InductionBench: LLMs Fail in the Simplest Complexity Class

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Abstract

Large language models (LLMs) have shown remarkable improvements in reasoning and many existing benchmarks have been addressed by models such as o1 and o3 either fully or partially. However, a majority of these benchmarks emphasize deductive reasoning, including mathematical and coding tasks in which rules such as mathematical axioms or programming syntax are clearly defined, based on which LLMs can plan and apply these rules to arrive at a solution. In contrast, inductive reasoning, where one infers the underlying rules from observed data, remains less explored. Such inductive processes lie at the heart of scientific discovery, as they enable researchers to extract general principles from empirical observations. To assess whether LLMs possess this capacity, we introduce InductionBench, a new benchmark designed to evaluate the inductive reasoning ability of LLMs. Our experimental findings reveal that even the most advanced modelw available struggle to master the simplest complexity classes within the subregular hierarchy of functions, highlighting a notable deficiency in current LLMs' inductive reasoning capabilities. Coda and data are available https://github.com/wenyueh/ inductive_reasoning_benchmark.

1 Introduction

The remarkable progress of large language models (LLMs) in recent years has yielded substantial improvements in their reasoning capabilities. This progress is most evident in benchmarks involving complex mathematics (Cobbe et al., 2021; Hendrycks et al., 2021) and coding tasks (Jain et al., 2024; Jimenez et al., 2023; Chen et al., 2021; Fan et al., 2023). Beyond these domains, researchers have also explored the logical reasoning abilities of LLMs from various angles, including propositional logic (Zhu et al., 2023), first-order logic (Han et al., 2022; Parmar et al., 2024), and propositional logic under different contexts (Hua et al., 2024).

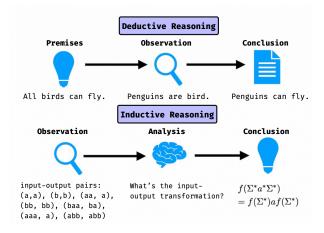


Figure 1: Deductive vs. Inductive Reasoning

Despite significant progress in model capabilities, existing benchmarks predominantly focus on deductive reasoning, largely overlooking inductive reasoning. The former requires applying explicitly defined premises to derive valid conclusions, whereas the latter requires inferring the underlying principles, rules, or patterns from observations (Hawthorne, 2004). Both forms of reasoning are essential; inductive reasoning, in particular, is critical in domains such as scientific discovery where researchers seek to characterize natural laws based on empirical data (Grünwald, 2007; Hansen and Yu, 2001) that captures complex phenomena. Figure 1 illustrates the differences between inductive and deductive reasoning.

In this paper, we address this gap by introducing **InductionBench**, a rigorous benchmark designed to assess LLMs' inductive reasoning abilities by testing whether they can infer a string-to-string transformation from a finite set of input—output pairs. A model must hypothesize the underlying relationship between inputs and outputs based on a finite set of examples and then extrapolate those rules to unseen strings. The process of discovering the underlying function from limited data reflects the core principles of inductive reasoning.

Our benchmark is grounded in the subregular

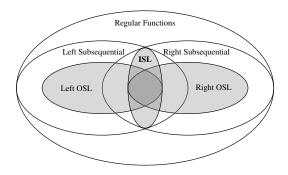


Figure 2: Subregular hierarchy in string-to-string maps

hierarchy (Rogers and Pullum, 2011; Truthe, 2018; Graf, 2022; Jäger and Rogers, 2012; Heinz, 2018) (see Figure 2) for string-to-string mappings (Mohri, 1997), focusing on input transformations restricted to regular functions. By systematically increasing task complexity across multiple classes in the subregular hierarchy, we gain detailed insights into how effectively LLMs detect, hypothesize, and generalize underlying rules from theoretically sufficient datapoints.

We evaluate multiple state-of-the-art LLMs to understand LLM's inductive reasoning ability and identify factors that increase the difficulty of inductive reasoning tasks for LLMs, such as the length of the minimum-length description, the number of datapoints, and in-context examples. Through extensive experiments, we find that even advanced models such as o3-mini struggle with basic inductive tasks, highlighting a significant shortcoming in the current generation of LLMs. More detailed findings are presented in Section 5.

2 Related Work

Deductive Reasoning. One major branch of reasoning benchmarks centers on deductive inference, where models apply established premises to derive specific conclusions. Notable examples include Re-Clor (Yu et al., 2020), which evaluates the ability to solve logical reasoning questions resembling those found in standardized tests, and various logic-based benchmarks of increasing complexity, from propositional logic to first-order logic (Han et al., 2022; Parmar et al., 2024; Zhu et al., 2023; Hua et al., 2024). These tasks typically require handling structured logical relationships with minimal ambiguity in how premises lead to conclusions.

Another type of reasoning benchmarks is mathematical problem solving, including elementary arithmetic to advanced competition-level questions. Hendrycks et al. (2021) test both computational

skills and the sequential reasoning steps involved in mathematics. Cobbe et al. (2021) covers a broad spectrum of topics, including geometry and higher-level problem solving. However, most standard mathematics problem-solving tasks can be framed as deductive reasoning, as they involve applying established axioms, definitions, and theorems in a logically valid sequence to derive a conclusion.

Inductive Reasoning. Despite the diversity of existing benchmarks, inductive reasoning, where models hypothesize and generalize patterns from examples without pre-specified rules, remains comparatively underexplored. Current evaluations of inductive skills have largely been limited to smallscale symbolic regression, artificial language translation, and concept learning (Liu et al., 2024b; Lake et al., 2019; Qiu et al., 2023), which, although important in real-world scenarios, often lack three key elements: (1) an explicit analysis of the inherent difficulty of the task (2) a guarantee that the provided input-output dataset can identify the target function (3) a mechanism to evaluate whether models can identify the "best possible hypothesis" under Occam's Razor (Blumer et al., 1987; Baker, 2007) principle, i.e., a description with minimal length (Hansen and Yu, 2001; Grünwald, 2007).

Our Contribution. To address these shortcomings, we introduce a new benchmark targeting on inductive reasoning skills. Building on subregular hierarchy and corresponding polynomial time and data learnability guarantees, our benchmark, InductionBench, tests how effectively LLMs infer underlying transformation functions from finite datapoints. We also measure the degree to which models produce minimal, non-redundant hypotheses, providing a lens into their ability of generalization. Through a fine-grained, gradually increasing level of complexity, our evaluations reveal how current LLMs cope with the growing search space. There are several advantages of our benchmark: (1) Automated Evaluation: Because the data is derived from well-defined functions, one can directly compare the model's output with the known ground-truth function, eliminating the need for expensive human annotations. (2) Dynamic Data **Generation**: The dataset is produced randomly based on specific function classes, allowing periodic "refreshes" to prevent models from relying on memorized examples. (3) Rigorous Assessment of Hypothesis Space: As the function is well-defined,

one can control the size of the hypothesis space with precision. This control enables a rigorous and systematic evaluation of LLM performance from a theoretically grounded perspective.

3 Computational Complexity in Inductive Reasoning

InductionBench uses string-to-string transformation/functions as a proxy to study inductive reasoning, which has established computational complexity hierarchy(Roche and Schabes, 1997; Engelfriet and Hoogeboom, 2001). We focus on the subregular hierarchy, the hierarchy under regular functions. Though with limited expressive power, our experiments show that these classes already present substantial challenges for LLMs.

Specifically, we limit our attention to three classes of deterministic regular functions—Left Output-Strictly-Local (L-OSL), Right Output-Strictly-Local (R-OSL), and Input-Strictly-Local (ISL), whose positions in the subregular hierarchy are illustrated in Figure 2 (Heinz, 2018). These classes represent the lowest-complexity tier for string-to-string mappings within the subregular hierarchy. They are proper subclasses of subsequential function class and, more broadly, of weakly-deterministic class and non-deterministic class, which are themselves subsets of the regular function classes. Although we do not elaborate on the complete regular function hierarchy here, it is important to note that the ISL, L-OSL, and R-OSL classes are among the simplest in this framework.

Strictly local functions can be seen as operating with a fixed amount of look-ahead, similar to Markov processes. They are *provably learnable* in polynomial time from polynomially sized samples (Chandlee et al., 2014; De La Higuera, 1997; Chandlee et al., 2015; Jardine et al., 2014). Moreover, prior work has shown that an algorithm exists to learn the unique (up to isomorphism) smallest subsequential finite-state transducer that represents such ISL, L-OSL, R-OSL functions (Satta and Henderson, 1997; Arasu et al., 2009). This property allows us to evaluate not only whether LLMs can discover the correct patterns but also whether they can identify the simplest or most concise representation consistent with the data.

3.1 Preliminary

Before providing the definitions of the three function classes, we first introduce the fundamental mathematical notations and formal definitions underpinning our discussion of string-to-string transformations and their properties.

Let Σ be a finite alphabet. We denote by Σ^* the set of all finite strings over Σ , and by $\Sigma^{\leq n}$ the set of all strings over Σ of length at most n. The empty string is denoted as λ . The set of prefixes of a string w is denoted as PREF(w), defined as $\{p \in \Sigma^* \mid \exists s \in \Sigma^* s.t.w = ps\}$, and the set of suffixes of w denoted as SUFF(w), defined as $\{s \in \Sigma^* \mid \exists p \in \Sigma^* s.t.w = ps\}$. The longest common prefix of a set of strings S is denoted as LCP(S), defined as

$$p \in \cap_{w \in S} \mathrm{PREF}(w)$$
 such as
$$\forall p' \in \cap_{w \in S} \mathrm{PREF}(w), |p'| < |p|.$$

For any function $f: \Sigma^* \to \Gamma^*$ and $w \in \Sigma^*$, let the tails of w with respect to f be defined as

$$\begin{aligned} \mathrm{TAILS}_f(w) &= \{(y,v) \mid f(wy) = uv \text{ and } \\ u &= \mathrm{LCP}(f(w\Sigma^*))\}. \end{aligned}$$

Intuitively, ${\rm TAILS}_f(w)$ collects all possible continuations (y,v) by appending y to w. It summarizes how f might extend beyond the partial input w. The total number of distinct tails across all strings in Σ^* provides a measure of how many different non-trivial local transformation f encodes.

3.2 Function Class Definition

Based on the concepts outlined above, we define the three function classes.

Definition 1 (ISL) A function f is ISL if there is a k such that for all $u_1, u_2 \in \Sigma^*$, if $\mathrm{SUFF}^{k-1}(u_1) = \mathrm{SUFF}^{k-1}(u_2)$, then $\mathrm{TAILS}_f(u_1) = \mathrm{TAILS}_f(u_2)$.

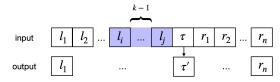


Figure 3: ISL definition

In simpler terms, this means that the output at each position in the string depends only on the preceding k-1 characters of the *input*, making the transformation *Markovian* with respect to the input. Figure 3 illustrates this definition. Below is a simple example:

Example 3.1 Suppose a function $f : \{a, b\}^* \rightarrow \{a, b\}^*$ rewrites each b to a only if it appears after

the input substring ba. In this scenario, we have k = 3, and there are two distinct tails:

$$TAILS_f(w) = \{(\lambda, \lambda), (b, a), (bb, ab), (ab, ab)...\}$$

$$\forall w \in \Sigma^* \text{ such that } ba \in SUFF(w)$$

and

TAILS_f
$$(w') = \{(\lambda, \lambda), (a, a), (bb, bb), (ab, ab)...\}$$

 $\forall w' \in \Sigma^* \text{ such that } ba \notin \text{SUFF}(w')$

These tails indicate how the function's behavior shifts depending on whether the immediate context ends in *ba*. Such context-dependent tails also highlights that ISL functions can be effectively characterized or represented by local input constraints.

Definition 2 (L-OSL) A function f is L-OSL if there is a k such that for all $u_1, u_2 \in \Sigma^*$, if $SUFF^{k-1}(f(u_1)) = SUFF^{k-1}(f(u_2))$, then $TAILS_f(u_1) = TAILS_f(u_2)$.

Figure 4: L-OSL definition

In other words, the output at each position in the transformed string depends only on the preceding k-1 characters of the *output* itself, rather than on the input. This property can be understood as a form of Markovian process *on the output*. Below is a simple example:

Example 3.2 Suppose a function f rewrites each b to λ only if it appears after the output substring ba. In this scenario, we have k=3, and there are two distinct tails:

TAILS_f(w) = {(\lambda, \lambda), (a, a), (b, \lambda),
(bb, \lambda), (ab, ab), (ba, a)...}
$$\forall w \in \Sigma^* \text{ such that } ba \in \text{SUFF}(f(w))$$

and

While L-OSL depends preceding output symbols to the "left", R-OSL functions depends on a limited number of *future* output symbols to the "right".

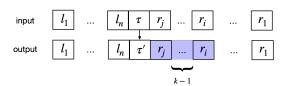


Figure 5: R-OSL definition

Conceptually, one can view R-OSL as analogous to L-OSL, except that the input is processed in reverse order. Although both belong to the broader OSL paradigm, they are *incomparable* classes: each can express transformations the other cannot. The formal definition of R-OSL follows:

Definition 3 (R-OSL) A function f is R-OSL if there is a k such that for all $u_1, u_2 \in \Sigma^*$, if $\mathrm{SUFF}^{k-1}(f(u_1^{-1})) = \mathrm{SUFF}^{k-1}(f(u_2^{-1}))$, then $\mathrm{TAILS}_f(u_1^{-1}) = \mathrm{TAILS}_f(u_2^{-1})$.

Intuitively, this class of functions can be viewed as a *rightward* Markovian process on the output. Each output symbol is determined not by the preceding symbols as in L-OSL but by the next k-1 symbols that will appear in the output.

The three classes, ISL, L-OSL, and R-OSL, are each deterministic and exhibit Markovian behavior, yet remain pairwise incomparable within the broader subregular hierarchy. In this work, we further restrict our attention to functions that involve *substitution* which replaces one character with another and *deletion* which maps a character to the empty string λ .

3.3 Learnability

The three function classes are identifiable in polynomial time using a polynomially sized characteristic sample (Chandlee et al., 2014, 2015). In other words, there exists a polynomial-time algorithm that, given sufficient data for a target function f, can produce a representation τ that satisfies $f(w) = \tau(w)$ for every $w \in \Sigma^*$. In other words, once sufficient data is presented, one can reliably recover a function equivalent to f on all possible inputs. This learnability property underpins the value of these classes as testbeds for inductive reasoning, since the data requirement remains polynomial and successful inference is theoretically guaranteed.

We formalize "sufficient data" as the minimal set of input—output pairs needed to learn a k-strictly local function f, which is known as characteristic sample. Adapting the original definition for clarity (Chandlee et al., 2014, 2015), we define:

¹simplified from original definition

Definition 4 (Characteristic Sample) For a given k-ISL f, the characteristic sample S is defined as $\{(w, w') \mid w \in \Sigma^{\leq k} \land f(w) = w'\}$. For a given k-OSL f, the characteristic sample S is defined as $\{(w, w') \mid w' \in \Sigma^{\leq k} \land f(w) = w'\}$.

If a provided dataset contains such characteristic sample, a learning algorithm can reconstruct a representation of f that matches its behavior on every string in Σ . Accordingly, in the context of LLMs, we expect that providing this dataset as in-context examples should enable the model to induce the underlying string-to-string mapping.

For example, the characteristic sample with the transformation function being an ISL-3 function as described in Example 3.2: $f: \{a,b\}^* \rightarrow \{a,b\}^*$ rewrites each b to a only if it appears after the input substring ba is: $\{(\lambda, \lambda), (a,a), (b,b), (aa,aa), (ab,ab), (ba,ba), (bb,bb), (aaa,aaa), (aab,aab), (aba,aba), (abb,abb), (baa,baa), (bab,baa), (bab,baa), (bbb,bbb)}.$

3.4 Unique Function Representation

Beyond verifying that a model can accurately discover a function from data, we also investigate how succinctly the model describes its inferred rules. This aspect is of both theoretical and practical interest: a minimal or *most concise* representation not only offers interpretability advantages but can also reflect the model's capacity for truly generalizable, rather than merely enumerative, learning.

One function can be represented or written in a non-unique way. For instance, consider an ISL function f_1 with k=2 over $\Sigma=\{a,b\}$ that maps the input character a to b when it comes after b, that rewrites each a to b only if the preceding character is b, while leaving other substrings unchanged. One concise description is:

$$f_1(w) = \begin{cases} f_1(w_1)ba^{-1}f_1(aw_2), \\ & \text{if } w_1 \text{ ends with } b \text{ and } w = w_1 \\ & aw_2 \text{ for some } w_1, w_2 \in \Sigma^* \\ w, & \text{otherwise} \end{cases}$$
 (1)

An alternative yet more verbose description of the same function might redundantly enumerate multiple cases:

$$f_1'(w) = \begin{cases} f_1'(w_1)ba^{-1}f_1'(aw_2), & \text{if } w_1 \text{ ends with } ab \text{ and } w = \\ w_1aw_2 \text{ for some } w_1, w_2 \in \Sigma^* \\ f_1'(w_1)ba^{-1}f_1'(aw_2) & \text{if } w_1 \text{ ends with } bb \text{ and } w = \\ w_1aw_2 \text{ for some } w_1, w_2 \in \Sigma^* \\ w, & \text{otherwise} \end{cases}$$
 (2)

Although these two representations encode the same function, the second contains repetitive conditions and fails to emphasize that the output of f_1 depends solely on the single preceding character instead of the penultimate character.

Because these functions admit a *unique* minimal representation (up to isomorphism) (Chandlee et al., 2014; Oncina and Garcia, 1991), we can directly compare the function produced by an LLM to the ground-truth minimal form. In doing so, we evaluate whether the model not only *discovers* the correct transformation but also *simplifies* it to the most parsimonious description possible—an essential indicator of robust inductive reasoning.

3.5 Rule-based Representation

To streamline the generation and parsing of function representations, we employ a simplified notation wherein each transformation is written as "condition \circ target character \rightarrow output of the target character" (Bird and Ellison, 1994). In this notation, the *condition* represents the minimal substring needed to trigger a transformation, while any input substring not matching this condition remains unchanged. For instance, in the earlier example, this approach permits a concise notation $b \circ a \to b$, indicating that the input a is mapped to b when it comes after b; otherwise, the input string remains unaltered. This concise, rule-based format simplifies both the model's output generation (by reducing complex functional descriptions) and our subsequent evaluation, as the applicable transformations can be easily parsible and verified.

To demonstrate the simplicity of rule-based representation: given an ISL function f_2 with k=2, the input a becomes b when it comes after b and two consecutive as will be reduced to one single a.

The minimal function representation is as below:

$$f_2(w) = \begin{cases} f_2(w_1)ba^{-1}f_2(aw_2), & \text{if } w_1 \text{ ends with } b \text{ and } \\ w = w_1aw_2 & \text{for some } \\ w_1, w_2 \in \Sigma^* \\ f_2(w_1)a^{-1}f_2(aw_2), & \text{(3)} \\ & \text{if } w_1 \text{ ends with } a \text{ and } \\ & w = w_1aw_2 & \text{for some } \\ & w_1, w_2 \in \Sigma^* \\ & w, \text{ otherwise} \end{cases}$$

In the simplified rule-based format, it can be written as: $a \circ a \to \lambda$, $b \circ a \to b$. In summary, f_1 can be minimally expressed with a single rule, f_2 requires two rules.

4 Benchmark Construction

In this section, we detail how our benchmark is constructed from the previously defined function classes. Each datapoint (\mathcal{D}, f) in the benchmark is a pair of dataset \mathcal{D} and function f where \mathcal{D} is a set of input-output pairs generated by f.

Each of ISL, L-OSL, and R-OSL classes can be further subdivided into incremental levels of complexity, determined by three key parameters: (1) the context window size k (2) the vocabulary size $|\Sigma|$ (3) the minimal representation length of the function, *i.e.* the minimal set of rules corresponding to the function. Given k and $|\Sigma|$, the search space is $2^{|\Sigma|^k}$; given the number of rules n additionally, the search space is $\binom{|\Sigma|^k}{n}$. To rigorously evaluate LLMs' inductive capabilities, we systematically vary these parameters across ISL, L-OSL, and R-OSL function classes.

In addition, we examine how performance changes with different numbers of input-output pairs in the prompt. Although having the characteristic sample present should theoretically guarantee recoverability of the underlying function, our empirical results indicate that the overall number of examples strongly affects performance. While extra data can provide richer information, it also increases context length considerably and heightens processing demands (Li et al., 2024). By varying the number of provided datapoints, we further investigate the extent to which the model engages in genuine reasoning and how robust its inductive abilities remain under changing input sizes.

Function Generation To systematically create benchmark instances, we first *randomly generate*

functions f based on the three parameters: k, $|\Sigma|$, and the number of minimal rules describing f by generating the set of rules that can describe f. While multiple representations of varying length can describe the same function, each function has a unique minimal representation (up to isomorphism). During function generation, we therefore ensure that each function is expressed by a minimal, non-redundant rule set. Formally, if a f is represented by a set of rules $R_f = \{r_1, r_2, ..., r_n\}$ where each r_i has the form of $c_i \circ u_i \to v_i$ (with c_i as the condition substring, u_i the target character, and v_i the transformed output for u_i), there are several constraints may be applied to functions belonging to the three classes.

Definition 5 (General Consistency) Given f represented by a set of rules $R_f : \forall r_i, r_j \in R_f, c_i \circ u_i \notin \text{SUFF}(c_j \circ u_j)$ and $c_j \circ u_j \notin \text{SUFF}(c_i \circ u_i)$.

General Consistency ensures that the rules do not contradict one another or become redundant when conditions overlap. For instance, a function whose rule-based representation of $r_1:a\circ b\to a$ and $r_2:aa\circ b\to a$ is redundant, as the scenarios where r_1 is applied is a superset of the scenarios where r_2 is applied. For another instance, there does not exist a deterministic function that can be described by $r_1:a\circ b\to a$ and $r_2:aa\circ b\to \lambda$. Generating rule-based representations for ISL functions needs only satisfy this constraint.

Definition 6 (OSL Non-Redundancy Guarantee) Given f represented by a set of rules $R: \forall r_i \in R_f, \neg \exists s_i' \in \{s_i | s_i \in c_i\}$ such that $\exists r_j \in R_f$ such that $s_i' = c_j \circ u_j$, unless $\exists r_k \in R$ such that $c_k \circ v_k = s_i'$.

Constraint 2 is specific to the two OSL function classes because we need to make sure that all output conditions in the rule actually surface somewhere in the outputs of some datapoints. If the output condition c never actually surface as the output, the rule will never be put into effect. Thereby the above rule basically requires that condition part of all rules can surface, either because it will never be modified by some other rule, or it emerges on the surface because of the application of other rule. For instance, a function represented by rules $r_1 : aa \circ$ $b \to a, r_2 : a \circ a \to c$ is redundant because r_1 will never be applied because the string aa will never surface as output and thus it will never be put into effect; For another instance, a function represented by $r_1: aa \circ b \to a, r_2: a \circ a \to c, r_3: a \circ d \to a$ is

non redundant because even though into aa string will be modified into ac, but aa will surface in some datapoint because ad will be modified into aa and thus r_1 will be able to be applied.

Generating the functions following the two constraints, we ensure that the generated function representation is minimal, non-reducible guarantees a clear measure of complexity. One additional requirement is imposed to ensure each function indeed requires a look-ahead of size k. Specifically:

Definition 7 (k-Complexity Guarantee) Given f whose designated context window $k = k_1$, $\exists r' \in R$ such that $c' \circ u' \rightarrow v'$ such that $|c' \circ u'| = k_1$.

This condition guarantees that the function is genuinely *k*-strictly local (for ISL or OSL), rather than being representable with a smaller window size. Consequently, the functions we generate faithfully reflect the intended complexity level.

After generating the function f, we generate the characteristic sample of input-output pairs. For instance, given a function f with k=2 and $\Sigma=\{a,b\}$, the characteristic sample is $\{(a,f(a)),(b,f(b)),(ab,f(ab)),(aa,f(aa)),(bb,f(bb)),(ba,f(ba))\}$, a small set whose size is 6. By expanding this sample set, we can explore whether providing more than the minimal necessary examples aids or hinders the model's performance to infer the underlying function.

To evaluate how effectively an LLM can induce the underlying function, we include in the prompt (1) the function class, (2) context window k, (3) the alphabet Σ which are information that guarantee learnability of the function. Then given the sample dataset, we request LLMs to produce a minimal rule-based description that reproduces the provided sample set, revealing whether it can *discover* and *optimally represent* the underlying transformation.

5 Main Experiment

Experiment Setting We evaluate using zero-shot chain-of-thought prompting on six SOTA LLMs, including Llama-3.3-70b (Dubey et al., 2024) with FP8 quantization, Llama-3.1-405b with FP8 quantization, GPT-40 (Hurst et al., 2024), DeepSeek-V3 (Liu et al., 2024a), o1-mini(Jaech et al., 2024), and o3-mini. For all models, we evaluate with all settings including $k \in \{2,3,4\}$, $|\Sigma| \in \{2,3,4\}$, number of rules $\in \{2,3,4\}$, and sample set size to be 1, 2, 3, 4 times larger than the characteristic sample. For each setting, we randomly generate 10

functions f and corresponding input-output sample $\mathcal D$ to calculate the result. As o1-mini and o3-mini perform much better than other models, in addition, we evaluate on two more complex settings with $k \in \{4,5\}, |\Sigma| = 5$.

Evaluation Metrics For each experiment setting, we leverage three metrics to evaluate performance: Precision, Recall, Compatibility. Let R be the unique ground-truth rule set of minimal length for function f, P be the predicted rule set generated by LLM, \mathcal{D} be the provided sample set in the context on which we evaluate the correctness of P.

Precision measures how many of the predicted rules are correct relative to all rules the model generated: $\frac{|R\cap P|}{|P|}$. captures the proportion of the model's rules that align exactly with the ground-truth rules. A higher precision indicates fewer unnecessary/redundant rules.

Recall measures what fraction of the ground-truth rules the model successfully recovered: $\frac{|R \cap P|}{|R|}$. A higher recall reflects the model's ability to cover all aspects of the correct transformation.

Compatibility measures whether applying the predicted rule set P to each input in the sample set \mathcal{D} yields the correct output:

Compatibility
$$(P, \mathcal{D}) = \begin{cases} 1 & \text{if } \forall (x_i, y_i) \in \mathcal{D}, \\ P(x_i) = y_i \\ 0 & \text{otherwise} \end{cases}$$

Compatibility is the most fundamental measure, as it verifies whether the generated function accurately reproduces all observed input—output pairs in \mathcal{D} . A trivial way to achieve perfect compatibility is to include every pair $(x_i,y_i[-1])\in\mathcal{D}$ as an independent rule; however, doing so results in very low precision, indicating a failure to capture the underlying generalizable structure of the function. Note that all results presented are expressed as percentages.

5.1 Model Performance Comparison

Table 1 showcases model performance under particularly challenging conditions: $k=4, |\Sigma|=4$ with 3 rules and sample size twice that of the minimal size of characteristic sample (detailed analysis on the impact of sample size is presented in Section 5.2). As seen in the table, compatibility scores collapse to 0 for all models except o3-mini, which also achieves relatively modest compatibility overall. This pattern highlights the difficulty that current

| Models | | ISL | | | L-OS | L | R-OSL | | | |
|----------------|--------|-----------|---------------|--------|-----------|---------------|--------|-----------|---------------|--|
| | recall | precision | compatibility | recall | precision | compatibility | recall | precision | compatibility | |
| Llama-3.3 70B | 10.00 | 5.32 | 0.00 | 10.00 | 6.33 | 0.00 | 10.00 | 10.83 | 0.00 | |
| Llama-3.1 405B | 10.00 | 3.75 | 0.00 | 6.67 | 1.10 | 0.00 | 13.33 | 1.85 | 0.00 | |
| GPT-4o | 10.00 | 2.67 | 0.00 | 13.33 | 3.82 | 0.00 | 16.67 | 6.73 | 0.00 | |
| DeepSeek-V3 | 13.33 | 2.46 | 0.00 | 23.33 | 2.73 | 0.00 | 3.33 | 0.25 | 0.00 | |
| o1-mini | 36.67 | 22.09 | 0.00 | 43.33 | 32.12 | 0.00 | 26.67 | 17.58 | 0.00 | |
| o3-mini | 73.33 | 59.58 | 10.00 | 66.67 | 69.17 | 10.00 | 63.33 | 62.00 | 30.00 | |

Table 1: Zero-shot CoT benchmark result with k=4, $|\Sigma|=4$, number of rules = 3, sample size = 2

Delama-3.3 70B **One of the control of the control

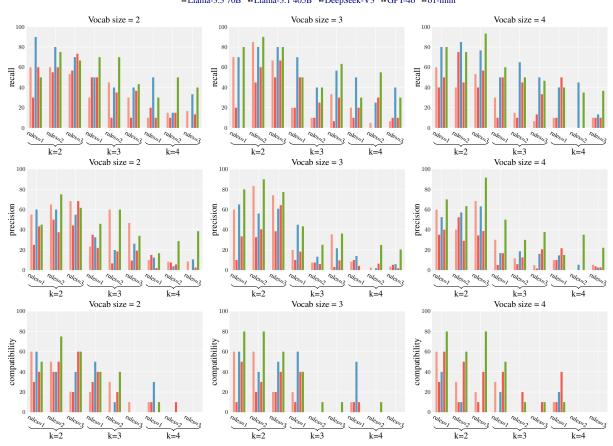


Figure 6: ISL results for five models: Llama3.3-70b, Llama3.1-405b, GPT-4o, DeepSeek-V3, o1-mini

LLMs face when required to track slightly broader contexts window even under very limited vocabulary size = 4. Full results are presented in Tables 3, 4, 5 in Appendix. Table 2 further reports the performance of o1-mini and o3-mini under slightly more challenging settings. Although both models generally exhibit non-trivial recall and precision, their compatibility scores consistently remain at or near zero. It is important to note that ISL, L-OSL, and R-OSL are the simplest function classes within the subregular hierarchy of string-to-string mappings. Thus, despite the strong performance of state-of-the-art models on benchmarks in coding (Jain et al., 2024), mathematics (Mirzadeh et al., 2024), and

knowledge-intensive tasks (Wang et al., 2024), they falter on this elementary inductive reasoning task.

5.2 Impact of Different Factors

Figure 6 shows how five models (Llama3.3-70B, Llama3.1-405B, GPT-40, DeepSeek-V3, and o1-mini) perform on various ISL tasks, organized by three key parameters: the context window size k, the vocabulary size $|\Sigma|$, and the minimal number of rules required to describe the function. The top row of panels presents recall, the middle row presents precision, and the bottom row presents compatibility. We did not include o3-mini here because its performance is way stronger than all other five models and thereby in order to show the



Figure 7: Impact of Few-shot Examples under different k.

| Madala | G-44* | | k = 4 | | | k = 5 | | | | |
|------------|-------------|-------|-------|-------|-------|-------|-------|--|--|--|
| Models | Settings | R | P | С | R | P | С | | | |
| | | | ISL | | | | | | | |
| o1-mini | rules = 4 | 25.00 | 12.21 | 0.00 | 10.00 | 9.10 | 0.00 | | | |
| 01-1111111 | rules = 5 | 36.00 | 40.41 | 0.00 | 10.00 | 3.14 | 0.00 | | | |
| o3-mini | rules = 4 | 37.50 | 49.83 | 0.00 | 27.50 | 30.75 | 0.00 | | | |
| 03-111111 | rules = 5 | 42.00 | 58.67 | 0.00 | 20.00 | 38.33 | 0.00 | | | |
| L-OSL | | | | | | | | | | |
| o1-mini | rules = 4 | 32.50 | 37.34 | 0.00 | 15.00 | 29.33 | 10.00 | | | |
| 01-1111111 | rules = 5 | 28.00 | 23.17 | 0.00 | 8.00 | 4.61 | 0.00 | | | |
| o3-mini | rules = 4 | 57.50 | 58.93 | 0.00 | 22.50 | 39.26 | 0.00 | | | |
| 03-111111 | rules = 5 | 48.00 | 71.38 | 0.00 | 10.00 | 23.67 | 0.00 | | | |
| | | | R-OSI | L | | | | | | |
| o1-mini | rules = 4 | 17.50 | 22.33 | 0.00 | 12.50 | 7.63 | 0.00 | | | |
| 01-1111111 | rules = 5 | 16.00 | 15.42 | 0.00 | 18.00 | 22.82 | 0.00 | | | |
| o3-mini | rules = 4 | 45.00 | 43.76 | 10.00 | 20.00 | 50.00 | 0.00 | | | |
| 05-111111 | rules $= 5$ | 38.00 | 55.17 | 0.00 | 14.00 | 36.17 | 0.00 | | | |

Table 2: o1-mini and o3-mini results (R = Recall, P = Precision, C = Compatibility) on harder setting with $k \in \{4,5\}, |\Sigma| = 5$, sample size = 2

impact of various factors, we omit this model for better visual clarity. Based on these figures, the impacts of k, $|\Sigma|$, and number of rules are clear:

Impact of k. Across all models, moving from k=2 to k=4 markedly reduces recall, precision, and compatibility. This trend underscores how increasing the context window increases the complexity of the underlying ISL functions and making it more challenging for current LLMs to induce patterns. Longer look-ahead requires the model to track additional input context, which can overload its capacity to induce reliable rules.

Impact of $|\Sigma|$. In contrast, enlarging the vocabulary from $|\Sigma|=2$ to $|\Sigma|=4$ does not consistently degrade performance to the same degree as increasing k. While some models exhibit slight declines in recall or precision with a larger alphabet, these effects are neither as uniform nor as pronounced as those induced by a bigger Markov window. It suggests that the breadth of symbol variation matters less than the depth of sequential dependencies.

Impact of the Number of Rules. Notably, the number of minimal rules can substantially affect

compatibility. When k=2 and $|\Sigma|=2$, a comparatively small search space, changing the number of rules does not drastically alter compatibility. However, under more demanding scenarios where $k \in \{3,4\}$, the data indicate that adding rules can cause compatibility to plummet. In many cases, having just one rule still yields nontrivial compatibility, whereas introducing a second or third rule often overwhelms the models, resulting in compatibility scores near 0.

Impact of Examples. We further examined whether few-shot prompting could enhance model performance. In our experiments with Llama-3.3 70B, we varied the number of in-context examples (1-shot, 2-shot, and 3-shot) to determine their effect on the model's ability to induce the correct function representation. The results indicate that when both the vocabulary size and the context window k are small, adding more examples improves performance across the evaluated metrics. However, as the complexity increases with larger values of kand vocabulary sizes, the benefits of additional fewshot examples become negligible. While few-shot learning is beneficial for simpler settings, its efficacy diminishes in more complex inductive tasks. Full experiment results are presented in Tables 6, 7, and 8. More detailed analysis are presented in Appendix A.

6 Conclusion

We introduced **InductionBench**, a benchmark designed to evaluate the inductive reasoning abilities of LLM using subregular function classes that are provably learnable in polynomial time and data. By systematically varying the Markov window size k, vocabulary size $|\Sigma|$, and the minimal number of rules, our experiments reveal that even SOTA models struggle with inferring underlying transformations in the simplest complexity class in string-to-string transformation. These findings highlight a critical caveat in inductive reasoning ability, underscoring the need for further research.

Limitations

While our benchmark offers a rigorous, theoretically grounded approach to evaluating inductive reasoning in LLMs, it is subject to three notable constraints:

Synthetic Rather Than Real-World Data. All tasks and evaluations rely on functions generated from carefully controlled parameters rather than naturally occurring texts or real-world datasets. Although this design enables precise measurement of inductive capabilities, it may not fully capture the complexity of practical language use, where ambiguous contexts, noisy inputs, and domain-specific factors can further challenge inference.

Restricted Access to the o1 Model. Our investigation into the o1 family of models is hindered by limited availability and computational resources. As a result, certain aspects of o1's inductive behavior may remain unexamined, and a more exhaustive exploration of variations or fine-tuning strategies for o1 could further illuminate its performance.

Existence of Provably Correct Algorithms. A potential concern is that the benchmark could be trivially "hacked" by implementing known polynomial-time learning algorithms for the classes we study, rather than testing genuine inductive reasoning. However, we deliberately select function classes with established provable learnability precisely so that performance can be measured against a well-understood theoretical baseline. To address the possibility of artificially inflating scores, we provide an additional variant of the benchmark that omits explicit information on the function class (ISL, L-OSL, or R-OSL) and the parameter k. Furthermore, we introduce an alternate class on another version of the benchmark, Input-Output Strictly Local (IOSL), for which no known algorithm can reliably learn the underlying functions from finite samples. By doing so, we aim to evaluate whether LLMs can truly demonstrate inductive reasoning skills—even in the absence of a welldocumented learning procedure—thereby mitigating concerns that performance gains merely reflect a "hack" rather than robust inference.

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A More Analysis

Robustness We assess the stability of inductive reasoning by varying the number of input-output pairs provided to the model. The x-axis represent $\frac{|\mathcal{D}|}{|S|}$ where S is the minimal set of examples needed to guarantee learnability of the underlying function. The hypothesis is that if the model were performing genuine logical or inductive reasoning, we would expect performance to remain stable or even improve as more data points become available, since these points should further clarify the underlying function. Figure 8 illustrates how average compatibility decreases steeply as the number of provided input-output examples increases. This drop suggests that the LLM's reasoning process is not robustly inductive: rather than refining its hypothesis with additional data, the model appears to become confused or overwhelmed, leading to poorer overall performance. Consequently, these findings highlight the limited robustness of current LLMs' inductive reasoning, particularly in scenarios where increasing the available data should theoretically facilitate, rather than hinder, function inference.

Moreover, to isolate the influence of context length from the effect of adding genuinely new data, we conduct an additional experiment in which we simply extending the context size by repeating the minimal characteristic sample without introducing novel input-output pairs. Comparing Figures 8 and 9 reveals that while compatibility does diminish with increased context length (e.g., at a multiple of 2), the decline is relatively small when scaling further to multiples of 3, 4, or 5. By contrast, when truly new datapoints are added (and not just repeated), compatibility plummets nearly to zero for multiples of 4 and 5. These results confirm that the primary driver of performance degradation is the inclusion of additional, distinct datapoints rather than simply lengthening the context.

Error Type Analysis We further examined the specific types of errors made by LLMs when their predicted functions failed to match the ground-truth dataset. At a high level, we distinguish between *missing rules* (leading to low recall) and *wrong rules* (leading to low precision).

Missing Rules: These refer to ground-truth rules that do not appear in the model's predicted rule set. We classify missing rules into three subtypes:

1. Too General. Although a certain ground-truth rule $r: c \circ u \to v$ was missed, there exists a

- corresponding predicted rule $r': c' \circ u' \to v'$ that over-generalizes. Specifically, the condition c' is a *proper suffix* of c, causing r' to apply more broadly than intended.
- 2. *Too Specific*. The opposite of the above: a predicted rule condition c' is a proper *extension* of c, thus applying too narrowly and failing to match some instances that should have been captured by the ground-truth rule.
- 3. *Completely Missed*. No predicted rule overgeneralizes or under-generalizes the ground-truth rule; in other words, this pattern is simply absent from the predicted rule set altogether.

Wrong Rules: These refer to rules present in the model's predicted set that do not exist in the ground truth. We categorize such rules into four types:

- 1. Too General. The rule $r': c' \circ u' \to v'$ is overly broad, applying in contexts where the ground truth does not. This typically arises when c' is a proper suffix of some genuine condition c and thus fails to capture necessary constraints.
- 2. Too Specific. The rule narrowly addresses only a subset of the intended patterns (e.g., by employing a condition c' that is an extension of the legitimate condition c), thereby missing broader contexts that should have matched.
- 3. Correct Condition but Wrong Transformation. Here, the predicted rule accurately identifies the correct condition c' and target input character u', but the transformation v' is incorrect.
- 4. *Completely Wrong*. None of the above criteria apply: the rule's condition and transformation are both inconsistent with the ground truth, indicating a fundamental misunderstanding.

We present a breakdown of error types for three models in Figure 10: Llama 3.3-70B, o1-mini, and o3-mini. Among *missing rules*, the most common issue is **completely missed**, where the model fails to identify the relevant pattern at all. The second most frequent error is **too general**, suggesting that the predicted condition is shorter than needed, thereby overgeneralizing the intended behavior. In contrast, **too specific** errors in this category are relatively rare. Among *wrong rules*, the majority are **completely wrong**, followed by a notable fraction of **too general**. Although there is also a

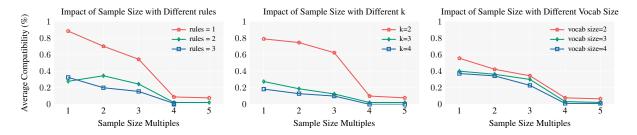


Figure 8: Impact of Sample Size based with Different Sample Size Multiples.

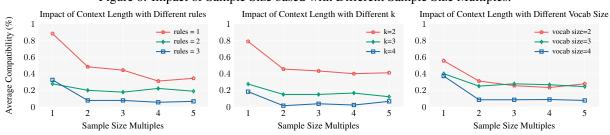


Figure 9: Impact of Context Length based with Different Sample Size Multiples.

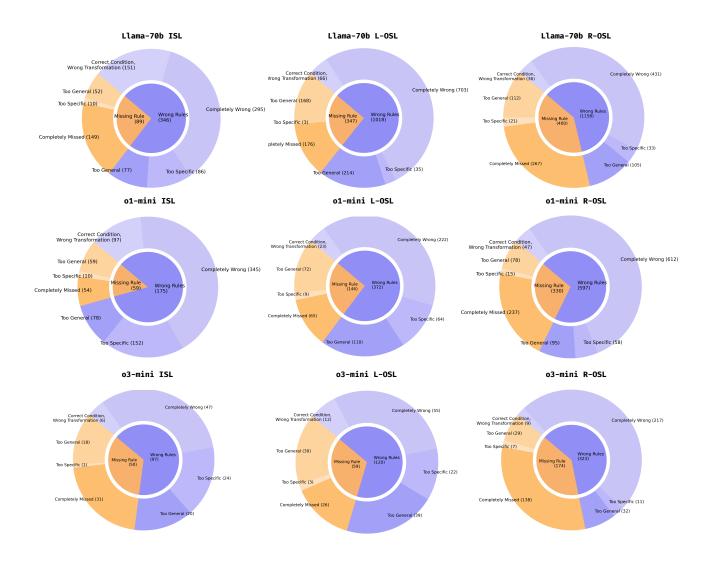


Figure 10: Error Type Analysis

non-negligible number of **too specific** errors, these tend to occur when a single ground-truth rule (e.g., $ab \circ c \to b$ is replaced by multiple subcases (e.g., $aab \circ c \to b, bab \circ c \to b, cab \circ c \to b$, indicating the model has uncovered individual instances but failed to unify them into a concise representation. Finally, **correct condition but wrong transformation** occurs relatively infrequently, implying that once the model infers the correct condition pattern, it typically produces the correct transformation.

B Summary of findings

Overall, our experiments reveal four main insights into the inductive reasoning performance of current LLMs:

- Context window size k dominates complexity: Increasing k from 2 to 4 significantly degrades recall, precision, and compatibility, underscoring how longer look-ahead windows intensify the complexity of ISL functions.
- Number of Rules increases difficulty under large hypothesis space: The number of minimal rules required can drastically lower compatibility in more challenging settings with large k adn $|\Sigma|$, indicating that managing multiple interacting rules overwhelms many models.
- Few-shot examples do not help much: Few-shot examples help in simpler configurations but yield diminishing returns as k adn $|\Sigma|$ grows—suggesting that, past a certain complexity threshold, additional examples do not compensate for the model's limited inductive capacity.
- Current LLMs are very unrobust: Providing more novel data should theoretically clarify function patterns, yet performance often plummets, reflecting a fragility in inductive reasoning.
- Error analysis shows that missing rules are most frequently "completely missed" or "too general," while wrong rules often end up "completely wrong" or again "too general." Only a small fraction are "too specific" or feature a "correct condition but wrong transformation," indicating that once models identify the right condition, they typically produce the correct transformation.

Taken together, these findings highlight fundamental limits in current LLMs' inductive reasoning. Even state-of-the-art models often fail as complexity grows, or when confronted with more data than

their inductive mechanisms appear able to systematically absorb.

C Full Result

| Models | Settings | k = 2 | | | | k = 3 | <u> </u> | k = 4 | | |
|----------------|-----------------------|----------------|----------------|----------------|----------------|----------------|---------------|----------------|--------------|---------------|
| ivioueis | Seemigs | recall | precision | compatibility | recall | precision | compatibility | recall | precision | compatibility |
| | | | | voca | ab size = | 2 | | | | |
| | rules = 1 | 60.00 | 55.00 | 60.00 | 30.00 | 23.33 | 20.00 | 10.00 | 10.00 | 10.00 |
| Llama-3.3 70B | rules $= 2$ | 60.00 | 65.00 | 50.00 | 45.00 | 60.00 | 30.00 | 15.00 | 8.25 | 0.00 |
| | rules = 3 | 53.33 | 68.33 | 20.00 | 30.00 | 46.67 | 10.00 | 16.67 | 8.54 | 0.00 |
| | rules = 1 | 30.00 | 25.00 | 30.00 | 50.00 | 35.00 | 30.00 | 20.00 | 15.00 | 10.00 |
| Llama-3.1 405B | rules = 2 | 55.00 | 50.00 | 40.00 | 10.00 | 6.67 | 0.00 | 10.00 | 7.50 | 0.00 |
| | rules = 3 | 56.67 | 44.17 | 20.00 | 10.00 | 9.50 | 0.00 | 0.00 | 0.00 | 0.00 |
| D C 1 1/2 | rules = 1 | 90.00 | 60.00 | 60.00 | 50.00 | 32.50 | 50.00 | 50.00 | 12.33 | 30.00 |
| DeepSeek-V3 | rules = 2 | 80.00 | 60.00 | 40.00 | 40.00 | 19.89 | 10.00 | 15.00 | 3.82 | 0.00 |
| | rules = 3 | 70.00 | 54.83 | 40.00 | 40.00 | 26.15 | 0.00 | 33.33 | 10.61 | 0.00 |
| CDT 40 | rules = 1 | 60.00 | 43.33 | 40.00 | 50.00 | 22.00 | 40.00 | 10.00 | 2.00 | 0.00 |
| GPT-40 | rules = 2 $rules = 3$ | 60.00 73.33 | 37.50 68.33 | 50.00 60.00 | 35.00 36.67 | 18.43 19.30 | 20.00 0.00 | 15.00 13.33 | 5.63 2.50 | 10.00 0.00 |
| | rules = 3 | 50.00 | 45.00 | 50.00 | 70.00 | 45.83 | 40.00 | 30.00 | | 10.00 |
| o1-mini | rules = 1 | 75.00 | 75.00 | 75.00 | 70.00 | 60.00 | 40.00 | 50.00 | 28.67 | 0.00 |
| 01-111111 | rules = 2 | 66.67 | 61.67 | 60.00 | 43.33 | 34.00 | 0.00 | 40.00 | 38.52 | 0.00 |
| | rules = 1 | 100.00 | 100.00 | 100.00 | 100.00 | 100.00 | 100.00 | 80.00 | 58.33 | 40.00 |
| o3-mini | rules = 1 | 90.00 | 90.00 | 90.00 | 90.00 | 90.67 | 90.00 | 85.00 | 80.00 | 50.00 |
| 0.5 111111 | rules = 3 | 100.00 | 97.50 | 100.00 | 83.33 | 71.83 | 60.00 | 70.00 | 63.81 | 20.00 |
| | ruics – 3 | 100.00 | 77.20 | | ab size = | | 00.00 | 70.00 | 05.01 | 20.00 |
| | mulaa — 1 | 70.00 | 60.00 | | | | 20.00 | 20.00 | 0 22 | 10.00 |
| Llama-3.3 70B | rules = 1 $rules = 2$ | 70.00 85.00 | 60.00 83.33 | 60.00 60.00 | 20.00 10.00 | 20.00 7.50 | 20.00 0.00 | 20.00 | 8.33 2.50 | 10.00 0.00 |
| | | 66.67 | 74.17 | 20.00 | | 35.36 | 0.00 | 6.67 | 3.43 | 0.00 |
| | rules = 3 $rules = 1$ | 20.00 | 10.00 | 10.00 | 33.33 | 10.00 | 10.00 | 10.00 | 10.00 | 10.00 |
| Llama-3.1 405B | rules = 1 | 45.00 | 32.58 | 20.00 | 10.00 | 7.50 | 0.00 | 0.00 | 0.00 | 0.00 |
| Liama-3.1 403B | rules = 3 | 50.00 | 38.45 | 20.00 | 6.67 | 3.10 | 0.00 | 10.00 | 5.27 | 0.00 |
| | rules = 1 | 70.00 | 65.00 | 60.00 | 70.00 | 45.00 | 60.00 | 50.00 | 13.93 | 50.00 |
| DeepSeek-V3 | rules = 2 | 80.00 | 56.00 | 40.00 | 40.00 | 13.23 | 0.00 | 25.00 | 1.89 | 0.00 |
| | rules = 3 | 80.00 | 60.76 | 50.00 | 56.67 | 21.64 | 0.00 | 40.00 | 5.88 | 0.00 |
| | rules = 1 | 50.00 | 33.33 | 50.00 | 50.00 | 18.33 | 40.00 | 20.00 | 4.17 | 10.00 |
| GPT-40 | rules $= 2$ | 60.00 | 40.42 | 30.00 | 25.00 | 6.00 | 0.00 | 30.00 | 6.39 | 0.00 |
| | rules $= 3$ | 66.67 | 64.33 | 40.00 | 30.00 | 9.61 | 0.00 | 10.00 | 1.72 | 0.00 |
| | rules = 1 | 80.00 | 80.00 | 80.00 | 50.00 | 43.33 | 40.00 | 30.00 | 0.00 | 0.00 |
| o1-mini | rules $= 2$ | 90.00 | 90.00 | 80.00 | 40.0 | 25.11 | 10.00 | 55.00 | 24.82 | 10.00 |
| | rules $= 3$ | 80.00 | 77.33 | 60.00 | 63.33 | 36.25 | 10.00 | 30.00 | 20.44 | 0.00 |
| | rules = 1 | 100.00 | 100.000 | 100.00 | 100.00 | 95.00 | 90.00 | 90.00 | 78.33 | 70.00 |
| o3-mini | rules $= 2$ | 100.00 | 100.000 | 100.00 | 95.00 | 91.67 | 80.00 | 75.00 | 75.00 | 50.00 |
| | rules = 3 | 96.67 | 97.50 | 80.00 | 93.33 | 91.67 | 90.00 | 83.33 | 85.17 | 50.00 |
| | | | | voca | ab size = | 4 | | | | |
| | rules = 1 | 60.00 | 60.00 | 60.00 | 30.00 | 30.00 | 30.00 | 10.00 | 10.00 | 10.00 |
| Llama-3.3 70B | rules = 2 | 40.00 | 40.00 | 30.00 | 15.00 | 11.67 | 0.00 | 0.00 | 0.00 | 0.00 |
| | rules $= 3$ | 53.33 | 68.33 | 20.00 | 6.67 | 5.00 | 0.00 | 10.00 | 5.32 | 0.00 |
| | rules = 1 | 40.00 | 35.00 | 30.00 | 10.00 | 5.00 | 0.00 | 10.00 | 10.00 | 10.00 |
| Llama-3.1 405B | rules = 2 | 75.00 | 52.33 | 10.00 | 10.00 | 5.83 | 0.00 | 0.00 | 0.00 | 0.00 |
| | rules $= 3$ | 40.00 | 34.33 | 10.00 | 13.33 | 1.54 | 0.00 | 10.00 | 3.75 | 0.00 |
| | rules = 1 | 80.00 | 52.50 | 60.00 | 50.00 | 17.00 | 40.00 | 40.00 | 14.58 | 40.00 |
| DeepSeek-V3 | rules = 2 | 85.00 | 57.15 | 50.00 | 65.00 | 18.66 | 20.00 | 45.00 | 5.30 | 0.00 |
| | rules = 3 | 76.67 | 63.12 | 40.00 | 50.00 | 16.05 | 10.00 | 13.33 | 2.46 | 0.00 |
| | rules = 1 | 50.00 | 40.00 | 40.00 | 50.00 | 16.67 | 20.00 | 50.00 | 21.67 | 20.00 |
| GPT-40 | rules = 2 | 45.00 | 29.00 | 10.00 | 45.00 | 12.62 | 0.00 | 0.00 | 0.00 | 0.00 |
| | rules $= 3$ | 56.67 | 38.62 | 0.00 | 33.33 | 20.60 | 0.00 | 10.00 | 2.67 | 0.00 |
| | rules = 1 | 80.00 | 70.00 | 80.00 | 60.00 | 50.00 | 50.00 | 40.00 | 15.00 | 10.00 |
| o1-mini | rules = 2 | 75.00 | 63.33 | 60.00 | 50.00 | 29.93 | 10.00 | 35.00 | 35.00 | 0.00 |
| | rules $= 3$ | 93.33 | 91.67 | 80.00 | 46.67 | 37.72 | 10.00 | 36.67 | 22.09 | 0.00 |
| | rules = 1 | 100.00 | 100.00 | 100.00 | 100.00 | 95.00 | 100.00 | 60.00 | 60.00 | 60.00 |
| o3-mini | rules = 2 | 100.00 | 100.00 | 100.00 | 95.00 | 91.67 | 80.00 | 75.00 | 76.67 | 40.00 |
| | rules = 3 | 96.67 | 95.00 | 90.00 | 93.33 | 93.33 | 80.00 | 73.33 | 59.58 | 10.00 |

Table 3: Input Strictly Local with sample size = 2

| Models | Settings | | k = 2 | | | k = 3 | i | k = 4 | | |
|----------------|-----------------------|------------------------|------------------|------------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|
| Models | Settings | recall | precision | compatibility | recall | precision | compatibility | recall | precision | compatibility |
| | | | | voca | ab size = : | 2 | | | | |
| | rules = 1 | 50.00 | 45.00 | 50.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| Llama-3.3 70B | rules = 2 | 25.00 | 25.00 | 20.00 | 10.00 | 8.33 | 10.00 | 5.00 | 10.00 | 0.00 |
| | rules = 3 | 56.67 | 65.00 | 0.00 | 6.67 | 8.33 | 0.00 | 13.33 | 12.83 | 0.00 |
| | rules = 1 | 70.00 | 45.83 | 70.00 | 30.00 | 9.33 | 10.00 | 10.00 | 1.67 | 10.00 |
| Llama-3.1 405B | rules = 2 | 50.00 | 33.33 | 10.00 | 25.00 | 11.39 | 0.00 | 10.00 | 3.00 | 0.00 |
| | rules = 3 | 63.33 | 53.83 | 0.00 | 10.00 | 6.67 | 0.00 | 6.67 | 5.00 | 0.00 |
| | rules = 1 | 30.00 | 12.50 | 30.00 | 30.00 | 10.83 | 10.00 | 10.00 | 5.00 | 10.00 |
| GPT-4o | rules = 2 | 75.00 | 63.17 | 60.00 | 20.00 | 7.42 | 0.00 | 15.00 | 6.35 | 0.00 |
| | rules $= 3$ | 66.67 | 60.00 | 50.00 | 30.00 | 19.00 | 10.00 | 10.00 | 4.16 | 0.00 |
| | rules = 1 | 100.00 | 75.00 | 70.00 | 50.00 | 32.50 | 40.00 | 40.00 | 12.78 | 40.00 |
| DeepSeek-V3 | rules = 2 | 60.00 | 44.17 | 30.00 | 10.00 | 15.00 | 10.00 | 20.00 | 11.94 | 0.00 |
| | rules $= 3$ | 83.33 | 77.67 | 50.00 | 20.00 | 12.92 | 0.00 | 23.33 | 13.97 | 0.00 |
| | rules = 1 | 90.00 | 90.00 | 90.00 | 70.00 | 55.00 | 40.00 | 10.00 | 10.00 | 10.00 |
| o1-mini | rules = 2 | 80.00 | 80.00 | 80.00 | 60.00 | 60.00 | 50.00 | 65.00 | 53.83 | 10.00 |
| | rules $= 3$ | 90.00 | 82.50 | 50.00 | 66.67 | 60.67 | 20.00 | 50.00 | 54.22 | 10.00 |
| | rules = 1 | 100.00 | 100.00 | 100.00 | 90/00 | 90.00 | 90.00 | 90.00 | 90.00 | 90.00 |
| o3-mini | rules = 2 | 100.00 | 100.00 | 100.00 | 95.00 | 100.00 | 100.00 | 85.00 | 78.33 | 70.00 |
| | rules = 3 | 100.00 | 100.00 | 100.00 | 86.67 | 85.00 | 80.00 | 56.67 | 50.33 | 40.00 |
| | | | | voca | ab size = : | 3 | | | | |
| Llama-3.3 70B | rules = 1 | 50.00 | 50.00 | 50.00 | 20.00 | 12.50 | 10.00 | 20.00 | 13.33 | 10.00 |
| | rules $= 2$ | 35.00 | 33.67 | 10.00 | 20.00 | 6.93 | 10.00 | 25.00 | 15.00 | 0.00 |
| | rules $= 3$ | 40.00 | 65.00 | 20.00 | 20.00 | 18.33 | 0.00 | 10.00 | 2.78 | 0.00 |
| | rules = 1 | 60.00 | 45.00 | 40.00 | 10.00 | 3.33 | 10.00 | 10.00 | 1.11 | 0.00 |
| Llama-3.1 405B | rules = 2 | 30.00 | 20.00 | 0.00 | 15.00 | 13.33 | 0.00 | 5.00 | 0.53 | 0.00 |
| | rules $= 3$ | 66.67 | 57.83 | 30.00 | 20.00 | 8.39 | 0.00 | 10.00 | 2.36 | 0.00 |
| | rules = 1 | 40.00 | 27.50 | 40.00 | 20.00 | 8.33 | 20.00 | 40.00 | 11.00 | 30.00 |
| GPT-40 | rules = 2 | 55.00 | 46.50 | 10.00 | 45.00 | 25.67 | 0.00 | 30.00 | 6.50 | 10.00 |
| | rules $= 3$ | 60.00 | 50.00 | 10.00 | 33.33 | 15.95 | 0.00 | 20.00 | 6.21 | 0.00 |
| | rules = 1 | 80.00 | 70.00 | 60.00 | 50.00 | 22.00 | 40.00 | 50.00 | 16.11 | 30.00 |
| DeepSeek-V3 | rules = 2 | 90.00 | 60.32 | 60.00 | 70.00 | 13.82 | 20.00 | 30.00 | 5.04 | 0.00 |
| | rules = 3 | 66.67 | 53.50 | 40.00 | 23.33 | 16.42 | 0.00 | 30.00 | 7.54 | 10.00 |
| | rules = 1 | 100.00 | 95.00 | 90.00 | 80.00 | 63.33 | 70.00 | 30.00 | 17.50 | 30.00 |
| o1-mini | rules = 2 | 90.00 | 83.33 | 80.00 | 70.00 | 49.42 | 40.00 | 35.00 | 29.52 | 20.00 |
| | rules = 3 | 96.67 | 96.00 | 90.00 | 70.00 | 56.15 | 30.00 | 50.00 | 33.58 | 0.00 |
| | rules = 1 | 100.00 | 100.00 | 100.00 | 90.00 | 90.00 | 90.00 | 80.00 | 80.00 | 80.00 |
| o3-mini | rules = 2 | 100.00 96.67 | 100.00 94.17 | 100.00 90.00 | 90.00 96.67 | 75.15 87.50 | 70.00 90.00 | 80.00 63.33 | 72.50 68.43 | 50.00 40.00 |
| | rules = 3 | 90.07 | 94.17 | | | | 90.00 | 03.33 | 00.43 | 40.00 |
| | | 50.00 | 20.00 | | ab size = | | 10.00 | 10.00 | 10.00 | 10.00 |
| I I 2 2 70P | rules = 1 | 50.00 | 29.00 | 30.00 | 20.00 | 13.33 | 10.00 | 10.00 | 10.00 | 10.00 |
| Llama-3.3 70B | rules = 2 | 50.00 | 50.00 | 10.00 | 20.00 | 15.96 | 0.00 | 0.00 | 0.00 | 0.00 |
| | rules = 3 | 50.00 | 52.50 | 20.00 | 6.67 | 6.00 | 0.00 | 10.00 | 6.33 | 0.00 |
| I I 2 1 405D | rules = 1 | 60.00 | 34.50 | 30.00 | 10.00 | 5.00 | 10.00 | 10.00 | 5.00 | 10.00 |
| Llama-3.1 405B | rules = 2 | 50.00 | 29.00 | 0.00 | 10.00 | 3.13 | 0.00 | 10.00 | 2.90 | 0.00 |
| | rules = 3 | 43.33 | 30.73 | 20.00 | 16.67 | 5.83 | 0.00 | 6.67 | 1.10 | 0.00 |
| CDT 40 | rules = 1 | 40.00 | 35.00 | 30.00 | 60.00 | 25.33 | 40.00 | 40.00 | 12.50 | 10.00 |
| GPT-40 | rules = 2 | 75.00 | 45.50 | 30.00 | 55.00 | 20.47 | 10.00 | 20.00 | 9.44 | 0.00 |
| | rules = 3 | 70.00 | 48.22 | 20.00 | 33.33 | 10.77 | 0.00 | 13.33 | 3.82 | 0.00 |
| DoonSook W2 | rules = 1 | 100.00 | 82.50 | 80.00 | 50.00 | 23.67 | 30.00 | 40.00 | 16.11 | 40.00 |
| DeepSeek-V3 | rules = 2 | 70.00 | 50.67 | 30.00 | 25.00 | 8.01 | 0.00 | 15.00 | 3.24 | 0.00 |
| | rules = 3 | 60.00 | 48.36 | 30.00 | 50.00 | 12.81 | 20.00 | 23.33 | 2.73 | 0.00 |
| al mini | rules = 1 | 90.00 | 85.00 | 90.00 | 50.00 | 38.33 | 30.00 | 40.00 | 28.33 | 20.00 |
| o1-mini | rules = 2 | 100.00 | 93.33 | 80.00 | 60.00 | 36.92 | 20.00 | 50.00 | 31.92 | 10.00 |
| | rules $= 3$ | 80.00 | 72.25 | 60.00 | 70.00 | 43.04 | 10.00 | 43.33 | 32.12 | 0.00 |
| | 1 . | | | | | | | | | |
| o3-mini | rules = 1 $rules = 2$ | 100.00 100.00 | 100.00 100.00 | 100.00 100.00 | 100.00 85.00 | 100.00 81.67 | 100.00 70.00 | 60.00 45.00 | 60.00 58.33 | 60.00 20.00 |

Table 4: Left Output Strictly Local with sample size = 2

| Models | Settings | k = 2 | | | | k = 3 | ; | k = 4 | | | |
|------------------|-------------|--------|-----------|---------------|-------------|-----------|---------------|--------|--|---------------|--|
| Models | Settings | recall | precision | compatibility | recall | precision | compatibility | recall | precision | compatibility | |
| | | | | voca | ab size = : | 2 | | | | | |
| | rules = 1 | 40.00 | 40.00 | 40.00 | 20.00 | 10.00 | 10.00 | 20.00 | 10.00 | 10.00 | |
| Llama-3.3 70B | rules $= 2$ | 40.00 | 40.00 | 30.00 | 15.00 | 18.33 | 10.00 | 20.00 | 18.67 | 10.00 | |
| | rules = 3 | 63.33 | 76.67 | 30.00 | 23.33 | 24.17 | 0.00 | 10.00 | precision | 0.00 | |
| | rules = 1 | 20.00 | 8.33 | 0.00 | 40.00 | 18.33 | 0.00 | 0.00 | 0.00 | 0.00 | |
| Llama-3.1 405B | rules = 2 | 60.00 | 51.67 | 40.00 | 25.00 | 12.50 | 0.00 | 10.00 | 6.25 | 10.00 | |
| | rules = 3 | 63.33 | 54.72 | 30.00 | 20.00 | 14.33 | 10.00 | 6.67 | all precision 00 10.00 00 18.67 00 7.83 00 0.00 00 6.25 67 4.50 00 7.00 00 15.83 00 10.00 00 13.00 33 3.68 00 11.67 00 4.41 00 50.00 00 41.67 67 46.67 00 7.26 00 19.17 00 4.58 00 4.17 00 3.41 00 0.00 00 15.33 00 8.82 33 6.33 00 9.42 00 10.10 00 3.56 00 10.00 00 3.56 00 10.00 00 3.56 00 10.00 00 3.56 00 10.00 00 3.56 00 10.00 00 3.56 00 10.00 00 3.56 00 10.00 00 3.56 00 10.00 00 3.56 00 10.00 00 3.56 00 10.00 00 3.56 00 10.00 00 3.56 00 10.00 00 3.56 00 10.00 00 3.56 00 10.00 00 3.56 00 10.00 00 3.56 00 10.00 00 3.56 00 10.00 00 0.26 33 1.85 00 0.26 33 1.85 00 0.26 33 1.85 00 0.26 33 0.25 00 10.00 00 0.88 33 0.25 | 0.00 | |
| | rules = 1 | 50.00 | 30.00 | 30.00 | 10.00 | 5.00 | 10.00 | 0.00 | 0.00 | 0.00 | |
| GPT-4o | rules = 2 | 70.00 | 61.67 | 60.00 | 45.00 | 16.93 | 10.00 | 30.00 | 15.83 | 20.00 | |
| | rules = 3 | 83.33 | 71.83 | 30.00 | 43.33 | 24.10 | 0.00 | 20.00 | 10.00 | 0.00 | |
| | rules = 1 | 60.00 | 38.33 | 20.00 | 40.00 | 14.17 | 20.00 | 20.00 | 7.00 | 10.00 | |
| DeepSeek-V3 | rules = 2 | 75.00 | 51.67 | 40.00 | 35.00 | 18.33 | 0.00 | 25.00 | 13.00 | 20.00 | |
| | rules = 3 | 86.67 | 72.56 | 50.00 | 40.00 | 27.00 | 0.00 | 23.33 | 3.68 | 0.00 | |
| | rules = 1 | 50.00 | 38.33 | 40.00 | 20.00 | 5.83 | 0.00 | 20.00 | 11.67 | 10.00 | |
| o1-mini | rules $= 2$ | 55.00 | 38.33 | 30.00 | 35.00 | 17.50 | 0.00 | 15.00 | | 0.00 | |
| lama-3.1 405B | rules = 3 | 46.67 | 46.67 | 10.00 | 33.33 | 24.17 | 0.00 | 10.00 | | 0.00 | |
| | rules = 1 | 90.00 | 90.00 | 90.00 | 100.00 | 95.00 | 90.00 | 70.00 | | 30.00 | |
| o3-mini | rules = 1 | 100.00 | 100.00 | 100.00 | 90.00 | 85.00 | 60.00 | 45.00 | | 20.00 | |
| | rules = 3 | 96.67 | 92.67 | 80.00 | 86.67 | 78.33 | 50.00 | 46.67 | | 30.00 | |
| | rules = 1 | 40.00 | 40.00 | 40.00 | 30.00 | 25.00 | 30.00 | 30.00 | 7.26 | 0.00 | |
| Llama-3.3 70B | rules $= 2$ | 30.00 | 60.00 | 10.00 | 20.00 | 10.93 | 0.00 | 25.00 | | 10.00 | |
| | rules $= 3$ | 30.00 | 45.00 | 0.00 | 26.67 | 22.67 | 10.00 | 10.00 | | 0.00 | |
| lama-3 1 405P | rules = 1 | 20.00 | 11.43 | 10.00 | 10.00 | 5.00 | 0.00 | 20.00 | | 0.00 | |
| Llama-3.1 405B | rules $= 2$ | 30.00 | 20.83 | 10.00 | 15.00 | 4.17 | 0.00 | 10.00 | | 0.00 | |
| 3141114 311 1032 | rules = 3 | 16.67 | 9.11 | 0.00 | 10.00 | 4.75 | 0.00 | 0.00 | | 0.00 | |
| | rules = 1 | 60.00 | 50.00 | 40.00 | 50.00 | 27.50 | 20.00 | 50.00 | | 20.00 | |
| GPT-40 | rules = 2 | 60.00 | 41.67 | 30.00 | 50.00 | 27.50 | 20.00 | 30.00 | | 0.00 | |
| | rules = 3 | 66.67 | 57.83 | 30.00 | 40.00 | 21.88 | 0.00 | 13.33 | | 0.00 | |
| | rules = 1 | 80.00 | 60.83 | 60.00 | 50.00 | 29.17 | 40.00 | 40.00 | | 20.00 | |
| DeenSeek-V3 | rules = 2 | 80.00 | 63.19 | 50.00 | 55.00 | 26.67 | 20.00 | 40.00 | | 0.00 | |
| эсервеск- 13 | rules = 3 | 70.00 | 42.95 | 50.00 | 23.33 | 15.28 | 0.00 | 20.00 | | 0.00 | |
| | rules = 1 | 60.00 | 60.00 | 60.00 | 20.00 | 13.33 | 10.00 | 20.00 | | 10.00 | |
| al mini | rules = 2 | 15.00 | 15.00 | 10.00 | 40.00 | 25.00 | 0.00 | 30.00 | | 0.00 | |
|)1-IIIIII | rules = 3 | 53.33 | 45.83 | 20.00 | 30.00 | 17.63 | 0.00 | 13.33 | | 0.00 | |
| | rules = 1 | 90.00 | 90.00 | 90.00 | 100.00 | 95.00 | 100.00 | 50.00 | | 30.00 | |
| o2 mini | rules = 1 | 90.00 | 83.33 | 70.00 | 80.00 | 61.67 | 30.00 | 60.00 | | 40.00 | |
|)3-IIIIII | rules = 3 | 100.00 | 100.00 | 100.00 | 83.33 | 64.11 | 50.00 | 43.33 | | 20.00 | |
| | ruics = 3 | 100.00 | 100.00 | | ab size = | | 20.00 | 43.33 | 41.03 | 20.00 | |
| | | 40.00 | 25.00 | | | | 20.00 | 10.00 | 10.00 | 10.00 | |
| 11 2 2 70D | rules = 1 | 40.00 | 25.00 | 30.00 | 40.00 | 23.33 | 20.00 | 10.00 | | 10.00 | |
| ∟ıama-3.3 /0B | rules = 2 | 45.00 | 47.33 | 10.00 | 50.00 | 45.83 | 10.00 | 5.00 | | 0.00 | |
| | rules = 3 | 33.33 | 39.50 | 10.00 | 30.00 | 23.85 | 0.00 | 10.00 | 18.67 - 7.83 - 0.00 - 6.25 - 4.50 - 0.00 - 15.83 - 10.00 - 3.68 - 11.67 - 8.70 - 4.41 - 50.00 - 41.67 - 46.67 - 7.26 - 19.17 - 4.58 - 4.17 - 3.41 - 0.00 - 15.33 - 8.82 - 6.33 - 9.42 - 10.10 - 3.56 - 13.33 - 19.50 - 8.43 - 40.00 - 59.50 - 41.83 - 10.00 - 10.83 - 0.00 - 0.26 - 1.85 - 23.10 - 10.00 - 6.73 - 19.77 - 0.88 - 0.25 - 40.00 - 34.00 - 17.58 - 50.00 - 17.58 - 50.00 | 0.00 | |
| [] 2 1 405P | rules = 1 | 10.00 | 10.00 | 10.00 | 0.00 | 0.00 | 0.00 | 0.00 | | 0.00 | |
| Liama-3.1 405B | rules = 2 | 15.00 | 12.00 | 0.00 | 10.00 | 13.33 | 0.00 | 5.00 | | 0.00 | |
| | rules = 3 | 33.33 | 22.67 | 0.00 | 3.33 | 16.67 | 0.00 | 13.33 | | 0.00 | |
| CDT 4 | rules = 1 | 70.00 | 49.17 | 50.00 | 60.00 | 19.50 | 50.00 | 50.00 | | 10.00 | |
| GPT-40 | rules = 2 | 80.00 | 78.10 | 40.00 | 40.00 | 16.02 | 0.00 | 20.00 | | 0.00 | |
| | rules $= 3$ | 66.67 | 43.00 | 0.00 | 20.00 | 11.02 | 0.00 | 16.67 | | 0.00 | |
| | rules = 1 | 80.00 | 65.00 | 70.00 | 50.00 | 18.83 | 20.00 | 60.00 | | 40.00 | |
| DeepSeek-V3 | rules = 2 | 70.00 | 59.17 | 30.00 | 45.00 | 27.79 | 20.00 | 10.00 | | 0.00 | |
| | rules $= 3$ | 73.33 | 60.17 | 40.00 | 43.33 | 13.45 | 0.00 | 3.33 | | 0.00 | |
| | rules = 1 | 70.00 | 53.33 | 40.00 | 30.00 | 18.33 | 10.00 | 40.00 | | 40.00 | |
| o1-mini | rules $= 2$ | 70.00 | 66.67 | 50.00 | 50.00 | 47.50 | 20.00 | 40.00 | | 0.00 | |
| | rules = 3 | 90.00 | 79.17 | 50.00 | 23.33 | 23.33 | 0.00 | 26.67 | 17.58 | 0.00 | |
| | rules = 1 | 90.00 | 90.00 | 90.00 | 100.00 | 93.33 | 90.00 | 50.00 | | 50.00 | |
| o3-mini | rules $= 2$ | 100.00 | 100.00 | 100.00 | 80.00 | 75.00 | 60.00 | 70.00 | 69.17 | 40.00 | |
| | rules = 3 | 100.00 | 100.00 | 100.00 | 76.67 | 78.33 | 50.00 | 63.33 | 62.00 | 30.00 | |

Table 5: Right Output Strictly Local with sample size = 2

| Models | Settings | | $\mathbf{k} = 2$ | 2 | | k = 3 | 3 | | k = 4 | 1 |
|-------------|----------|--------|------------------|---------------|----------|-----------|---------------|--------|-----------|---------------|
| Models | Settings | recall | precision | compatibility | recall | precision | compatibility | recall | precision | compatibility |
| | | | | | vocab si | ze = 2 | | | | |
| | 0-shot | 60.00 | 55.00 | 60.00 | 30.00 | 23.33 | 20.00 | 10.00 | 10.00 | 10.00 |
| rules = 1 | 1-shot | 60.00 | 60.00 | 60.00 | 50.00 | 35.00 | 40.00 | 10.00 | 5.00 | 0.00 |
| | 2-shot | 70.00 | 70.00 | 70.00 | 70.00 | 50.00 | 60.00 | 20.00 | 10.00 | 10.00 |
| | 3-shot | 80.00 | 80.00 | 80.00 | 60.00 | 55.00 | 60.00 | 10.00 | 5.00 | 10.00 |
| | 0-shot | 60.00 | 65.00 | 50.00 | 45.00 | 60.00 | 30.00 | 15.00 | 8.25 | 0.00 |
| rules = 2 | 1-shot | 65.00 | 70.00 | 60.00 | 40.00 | 53.00 | 30.00 | 20.00 | 18.33 | 10.00 |
| | 2-shot | 85.00 | 85.00 | 80.00 | 45.00 | 56.67 | 20.00 | 25.00 | 23.33 | 0.00 |
| | 3-shot | 60.00 | 65.00 | 40.00 | 35.00 | 36.67 | 10.00 | 20.00 | 20.00 | 0.00 |
| | 0-shot | 53.33 | 68.33 | 20.00 | 30.00 | 46.67 | 10.00 | 16.67 | 8.54 | 0.00 |
| rules = 3 | 1-shot | 76.67 | 83.33 | 60.00 | 43.33 | 57.67 | 0.00 | 20.00 | 18.33 | 0.00 |
| | 2-shot | 86.67 | 86.67 | 60.00 | 26.67 | 28.33 | 0.00 | 13.33 | 16.67 | 0.00 |
| | 3-shot | 90.00 | 93.33 | 70.00 | 46.67 | 52.50 | 20.00 | 16.67 | 21.17 | 0.00 |
| | | | | | vocab si | ze = 3 | | | | |
| | 0-shot | 70.00 | 60.00 | 60.00 | 20.00 | 20.00 | 20.00 | 20.00 | 8.33 | 10.00 |
| rules = 1 | 1-shot | 90.00 | 90.00 | 90.00 | 50.00 | 50.00 | 50.00 | 30.00 | 30.00 | 30.00 |
| | 2-shot | 70.00 | 70.00 | 70.00 | 30.00 | 20.00 | 20.00 | 10.00 | 10.00 | 10.00 |
| | 3-shot | 40.00 | 40.00 | 40.00 | 40.00 | 35.00 | 40.00 | 30.00 | 18.33 | 20.00 |
| | 0-shot | 85.00 | 83.33 | 60.00 | 10.00 | 7.50 | 0.00 | 5.00 | 2.50 | 0.00 |
| rules = 2 | 1-shot | 90.00 | 95.00 | 80.00 | 10.00 | 13.33 | 0.00 | 5.00 | 2.50 | 0.00 |
| | 2-shot | 65.00 | 65.00 | 40.00 | 30.00 | 28.33 | 10.00 | 5.00 | 2.00 | 0.00 |
| | 3-shot | 65.00 | 75.00 | 30.00 | 5.00 | 3.33 | 0.00 | 5.00 | 2.50 | 0.00 |
| | 0-shot | 66.67 | 74.17 | 20.00 | 33.33 | 35.36 | 0.00 | 6.67 | 3.43 | 0.00 |
| rules = 3 | 1-shot | 70.00 | 69.17 | 40.00 | 20.00 | 22.50 | 0.00 | 10.00 | 13.33 | 0.00 |
| | 2-shot | 76.67 | 76.67 | 50.00 | 33.33 | 43.33 | 0.00 | 10.00 | 13.33 | 0.00 |
| | 3-shot | 60.00 | 60.83 | 10.00 | 23.33 | 31.67 | 0.00 | 16.67 | 19.76 | 0.00 |
| | | | | | vocab si | ze = 4 | | | | |
| | 0-shot | 60.00 | 60.00 | 60.00 | 30.00 | 30.00 | 30.00 | 10.00 | 10.00 | 10.00 |
| rules = 1 | 1-shot | 40.00 | 40.00 | 40.00 | 50.00 | 31.67 | 50.00 | 20.00 | 13.33 | 20.00 |
| | 2-shot | 70.00 | 57.00 | 60.00 | 30.00 | 25.00 | 30.00 | 10.00 | 5.00 | 0.00 |
| | 3-shot | 60.00 | 60.00 | 60.00 | 20.00 | 15.00 | 20.00 | 10.00 | 10.00 | 10.00 |
| | 0-shot | 40.00 | 40.00 | 30.00 | 15.00 | 11.67 | 0.00 | 0.00 | 0.00 | 0.00 |
| rules = 2 | 1-shot | 60.00 | 60.00 | 30.00 | 15.00 | 23.33 | 0.00 | 0.00 | 0.00 | 0.00 |
| | 2-shot | 80.00 | 90.00 | 60.00 | 15.00 | 12.50 | 0.00 | 15.00 | 10.67 | 0.00 |
| | 3-shot | 70.00 | 70.00 | 70.00 | 15.00 | 18.33 | 0.00 | 10.00 | 10.00 | 0.00 |
| | 0-shot | 53.33 | 68.33 | 20.00 | 6.67 | 5.00 | 0.00 | 10.00 | 5.32 | 0.00 |
| rules $= 3$ | 1-shot | 66.67 | 70.83 | 30.00 | 30.00 | 47.50 | 0.00 | 3.00 | 5.00 | 0.00 |
| | 2-shot | 66.67 | 73.33 | 30.00 | 30.00 | 55.00 | 0.00 | 3.33 | 3.33 | 0.00 |
| | 3-shot | 60.00 | 71.67 | 10.00 | 20.00 | 39.24 | 0.00 | 0.00 | 0.00 | 0.00 |

Table 6: Input Strictly Local with sample size = 2 with few-shot example

| Models | Settings | | k = 2 | | | k = . | 3 | | k = 4 | 4 |
|-----------|----------|--------|-----------|---------------|----------|-----------|---------------|--------|-----------|---------------|
| Wiodels | Settings | recall | precision | compatibility | recall | precision | compatibility | recall | precision | compatibility |
| | | | | 1 | ocab siz | e = 2 | | | | |
| | 0-shot | 50.00 | 45.00 | 50.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| rules = 1 | 1-shot | 80.00 | 80.00 | 80.00 | 40.00 | 33.33 | 30.00 | 20.00 | 5.00 | 20.00 |
| | 2-shot | 80.00 | 75.00 | 70.00 | 30.00 | 25.00 | 30.00 | 30.00 | 13.33 | 10.00 |
| | 3-shot | 80.00 | 80.00 | 80.00 | 20.00 | 15.00 | 20.00 | 20.00 | 15.00 | 20.00 |
| | 0-shot | 25.00 | 25.00 | 25.00 | 10.00 | 8.33 | 10.00 | 5.00 | 10.00 | 0.00 |
| rules = 2 | 1-shot | 80.00 | 85.00 | 70.00 | 30.00 | 30.83 | 10.00 | 30.00 | 19.00 | 10.00 |
| | 2-shot | 85.00 | 85.00 | 80.00 | 20.00 | 21.67 | 10.00 | 25.00 | 27.90 | 0.00 |
| | 3-shot | 75.00 | 80.00 | 60.00 | 25.00 | 20.83 | 10.00 | 20.00 | 20.83 | 0.00 |
| | 0-shot | 56.67 | 65.00 | 0.00 | 6.67 | 8.33 | 0.00 | 13.33 | 12.83 | 0.00 |
| rules = 3 | 1-shot | 80.00 | 80.00 | 80.00 | 40.00 | 42.00 | 0.00 | 10.00 | 11.67 | 0.00 |
| | 2-shot | 80.00 | 75.00 | 70.00 | 33.33 | 48.33 | 0.00 | 13.33 | 28.33 | 0.00 |
| | 3-shot | 80.00 | 80.00 | 80.00 | 33.33 | 39.17 | 0.00 | 16.67 | 26.67 | 0.00 |
| | | | | • | ocab siz | e = 3 | | | | |
| | 0-shot | 50.00 | 50.00 | 50.00 | 20.00 | 12.50 | 10.00 | 20.00 | 13.33 | 10.00 |
| rules = 1 | 1-shot | 100.00 | 100.00 | 100.00 | 40.00 | 23.33 | 40.00 | 0.00 | 0.00 | 0.00 |
| | 2-shot | 70.00 | 70.00 | 70.00 | 30.00 | 23.33 | 20.00 | 10.00 | 5.00 | 0.00 |
| | 3-shot | 80.00 | 75.00 | 80.00 | 20.00 | 20.00 | 20.00 | 20.00 | 20.00 | 20.00 |
| | 0-shot | 35.00 | 33.67 | 10.00 | 20.00 | 6.93 | 10.00 | 25.00 | 15.00 | 0.00 |
| rules = 2 | 1-shot | 80.00 | 76.67 | 80.00 | 30.00 | 30.33 | 10.00 | 10.00 | 15.00 | 0.00 |
| | 2-shot | 50.00 | 55.00 | 30.00 | 30.00 | 38.33 | 0.00 | 25.00 | 21.67 | 0.00 |
| | 3-shot | 70.00 | 70.00 | 70.00 | 20.00 | 30.00 | 0.00 | 20.00 | 35.00 | 0.00 |
| | 0-shot | 40.00 | 65.00 | 20.00 | 20.00 | 18.33 | 0.00 | 10.00 | 2.78 | 0.00 |
| rules = 3 | 1-shot | 70.00 | 66.67 | 40.00 | 30.00 | 24.83 | 0.00 | 10.00 | 20.30 | 10.00 |
| | 2-shot | 83.33 | 90.00 | 60.00 | 33.33 | 40.83 | 0.00 | 30.00 | 43.33 | 0.00 |
| | 3-shot | 70.00 | 78.33 | 30.00 | 23.33 | 44.50 | 0.00 | 16.67 | 18.33 | 0.00 |
| | | | | , | ocab siz | e = 4 | | | | |
| | 0-shot | 50.00 | 29.00 | 30.00 | 20.00 | 13.33 | 10.00 | 10.00 | 10.00 | 10.00 |
| rules = 1 | 1-shot | 50.00 | 50.00 | 50.00 | 50.00 | 50.00 | 50.00 | 20.00 | 15.00 | 20.00 |
| | 2-shot | 60.00 | 60.00 | 60.00 | 10.00 | 10.00 | 10.00 | 20.00 | 20.00 | 20.00 |
| | 3-shot | 20.00 | 20.00 | 20.00 | 30.00 | 25.00 | 30.00 | 20.00 | 20.00 | 20.00 |
| | 0-shot | 50.00 | 50.00 | 10.00 | 20.00 | 15.96 | 0.00 | 0.00 | 0.00 | 0.00 |
| rules = 2 | 1-shot | 55.00 | 56.67 | 30.00 | 20.00 | 28.33 | 0.00 | 0.00 | 0.00 | 0.00 |
| | 2-shot | 55.00 | 50.00 | 20.00 | 35.00 | 55.00 | 10.00 | 5.00 | 10.00 | 0.00 |
| | 3-shot | 10.00 | 20.00 | 0.00 | 30.00 | 33.33 | 10.00 | 10.00 | 20.00 | 0.00 |
| | 0-shot | 50.00 | 52.50 | 20.00 | 6.67 | 6.00 | 0.00 | 10.00 | 6.33 | 0.00 |
| rules = 3 | 1-shot | 56.67 | 68.33 | 20.00 | 20.00 | 36.25 | 0.00 | 16.7 | 22.83 | 0.00 |
| | 2-shot | 66.67 | 67.50 | 50.00 | 16.67 | 26.67 | 0.00 | 6.67 | 15.00 | 0.00 |
| | 3-shot | 3.33 | 3.33 | 0.00 | 23.33 | 40.83 | 0.00 | 3.33 | 3.33 | 0.00 |

Table 7: Left Output Strictly Local with sample size = 2 with few-shot example

| Models | Settings | _ | $\mathbf{k} = 2$ | 2 | | k = 3 | 3 | | k = 4 | 1 |
|-----------|----------|--------|------------------|---------------|----------|-----------|---------------|--------|-----------|---|
| 1/10ucis | Seemings | recall | precision | compatibility | recall | precision | compatibility | recall | precision | 10.00 10.00 20.00 10.00 - 10.00 0.00 0.00 0.00 0.00 0.00 10.00 30.00 10.00 10.00 0.00 |
| | | | | | vocab si | ze = 2 | | | | |
| | 0-shot | 40.00 | 40.00 | 40.00 | 20.00 | 10.00 | 10.00 | 20.00 | 10.00 | 10.00 |
| rules = 1 | 1-shot | 60.00 | 60.00 | 60.00 | 50.00 | 40.00 | 50.00 | 30.00 | 18.33 | 10.00 |
| | 2-shot | 60.00 | 60.00 | 60.00 | 40.00 | 35.00 | 40.00 | 30.00 | 25.00 | 20.00 |
| | 3-shot | 60.00 | 60.00 | 60.00 | 50.00 | 40.00 | 50.00 | 10.00 | 2.50 | 10.00 |
| | 0-shot | 40.00 | 40.00 | 30.00 | 15.00 | 18.33 | 10.00 | 20.00 | 18.67 | 10.00 |
| rules = 2 | 1-shot | 60.00 | 60.00 | 50.00 | 40.00 | 42.50 | 20.00 | 30.00 | 33.33 | 0.00 |
| | 2-shot | 70.00 | 80.00 | 60.00 | 45.00 | 43.33 | 30.00 | 20.00 | 27.50 | 0.00 |
| | 3-shot | 90.00 | 90.00 | 90.00 | 45.00 | 41.67 | 30.00 | 15.00 | 15.00 | 0.00 |
| | 0-shot | 63.33 | 76.67 | 30.00 | 23.33 | 24.17 | 0.00 | 10.00 | 7.83 | 0.00 |
| rules = 3 | 1-shot | 60.00 | 60.00 | 60.00 | 40.00 | 47.83 | 0.00 | 20.00 | 24.17 | 0.00 |
| | 2-shot | 60.00 | 60.00 | 60.00 | 50.00 | 48.33 | 20.00 | 16.67 | 18.33 | 0.00 |
| | 3-shot | 60.00 | 60.00 | 60.00 | 43.33 | 46.67 | 10.00 | 16.67 | 25.00 | 0.00 |
| | | | | | vocab si | ze = 3 | | | | |
| | 0-shot | 40.00 | 40.00 | 40.00 | 30.00 | 25.00 | 30.00 | 30.00 | 7.26 | 0.00 |
| rules = 1 | 1-shot | 70.00 | 65.00 | 60.00 | 40.00 | 35.00 | 40.00 | 20.00 | 15.00 | 10.00 |
| | 2-shot | 80.00 | 75.00 | 70.00 | 50.00 | 50.00 | 50.00 | 30.00 | 18.33 | 30.00 |
| | 3-shot | 70.00 | 65.00 | 60.00 | 40.00 | 35.00 | 40.00 | 20.00 | 15.00 | 10.00 |
| | 0-shot | 30.00 | 60.00 | 10.00 | 20.00 | 10.93 | 0.00 | 25.00 | 19.17 | 10.00 |
| rules = 2 | 1-shot | 65.00 | 70.00 | 40.00 | 30.00 | 45.00 | 10.00 | 15.00 | 11.67 | 0.00 |
| | 2-shot | 60.00 | 70.00 | 40.00 | 50.00 | 44.17 | 10.00 | 20.00 | 20.00 | 0.00 |
| | 3-shot | 65.00 | 70.00 | 40.00 | 30.00 | 45.00 | 10.00 | 15.00 | 11.67 | 0.00 |
| | 0-shot | 30.00 | 45.00 | 0.00 | 26.67 | 22.67 | 10.00 | 10.00 | 4.58 | 0.00 |
| rules = 3 | 1-shot | 80.00 | 80.83 | 40.00 | 30.00 | 37.59 | 0.00 | 13.33 | 11.00 | 0.00 |
| | 2-shot | 73.33 | 71.67 | 30.00 | 26.67 | 34.50 | 0.00 | 33.33 | 47.00 | 0.00 |
| | 3-shot | 80.00 | 80.83 | 40.00 | 30.00 | 37.60 | 0.00 | 13.33 | 11.00 | 0.00 |
| | | | | | vocab si | ze = 4 | | | | |
| | 0-shot | 40.00 | 25.00 | 30.00 | 40.00 | 23.33 | 20.00 | 10.00 | 10.00 | 10.00 |
| rules = 1 | 1-shot | 60.00 | 60.00 | 60.00 | 50.00 | 31.67 | 50.00 | 10.00 | 10.00 | 10.00 |
| | 2-shot | 80.00 | 68.33 | 80.00 | 60.00 | 33.33 | 30.00 | 20.00 | 20.00 | 20.00 |
| | 3-shot | 70.00 | 70.00 | 70.00 | 40.00 | 19.50 | 40.00 | 20.00 | 20.00 | 20.00 |
| | 0-shot | 45.00 | 47.33 | 10.00 | 50.00 | 45.83 | 10.00 | 5.00 | 1.67 | 0.00 |
| rules = 2 | 1-shot | 80.00 | 70.00 | 40.00 | 45.00 | 61.67 | 10.00 | 5.00 | 10.00 | 0.00 |
| | 2-shot | 65.00 | 65.00 | 40.00 | 45.00 | 52.50 | 20.00 | 0.00 | 0.00 | 0.00 |
| | 3-shot | 75.00 | 75.00 | 70.00 | 45.00 | 48.33 | 20.00 | 15.00 | 30.00 | 0.00 |
| | 0-shot | 33.33 | 39.50 | 10.00 | 30.00 | 23.85 | 0.00 | 10.00 | 10.83 | 0.00 |
| rules = 3 | 1-shot | 66.67 | 71.83 | 30.00 | 23.33 | 30.83 | 0.00 | 3.33 | 2.50 | 0.00 |
| | 2-shot | 83.33 | 86.50 | 50.00 | 26.67 | 37.50 | 0.00 | 13.33 | 28.83 | 0.00 |
| | 3-shot | 76.67 | 80.00 | 50.00 | 40.00 | 51.67 | 10.00 | 13.33 | 20.00 | 0.00 |

Table 8: Right Output Strictly Local with sample size = 2 with few-shot example