KNOWSHIFTQA: How Robust are RAG Systems when Textbook Knowledge Shifts in K-12 Education?

Tianshi Zheng*♠, Weihan Li*♣, Jiaxin Bai♠, Weiqi Wang♠, Yangqiu Song♠
♠Department of Computer Science and Engineering, HKUST, Hong Kong SAR, China
♣Department of Mechanical Engineering, The University of Tokyo, Tokyo, Japan
tzhengad@connect.ust.hk

Abstract

Retrieval-Augmented Generation (RAG) systems show remarkable potential as question answering tools in the K-12 Education domain, where knowledge is typically queried within the restricted scope of authoritative textbooks. However, discrepancies between these textbooks and the parametric knowledge inherent in Large Language Models (LLMs) can undermine the effectiveness of RAG systems. To systematically investigate RAG system robustness against such knowledge discrepancies, we introduce **KNOWSHIFTQA**¹. This novel question answering dataset simulates these discrepancies by applying deliberate hypothetical knowledge updates to both answers and source documents, reflecting how textbook knowledge can shift. KNOWSHIFTQA comprises 3,005 questions across five subjects, designed with a comprehensive question typology focusing on context utilization and knowledge integration. Our extensive experiments on retrieval and question answering performance reveal that most RAG systems suffer a substantial performance drop when faced with these knowledge discrepancies. Furthermore, questions requiring the integration of contextual (textbook) knowledge with parametric (LLM) knowledge pose a significant challenge to current LLMs.

1 Introduction

In K-12 education, Question Answering (QA) systems serve as an important resource for learning assistance, where answers are precisely provided within a restricted knowledge scope from authoritative sources (i.e., textbooks) (Raamadhurai et al., 2019; Soares et al., 2021). Meanwhile, benefiting from the emergent abilities (Wei et al., 2022) of Large Language Models (LLMs) and advanced information retrieval (IR) methods,

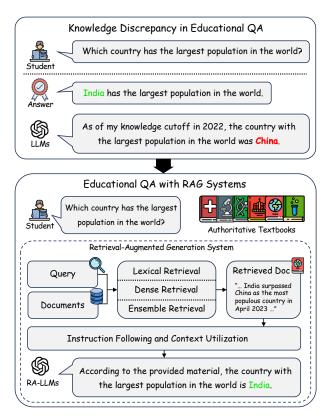


Figure 1: An illustration of knowledge discrepancy in educational QA and the application of RAG systems.

Retrieval-Augmented Generation (RAG) systems have achieved remarkable performance in various knowledge-intensive tasks in natural language processing (Lewis et al., 2020; Jiang et al., 2023; Gao et al., 2024), demonstrating their great potential as QA systems in K-12 education (Gan et al., 2023; Kasneci et al., 2023; Yan et al., 2024).

In K-12 educational QA, one of the primary concerns is ensuring that the knowledge conveyed in the answer is consistent with the officially designated textbooks (Extance, 2023). However, notable knowledge shifts (i.e. factuality discrepancies) may exist between the knowledge in textbooks and the internal knowledge of LLMs, due to the evolving nature of facts (Arbesman, 2012), updates in peda-

^{*} Equal Contribution

¹https://github.com/HKUST-KnowComp/KnowShiftQA

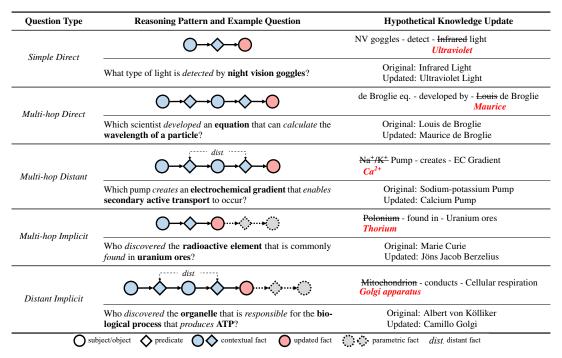


Table 1: Five question types in KNOWSHIFTQA with their reasoning patterns, example questions, and hypothetical knowledge update illustrated in factual triplets and answers. In example questions, subjects and objects are marked in **bold**, while predicates are marked in *italic*.

gogical approaches (Provenzo et al., 2011), as well as regional and cultural variations in content (Patel, 2015). It remains unclear whether RAG systems can robustly incorporate knowledge from authoritative sources and generate consistent answers under such knowledge discrepancies (scenario illustrated in Figure 1).

To fill this gap, we aim to systematically assess the robustness of RAG systems in performing question answering in K-12 education when encountering knowledge shifts. We present KNOWSHIFTQA, a new dataset containing 3,005 multiple-choice questions covering the subjects of Physics, Chemistry, Biology, Geography, and History from the middle-school curriculum. To simulate the factuality discrepancy between LLMs and textbooks, we conduct a hypothetical knowledge update, in which we modify the original factual knowledge from the textbooks into plausible alternatives while maintaining coherent and consistent context. Moreover, we tailored a comprehensive question typology to stress-test the context utilization and knowledge integration abilities of LLMs under such scenarios.

We conducted extensive experiments with various retrieval methods and LLMs. Our findings indicate that most RAG systems exhibit a considerable performance degradation under knowledge

shifts. Notably, while many LLMs can effectively incorporate distant contextual facts, they struggle to seamlessly integrate their parametric knowledge with this contextual information. In terms of retrieval, traditional lexical-based methods demonstrate advantages due to the specificity of academic terms; their performance can be further enhanced through an ensemble re-ranking mechanism. Supervised retrieval methods (e.g., Contriever), when fine-tuned directly on our dataset, yield superior performance. Overall, our results highlight the fragility of current RAG systems under knowledge shifts and the challenges LLMs face in effectively combining contextual and parametric knowledge for complex question answering.

2 The KNOWSHIFTQA Dataset

In this section, we introduce the methodology of hypothetical knowledge update and the design of our question typology. The curation pipeline and detailed statistics of the KNOWSHIFTQA dataset are provided in Appendix B and E, respectively.

2.1 Hypothetical Knowledge Update

One of the core objectives of our dataset is to simulate the knowledge discrepancy between LLMs and authoritative textbooks when performing educational QA. However, such discrepancies are often

fuzzy and highly sparse in real-world data, making it infeasible to collect and organize. Consequently, we designed the methodology of hypothetical knowledge update, performing it on highquality open-source textbooks. The general procedures are as follows: 1) Curate factual questions from textbook paragraphs following our designed question typology. 2) Select a plausible but factually incorrect answer as the updated ground-truth answer. 3) Replace all occurrences of the original answer in the paragraph with the updated answer and adjusted other relevant statements in the context to ensure that the updated paragraph is coherent and consistent. This process is further guaranteed through extensive human curation and verification. Examples of hypothetical knowledge updates in our dataset are provided in Appendix D.

2.2 Question Typology

We identify two potential challenges for LLMs when performing QA under knowledge shifts: 1) Context Utilization: Whether LLMs can identify and utilize the corresponding facts from the context; and 2) Knowledge Integration: Whether LLMs can incorporate their own parametric knowledge with contextual facts in question answering. To this end, we designed our question typology, as illustrated in Table 1, to investigate such abilities. The two basic question types, Simple Direct and Multi-hop Direct, aim to evaluate LLMs on simple factual recall and multi-hop reasoning. Based on these two types, we developed the Multi-hop Distant type to evaluate the context utilization ability for distant facts from the passage, and the Multi-hop Implicit² type to evaluate the knowledge integration ability that combines their own factual knowledge with retrieved facts. Moreover, the Distant Implicit type poses a greater challenge by combining both features. To ensure our evaluation of knowledge integration ability is independent of knowledge coverage, we restrict the facts requiring LLMs' own knowledge to be head-knowledge only (Sun et al., 2024).

3 Experiments and Analyses

Typically, RAG systems first conduct document retrieval based on given queries, then perform question answering with LLMs based on the retrieved information loaded in the context. In this section,

| Retrieval Methods | Category | R@1 | R@5 |
|-----------------------------------|---------------|-------|-------|
| TF-IDF (Spärck Jones, 1972) | Lexical | 65.82 | 88.72 |
| BM25 (Robertson et al., 1994) | Lexical | 82.73 | 95.27 |
| SPLADE (Formal et al., 2021) | Lexical/Dense | 78.04 | 90.12 |
| Contriever (Izacard et al., 2022) | Dense | 53.18 | 81.80 |
| Conmsmarco (Izacard et al., 2022) | Dense | 76.17 | 93.54 |
| Mistral-embed (Mistral, 2023a) | Dense | 78.74 | 95.31 |
| Ada-002 (OpenAI, 2022) | Dense | 79.23 | 95.44 |
| Query Rewrite (Ma et al., 2023) | Pre-Retrieval | 78.87 | 94.21 |
| Hybrid Rerank (BM25 + Ada-002) | Ensemble | 84.43 | 96.04 |
| Contriever (fine-tuned) | Dense+FT | 84.19 | 98.96 |
| Conmsmarco (fine-tuned) | Dense+FT | 87.95 | 99.50 |

Table 2: Document retrieval performances (in recall @ 1/5 %) of retrieval methods from different categories in the KNOWSHIFTQA dataset. The highest scores are marked as **bold**, while the 2nd and 3rd-best scores are <u>underlined</u>. The retrieval granularity is set to paragraph.

we comprehensively evaluate and analyze the performance of retrieval methods and LLMs on the KNOWSHIFTQA dataset. For details of all tested methods and models, please refer to Appendix C.

3.1 Retrieval Performance

Experimental results of the retrieval methods are presented in Table 2. Traditional lexical retrieval methods, such as BM25, demonstrated strong performance on our dataset, while dense retrieval methods, such as Mistral-embed and Ada-002, achieved comparable performance. Since our dataset focuses on the K-12 education domain, lexical retrieval effectively captures domain-specific keywords in the queries and identifies the corresponding documents. This characteristic underscores the need for fine-tuning dense retrieval models on our dataset. To this end, we fine-tuned both Contriever and Contriever-msmarco on our documents, resulting in significant improvements and highlighting the importance of corpus-specific finetuning in educational document retrieval.

Moreover, ensemble methods have demonstrated their effectiveness in various information retrieval tasks (Thakur et al., 2021). We implemented a hybrid approach that retrieves the top k^3 documents with Ada-002, followed by re-ranking with BM25. This ensemble method marginally improved the retrieval performance in both metrics. Conversely, query rewriting⁴ (Ma et al., 2023) implemented upon BM25 did not yield performance gains. Detailed results across subjects and question types are provided in Appendix F.

²The word 'implicit' indicates that the questions indirectly query the updated facts by embedding them within the middle of the multi-hop reasoning chain.

³We use k = 6 as the optimal hyperparameter setting.

⁴We use Mistral-small-2409 as the LLM query rewriter.

| Large Language Models | | | Question Typolog | y | | Average |
|--------------------------------------|---------------|------------------|-------------------|--------------------|------------------|---------|
| | Simple Direct | Multi-hop Direct | Multi-hop Distant | Multi-hop Implicit | Distant Implicit | |
| Mistral-7b (Mistral, 2023b) | 77.70 | 69.31 | 72.74 | 45.32 | 33.98 | 61.26 |
| Mixtral-8x22b (Mistral, 2023c) | 84.10 | 84.58 | 87.15 | 73.86 | 65.37 | 79.67 |
| Mistral-small-2409 (Mistral, 2024a) | 87.87 | 88.70 | 89.69 | 72.18 | 60.81 | 80.77 |
| Mistral-large-2407 (Mistral, 2024b) | 83.93 | 83.51 | 87.29 | 82.25 | 70.57 | 81.66 |
| Gemini-1.5-flash (Google, 2024a) | 80.98 | 82.44 | 87.57 | 76.02 | 63.25 | 78.54 |
| Gemini-1.5-pro (Google, 2024b) | 86.56 | 87.63 | 88.42 | 76.26 | 63.58 | 81.10 |
| Llama3-8b (Meta, 2024) | 90.33 | 88.85 | 89.69 | 63.55 | 49.43 | 77.77 |
| Llama3-70b (Meta, 2024) | 96.72 | 96.49 | 96.89 | 79.14 | 63.25 | 87.42 |
| GPT-3.5-turbo (OpenAI, 2022) | 92.62 | 90.53 | 91.24 | 71.22 | 57.72 | 81.73 |
| GPT-4 (OpenAI, 2023a) | 89.51 | 89.47 | 90.68 | 78.66 | 70.89 | 84.46 |
| GPT-4-turbo (OpenAI, 2023b) | 95.74 | 96.18 | 96.19 | 81.06 | 71.71 | 88.99 |
| GPT-4o (OpenAI, 2024a) | 91.97 | 94.81 | 93.64 | 81.29 | 70.41 | 87.09 |
| Claude-3-sonnet (Anthropic, 2024a) | 94.59 | 92.82 | 93.64 | 77.70 | 60.65 | 84.69 |
| Claude-3.5-sonnet (Anthropic, 2024b) | 97.54 | 96.49 | 95.62 | 83.69 | 73.82 | 90.08 |
| o1-mini (OpenAI, 2024b) | 95.90 | 95.73 | 97.03 | 85.85 | 75.45 | 90.55 |
| o1-preview (OpenAI, 2024b) | 95.08 | 97.71 | 97.46 | 86.33 | 78.86 | 91.68 |

Table 3: Question answering performances (in accuracy %) of LLMs in the KNOWSHIFTQA benchmark with corresponding documents provided. The highest scores are marked as **bold**, while the 2nd and 3rd-best scores are <u>underlined</u>. All LLMs are tested under zero-shot settings, with a *Locate-and-Answer* prompting approach that facilitates active information acquisition from contextual documents, with details in Appendix G.

| RAG System | Hypothetica | Drop | |
|---------------------|-------------|-------|-------|
| - | Before | After | |
| Llama3-8b + Ada-002 | 87.49 | 62.60 | 24.89 |
| Llama3-8b + Rerank | 88.49 | 66.02 | 22.47 |
| GPT-40 + Ada-002 | 96.57 | 69.65 | 26.92 |
| GPT-40 + Rerank | 97.10 | 73.71 | 23.39 |

Table 4: Performance drop of RAG systems with hypothetical knowledge updates in our benchmark.

3.2 Question Answering Performance

Experimental results of LLMs in question answering are presented in Table 3. Most LLMs exhibited comparable performance for question types Simple Direct, Multi-hop Direct, and Multi-hop Distant. This suggests that both multi-hop reasoning and distant context utilization do not pose significant challenges for modern LLMs. However, for Multi-hop Implicit questions, which requires the integration of contextual and internal knowledge, a substantial performance disparity emerges between smaller open-source LLMs and advanced models. This disparity is further amplified for *Distant Im*plicit questions, where the reasoning chains are getting more complexed. The most capable model we tested, o1-preview, attains over 80% accuracy on Implicit questions, whereas Mistral-7b's performance falls below 40%. These findings indicate that context-memory knowledge integration is an emergent capability presenting greater difficulties for LLMs under knowledge discrepancies, particularly when coupled with the need for distant context utilization.

3.3 Overall Performance

How do knowledge shifts affect the performance of RAG systems in educational question-answering applications? To answer this question, we selected two representative LLMs: Llama3-8b from open-source models and GPT-4o from proprietary models. These were combined with two highperforming retrieval methods: Ada-002 and hybrid rerank. The resulting RAG systems were tested on questions *before* and *after* hypothetical knowledge updates, with the results presented in Table 4. We observed a significant accuracy drop of 22–27% after these knowledge shifts, indicating substantial performance degradation in modern RAG systems when faced with such scenarios.

4 Related Work

Retrieval-Augmented Generation Following the categorization by Gao et al. (2024), the RAG methods employed in our experiment fall into the categories of *Naive RAG* (lexical, dense) and *Advanced RAG* (rerank, rewrite). Recently, *Modular RAG* has emerged to enhance the adaptability and versatility of RAG systems (Shao et al., 2023; Asai et al., 2023). Furthermore, recent advances in vector databases (Han et al., 2023) and neural graph databases (Bai et al., 2025) highlight the potential for adaptive and generalizable RAG search with structured data (Deng et al., 2024).

Educational Question Answering Prior to the emergence of RAG systems utilizing LLMs, various educational QA systems were developed to provide pedagogically appropriate responses to student inquiries (Abdi et al., 2018; Agarwal et al., 2019). While recent literature explores LLM applications in QA and learning assistance roles (Nye et al., 2023; Kuo et al., 2023; Wang et al., 2024), it is also crucial to leverage logical inference abilities, such as abductive reasoning (Bai et al., 2024; Yim et al., 2024; Zheng et al., 2025) and inductive reasoning (Qiu et al., 2024; Li et al., 2025; Zheng et al., 2025a), for understanding students' learning outcomes in response to their queries.

Knowledge Discrepancy in LLMs Mitigating knowledge discrepancies or conflicts within LLM applications is a fundamental challenge in LLM research (Xu et al., 2024). Researchers have proposed tuning-based (Li et al., 2022) and prompting-based (Zhou et al., 2023) methods to enhance LLMs' robustness to such conflicts. However, the implications of these conflicts in educational applications and RAG systems remain relatively underexplored. Moreover, it is important to consider the trade-off between factuality robustness (Yu et al., 2024; Zong et al., 2024; Zheng et al., 2025c) and flexibility in instruction following when such discrepancies are present.

5 Conclusion

This paper systematically evaluates the robustness of RAG systems in K-12 educational question answering under knowledge discrepancies using a comprehensive dataset KNOWSHIFTQA. Experimental findings reveal substantial performance degradation in RAG systems when faced with knowledge discrepancies, which is primarily attributed to deficiencies in incorporating contextual and parametric knowledge in question answering—an emergent and challenging ability for modern large language models.

Limitations

We discuss three main limitations of our work.

First, KNOWSHIFTQA employs the approach of hypothetical knowledge updates to effectively simulate real-world knowledge discrepancies for two primary reasons: (1) Real-world knowledge conflicts are often sparse, noisy, and difficult to systematically collect or organize into a cohesive

dataset suitable for large-scale evaluation. Hypothetical updates provide a scalable and controlled alternative, allowing us to bypass these limitations. (2) By leveraging a systematic annotation and curation pipeline, we can generate questions with diverse and well-defined reasoning patterns that align with our typology, enabling more robust evaluation of complex question-answering tasks. For future research centered on real-world knowledge discrepancies, we recommend an alternative methodology that incorporates temporal attributes (Chen et al., 2021; Zhang and Choi, 2024). This approach focuses on identifying outdated facts and capturing time-sensitive data (e.g., economic trends, annual events, or societal changes) to construct datasets that reflect real-world knowledge updates. While promising, this method is constrained by the limited overlap between time-sensitive data—often numerical or attribute-specific—and the broader contextual needs of educational question-answering tasks, which may reduce the comprehensiveness of the resulting datasets.

Next, regarding document retrieval, some recent hierarchical retrieval paradigms, such as GraphRAG (Edge et al., 2024) and HippoRAG (Gutiérrez et al., 2024), are not included in our experiments due to their implementation complexity. However, we believe that such structured paradigms could effectively enhance retrieval performance in our scenario, as educational documents are well-structured and contain high-quality factual knowledge.

Finally, this paper primarily evaluates the robustness of RAG systems in the proposed scenario, with experiments conducted using various retrieval methods and large language models. Potential improvements could be achieved through the design of tailored reasoning frameworks via prompting, in-context learning or alignment in LLMs, which we leave for future research.

Ethics Statement

In constructing the KNOWSHIFTQA dataset, we collected text from open-access textbooks. Detailed sources and licenses are provided in Appendix A. The human curation and verification in our annotation pipeline were carried out by a group of postgraduate students with extensive experience in NLP research. We ensured that the updated knowledge is free from harmful or toxic content. It is important to note that our dataset

is designed solely to evaluate the robustness of Retrieval-Augmented Generation systems under scenarios with knowledge discrepancies and is not suitable for assessing the factual accuracy of QA systems.

Acknowledgments

The authors of this paper were supported by the ITSP Platform Research Project (ITS/189/23FP) from ITC of Hong Kong, SAR, China, and the AoE (AoE/E-601/24-N), the RIF (R6021-20) and the GRF (16205322) from RGC of Hong Kong SAR, China.

References

- Asad Abdi, Norisma Idris, and Zahrah Ahmad. 2018. Qapd: an ontology-based question answering system in the physics domain. *Soft Computing*, 22:213–230.
- A. Agarwal, N. Sachdeva, R. K. Yadav, V. Udandarao, V. Mittal, A. Gupta, and A. Mathur. 2019. Eduqa: Educational domain question answering system using conceptual network mapping. In *ICASSP* 2019 2019 IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP), pages 8137–8141.
- Anthropic. 2024a. Blog: Introducing the next generation of claude.
- Anthropic. 2024b. Introducing claude 3.5 sonnet.
- S. Arbesman. 2012. *The Half-life of Facts: Why Everything We Know Has an Expiration Date*. Human body. Current.
- Akari Asai, Zeqiu Wu, Yizhong Wang, Avirup Sil, and Hannaneh Hajishirzi. 2023. Self-rag: Learning to retrieve, generate, and critique through self-reflection.
- Jiaxin Bai, Yicheng Wang, Tianshi Zheng, Yue Guo, Xin Liu, and Yangqiu Song. 2024. Advancing abductive reasoning in knowledge graphs through complex logical hypothesis generation.
- Jiaxin Bai, Zihao Wang, Yukun Zhou, Hang Yin, Weizhi Fei, Qi Hu, Zheye Deng, Jiayang Cheng, Tianshi Zheng, Hong Ting Tsang, Yisen Gao, Zhongwei Xie, Yufei Li, Lixin Fan, Binhang Yuan, Wei Wang, Lei Chen, Xiaofang Zhou, and Yangqiu Song. 2025. Top ten challenges towards agentic neural graph databases.
- Jiaxin Bai, Tianshi Zheng, and Yangqiu Song. 2023. Sequential query encoding for complex query answering on knowledge graphs.
- Wenhu Chen, Xinyi Wang, and William Yang Wang. 2021. A dataset for answering time-sensitive questions.

- Zheye Deng, Chunkit Chan, Weiqi Wang, Yuxi Sun, Wei Fan, Tianshi Zheng, Yauwai Yim, and Yangqiu Song. 2024. Text-tuple-table: Towards information integration in text-to-table generation via global tuple extraction.
- Darren Edge, Ha Trinh, Newman Cheng, Joshua Bradley, Alex Chao, Apurva Mody, Steven Truitt, and Jonathan Larson. 2024. From local to global: A graph rag approach to query-focused summarization.
- Andy Extance. 2023. ChatGPT has entered the classroom: how LLMs could transform education. *Nature*, 623:474–477.
- Thibault Formal, Carlos Lassance, Benjamin Piwowarski, and Stéphane Clinchant. 2021. Splade v2: Sparse lexical and expansion model for information retrieval.
- Wensheng Gan, Zhenlian Qi, Jiayang Wu, and Jerry Chun-Wei Lin. 2023. Large language models in education: Vision and opportunities.
- Yunfan Gao, Yun Xiong, Xinyu Gao, Kangxiang Jia, Jinliu Pan, Yuxi Bi, Yi Dai, Jiawei Sun, Meng Wang, and Haofen Wang. 2024. Retrieval-augmented generation for large language models: A survey.
- Google. 2024a. Gemini flash google deepmind.
- Google. 2024b. Gemini pro google deepmind.
- Bernal Jiménez Gutiérrez, Yiheng Shu, Yu Gu, Michihiro Yasunaga, and Yu Su. 2024. Hipporag: Neurobiologically inspired long-term memory for large language models.
- Yikun Han, Chunjiang Liu, and Pengfei Wang. 2023. A comprehensive survey on vector database: Storage and retrieval technique, challenge.
- Gautier Izacard, Mathilde Caron, Lucas Hosseini, Sebastian Riedel, Piotr Bojanowski, Armand Joulin, and Edouard Grave. 2022. Unsupervised dense information retrieval with contrastive learning.
- Zhengbao Jiang, Frank F. Xu, Luyu Gao, Zhiqing Sun, Qian Liu, Jane Dwivedi-Yu, Yiming Yang, Jamie Callan, and Graham Neubig. 2023. Active retrieval augmented generation.
- Enkelejda Kasneci, Kathrin Sessler, Stefan Küchemann, Maria Bannert, Daryna Dementieva, Frank Fischer, Urs Gasser, Georg Groh, Stephan Günnemann, Eyke Hüllermeier, Stephan Krusche, Gitta Kutyniok, Tilman Michaeli, Claudia Nerdel, Jürgen Pfeffer, Oleksandra Poquet, Michael Sailer, Albrecht Schmidt, Tina Seidel, Matthias Stadler, Jochen Weller, Jochen Kuhn, and Gjergji Kasneci. 2023. Chatgpt for good? on opportunities and challenges of large language models for education. *Learning and Individual Differences*, 103:102274.

- Bor-Chen Kuo, Frederic T. Y. Chang, and Zong-En Bai. 2023. Leveraging llms for adaptive testing and learning in taiwan adaptive learning platform (talp). In *Empowering Education with LLMs the Next-Gen Interface and Content Generation*, volume 3487, pages 1–14, Tokyo, Japan. CEUR Workshop Proceedings, CEUR-WS.org.
- Patrick Lewis, Ethan Perez, Aleksandra Piktus, Fabio Petroni, Vladimir Karpukhin, Naman Goyal, Heinrich Küttler, Mike Lewis, Wen-tau Yih, Tim Rocktäschel, et al. 2020. Retrieval-augmented generation for knowledge-intensive nlp tasks. *Advances in Neural Information Processing Systems*, 33:9459–9474.
- Chunyang Li, Weiqi Wang, Tianshi Zheng, and Yangqiu Song. 2025. Patterns over principles: The fragility of inductive reasoning in llms under noisy observations.
- Daliang Li, Ankit Singh Rawat, Manzil Zaheer, Xin Wang, Michal Lukasik, Andreas Veit, Felix Yu, and Sanjiv Kumar. 2022. Large language models with controllable working memory. *arXiv preprint arXiv:2211.05110*.
- Xinbei Ma, Yeyun Gong, Pengcheng He, Hai Zhao, and Nan Duan. 2023. Query rewriting for retrieval-augmented large language models.
- Meta. 2024. Introducing meta llama 3: The most capable openly available llm to date.
- Mistral. 2023a. Embeddings | mistral ai large language models.
- Mistral. 2023b. Mistral 7b | frontier ai in your hands.
- Mistral. 2023c. Mixtral of experts | frontier ai in your hands.
- Mistral. 2024a. Ai in abundance | mistral ai | frontier ai in your hands.
- Mistral. 2024b. Large enough | mistral ai | frontier ai in your hands.
- Benjamin D. Nye, Dillon Mee, and Mark G. Core. 2023. Generative large language models for dialog-based tutoring: An early consideration of opportunities and concerns. In *Empowering Education with LLMs the Next-Gen Interface and Content Generation*, volume 3487, pages 1–15, Tokyo, Japan. CEUR Workshop Proceedings, CEUR-WS.org.
- OpenAI. 2022. Chatgpt: Optimizing language models for dialogue.
- OpenAI. 2022. New and improved embedding model.
- OpenAI. 2023a. Gpt-4 technical report.
- OpenAI. 2023b. New models and developer products announced at devday.
- OpenAI. 2024a. Hello gpt-4o.
- OpenAI. 2024b. Introducing openai o1.

- Leigh Patel. 2015. *Decolonizing Educational Research:* From Ownership to Answerability, 1 edition. Routledge, New York.
- E.F. Provenzo, A.N. Shaver, and M. Bello. 2011. *The Textbook as Discourse: Sociocultural Dimensions of American Schoolbooks*. Taylor & Francis.
- Linlu Qiu, Liwei Jiang, Ximing Lu, Melanie Sclar, Valentina Pyatkin, Chandra Bhagavatula, Bailin Wang, Yoon Kim, Yejin Choi, Nouha Dziri, and Xiang Ren. 2024. Phenomenal yet puzzling: Testing inductive reasoning capabilities of language models with hypothesis refinement. In *The Twelfth International Conference on Learning Representations*.
- Srikrishna Raamadhurai, Ryan Baker, and Vikraman Poduval. 2019. Curio SmartChat: A system for natural language question answering for self-paced k-12 learning. In *Proceedings of the Fourteenth Workshop on Innovative Use of NLP for Building Educational Applications*, pages 336–342, Florence, Italy. Association for Computational Linguistics.
- Stephen E Robertson, Steve Walker, Susan Jones, Micheline Hancock-Beaulieu, and Mike Gatford. 1994. Okapi at trec-3. In *Overview of the Third Text REtrieval Conference (TREC-3)*. NIST.
- Zhihong Shao, Yeyun Gong, Yelong Shen, Minlie Huang, Nan Duan, and Weizhu Chen. 2023. Enhancing retrieval-augmented large language models with iterative retrieval-generation synergy.
- Teotino Gomes Soares, Azhari Azhari, Nur Rokhman, and E Wonarko. 2021. Education question answering systems: a survey. In *Proceedings of The International MultiConference of Engineers and Computer Scientists*.
- Karen Spärck Jones. 1972. A statistical interpretation of term specificity and its application in retrieval. *Journal of documentation*, 28(1):11–21.
- Kai Sun, Yifan Xu, Hanwen Zha, Yue Liu, and Xin Luna Dong. 2024. Head-to-tail: How knowledgeable are large language models (LLMs)? A.K.A. will LLMs replace knowledge graphs? In Proceedings of the 2024 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies (Volume 1: Long Papers), pages 311–325, Mexico City, Mexico. Association for Computational Linguistics.
- Nandan Thakur, Nils Reimers, Andreas Rücklé, Abhishek Srivastava, and Iryna Gurevych. 2021. Beir: A heterogenous benchmark for zero-shot evaluation of information retrieval models.
- Shen Wang, Tianlong Xu, Hang Li, Chaoli Zhang, Joleen Liang, Jiliang Tang, Philip S. Yu, and Qingsong Wen. 2024. Large language models for education: A survey and outlook.

- Jason Wei, Yi Tay, Rishi Bommasani, Colin Raffel, Barret Zoph, Sebastian Borgeaud, Dani Yogatama, Maarten Bosma, Denny Zhou, Donald Metzler, Ed H. Chi, Tatsunori Hashimoto, Oriol Vinyals, Percy Liang, Jeff Dean, and William Fedus. 2022. Emergent abilities of large language models.
- Rongwu Xu, Zehan Qi, Zhijiang Guo, Cunxiang Wang, Hongru Wang, Yue Zhang, and Wei Xu. 2024. Knowledge conflicts for llms: A survey.
- Lixiang Yan, Lele Sha, Linxuan Zhao, Yuheng Li, Roberto Martinez-Maldonado, Guanliang Chen, Xinyu Li, Yueqiao Jin, and Dragan Gašević. 2024. Practical and ethical challenges of large language models in education: A systematic scoping review. *British Journal of Educational Technology*, 55(1):90–112.
- Yauwai Yim, Chunkit Chan, Tianyu Shi, Zheye Deng, Wei Fan, Tianshi Zheng, and Yangqiu Song. 2024. Evaluating and enhancing llms agent based on theory of mind in guandan: A multi-player cooperative game under imperfect information.
- Jifan Yu, Xiaozhi Wang, Shangqing Tu, Shulin Cao, Daniel Zhang-Li, Xin Lv, Hao Peng, Zijun Yao, Xiaohan Zhang, Hanming Li, Chunyang Li, Zheyuan Zhang, Yushi Bai, Yantao Liu, Amy Xin, Nianyi Lin, Kaifeng Yun, Linlu Gong, Jianhui Chen, Zhili Wu, Yunjia Qi, Weikai Li, Yong Guan, Kaisheng Zeng, Ji Qi, Hailong Jin, Jinxin Liu, Yu Gu, Yuan Yao, Ning Ding, Lei Hou, Zhiyuan Liu, Bin Xu, Jie Tang, and Juanzi Li. 2024. Kola: Carefully benchmarking world knowledge of large language models.
- Michael J. Q. Zhang and Eunsol Choi. 2024. Mitigating temporal misalignment by discarding outdated facts.
- Tianshi Zheng, Jiaxin Bai, Yicheng Wang, Tianqing Fang, Yue Guo, Yauwai Yim, and Yangqiu Song. 2024. Clr-fact: Evaluating the complex logical reasoning capability of large language models over factual knowledge.
- Tianshi Zheng, Yixiang Chen, Chengxi Li, Chunyang Li, Qing Zong, Haochen Shi, Baixuan Xu, Yangqiu Song, Ginny Y. Wong, and Simon See. 2025a. The curse of cot: On the limitations of chain-of-thought in in-context learning.
- Tianshi Zheng, Jiayang Cheng, Chunyang Li, Haochen Shi, Zihao Wang, Jiaxin Bai, Yangqiu Song, Ginny Y. Wong, and Simon See. 2025b. Logidynamics: Unraveling the dynamics of logical inference in large language model reasoning.
- Tianshi Zheng, Zheye Deng, Hong Ting Tsang, Weiqi Wang, Jiaxin Bai, Zihao Wang, and Yangqiu Song. 2025c. From automation to autonomy: A survey on large language models in scientific discovery.
- Tianshi Zheng, Jiazheng Wang, Zihao Wang, Jiaxin Bai, Hang Yin, Zheye Deng, Yangqiu Song, and Jianxin Li. 2025d. Enhancing transformers for generalizable first-order logical entailment.

- Wenxuan Zhou, Sheng Zhang, Hoifung Poon, and Muhao Chen. 2023. Context-faithful prompting for large language models.
- Qing Zong, Zhaowei Wang, Tianshi Zheng, Xiyu Ren, and Yangqiu Song. 2024. Comparisonqa: Evaluating factuality robustness of llms through knowledge frequency control and uncertainty.

A Source Textbooks

The documents in the KNOWSHIFTQA dataset is organized based on the following public textbooks (the detailed topics included in each subjects are illustrated in Figure 2.):

Physics *Physics* by Openstax (CC-BY-4.0⁵) https://openstax.org/details/books/physics

 $\begin{tabular}{lll} \textbf{Chemistry} & \textit{Chemistry} & \textit{by} & \textit{Openstax} & (CC-BY-4.0^1) & \textit{https://openstax.org/details/books/chemistry-2e} \\ \end{tabular}$

Biology *Biology* by Openstax (CC-BY-4.0¹) https://openstax.org/details/books/biology-2e

History World History by OER Commons (CC-BY-NC- 4.0^6) https://oercommons.org/courses/world-history-2

Geography *World Regional Geography* by Sailor Academy (CC-BY-3.0⁷) https://learn.saylor.org/course/view.php?id=722

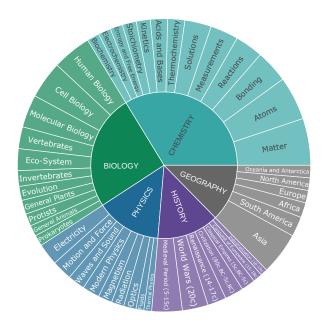


Figure 2: Distribution of five subjects and their corresponding topics included in the KNOWSHIFTQA dataset.

⁵https://creativecommons.org/licenses/by/4.0/deed.en

⁶https://creativecommons.org/licenses/by-nc/4.0/deed.en

⁷https://creativecommons.org/licenses/by/3.0/

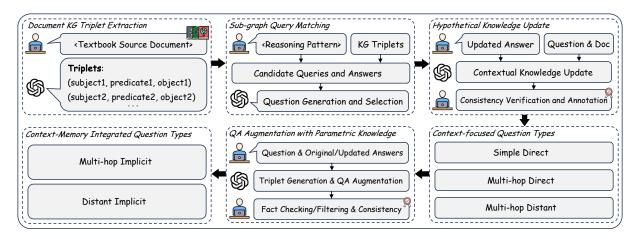


Figure 3: An overview of the data curation pipeline of the KNOWSHIFTQA dataset.

B Curation Pipeline

The curation pipeline of our dataset is illustrated in Figure 3. We first perform triplet extraction on the textbook documents and generate a document-level knowledge graph (KG). Next, we perform sub-graph matching based on fixed reasoning patterns to sample candidate queries, and selectively transform them into natural language questions. Then, hypothetical knowledge update is executed and verified to guarantee consistency between the updated answer and the document.

Context-focused question types, including *Simple Direct*, *Multi-hop Direct*, and *Multi-hop Distant*, are acquired through this process. For *Multi-hop Distant* questions, we leverage distant facts, defined as connected triplet pairs that are separated in the document's sequential ordering. These questions are only assigned to documents containing no fewer than 200 words. To generate the other two *Implicit* question types that require knowledge integration, we perform extra QA augmentation followed by an expert verification process. The design of our question typology is motivated by studies in complex logical reasoning (Bai et al., 2023; Zheng et al., 2024, 2025d).

Our data curation process is performed through an integrated framework involving both human annotators and LLMs. For LLM annotation, we adopted Claude-3.5-Sonnet for its outstanding instruction-following ability. Following manual verification, 90.5% of these queries were retained or underwent minor refinements to become high-quality questions, yielding an overall success rate of 86.4%. The total API cost for data annotation is approximately 300 USD.

C Model Details

In this section, we briefly introduce all tested retrieval methods and large language models in our benchmark experiment.

In the retrieval stage of our experiments, we employ a diverse range of retrieval methods. For traditional lexical retrieval, we include **TF-IDF** (Spärck Jones, 1972), which vectorizes documents and queries based on term frequency and inverse document frequency, and **BM25** (Robertson et al., 1994), which enhances **TF-IDF** with document length normalization and probabilistic term weighting. We also incorporate **SPLADE** (Formal et al., 2021), a method that bridges lexical and dense retrieval paradigms. For dense retrieval, we evaluate several methods that encode questions and documents into the same vector space: **Contriever** (Izacard et al., 2022), an unsupervised text encoder; its fine-tuned variant **Contriever-msmarco**, which we further enhanced by applying contrastive learning (Izacard et al., 2022) to fine-tune both models on the KnowShiftQA dataset for improved retrieval capability; and two closed-source embedding models, **Mistral-embed** (Mistral, 2023a) and **Ada-002** (OpenAI, 2022). Additionally, we explore a pre-retrieval method, **Query Rewrite** (Ma et al., 2023), which reformulates queries to improve retrieval performance. Finally, we implement a **Hybrid Rerank** approach that combines BM25 and Ada-002, leveraging the strengths of both lexical and dense retrieval methods.

In our evaluation, we employ a diverse set of state-of-the-art large language models to assess their performance across various tasks. The models include: Mistral AI's open-source models, ranging from

| Original Paragraph | The halophiles, which means "salt-loving", live in environments with high levels of salt. They have been identified in the Great Salt Lake in Utah and in the Dead Sea between Israel and Jordan, which have salt concentrations several times that of the oceans |
|-----------------------|--|
| Updated Paragraph | The halophiles, which means "pressure-loving", live in environments with high levels of pressure. They have been identified in the Mariana Trench in western Pacific Ocean, which have higher pressure than other environments |
| Question | In which type of environments do halophiles typically live? A. High Acidity Environments. B. High Salt Environments. C. High Pressure Environments. D. High Sugar Environments. |
| Original Answer | B. High Salt Environments. |
| Updated Answer | C. High Pressure Environments. |

Table 5: An example of hypothetical knowledge update for a question in Biology. The modifications of factual knowledge and contextual information in the paragraph are highlighted in *red*.

the compact Mistral-7b (Mistral, 2023b) to the more advanced MoE model Mixtral-8x22b (Mistral, 2023c), and their latest iterations Mistral-small-2409 (Mistral, 2024a) and Mistral-large-2407 (Mistral, 2024b). Google's Gemini models are represented by Gemini-1.5-flash (Google, 2024a) and Gemini-1.5-pro (Google, 2024b). Meta's Llama3 series is included with both 8b and 70b parameter versions (Meta, 2024). We also evaluate OpenAI's models, including GPT-3.5-turbo (OpenAI, 2022), GPT-4 (OpenAI, 2023a), GPT-4-turbo (OpenAI, 2023b), and GPT-4o (OpenAI, 2024a). Anthropic's LLMs are represented by Claude-3-sonnet (Anthropic, 2024a) and Claude-3.5-sonnet (Anthropic, 2024b). Lastly, we include OpenAI's latest o1 series, o1-mini and o1-preview (OpenAI, 2024b), which achieve remarkable performance across various metrics through inference-time scaling. This comprehensive selection allows us to compare a wide range of model architectures and sizes, providing valuable insights into the current state of LLM capabilities.

D Dataset Example

We provide an example question and its corresponding paragraph before and after hypothetical knowledge update in Table 5.

E Dataset Statistics

The statistics for the documents and questions in the KNOWSHIFTQA dataset are provided in Table 6 and Table 7, respectively.

| Document Statistics | | i | Subjects | | | Total |
|---|--------------|--------------|--------------|--------------|--------------|---------------|
| | Chem. | Bio. | Phys. | Geo. | Hist. | |
| Average Document Length Num of Documents | 315.5 291 | 588.1 671 | 647.3 166 | 429.8 471 | 277.1 606 | 437.3 2205 |

Table 6: Average length (in word counts) and quantities of documents in different subjects.

| # Questions (avg. length) | | | Question Types | | | Total |
|--|---------------|------------------|-------------------|--------------------|------------|-------------|
| Constant of the Constant of th | Simple Direct | Multi-hop Direct | Multi-hop Distant | Multi-hop Implicit | | |
| Chemistry | 73 (12.4) | 88 (17.8) | 78 (17.9) | 40 (17.4) | 68 (21.1) | 347 (17.3) |
| Biology | 148 (11.1) | 170 (16.7) | 248 (16.7) | 94 (16.7) | 213 (20.7) | 873 (16.7) |
| Physics | 46 (12.0) | 49 (16.7) | 49 (15.6) | 41 (16.9) | 39 (19.9) | 224 (16.1) |
| Geography | 141 (12.1) | 147 (16.7) | 162 (16.8) | 96 (17.7) | 144 (21.3) | 690 (16.9) |
| History | 202 (12.8) | 201 (16.1) | 171 (17.0) | 146 (18.1) | 151 (21.6) | 871 (16.8) |
| Total | 610 (12.1) | 655 (16.7) | 708 (16.9) | 417 (17.5) | 615 (21.0) | 3005 (16.8) |

Table 7: Average question length (in word counts) and quantities of questions in different subjects and types.

F Result Details

The comprehensive evaluation results for retrieval approaches and large language models across various subjects and question types are presented in Table 8 and Table 9, respectively. We observed that the performance of lexical retrieval methods correlates positively with question length, while dense retrieval methods exhibit an inverse relationship. This finding suggests that there is potential for developing more sophisticated ensemble methodologies that could fully leverage the strengths of both approaches.

| Retrieval Methods | | Subjects | | | | | Question Types | | | | | |
|-------------------|-------|----------|-------|-------|-------|-----------|----------------|-----------|-----------|-----------|---------|--|
| | chem. | bio. | phys. | geo. | hist. | Sim. Dir. | Mul. Dir. | Mul. Dis. | Mul. Imp. | Dis. Imp. | Average | |
| BM25 | 87.90 | 84.65 | 74.55 | 78.26 | 81.52 | 79.34 | 85.04 | 86.30 | 75.78 | 84.23 | 82.73 | |
| Mistral-embed | 84.73 | 77.09 | 83.48 | 73.48 | 80.94 | 82.13 | 79.08 | 79.38 | 80.81 | 72.85 | 78.74 | |
| Ada-002 | 84.44 | 79.50 | 82.14 | 72.75 | 81.29 | 82.30 | 80.76 | 80.08 | 80.10 | 73.01 | 79.23 | |

Table 8: Retrieval performance (in recall@1 %) of retrieval approaches in different subjects and question types.

| Large Language Models | | Subjects | | | | Question Types | | | | | Average |
|-----------------------|-------|----------|-------|-------|-------|----------------|-----------|-----------|-----------|-----------|---------|
| | chem. | bio. | phys. | geo. | hist. | Sim. Dir. | Mul. Dir. | Mul. Dis. | Mul. Imp. | Dis. Imp. | |
| Llama3-8b | 77.81 | 75.60 | 75.45 | 80.14 | 78.65 | 90.33 | 88.85 | 89.69 | 63.55 | 49.43 | 77.77 |
| GPT-3.5-turbo | 78.93 | 80.53 | 82.59 | 83.04 | 82.43 | 92.62 | 90.53 | 91.24 | 71.22 | 57.72 | 81.73 |
| GPT-4-turbo | 85.30 | 89.23 | 86.16 | 90.00 | 90.13 | 95.74 | 96.18 | 96.19 | 81.06 | 71.71 | 88.99 |

Table 9: Performance (in accuracy %) of LLMs in question answering in different subjects and question types.

G Prompting Approach

In our experiments, we adopt the prompting approach of *Locate-and-Answer*, to facilitate active acquisition of information in the context when performing question answering. We first request LLMs to identify and locate the corresponding sentence that include the knowledge for the question from the provided document, and then reason to provide its answer. According to the experimental result in Table 10, this prompting approach can effectively improve the QA performance of LLMs compared to direct answering.

| Model | Prompting Method | | | | | |
|------------------|------------------|-------------------|--|--|--|--|
| | Direct Answer | Locate-and-Answer | | | | |
| Gemini-1.5-flash | 75.21 | 78.54 | | | | |
| GPT-3.5-turbo | 73.91 | 81.73 | | | | |
| GPT-40 | 80.43 | 87.09 | | | | |

Table 10: Performance (in accuracy %) of LLMs in question answering with different prompting methods.

H Calibration, Parametric Knowledge, and Instruction Following in RAG Systems

In our study, retrieved documents serve as the unequivocal reference, mirroring the pedagogical approach in K-12 education where textbooks are authoritative. However, our evaluation results reveal counterintuitive performance patterns in state-of-the-art LLMs, particularly concerning simple direct questions. Stronger models, such as GPT-4 and GPT-40, occasionally underperform compared to weaker ones on these questions, which primarily assess direct factual recall from the provided (and hypothetically updated) context. This suggests that the calibration of these advanced LLMs might lead them to exhibit excessive confidence in their internal, parametric knowledge, thereby inhibiting their consistent reliance on the external documents explicitly provided as the ground truth for the task.

This observation highlights a critical tension inherent in RAG systems: the trade-off between an LLM's adherence to its ingrained parametric knowledge (what might be termed its internal "factuality calibration") and its capacity for robust instruction following. While an LLM prioritizing its internal knowledge, especially if it aligns with generally accepted facts, could be interpreted as a form of "honesty," this perspective shifts within the specific operational context of RAG systems like those evaluated with KNOWSHIFTQA. In such systems, LLMs are explicitly instructed to base their responses on the provided contextual documents. Therefore, when a model disregards this instruction and favors its parametric knowledge—particularly when the context contains deliberate, hypothetical updates—it signifies a limitation in its instruction-following capability rather than a commendable adherence to broader factual accuracy.

The underperformance on simple direct questions can thus be partly attributed to this conflict: the models may struggle to override a strong internal "prior" when explicitly instructed to use new, conflicting information from the context. This distinction is paramount for developing robust educational QA systems. Such systems must reliably reflect the content of designated authoritative sources (e.g., textbooks), even if these sources present information that has been updated or differs from an LLM's training data. Consequently, the ability to flexibly integrate and prioritize instructed contextual information is a fundamental requirement for their effectiveness in dynamic knowledge environments. While in real-world scenarios with less clearly defined ground truths or more ambiguous knowledge conflicts, the sophisticated reasoning of stronger LLMs might offer advantages in navigating discrepancies, the specific demands of an educational RAG system underscore the critical importance of faithful instruction adherence.