TABGEN-ICL: Residual-Aware In-Context Example Selection for Tabular Data Generation

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Abstract

Large Language models (LLMs) have achieved encouraging results in tabular data generation. However, existing approaches require finetuning, which is computationally expensive. This paper explores an alternative: prompting a fixed LLM with in-context examples. We observe that using randomly selected in-context examples hampers the LLM's performance, resulting in sub-optimal generation quality. To address this, we propose a novel in-context learning framework: TABGEN-ICL, to enhance the in-context learning ability of LLMs for tabular data generation. TABGEN-ICL operates iteratively, retrieving a subset of real samples that represent the *residual* between currently generated samples and true data distributions. This approach serves two purposes: locally, it provides more effective in-context learning examples for the LLM in each iteration; globally, it progressively narrows the gap between generated and real data. Extensive experiments on five real-world tabular datasets demonstrate that TABGEN-ICL significantly outperforms the random selection strategy. Specifically, it reduces the error rate by a margin of up to 42.2%on fidelity metrics. We demonstrate for the first time that prompting a fixed LLM can yield high-quality synthetic tabular data. The code is provided in the link.

1 Introduction

Tabular data, despite being one of the most prevalent data modalities in real-world applications (Benjelloun et al., 2020), often encounters several issues in practical use. These include imbalanced data categories (Cao et al., 2019), privacy concerns (Gascón et al., 2016) (as many tabular datasets contain sensitive personal information that cannot be directly shared), insufficient data quality (Lin and Tsai, 2020), and high data collection costs (Even et al., 2007). Tabular generation is an important

means to address these problems. Classic tabular generation methods such as GANs (Xu et al., 2019), VAEs (Liu et al., 2023), and diffusion models (Kim et al., 2023; Lee et al., 2023; Kotelnikov et al., 2023; Zhang et al., 2024) have two main limitations. First, they require large amounts of tabular data for training, which leads to a noticeable decline in performance in low-resource scenarios. This is particularly problematic considering that most real-world situations requiring tabular generation lack abundant data. Second, they need special preprocessing to handle heterogeneous data types, making them less flexible.

The rapid development of large language models (LLMs) brings new possibilities for solving table data generation problems with their powerful semantic understanding, reasoning, and generation capabilities. LLMs can understand and process various data types and structures without complicated data preprocessing, offering more flexible and principled solutions. Moreover, LLMs' few-shot learning ability may alleviate data scarcity issues, enabling excellent performance in low-resource scenarios. Previous works (Borisov et al., 2023; Solatorio and Dupriez, 2023; Zhang et al., 2023; Zhao et al., 2023; Gulati and Roysdon, 2023; Xu et al., 2024a; Wang et al., 2024) resort to fine-tuning general-purpose LLMs on target tables. While effective, fine-tuning requires substantial computational resources, making it inapplicable in resourcescarce scenarios.

In-context learning effectively solves such problems. By adding examples to the context, distribution characteristics can be provided to LLMs, guiding them to generate data that conforms to the target distribution without specific fine-tuning (Gao et al., 2023). However, simple in-context learning strategies still face challenges. Figure 1(a) shows that even without in-context examples (see the full prompt at Appendix A.2), LLMs can generate reasonable distributions, reflecting the influ-

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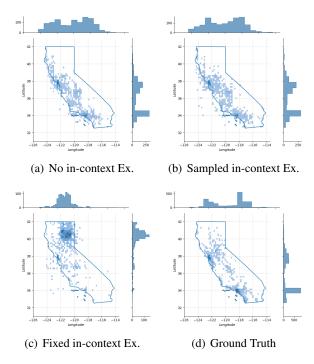


Figure 1: Comparison of samples generated with different in-context learning examples. Plots show the latitude and longitude coordinates of California housing, with the solid line representing the state boundary. (a) 2000 samples generated by LLM with only the table header as input, **without** any in-context examples. (b) 2000 samples generated by LLM, giving in-context examples sampled from the real dataset. (c) 2000 synthetic samples generated by LLM, giving in-context examples with latitude and longitude in a fixed range. (d) 2000 samples from the ground truth training table.

ence of the LLM's pre-training distribution. Figure 1(b) demonstrates the strategy proposed by (Seedat et al., 2024), which involves random sampling from Ground Truth as in-context examples. Although the generated results are closer to the Ground Truth shown in Figure 1(d) compared to Figure 1(a), they are still mainly influenced by the LLM's original distribution and struggle to fit the Ground Truth.

This phenomenon reveals the importance of choosing in-context examples. In this work, we propose TABGEN-ICL, a dynamic in-context example selection method. Inspired by the observation in Figure 1(c), we found that using fixed range incontext examples leads to generated distributions closely mimicking those examples, significantly differing from the LLM's original distribution. This indicates in-context learning's ability to simulate distributions. By carefully selecting in-context examples, we can more effectively guide LLMs to generate distributions closer to the ground truth.

Central to our framework is the design of an auto-

mated strategy for selecting effective in-context examples while ensuring global consistency with the real data distribution. Our key idea is to utilize simple, discernible patterns in subsets of real samples, which can effectively guide LLMs in generating realistic tabular data. Specifically, TABGEN-ICL identifies subsets of real samples that exhibit simple patterns and closely match the residual between the current generated data distribution and the real data distribution. This idea can be categorized as a novel residual-aware RAG technique, where we retrieve in-context examples based on the residual between the generated and real data distributions.

The residual-aware sampling measures the discrepancy between the generated and real data distributions, focusing on areas where the model needs improvement. This approach enables TABGENICL to progressively narrow the distribution gap while maintaining the use of easily learnable patterns in the in-context examples. Our sampling technique offers two key advantages: flexibility in selecting simple patterns for effective learning, and consistent generation through progressive distribution alignment. The contributions of this paper are as follows:

- We propose TABGEN-ICL, an in-context learning selection method that retrieves in-context examples by leveraging residual between currently generated samples and true data distributions.
- 2. We conduct extensive experiments on five datasets, evaluated under three distinct groups of synthetic data evaluation metrics. Experiment results show that TABGEN-ICL outperforms the previous in-context learning method by a margin of 3.5% 42.2% across multiple fidelity metrics. Notably, TABGEN-ICL surpasses state-of-the-art deep generative models under the data-scarce scenarios.

2 Related works

Deep generative models for synthetic tabular data generation Generative models for tabular data have become increasingly important and have widespread applications (Assefa et al., 2021; Zheng and Charoenphakdee, 2022; Hernandez et al., 2022). For example, CTGAN and TAVE (Xu et al., 2019) deal with mixed-type tabular data generation using the basic GAN (Goodfellow et al., 2014) and VAE (Kingma and Welling, 2013) framework. GOGGLE (Liu et al., 2023) incorporates

Graph Attention Networks in a VAE framework such that the correlation between different data columns can be explicitly learned. Recently, inspired by the success of Diffusion models in image generation, a lot of diffusion-based methods have been proposed, such as TabDDPM (Kotelnikov et al., 2023), STaSy (Kim et al., 2023), CoDi (Lee et al., 2023), and TabSyn (Zhang et al., 2024).

LLMs for synthetic tabular data generation.

Collecting high-quality training data for advanced deep learning models is often costly and timeconsuming. Pre-trained large language models (LLMs), been exposed to vast corpora, have emerged as a promising direction for synthetic data generation. However, while LLMs have demonstrated strong capabilities in generating highquality natural language, their ability to accurately replicate tabular data distributions at scale remains uncertain (Xu et al., 2024b). To address this challenge, several works have explored fine-tuning LLMs such as GPT-2 to generate synthetic tabular data more effectively (Borisov et al., 2023; Solatorio and Dupriez, 2023; Yang et al., 2024). Another line of work leverages the in-context learning abilities of LLMs (Seedat et al., 2023), which is closely related to our method. Seedat et al. (2023) adopts a straightforward strategy to uniformly sample in-context examples; we identify the root of inefficiency of this strategy and instead propose a residual-aware in-context example selection strategy, which is shown to improve the generation quality.

3 Preliminaries

Notation. Tabular dataset refers to data organized in a tabular format with N row and D columns, where each row denotes a data record or sample, and each column denotes an attribute or feature. Each attribute can be either discrete (e.g. categorical) or continuous (e.g. real number \mathbb{R}). We use $\mathbb{P}(x)$ to denote the probability distribution of x.

Data Setup. We have access to a training dataset of N samples: $\mathcal{D}_{train} = \{x_i\}_{i=1}^{N}$, each sample x_i is *i.i.d.* drawn from an unknown distribution $\mathbb{P}(x)$.

Objective. The goal is to generate a **new** dataset $\mathcal{D}_{syn} = \{\hat{x}_i\}_{i=1}^N$ such that \hat{x}_i is *i.i.d.* sampled from $\mathbb{P}(x)$. Direct copy of training data is not allowed.

Serialization. As LLMs primarily process text input, it is necessary to convert tabular data

into a suitable textual format. There are many serialization formats for tabular data, such as JSON (Singha et al., 2023), Markdown (Sui et al., 2024), Sentences (Borisov et al., 2023), etc. Notably, the JSON format is widely supported by LLMs, with models like GPT-40 capable of generating structured outputs in JSON format through constrained decoding (Liu et al., 2024). Therefore, in this study, we adopt a JSON format to serialize tabular data. For instance, a row from a table containing three columns—name (categorical), age (numerical), and city (categorical)—is transformed into a JSON object: {name: 'Alice', age:25, city: 'New York'}. For a table comprising N rows, the serialized data becomes a list of N JSON objects. See Appendix A.3 for the implementation of the JSON schema. During each prompting iteration, TABGEN-ICL retrieves a subset of these JSON objects to serve as in-context examples. This process will be elaborated upon in subsequent sections.

4 TABGEN-ICL

This section presents TABGEN-ICL framework for tabular data generation. TABGEN-ICL retrieves a subset of samples from the training dataset that satisfy two properties: 1) **Local**: at each prompting iteration, the LLMs can effectively extract patterns from the in-context examples; 2) **Global**: after enough iterations, the overall generated samples mimic the distribution of the real samples. In the following, we will introduce each component of TABGEN-ICL in detail.

4.1 LLM Generation with In-context Examples

Our key observation is LLMs have strong prior distribution, and LLMs tend to generate samples following their prior distribution, neglecting the incontext examples, see Figure 1. Formally, given incontext examples, we assume the LLMs generate samples following a mixture distribution:

Definition 1 (LLM Generation Distribution). Given the empirical distribution of in-context example: \mathbb{P}_{ic} . We define the LLMs generation distribution to be the following mixture of distributions:

$$\mathbb{P}_{gen} := \lambda \mathbb{P}_{llm} + (1 - \lambda) \mathbb{P}_{ic} \tag{1}$$

where \mathbb{P}_{llm} is the prior distribution of LLMs, $\lambda \in [0,1]$. To sample from \mathbb{P}_{gen} , we first sample an index z from a categorical distribution over $\{0,1\}$

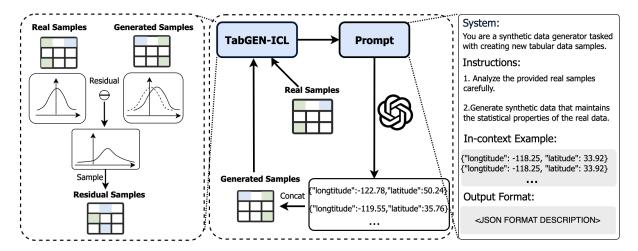


Figure 2: Overview of TABGEN-ICL framework. We generate synthetic samples in batches, at each prompt iteration, TABGEN-ICL retrieves a subset of real samples that acts as a *residual* between the currently generated samples and the real data. The residual samples will be used as in-context examples to prompt LLMs in the next iteration. The full prompt template is available in the Appendix A.1.

with parameter λ , then sample from the corresponding distribution:

$$\mathbb{P}_{gen}(oldsymbol{x}) = egin{cases} \mathbb{P}_{llm}(oldsymbol{x}) & ext{if } z = 1 \ \mathbb{P}_{ic}(oldsymbol{x}) & ext{if } z = 0 \end{cases}$$

Definition 1 quantifies how the in-context examples steer the LLMs' generation from its own prior distribution towards the target distribution. Intuitively, the more in-context examples being provided, λ will be closer to 0, meaning the LLMs is more likely to generate samples following the empirical distribution of in-context examples. In practice, due to the limited context window of LLMs, only a small number of in-context examples can be provided, thus we expect λ to be close to 1.

4.2 In-context Examples Selection

Recall our goal is to let LLMs generate samples that follow the same distribution as the training table, i.e. $\mathbb{P}_{qen} \approx \mathbb{P}_{train}$. It is tempting to choose the incontext examples by sampling from the empirical distribution of the training table, i.e. $\mathbb{P}_{ic} = \mathbb{P}_{train}$ (Seedat et al., 2024). However, as the LLMs' generation is affected by the prior distribution \mathbb{P}_{llm} , the actual output distribution of LLMs would be $\mathbb{P}_{qen} = \lambda \mathbb{P}_{llm} + (1 - \lambda) \mathbb{P}_{train}$, which is not our target distribution \mathbb{P}_{train} . Instead, a more plausible way is to select in-context examples s.t., when combined with λ proportion of data generated from \mathbb{P}_{llm} , the resulting distribution is close to \mathbb{P}_{train} . In other words, the in-context examples can be understood as the *residual* of \mathbb{P}_{train} w.r.t. \mathbb{P}_{llm} . Formally, we introduce the definition of residual as follows:

Definition 2 (**Residual**). Let X be a set of N i.i.d. samples from a data distribution $\mathbb{P}(x)$, and let Y be an arbitrary set of samples with the same dimension as X. We define the **residual** (abbrev. RES) of X w.r.t. Y as a subset of n samples of X such that, when concatenated with Y, the empirical distribution of the concatenated samples is most similar to the data distribution $\mathbb{P}(x)$:

$$RES(\boldsymbol{X}, \boldsymbol{Y}, n) := \underset{\boldsymbol{X}' \subseteq \boldsymbol{X}, |\boldsymbol{X}'| = n}{\arg \min} d(\boldsymbol{X}, \boldsymbol{Y} \cup \boldsymbol{X}')$$
(2)

where d can be any distance metric between two empirical distributions.

Remark 1. In our case, X is the real tabular samples, and Y is the current generated samples by a LLM. Intuitively, the residual samples capture the part of the real samples that LLM has not yet grasped, thus named as *residual*. To prevent overly long context prompts when interacting with the LLM, we enforce an upper-bound n on the size of the residual samples. In our experiments, we set n=500 and instantiate d as Jensen-Shannon Divergence (JSD) and Kolmogorov-Smirnov Distance (KSD).

Since brute-force way of computing the residual is computationally prohibitive for large N and n, we introduce a heuristic for sampling the residual. We describe details in the following—pseudo-code is provided in Appendix 1.

4.3 Compute Residual

We propose to use a simple heuristic to shrink the search space. Specifically, we first randomly select a column, then we group the real samples X based on the value of the selected column¹. Each group of samples is then concatenated with the generated samples Y. Finally, we select the group that has the smallest distance to the real samples X as the residual. The time complexity of this heuristic search algorithm is O(N). Additionally, the final residual subset always exhibits a consistent pattern—either sharing the same category or falling within a narrow numerical range in one of its columns. We hypothesize that this simple pattern makes the residual samples particularly effective as in-context examples for LLMs (see Figure 1 (c)).

4.4 Table Generation by TABGEN-ICL

TABGEN-ICL can be easily integrated with LLMs to generate high-quality synthetic tabular data. See Fig. 2 for an overview of the procedure. Here are the concrete steps involved in this procedure:

- 1. **In-context Prompting:** For the first iteration, we randomly select n samples from the real dataset X as the initial set of in-context examples. Otherwise, we plug the residual samples computed in the previous iteration into the prompt template to prompt LLMs. We append the generated samples into Y.
- 2. **Residual Computation:** We then compute the residual of X w.r.t. Y: RES(X, Y, n). Specifically, if the current iteration is an even number, we instantiate d as JSD, otherwise, we instantiate d as KSD.
- 3. **Iterative Refinement:** Repeat the above steps until enough synthetic samples are generated.

5 Experiments

We validate the performance of TABGEN-ICL through extensive experiments. In particular, we investigate the following questions:

- Can TABGEN-ICL improve generation quality compared to previous LLM-based methods? (Table. 1, 2, Fig. 5)
- How does TABGEN-ICL perform, compared to training-based deep generative models, under a data-scarcity setting? (Fig. 3)
- Does TABGEN-ICL generate new synthetic data instead of copying the training dataset? (Fig. 4)

5.1 Setup

Datasets. We select five real-world tabular datasets containing both numerical and categorical attributes: **Adult, Default, Shoppers, Magic** and **California**. The statistics of the datasets are summarized in Table 5 in Appendix A.5.

Baselines. To comprehensively assess TABGEN-ICL's performance, we conduct comparisons against a wide range of traditional deep generative models and LLM-based methods, which we categorize into the following two groups:

- Deep generative models: 1) VAE-based method TVAE (Xu et al., 2019), 2) GAN-based method CTGAN (Xu et al., 2019), 3) Diffusion-based method TabSyn (Zhang et al., 2024), TabDDPM (Kotelnikov et al., 2023), CoDi (Lee et al., 2023), STaSy (Kim et al., 2023), 4) Autoregressive method TabMT (Gulati and Roysdon, 2023), RealTabformer (RTF) (Solatorio and Dupriez, 2023).
- LLM-based methods: 1) with fine-tuning: GReaT (Borisov et al., 2023) 2) without fine-tuning: CLLM (Seedat et al., 2024). CLLM was originally employed with GPT-3.5 and GPT-4, to ensure a fair comparison to CLLM, we employ CLLM with stronger models: GPT-40-mini and GPT-40, and we keep all the other experimental settings the same as ours.

To the best of our knowledge, CLLM (Seedat et al., 2024) is the only prior training-free method that relies solely on in-context learning for synthetic tabular data generation. It consists of two main stages: 1) Generation Stage: A large language model (LLM) is prompted repeatedly to generate new samples, using in-context examples randomly selected from the training dataset; 2) Curation Stage: After generating a sufficient number of samples, CLLM trains a separate classifier to identify and filter out low-quality samples based on training dynamics. To ensure that the performance gains are solely attributable to the enhanced in-context sampling strategy, we omit the curation stage of CLLM. We keep all other experimental settings, including hyperparameters, identical between the two methods to enable a fair and controlled comparison.

Implementation details. Our main experiments employ GPT-40-mini and GPT-40 as the LLMs. For all LLMs, we set the temperature to 1.0. We

¹For categorical columns, we group by the categorical values. For continuous columns, we discretize them into a fixed number of bins and group by the bin index.

Method	Marginal↓ %	Corr↓ %	Precision↓ %	Recall↓ %	C2ST↓ %	JSD ↓ 10 ⁻²		
VAE-based								
TVAE (Xu et al., 2019)	14.61	17.32	11.65	9.11	41.72	0.63		
GAN-based								
CTGAN (Xu et al., 2019)	16.36	20.33	30.65	11.41	42.90	0.91		
	Diff	usion-base	ed					
STaSy (Kim et al., 2023)	12.35	9.72	11.09	2.66	55.82	1.34		
CoDi (Lee et al., 2023)	21.70	24.92	9.89	6.74	57.88	1.07		
TabDDPM (Kotelnikov et al., 2023)	14.04	8.16	13.37	2.27	24.21	0.85		
TabSyn (Zhang et al., 2024)	1.40	2.36	3.76	2.29	2.64	0.05		
	Autoregressive Models							
RTF (Solatorio and Dupriez, 2023)	5.31	10.42	3.53	5.25	28.16	0.45		
TabMT (Gulati and Roysdon, 2023)	4.46	8.24	33.88	50.44	44.77	0.63		
	LLM	-Finetuned						
GReaT (Borisov et al., 2023)	15.53	40.48	1.49	10.06	48.28	1.06		
	LLM-Prompt-Only							
CLLM w. GPT-4o-mini	13.17	19.57	6.63	8.08	39.02	0.78		
TABGEN-ICL w. GPT-4o-mini (Ours)	11.39	17.07	5.54	4.67	37.63	0.80		
Improvement	$\boldsymbol{13.5\%}$	$\boldsymbol{12.8\%}$	19.7 %	42.2 %	3.5 %	_		
CLLM w. GPT-4o	10.57	13.46	4.00	4.25	31.51	0.63		
TABGEN-ICL w. GPT-40 (Ours)	9.14	12.86	4.93	2.80	26.70	0.62		
Improvement	13.6 %	4.5 %	_	34.1 %	15.3 %	1.6 %		

Table 1: **Fidelity comparison**: Comparison of various methods on fidelity metrics. Results are averaged over all datasets. Values are scaled by dividing by 10^{-2} , then reversed by computing their complement: (1 - original value), so that the lower the better.

generate 3000 samples (N=3000) for each dataset. Each experiment is conducted 5 times, and the average results are reported.

Evaluation metrics. We evaluate the synthetic tabular data from three distinct dimensions: (1) Fidelity - if the synthetic data faithfully recovers the ground-truth data distribution. We evaluate fidelity by 5 metrics: 1) Marginal distribution through Kolmogorov-Smirnov Test, 2) Pair-wise column correlation (Corr.) by computing Pearson Correlation, 3) Classifier Two Sample Test (C2ST), 4) Precision and Recall, 5) Jensen-Shannon Divergence (JSD). ② Utility - the utility of the synthetic data when used to train downstream models, we use the Train-on-Synthetic-Test-on-Real (TSTR) protocol to evaluate the AUC score of the XGBoost model on predicting the target column of each dataset. ③ *Privacy* - if the synthetic data is not copied from the real records, we employ the Distance to Closest Record (DCR) metric. We defer the full description of the metrics to Appendix A.6.

Notably, previous works (Borisov et al., 2023; Seedat et al., 2024) on evaluating LLMs for tabular data generation focus only on Machine Learning Utility and Privacy protection. Our paper fills this gap by providing the first comprehensive evaluation

of LLMs' ability on tabular data synthesis.

5.2 TABGEN-ICL outperforms LLM-based baseline methods

As shown in Table 1, TABGEN-ICL consistently outperforms existing LLM-based approaches on fidelity metrics, including both the training-free method CLLM and the fine-tuning-based method GREAT. Specifically, with GPT-4o-mini, TABGEN-ICL achieves fidelity improvements ranging from 3.5% to 42.2%; with GPT-40, the gains range from 1.6% to 34.1% across various metrics. The most significant improvements are observed in Recall, with increases of 42.2% for GPT-4o-mini and 34.1% for GPT-40. Recall quantifies how well the synthetic data covers the diversity of the real data distribution. Thus, improvements in Recall indicate enhanced diversity in the generated samples. This substantial gain is primarily attributed to TABGEN-ICL 's residual-based sampling strategy, which identifies underrepresented regions of the data distribution at each prompt iteration and targets them in subsequent generations. By iteratively refining generation based on residuals, TABGEN-ICL effectively enhances coverage and diversity, validating the utility of its residual-aware mechanism.

Method	California AUC↑	Adult AUC↑	Shoppers AUC↑	Magic AUC↑	Default AUC↑				
Real	0.999	0.927	0.926	0.946	0.770				
VAE-based									
TVAE (Xu et al., 2019)	0.986	0.846	0.898	0.912	0.744				
GAN-based									
CTGAN (Xu et al., 2019)	0.925	0.874	0.868	0.874	0.736				
Diffusion-based									
STaSy (Kim et al., 2023)	0.997	0.903	0.909	0.923	0.749				
CoDi (Lee et al., 2023)	0.981	0.829	0.855	0.930	0.497				
TabDDPM (Kotelnikov et al., 2023)	0.992	0.911	0.915	0.933	0.763				
TabSyn (Zhang et al., 2024)	0.993	0.904	0.913	0.934	0.764				
Autor	egressive M	Models							
RTF (Solatorio and Dupriez, 2023)	0.948	0.925	_	0.931	0.764				
TabMT (Gulati and Roysdon, 2023)	0.988	0.873	0.912	0.822	0.714				
Ĺ	LM-Finetune	ed							
GReaT (Borisov et al., 2023)	0.996	0.913	0.902	0.888	0.755				
LLM-Prompt-Only									
CLLM w. GPT-4o-mini	0.840	0.879	0.708	0.826	0.557				
TABGEN-ICL w. GPT-4o-mini (Ours)	0.947	0.894	0.792	0.891	0.628				
Improvement	12.7 %	1.7 %	11.9 %	7.9 %	$\boldsymbol{12.7\%}$				
CLLM w. GPT-4o	0.947	0.891	0.865	0.885	0.718				
TABGEN-ICL w. GPT-40 (Ours)	0.975	0.892	0.879	0.903	0.713				
Improvement	3.0 %	0.1 %	1.4 %	1.8%	0.5 %				

Table 2: **Utility comparison**: AUC scores of Train-on-synthetic-Test-on-real (TSTR) XGBoost model predicting the target column of each table. ↑ indicates the higher the better. − indicates training failure.

5.3 TABGEN-ICL outperforms deep generative models under data-scarcity

One important application of tabular data synthesis is addressing data scarcity. In many cases, we have access to only a limited number of real data points, yet we require a much larger dataset to adequately train our downstream models. To generate sufficient training data, generative models can be employed. In our experiments, we evaluate the performance of TABGEN-ICL in comparison with other deep generative models under data-scarce conditions. To simulate such scenarios, we created training sets by randomly sampling 100, 500, 1000, 2000, and 3000 rows from the Default dataset. The generative models were then trained on these subsets, and the quality of the synthesized data was evaluated using the original full training set of 30,000 rows.

As shown in Figure 3, deep generative models such as TVAE, CTGAN, and TabDDPM exhibit substantial performance degradation and instability when trained on limited data. In contrast, TABGEN-ICL and CLLM maintain performance levels comparable to those achieved in the full-data setting, benefiting from the strong prior knowledge

encoded in large language models (LLMs). Notably, the performance of TABGEN-ICL closely aligns with that of CLLM in low-resource scenarios. This is because, when the dataset is small, the entire training set can be used as in-context examples, rendering the residual-aware sampling strategy effectively equivalent to random sampling.

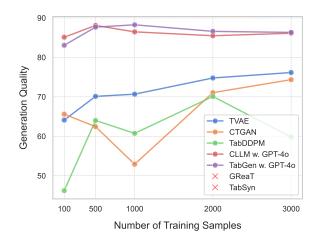


Figure 3: **Quality comparison under data scarcity.** Under the few-shot setting, TABGEN-ICL and CLLM achieve the highest quality scores, demonstrating strong generation capabilities with limited data. In contrast, TabSyn and GReaT fail to produce meaningful outputs.

5.4 TABGEN-ICL Does Not Copy Training Data

In Figure 4, we compare the distribution of L2 distances, also referred to as DCR scores, between synthetic samples and both the training and heldout datasets for CLLM, GReaT, REaLTabFormer, and TABGEN-ICL. Ideally, DCR scores should be larger than zero, and their distribution relative to the training set should closely match that of the holdout set, indicating low risk of data memorization. Among the models evaluated, GReaT achieves the most favorable profile: its DCR scores remain far from zero, and the distance distributions to the training and holdout sets are well-aligned, suggesting minimal copying. Both TABGEN-ICL and CLLM also show nearly overlapping DCR distributions between the training and holdout sets, further indicating that they do not overfit or memorize training data. In contrast, REaLTabFormer exhibits more divergent distributions between the two sets, which implies a greater tendency to rely on or replicate training data, raising concerns about potential memorization.

5.5 Ablation Study

Effect of d. We examine the effect of the distribution distance metric d used for quantifying residual in Equation 2. We test TABGEN-ICL (w. GPT-4omini) with only KSD or JSD metric and compare it with our alternating strategy (KSD+JSD) on the California dataset. As shown in Table 3, the alternating strategy achieves the best performance.

d	KSD	JSD	KSD+JSD
	$92.43_{\pm 0.005}$		
Corr.	$88.41_{\pm 0.022}$	$90.67_{\pm 0.021}$	$91.24{\scriptstyle\pm0.016}$

Table 3: Ablation study for d.

Effect of Large Language Models. In this section, we investigate the impact of large language model (LLM) capabilities on TABGEN-ICL's performance. We evaluate TABGEN-ICL using LLMs of varying parameter sizes, including Gemini-1.5-Flash, Gemini-1.5-Pro (Team et al., 2023), Claude-3-Haiku and Claude-3-Sonnet (cla). We assess the average of the marginal and the correlation metrics on the California dataset, with results presented in Table 4. Our findings reveal a correlation between LLM capacity and synthetic data generation quality. As the LLMs' capacity increases, the quality of

generated synthetic data improves. We hypothesize that this improvement stems from larger models' enhanced ability to capture and reproduce complex patterns within the data, resulting in more realistic synthetic outputs. This relationship underscores the importance of model capacity in generating high-quality synthetic data.

Model		Rank
GPT-4o-mini	91.86 ± 0.008	3
GPT-4o	$94.69{\scriptstyle\pm0.006}$	1
Gemini-1.5-Flash	89.96 ± 0.017	4
Gemini-1.5-Pro	$92.21_{\pm 0.033}$	2
Claude-3-Haiku	$89.17_{\pm 0.031}$	5
Claude-3-Sonnet	$88.97 \scriptstyle{\pm 0.068}$	6

Table 4: Effect of large language models on the performance of TABGEN-ICL.

6 Conclusion

This work introduces TABGEN-ICL, an in-context learning (ICL) framework for tabular data generation using large language models (LLMs). By iteratively identifying and sampling from underrepresented regions in the data distribution, TABGEN-ICL effectively steers the LLM's prior toward the real data distribution. This residual-aware generation process enables more diverse and faithful synthetic samples. Extensive experiments validate the effectiveness of our approach across a variety of domains. A key strength of TABGEN-ICL lies in its ability to leverage the rich prior knowledge embedded in pre-trained LLMs, making it particularly valuable in practical scenarios where collecting large-scale datasets is costly or infeasible.

7 Limitations

While TABGEN-ICL demonstrates strong empirical performance, it is subject to several limitations. First, the method for computing *residual* samples is based on a simple heuristic search algorithm. This approach is efficient in practice but does not provide theoretical guarantees of optimality. One future direction is to develop more principled methods for residual computation, which may improve both the quality and consistency of the generated samples. Second, TABGEN-ICL currently relies on closed-source LLMs (e.g., GPT-40) as the backbone model. While those models offer powerful exhibits of strong performance, they introduce significant computational overhead. This reliance may

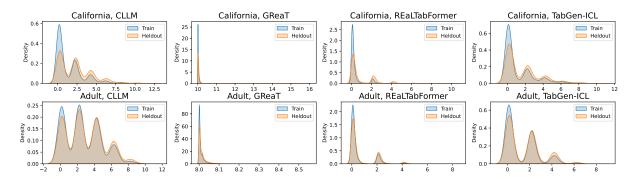


Figure 4: **Privacy comparison**: Distributions of the DCR scores between the synthetic dataset and the training/hold-out datasets. TABGEN-ICL and Curated-LLM (CLLM) are both employed with GPT-40-mini.

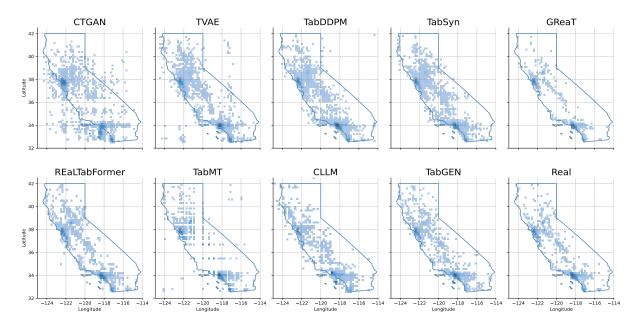


Figure 5: **Visual comparison**: 2D scatter plot of Longitude and Latitude attributes of California dataset. Real represents the original training datasets. All sets are downsampled to 3000 rows for better visualization. TABGENICL generates spatially coherent synthetic data that closely matches the distribution of the original dataset.

limit the scalability and deployment of TABGEN-ICL in time-sensitive or resource-constrained environments. A promising direction for future work is to replace GPT-40 with lighter-weight models with lower inference latency.

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A Appendix

A.1 Prompts used for generating tabular data

This prompt template is used in Section 4 to generate realistic data that follows the same distribution as the given real data.

```
ı You are a synthetic data generator tasked with creating new tabular data samples
      that closely mirror the distribution and characteristics of the original dataset
3 # Instruction
4 1. Analyze the provided real samples carefully.
5 2. Generate synthetic data that maintains the statistical properties of the real
6 3. Ensure all attributes cover their full expected ranges, including less common or
      extreme values.
	au 4. Maintain the relationships and correlations between different attributes.
8 5. Preserve the overall distribution of the real data while introducing realistic
      variations.
10 # Key points to consider
- Replicate the data types of each column (e.g., numerical, categorical).
- Match the range and distribution of numerical attributes.
13 - Maintain the frequency distribution of categorical attributes.
14 - Reflect any patterns or trends present in the original data.
15 - Introduce realistic variability to avoid exact duplication.
17 # Real samples
18 {data}
20 # Output format:
21 Please present the generated data in a JSON format, structured as a list of objects,
  where each object represents a single data point with all attributes.
```

A.2 Dummy Prompt

The following prompt only contains the column names, but not any actual data in it. It is used to produce the results in Fig.1 (a).

```
You are a synthetic data generator tasked with creating new tabular data samples that closely mirror the distribution and characteristics of the original dataset.

Generate 50 samples of synthetic data.

Each sample should include the following attributes:

{attributes_list}

Make sure that the numbers make sense for each attribute.

Output Format:

Present the generated data in a JSON format, structured as a list of objects, where each object represents a single data point with all attributes.
```

A.3 JSON Schema

The following code define the JSON data class for the structured output function of GPT-4o and GPT-4o-mini

```
def create_json_model(df: pd.DataFrame, dataname=None) -> BaseModel:
    fields = {}

for column in df.columns:
        if df[column].dtype == 'object':
            fields[column] = (str, ...)
        elif df[column].dtype == 'int64':
            fields[column] = (int, ...)
    elif df[column].dtype == 'float64':
            fields[column] = (float, ...)
```

```
elif df[column].dtype == 'bool':
12
               fields[column] = (bool, ...)
13
               raise TypeError(f"Unexpected dtype for column {column}: {df[column].
      dtype }")
15
      JSONModel = create_model(dataname, **fields)
16
17
      class JSONListModel(BaseModel):
18
          JSON: List[JSONModel]
19
20
      return JSONListModel
```

A.4 Heuristic for computing residual

In this section, we provide the pseudo-code of our heuristic strategy for computing the residual.

Algorithm 1 Compute residual

Require: current dataset X, target dataset Y, distribution distance d.

- 1: Randomly select a column index j
- 2: **if** column j is categorical **then**
- 3: Let C_j be the number of categories in column j
- 4: Group samples in Y into C_j number of subsets based on its category on column j, denote the set of subsets by $(Y_i^i)_{i=1}^{C_j}$
- 5: **else**
- 6: Quantize column i into 50 bins
- 7: $C_j \leftarrow 50$
- 8: Group samples in Y into C_j number of subsets based on its bin index on column j, denote the set of subsets by $(Y_i^i)_{i=1}^{C_j}$
- 9: end if
- 10: **for** i = 1 to C_j **do**
- 11: Compute distance between $Y_i^i \cup X$ and $Y: d_i = d(Y_i^i \cup X, Y)$
- 12: end for
- 13: **return** subset Y_i^i that attains the minimal distance.

A.5 Datasets

We use five real-world datasets of varying scales, and all of them are available at Kaggle² or the UCI Machine Learning repository³. We consider five datasets containing both numerical and catergorical attributes: California⁴, Magic⁵, Adult⁶, Default⁷, Shoppers⁸. The statistics of these datasets are presented in Table 5.

A.6 Evaluation Metrics

Fidelity To evaluate if the generated data can faithfully recover the ground-truth data distribution, we employ the following metrics: 1) **Marginal distribution:** The Marginal metric evaluates if each column's marginal distribution is faithfully recovered by the synthetic data. We use Kolmogorov-Sirnov Test for continuous data and Total Variation Distance for discrete data. 2) **Pair-wise column correlation:** This metric evaluates if the correlation between every two columns in the real data is captured by the synthetic

```
<sup>2</sup>https://www.kaggle.com/
```

https://archive.ics.uci.edu/

⁴https://www.kaggle.com/datasets/camnugent/california-housing-prices

⁵https://archive.ics.uci.edu/dataset/159/magic+gamma+telescope

⁶https://archive.ics.uci.edu/dataset/2/adult

⁷https://archive.ics.uci.edu/dataset/350/default+of+credit+card+clients

⁸https://archive.ics.uci.edu/dataset/468/online+shoppers+purchasing+intention+dataset

Table 5: Statistics of datasets. # Num stands for the number of numerical columns, and # Cat stands for the number of categorical columns.

Dataset	# Rows	# Num	# Cat	# Train	# Test
California Housing	20,640	9	1	18,390	2,250
Magic Gamma Telescope	19,021	10	1	17,118	1,903
Adult Income	32,561	6	8	22,792	9,769
Default of Credit Card Clients	30,000	14	10	27,000	3,000
Online Shoppers Purchase	12,330	10	7	11,098	1,232

data. We compute the Pearson Correlation between all pairs of columns then take average. In addition, we present joint density plots for the Longitude and Latitude features in the California Housing data set in Figure 5. 3) Classifier Two Sample Test (C2ST): This metric evaluates how difficult it is to distinguish real data from synthetic data. Specifically, we create an augmented table that has all the rows of real data and all the rows of synthetic data. Add an extra column to keep track of whether each original row is real or synthetic. Then we train a Logistic Regression classifier to distinguish real and synthetic rows. 4) Precision and Recall: Precision measures the quality of generated samples. High precision means the generated samples are realistic and similar to the true data distribution. Recall measures how much of the true data distribution is covered by the generated distribution. High recall means the model captures most modes/variations present in the true data. 5) Jensen-Shannon Divergence (JSD): This metric evaluates the Jensen-Shannon divergence (Nielsen, 2019) between the distributions of real data and synthetic data.

Utility We evaluate the utility of the generated data by assessing their performance in Machine Learning Efficiency (MLE). Following the previous works (Zhang et al., 2024), we first split a real table into a real training and a real testing set. The generative models are trained on the real training set, from which a synthetic set of equivalent size is sampled. This synthetic data is then used to train a classification/regression model (XGBoost Classifier and XGBoost Regressor (Chen and Guestrin, 2016)), which will be evaluated using the real testing set. The performance of MLE is measured by the AUC score for classification tasks and RMSE for regression tasks.

Privacy A high-quality synthetic dataset should accurately reflect the underlying distribution of the original data, rather than merely replicating it. To assess this, we employ the Distance to Closest Record (DCR) metric. We begin by splitting the real data into two equal parts: a training set and a holdout set. Using the training set, we generate a synthetic dataset. We then measure the distances between each synthetic data point and its nearest neighbor in both the training and holdout sets. In theory, if both sets are drawn from the same distribution, and if the synthetic data effectively captures this distribution, we should observe an equal proportion (around 50%) of synthetic samples closer to each set. However, if the synthetic data simply copies the training set, a significantly higher percentage would be closer to the training set, well exceeding the expected 50%.

A.7 Scalability of TABGEN-ICL

To evaluate the scalability of TABGEN-ICL, we compare TABGEN-ICL with CLLM on a large-scale dataset: Covertype dataset. This dataset consists of 581,012 instances and 54 features. TABGEN-ICL and CLLM use iterative in-context learning to generate samples, thus the running time of these two methods are agnostic to the size of the training dataset, making them scalable to large datasets. In the following table, we compare TABGEN-ICL with CLLM, employed with both GPT-40 mini and GPT-40.

Model	Marginal ↓	Corr↓	C2ST↓	Precision ↓	Recall ↓	JSD ↓	AUC ↑
CLLM w. GPT-40	3.28	10.70	55.67	32.32	1.95	0.6078	0.8822
TabGEN w. GPT-40	2.83	11.10	49.91	24.03	1.27	0.5109	0.9070
Improvement (%)	13.72 %	-	10.34 %	25.62 %	34.87 %	15.94 %	2.81 %
CLLM w. GPT-40 mini	5.35	13.70	0.7796	0.3225	0.0591	0.8743	0.7113
TabGEN w. GPT-40 mini	5.09	12.62	0.7554	0.2876	0.0436	0.9353	0.8311
Improvement (%)	$\boldsymbol{4.86\%}$	7.88 %	3.11 %	10.81 %	26.25 %	-	16.86 %

The results demonstrate that TABGEN-ICL outperforms CLLM on most of the metrics. Notably, the Recall metric again shows the greatest improvement: 34.85% on GPT-40 and 26.25% on GPT-40 mini. This observation is consistent with our original findings in Sec. 5.2. We believe these results strongly support TABGEN-ICL's scalability to larger, more complex datasets.