated how transformer architecture and dataset structure influence memorization capacity, introducing a practical framework for evaluating memorization on real-world data, such as the SNOMED knowledge graph.

Key findings show that embedding size and activation function have more impact than depth, while larger datasets improved memorization but required longer training. Triplets performed well in simpler models, whereas sequences excelled but introduced fluctuations. Challenges remain in efficiency, layer-specific contributions, and generalization, necessitating further research on scalability, compression, and architecture optimization.

For practical use of small transformers in medical smart devices, models must efficiently store specialized knowledge while maintaining computational feasibility. Future work should explore longer sequences, adaptive memory compression, and layer-wise analysis to enhance structured knowledge memorization in practical deployments.

6 Limitations

Although this study provides meaningful information, several open questions remain:

- Misclassification patterns were not systematically analyzed; unlearned samples may be the result of optimization bottlenecks or dataspecific challenges. Strategies, such as curriculum learning (Kim and Lee, 2024), or loss re-weighting (Sow et al., 2025) could address these gaps.
- Future research should test these findings on longer sequences and larger datasets to confirm them at scale.
- Layer similarity or redundancy was not directly assessed; future probing and pruning studies (see Allen-Zhu and Li (2024)) could clarify each layer's role and enhance efficiency.
- Integrating sparse autoencoders (Bricken et al., 2023) or transcoders (Paulo et al., 2025) can help distinguish memorization from generalization, clarifying whether certain layers store specific relationships or contribute to greater generalizability.
- While proposed sequence generation method reflects realistic ontology traversal, more explicit alignment with clinical reasoning patterns (e.g., decision trees or symptom pathways) is an open direction. Testing on

other biomedical graphs, such as GenomicKB (Feng et al., 2022), which encodes large-scale genomic and transcriptomic relationships, could assess whether memorization patterns generalize to domains with different graph structures.

 We did not conduct experiments under quantization or activation sparsity constraints, which may affect architectural recommendations for edge applications and warrant follow-up work.

Addressing these limitations will further refine transformer optimization strategies for structured data modeling and knowledge retention.

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A Appendix: Additional Representations of the Results

This appendix provides supplementary visualizations and tables for the experiments conducted:

- Second experiment:
 - Figure 6: Accuracy trends during training.
 - Table 2: Final capacities.
- Third experiment:
 - Table 3: Final capacities.
- Fourth experiment:
 - Figure 7: Accuracy trends during training.
 - Table 4: Final capacities.

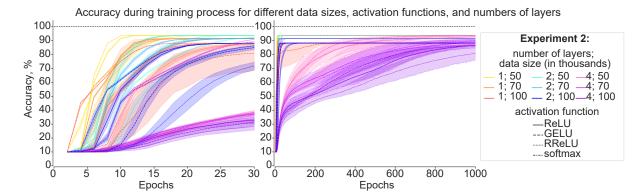


Figure 6: Trends in training accuracy for the second setup (different data sizes, activation functions, and numbers of layers for triplets dataset). Left: first 30 epochs; right: full training process of 1000 epochs.

activation function	layers count	data sizes			
		50,000	70,000	100,000	
ReLU	1	$46,898 \pm 158$	$64,091 \pm 192$	$88,148 \pm 312$	
	2	$46,920 \pm 112$	$64,086 \pm 130$	$88,217 \pm 125$	
	4	$46,391 \pm 2,268$	$61,931 \pm 8,480$	$86,\!558 \pm 3,\!291$	
GELU	1	$46,925 \pm 105$	$64,096 \pm 184$	$88,195 \pm 123$	
	2	$46,926 \pm 115$	$64,080 \pm 120$	$88,215 \pm 128$	
	4	$46,798 \pm 156$	$62,949 \pm 1,906$	$86,589 \pm 2,202$	
RReLU	1	$46,930 \pm 125$	$64,080 \pm 122$	$88,180 \pm 180$	
	2	$46,927 \pm 121$	$64,088 \pm 117$	$88,\!208 \pm 132$	
	4	$46,730 \pm 223$	$62,\!818 \pm 3,\!680$	$80,755 \pm 15,844$	
softmax	1	$46,924 \pm 87$	$64,082 \pm 166$	$88,211 \pm 192$	
	2	$46,908 \pm 127$	$64,074 \pm 134$	$88,213 \pm 171$	
	4	$46,923 \pm 104$	$64,085 \pm 131$	$88,197 \pm 134$	
all	1	$46,919 \pm 119$	$64,087 \pm 162$	$88,183 \pm 210$	
	2	$46,920 \pm 115$	$64,082 \pm 121$	$88,\!213\pm135$	
	4	$46,710 \pm 1169$	$62,945 \pm 4,92$	$85{,}525 \pm 9{,}720$	

Table 2: Final capacity after the full training process for the second setup (different numbers of layers, data sizes, and activation functions for triplets dataset).

embedding parameters	layers count	data sizes			
	layers count	1,000	10,000	50,000	100,000
16	1	$1,000 \pm 1$	$9,870 \pm 10$	$46,937 \pm 148$	$88,236 \pm 74$
	2	998 ± 3	$9,\!875 \pm 4$	$46,858 \pm 93$	$85,935 \pm 153$
32	1	998 ± 3	$9,872 \pm 11$	$46,955 \pm 119$	$88,234 \pm 62$
	2	999 ± 3	$9,\!876 \pm 9$	$46,927 \pm 128$	$88,\!252\pm82$
64	1	999 ± 2	$9,\!878 \pm 9$	$46,932 \pm 122$	$88,242 \pm 102$
	2	999 ± 3	$9,\!876\pm7$	$46,919 \pm 96$	$88,\!237 \pm 58$
128	1	999 ± 2	$9,877 \pm 12$	$46,930 \pm 85$	$88,248 \pm 29$
	2	999 ± 3	$9,\!872 \pm 6$	$46,938 \pm 131$	$88,\!214 \pm 53$
all	1	999 ± 2	$9,874 \pm 11$	$46,939 \pm 105$	$88,240 \pm 62$
	2	999 ± 3	$9,875 \pm 7$	$46,911 \pm 117$	$87,660 \pm 2,082$

Table 3: Final capacity after the full training process for the third setup (different data sizes, numbers of parameters, and numbers of layers for triplets dataset).

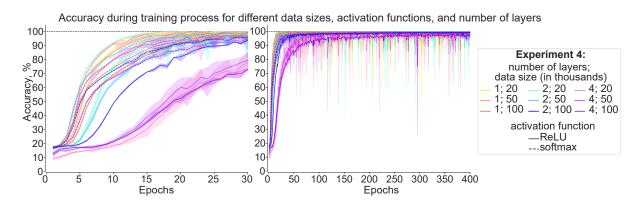


Figure 7: Trends in training accuracy for the fourth setup (different data sizes, activation functions, and numbers of layers for sequences dataset). Left: first 30 epochs; right: full training process of 400 epochs.

activation function	layers count	# of sequences (# of predictions)			
		20,000 (34,908)	50,000 (85,972)	100,000 (167,965)	
RReLU	1	$34,908 \pm 0$	$85,936 \pm 31$	$166,934 \pm 243$	
	2	$34,908 \pm 0$	$85,917 \pm 34$	$166,995 \pm 118$	
	4	$34,908 \pm 0$	$85,\!647 \pm 270$	$165,\!271 \pm 1,\!068$	
softmax	1	$34,908 \pm 0$	$85,931 \pm 18$	$166,992 \pm 110$	
	2	$34,908 \pm 0$	$85,\!888 \pm 33$	$166,985 \pm 904$	
	4	$34,908 \pm 0$	$85,771 \pm 42$	$166,825 \pm 319$	
all	1	$34,908 \pm 0$	$85,934 \pm 23$	$166,963 \pm 180$	
	2	$34,908 \pm 0$	$85,903 \pm 44$	$166,990 \pm 577$	
	4	$34,908 \pm 0$	$85,709 \pm 220$	$166,048 \pm 1,842$	

Table 4: Final capacity after the full training process for the fourth setup (different data sizes, activation functions, and numbers of layers for sequences dataset).