Consistency-Aware Online Multi-Objective Alignment for Related Search Query Generation

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Abstract

Modern digital platforms rely on related search query recommendations to enhance engagement, yet existing methods fail to reconcile click-through rate (CTR) optimization with topic expansion. We propose CMAQ, a Consistent Multi-Objective Aligned Query generation framework that harmonizes these goals through three components: (1) reward modeling to quantify objectives, (2) style alignment for format compliance, and (3) consistency-aware optimization to coordinate joint improvements. CMAQ employs adaptive β -scaled DPO with geometric mean rewards, balancing CTR and expansion while mitigating objective conflicts. Extensive offline and online evaluations in a large-scale industrial setting demonstrate CMAQ's superiority, achieving significant CTR gains (+2.3%) and higher human-rated query quality compared to stateof-the-art methods. Our approach enables highquality query generation while sustaining user engagement and platform ecosystem health.

1 Introduction

Modern digital platforms use related search query recommendation to enhance user experience. An example is illustrated in Figure 1. When users interact with content, the system displays a single related query below it, minimizing disruption. This design serves three key functions: (1) proactive discovery, reducing exploration friction via contextual suggestions; (2) interest scaffolding, enabling gradual topic expansion while avoiding choice overload; and (3) feedback enrichment, where user interactions refine search ranking and content recommendations. By improving user satisfaction and understanding of emerging topics, this mechanism boosts user retention and ecosystem health.

Despite its industrial significance, academic research on related search query recommendation

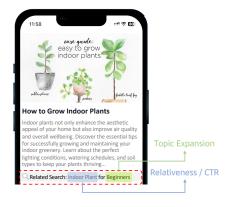


Figure 1: An illustration of the related search query recommendation scenario. A good query should excel in both CTR and topic expansion.

remains limited. Existing methods fall into two categories: retrieval-based and generation-based approaches. Retrieval-based methods (Wang et al., 2023c; Huang et al., 2018; Cao et al., 2008) rely on historical user behavior to retrieve queries from a pool, aligning with sequential patterns but struggling with cold-start content and seamless integration with primary content. In contrast, generation-based methods (Sannigrahi et al., 2024; Wang et al., 2024b), which directly generate queries by considering user interests and context, exhibit superior generalization for cold-start scenarios. Thus, we focus on the generative approach.

An effective query recommendation system must balance two key dimensions: *relevance* to the user's immediate interests, measurable via click-through rate (CTR), and *topic expansion*, crucial for avoiding filter bubbles (Gao et al., 2023a,b; Bi et al., 2024) and maintaining diversity (Gao et al., 2025b; Kang et al., 2025). However, these objectives often conflict: over-prioritizing relevance leads to narrow recommendations, while excessive focus on topic expansion risks deviating from user intent. Existing methods fail to address this trade-off, motivating our work to align both objectives consistently.

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We leverage large language models (LLMs) (Li et al., 2024; Wang et al., 2023b), whose powerful capabilities make them well-suited for query generation. To mitigate LLM inference latency, we precompute query candidates offline for use in online scenarios. However, directly deploying pre-trained LLMs yields suboptimal performance due to misalignment with task-specific preferences—relevance and topic expansion. Aligning LLMs with these objectives is challenging, as reliable reward signals are hard to obtain: CTR requires extensive online exposure, and topic expansion relies on costly manual annotations. How to consistently enhance the model to achieve both objectives is also critical in this task, i.e., generating queries that offer substantial topic expansion while maintaining a high CTR.

To address these challenges, we propose Consistent Multi-Objective Aligned Query Generation (CMAQ). CMAQ consists of three steps: (1) precise reward modeling, training reward models using annotated content-query pairs; (2) query style alignment, fine-tuning the LLM to produce correctly formatted queries; and (3) consistent multi-objective alignment, introducing a novel training strategy to balance both objectives. The optimization process follows an iterative online DPO paradigm, where generated queries are evaluated by reward models and used to refine the policy. Extensive evaluations demonstrate CMAQ's effectiveness in generating high-quality search queries. Our key contributions are:

- Formulating related search query recommendation as a multi-objective query generation task.
- Proposing CMAQ, a framework for consistent multi-objective alignment in LLMs, balancing CTR and topic expansion.
- Demonstrating significant improvements via comprehensive offline and online evaluations in a large-scale industrial setting.

2 Related Work

Query Generation. Query generation in content platform is the process of generating new search queries that align with a user's current interests (Li et al., 2024). Existing techniques primarily address scenarios where users have already entered a query prefix, aiming to refine these queries through methods such as query suggestion (Wang et al., 2020; Bacciu et al., 2024), query rewrite (Wang et al., 2023a; Feng et al., 2024; Peng et al., 2024), and

personalized query suggestion (Baek et al., 2024; Zhong et al., 2020) incorporating user history and interactions. These approaches assume that users have already demonstrated active search behavior and have initiated a search process.

Our work differs by aiming to provide potential search options to users while they are browsing content, thereby stimulating their interest in active exploration. In this context, early studies on seq2seq models were proposed by (Nogueira et al., 2019; Penha et al., 2023). Recently, some researchers have explored using LLM prompts to generate search terms from context (Sannigrahi et al., 2024), while others have focused on generating search queries in a multimodal context (Wang et al., 2024b). However, these methods overlook the multi-objective alignment problem in query generation. Our approach addresses this gap by simultaneously consider both CTR objective and expansion objective.

Direct Preference Optimization. Learning from human feedback is essential for aligning LLMs with human values (Bai et al., 2022; Ouyang et al., 2022; Ziegler et al., 2019). Recently, DPO-based methods (Rafailov et al., 2023; Ethayarajh et al., 2024; Meng et al., 2024; Wu et al., 2024; Gao et al., 2025a) directly align LLMs with an offline preference dataset, showcasing enhanced training stability and reduced training cost in comparison to traditional RL-based methods (Schulman et al., 2017). Online DPO (Yuan et al., 2024; Xiong et al., 2024; Pang et al., 2024) extends fixed offline preference dataset by continuously updating model preferences from real-time generated responses, enabling dynamic adaptation. Multi-objective DPO (Ramé et al., 2023; Wang et al., 2024a; Zhou et al., 2024; Shi et al., 2024) incorporates multiple criteria for alignment, allowing the model to balance and optimize different human values simultaneously. In industrial scenarios, aligning human preference also attracted attentions, such as query rewrite (Peng et al., 2024), advertising image generation (Chen et al., 2025) and advertising text generation (Wei et al., 2022), however, they primarily focus on aligning their tasks with the CTR objective, overlooking the alignment with broader objectives that impact generation quality, potentially resulting in diminished user experience. In contrast, our method accounts for multi-objective alignment.

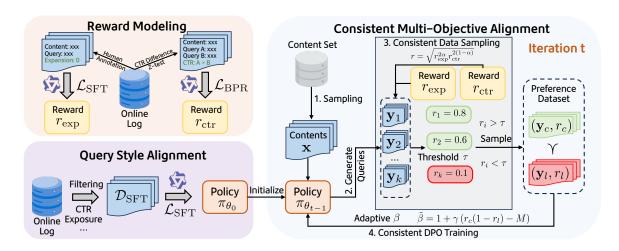


Figure 2: The framework of our proposed CMAQ framework.

3 Methodology

In this section, we introduce our CMAQ framework (*cf.* Figure 2), which consists of three components: reward modeling, query style alignment, and consistent multi-objective alignment. For multi-objective alignment, we primarily focus on the CTR objective and the expansion objective, while our framework is flexible and can be extended to accommodate additional objectives.

3.1 Reward Modeling

To align generated queries with online user preferences, we train two reward models (RMs) using user feedback data, focusing on CTR and topic expansion. These RMs are integrated into the query generation pipeline to guide optimization. Both RMs are based on Qwen2.5-1.5B (Yang et al., 2025) and fine-tuned using LoRA (Hu et al., 2022).

Reward Model for Topic Expansion This RM is designed to determine whether a query extends the context of a given content item, formulated as a binary classification problem. We utilize 337,291 outsourced labeled samples, split 8:2 for training and testing. Among these, 48.8% are labeled as positive (represented by token "1") and the remainder as negative (represented by token "0"). Let x denote the content and y the query. The expansion reward $r_{\rm exp}({\bf x},{\bf y})$ is computed as: $r_{\rm exp}({\bf x},{\bf y})=$ $\frac{p(\text{"1"}|\mathbf{x},\mathbf{y})}{p(\text{"0"}|\mathbf{x},\mathbf{y})+p(\text{"1"}|\mathbf{x},\mathbf{y})}$, where $p(\text{"1"}|\mathbf{x},\mathbf{y})$ represents the probability of the RM predicting the positive token "1". We use the standard next-token prediction loss to train this RM. The prompt template used for fine-tuning is detailed in Appendix A.1. The final model achieves a classification accuracy of 72.5%.

Reward model for CTR The RM for CTR is designed to predict which of two queries, given the same content, is expected to achieve a higher CTR. This model extends the base architecture with a regression head. We sampled content-query pairs (\mathbf{x}, \mathbf{y}) with more than 100 impressions and performed z-tests on impressions and clicks to identify pairs with statistically significant CTR differences (p < 0.01). This process yielded 328,328 $(\mathbf{x}, \mathbf{y}_+, \mathbf{y}_-)$ pairs, where \mathbf{y}_+ denotes the query with higher CTR for the content \mathbf{x} and \mathbf{y}_- denotes the query with lower CTR for the content \mathbf{x} . For the training of the RM, we use Bayesian Personalized Ranking (BPR) loss (Rendle et al., 2009), ensuring reliable distinctions in CTR:

$$\mathcal{L}_{BPR} = -\log \sigma \left(r_{ctr}(\mathbf{x}, \mathbf{y}_{+}) - r_{ctr}(\mathbf{x}, \mathbf{y}_{-}) \right). \tag{1}$$

The dataset was split 8:2 for training and testing, achieving a pair accuracy of 91.9%, which measures whether the query with a higher CTR receives a higher reward. In practice, the regression output directly serves as the CTR reward $r_{\rm ctr}({\bf x},{\bf y})$.

3.2 Query Style Alignment

Initially, we attempted zero-shot or few-shot prompting without fine-tuning the backbone LLM. However, this approach often produced queries that were either non-compliant with instructions, stylistically mismatched with the platform, or contained hallucinated information. To address this, we focused on aligning the query style of the LLM. We constructed a large-scale offline training set $\mathcal{D}_{SFT} = \{(\mathbf{x}_i, \mathbf{y}_i)\}$ containing 1,292,031 samples extracted from online logs, leveraging exposure and CTR data to guide this alignment. Supervised

Fine-Tuning (SFT) was then applied to preliminarily align the LLM with the platform's query style, ensuring that generated queries adhere to the expected format and tone:

$$\mathcal{L}_{SFT} = -\mathbb{E}_{(\mathbf{x}, \mathbf{y}) \sim \mathcal{D}_{SFT}} \frac{1}{|\mathbf{y}|} \sum_{i=1}^{|\mathbf{y}|} \log \pi_{\theta}(y_i | \mathbf{x}, \mathbf{y}_{< i}),$$
(2)

where π_{θ} denotes the model's predicted probability for token y_i given prior tokens and the content.

3.3 Consistent Multi-Objective Alignment

While query style alignment enables the model to mimic real query styles, it does not guarantee high-quality query generation. High-quality queries should not only attract user clicks (high CTR) but also stimulate new search demands (high topic expansion). Therefore, further alignment of these dual objectives is crucial. To minimize reliance on extensive online logs and manual labeling, we employed an online DPO approach. Additionally, we introduced a consistency-aware strategy to mitigate conflicts between the two objectives during both data sampling and training stages.

3.3.1 Consistent Data Sampling

In each iteration t, we sample N content from the offline dataset \mathcal{D}_{SFT} . For each content \mathbf{x} , the model from the previous iteration samples k queries $(\mathbf{y}_1,\ldots\mathbf{y}_k)\sim\pi_{\theta_{t-1}}(\cdot|\mathbf{x})$, each evaluated on both objectives. To ensure the same scaling of both rewards, we normalize r_{ctr} into [0,1]. To ensure consistency across both objectives, we used the geometric weighted average $r(\mathbf{x},\mathbf{y}_i)=\sqrt{r_{\text{exp}}(\mathbf{x},\mathbf{y}_i)^{2\alpha}r_{\text{ctr}}(\mathbf{x},\mathbf{y}_i)^{2(1-\alpha)}}$ as the consistency criterion for the queries. By setting two thresholds τ_1 and τ_2 we sample a positive sample \mathbf{y}_c from those with the reward $r>\tau_1$, and a negative sample \mathbf{y}_l with $r<\tau_2$, forming the preference dataset $\mathcal{D}_t=\{(\mathbf{x},\mathbf{y}_c,\mathbf{y}_l,r_c,r_l)\}$ for the DPO training in the iteration t.

Remark: We use the geometric average instead of the arithmetic average as the overall reward $r(\mathbf{x}, \mathbf{y}_i)$ since it enforces stricter consistency between the two objectives. As illustrated in Figure 3, when one reward approaches zero, the geometric average collapses toward zero regardless of the other reward, ensuring consistent optimization on both rewards.

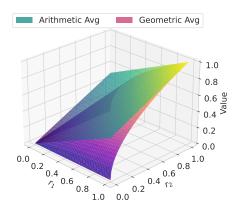


Figure 3: Illustration of the arithmetic average: $(r_1 + r_2)/2$ and geometric average $\sqrt{r_1r_2}$ over the domain $[0,1] \times [0,1]$, demonstrating that the geometric average is more suitable for reflecting consistent multi-objective improvement.

3.3.2 Consistent Training

We adapt and extend DPO (Rafailov et al., 2023) in CMAQ. In DPO, the hyperparameter β controls the strength of KL-divergence regularization between the policy model π_{θ_t} and the reference model $\pi_{\theta_{t-1}}$. The optimal value of β depends on the quality of pairwise preference data (Wu et al., 2024). In our task, the consistency criterion r serves as a proxy for data quality: high-quality pairs exhibit a significantly higher r_c (positive sample) and a substantially lower r_l (negative sample), while lowquality pairs lack this distinction. To account for this variability, we propose a sample-level adaptive β , which dynamically scales β based on the consistency of each training pair. This approach amplifies the influence of high-consistency samples while reducing the impact of low-consistency ones.

For a sample $(\mathbf{x}, \mathbf{y}_c, \mathbf{y}_l, r_c, r_l)$, we compute the sample-level $\tilde{\beta}$ as: $\tilde{\beta} = 1 + \gamma \left(r_c (1 - r_l) - M \right)$, where $M = \frac{1}{|\mathcal{D}_t|} \sum_{(r_c, r_l) \in \mathcal{D}_t} r_c (1 - r_l)$ represents the average consistency across the dataset. Following (Pang et al., 2024), we incorporate an NLL loss term, weighted by λ , to prevent over-suppression when the chosen query closely resembles the rejected query. The final loss is given by:

$$\mathcal{L}_{\theta_{t}} = -\mathbb{E}_{(\mathbf{x}, \mathbf{y}_{c}, \mathbf{y}_{l}) \sim \mathcal{D}_{t}} \left[\ell(\pi_{\theta}, \mathbf{x}, \mathbf{y}_{c}, \mathbf{y}_{l}) + \lambda \frac{\log \pi_{\theta_{t}}(\mathbf{y}_{c}|\mathbf{x})}{|\mathbf{y}_{c}|} \right],$$
with $\ell(\cdot) = \log \sigma \left(\tilde{\beta} \frac{\pi_{\theta_{t}}(\mathbf{y}_{c}|\mathbf{x})}{\pi_{\theta_{t-1}}(\mathbf{y}_{c}|\mathbf{x})} - \tilde{\beta} \frac{\pi_{\theta_{t}}(\mathbf{y}_{l}|\mathbf{x})}{\pi_{\theta_{t-1}}(\mathbf{y}_{l}|\mathbf{x})} \right).$
(3)

4 Experiments

4.1 Experiment Setting

Datasets To the best of our knowledge, no public dataset exists for related search query generation. Therefore, we collected data from a leading content platform. The statistics of the training data are presented in §3. For the test dataset, we randomly sampled 3,124 content items from the training dataset \mathcal{D}_{SFT} . To prevent data leakage, any samples with identical content in the test dataset were excluded from \mathcal{D}_{SFT} . More detailed information on data preprocessing and filtering is provided in A.4.

Baselines We selected two types of comparative approaches. The first type includes non-multi-objective approaches: (1) Zero-shot, where queries are generated directly by LLM without fine-tuning. (2) QSA (Query Style Alignment), as discussed in $\S 3.\overline{2}$, aligns the query style using SFT within \mathcal{D}_{SFT} . (3) DPO (Rafailov et al., 2023), We employ pairwise preference data for CTR reward modeling to fine-tune the QSA model directly using DPO loss.

The second type includes multi-objective alignment approaches, which use the RMs described in §3.1 to obtain two scores for their generated responses, and further fine-tuned on the QSA model: (1) <u>DPO-LW</u> (Zhou et al., 2024), which uses weighted arithmetic average to combines the DPO losses for each objective to form the final loss. (2) <u>DPO-Soup</u> (Ramé et al., 2023), which involves training two models that align with each objective separately, followed by a weighted parameter merge to derive the final model. (3) <u>MORL</u> (Wu et al., 2023), which performs a weighted arithmetic average of the two rewards and then selects the highest and lowest ones to form preference pairs.

Implementation Details All baselines are based on Qwen-2.5-7B-Instruct and fine-tuned using LoRA to ensure a fair comparison. For all DPO-based baselines, we fine-tuned the model for 3 epochs. In the case of multi-objective alignment baselines, the preference dataset is generated at the start of training and remains fixed throughout the training process. For CMAQ, we trained it for 3 iterations, with each iteration comprising 1 epoch. We set the number of training samples per epoch to N=20,000, the number of generated query candidates k=8, the weight for the NLL loss $\lambda=0.5$, and $\gamma=0.2$. The trade-off weight in data sampling α is tuned in [0.2,0.4,0.6,0.8] for all multi-objective baselines, larger α indicates more

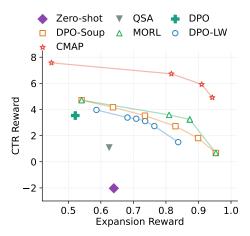


Figure 4: Pareto Fronts of all compared methods.

attention on expansion objective. More experimental details can be found in A.4.

Evaluation Our framework prioritizes CTR and expansion of generated query: in offline experiments, we directly adopt $r_{\rm ctr}$ and $r_{\rm exp}$ as evaluation metrics, bypassing traditional NLG metrics like BLEU or ROUGE. For online validation, we measure actual CTR on content platforms and incorporate human-annotated quality assessments to holistically evaluate both the practical impact and creative coherence of the outputs.

4.2 Offline Experiments

The performance comparison on the Pareto Fronts of all compared methods is presented in Figure 4. It is important to note that for non-multi-objective baselines, only a single run is conducted as no tradeoff is required. From the results, we can observe the following: (1) The Pareto Front of CMAQ significantly exceeds all baseline methods, demonstrating its effectiveness in achieving consistent improvements in both CTR and expansion objectives. (2) Multi-objective methods exhibit superior Pareto Fronts compared to non-multi-objective baselines, highlighting the effectiveness of considering both objectives along with the guidance provided by reward signals. (3) DPO achieves higher CTR rewards while showing a decline in expansion compared to QSA, indicating the presence of conflicts between the two objectives. Therefore, it is crucial to consider consistent optimization for multiple objectives in query generation.

4.3 In-depth Analysis

Ablation Study To validate the effectiveness of each component within our framework, we con-

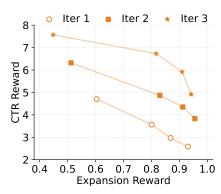


Figure 5: Pareto Fronts of different iterations.

duct ablation studies on three variants of CMAQ: (1) Removing the online query generation at the start of each iteration by utilizing a fixed preference dataset for each iteration, denoted as w/o OT; (2) Removing consistent data sampling by using a weighted arithmetic average instead of a geometric average, denoted as w/o CDS; (3) Removing consistent training by employing a static β in DPO training, denoted as w/o CT.

Table 1 displays the performance of CMAQ and its three variants under two distinct settings, $\alpha=0.4$ and $\alpha=0.6$. From the results we can see that (1) removing each component in our framework decreases the performance, validating their effectiveness. (2) The removal of online training leads to a significant deterioration in $r_{\rm ctr}$, primarily attributed to the absence of iterative on-policy training sample updates. This deficiency substantially diminishes the capacity of training samples to provide effective optimization guidance for model enhancement as the model has already aligned well with the original dataset. (3) The elimination of CDS results in heightened sensitivity to the parameter α , exhibiting a "seesaw effect" where small changes in α lead to sudden shifts in optimization, disproportionately favoring either the CTR or expansion objectives. This issue arises from the limitations of arithmetic mean-based optimization, as discussed in §3, which fails to effectively consistent improvements between dual objectives.

The Impact of Training Iterations To further illustrate the impact of online training, Figure 5 displays the Pareto Front of CMAQ at each iteration. As iterations progress, we observe improved performance, demonstrating the effectiveness of the online training paradigm.

Table 1: Ablation studies on CMAQ. Here, OT, CDS, CT stand for *Online Training*, *Consistent Data Sampling*, and *Consistent Training*, respectively.

Setting	$\alpha = 0.4$		$\alpha = 0.6$	
	$r_{ m ctr}$	$r_{\rm exp}$	$r_{ m ctr}$	$r_{\rm exp}$
CMAQ	6.730	0.817	5.918	0.912
w/o OT	4.055	0.812	3.032	0.906
w/o CDS	6.958	0.481	3.260	0.959
w/o CT	6.672	0.792	5.348	0.910

4.4 Online Experiments

Online Deployment To evaluate the effectiveness of our proposed method in real-world industrial settings, we deployed CMAQ on a local lifestyle information app Dianping, and conducted an online A/B test over a one-week period. We propose to leverage LLMs for query generation as an additional recall pathway in related search scenario. Specifically, we conducted a week-long A/B test involving approximately 3,000,000 contents, where each method employed beam search to sample 5 queries per content. Upon completion of query generation, we further filtered all generated queries through a series of criteria, including lexical quality, relevance, and harmfulness, resulting in the removal of less than 10% of the generated queries. The retained queries were then associated with their respective content and cached in the recall pool. During online service, a fine-grained ranking model determines whether to expose these queries to users. The entire inference process can be executed in offline or nearline modes, allowing for pre-computation and caching of new content, thereby eliminating the need for real-time inference upon user requests and ensuring service efficiency and latency requirements are met.

Online Results The results are presented in Table 2. For data security reasons, CTR results are reported in relative terms, with QSA serving as the baseline model in the A/B test. This experiment gathered over 20 million impressions to ensure the reliability and statistical significance of the CTR results. More detailed online settings can be found in A.4. From the results, we observe the following: (1) DPO demonstrates significant improvement over QSA, highlighting the effectiveness of CTR objective alignment. (2) Multi-objective based methods consistently outperform DPO, suggesting that optimizing for expansion may also contribute positively to CTR. (3) CMAQ achieves the best online CTR

Table 2: The performance of different methods in online A/B test. Δ CTR stands for the relative CTR improvement over QSA: $\frac{\text{CTR}_{\text{method}} - \text{CTR}_{\text{QSA}}}{\text{CTR}_{\text{QSA}}}.$

Method	Δ CTR		
DPO	+0.985%		
MORL	+1.401%		
CMAQ	+2.305%		

	Good	b	Same		Bad
CMAQ	34%				9%
MORL	28%				14%
DPO	26%				20%

Figure 6: Human Evaluation.

performance, indicating its capability to minimize conflicts between the two objectives.

4.5 Human Evaluation

To validate the quality of queries generated by the model, we conducted a manual GSB (Good-Same-Bad) test on the online methods. Specifically, we randomly selected 200 contents and had human evaluators compare the query quality generated by the online models and QSA. The evaluation criteria included relevance, expansion, and spelling errors. As shown in Figure 6, our proposed CMAQ achieved the best results in comparison with QSA, demonstrating the improvement in query quality offered by our method.

5 Conclusion

In this paper, we introduce CMAQ, a query generation method that formulates related search query generation as a multi-objective alignment task, aligning both CTR and expansion objectives through the online DPO paradigm. We employ consistent data sampling and training strategies to enhance the effectiveness of this multi-objective alignment. Both offline and online experiments demonstrate that CMAQ yields significant improvements in key industrial metrics.

In the future, we aim to take personalization into LLM-based query generation and expand the range of objectives considered in the alignment. We also plan to improve the diversity of the LLM-generated queries while maintaining the performance.

Acknowledgments

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Ethical Considerations

In deploying our query generation model as a supplemental recall mechanism, we prioritize two key ethical principles. (1) Data Privacy Protection: All training and inference processes exclusively utilize fully anonymized search session data, with no access to user-specific profiles, search histories, or demographic identifiers. The model operates solely on aggregated query patterns, ensuring complete dissociation from individual users. (2) Content Safety Risks: While our framework filters explicit harmful content, automatically generated queries might inadvertently propagate subtle biases from historical search distributions. We mitigate this through regular human audits of sampled outputs and explicit exclusion of sensitive topics during candidate generation.

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A Appendix

A.1 Prompts

Here, we introduce the prompts used in the query generation and expansion reward models. For the CTR reward model, as it is treated as a regression task, we do not design a specific prompt template. Instead, the input to the CTR reward model is simply the concatenation of (title, content, shopinfo, query).

Prompt for Query Generation

You are a user of a leading local lifestyle information platform that provides shop info, consumer reviews, discounts, and nearby lifestyle information. You often browse user-generated content and excel at summarizing and extending related interest queries to help other users explore more related information.

Requirements:

- 1. Provide only one answer, keep it within 15 words.
- 2. Output the answer directly, without any explanations or unnecessary prefixes.
- 3. The answer should be related to the content but not just a summary, guiding users to search for more related topics.

Given a note, please summarize and extend the interest queries for the content.

##Note Content Title: {{title}}

Content: {{content_body}}
Shop info: {{shopinfo}}

Answer:

Prompt for Expansion Reward Model

You are a search term quality assessment expert. Based on the following note content and query, score the query's expansion (0 or 1), and output the result in the specified format without explanations.

Expansion: Does the search query include information beyond the note content that can spark user interest for further exploration? It might involve novel, interesting, or trending topics that seem worth delving into.

Score 0: Completely redundant information (directly copying POI name/title queries), with no apparent extensibility, as the information is fully covered by the note content, and users can get complete information without further clicking.

Score 1: Has a certain extensibility. Even if the note doesn't mention this information, if the query can guide users to acquire new useful information (like reservation methods) or encourage comprehensive exploration of the place (like "exploring shop" queries), it is considered to have extensibility.

##Note Content
Title: {{title}}

Content: {{content_body}}
Shop info: {{shopinfo}}
Output ({content_body})

Query: {{query}}

Answer:

Algorithm 1: Consistent Multi-Objective Alignment

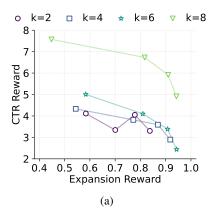
```
Data: Offline content dataset \mathcal{D}_{SFT}, QSA model \pi_{\theta_{OSA}}, Threshold \tau_1, \tau_2, Adaptation rate \gamma,
                 Trade-off parameter \alpha, Sample number N, Generation number k, Max iteration T
Initialize policy \pi_{\theta_0} \leftarrow \pi_{\theta_{\text{OSA}}};
for iteration t = 1, 2, \dots T do
         \mathcal{D}_t \leftarrow \emptyset;
         Sample contents \{\mathbf{x}\}_1^N \sim \mathcal{D}_{SFT}; for content \mathbf{x} \in \{\mathbf{x}\}_1^N do
                  Generate queries \{\mathbf{y}_1, \mathbf{y}_2, ..., \mathbf{y}_k\} \sim \pi_{\theta_{t-1}}(\cdot | \mathbf{x});
Compute rewards r_i = \sqrt{r_{\mathrm{exp}}^{2\alpha}(\mathbf{x}, \mathbf{y}_i) r_{\mathrm{ctr}}^{2(1-\alpha)}(\mathbf{x}, \mathbf{y}_i)} for each \mathbf{y}_i;
                   \mathcal{D}_{pos}, \mathcal{D}_{neg} \leftarrow \emptyset, \emptyset;
                   for query i = 1, 2, \dots k do
                            if r_i > \tau_1 then
                            \begin{array}{l} & \quad \text{if } r_i < \tau_1 \text{ then} \\ & \quad \mathcal{D}_{\text{pos}} \leftarrow \mathcal{D}_{\text{pos}} \cup \{(\mathbf{x}, \mathbf{y}_i, r_i)\}; \\ & \quad \text{if } r_i < \tau_2 \text{ then} \\ & \quad \mathcal{D}_{\text{neg}} \leftarrow \mathcal{D}_{\text{neg}} \cup \{(\mathbf{x}, \mathbf{y}_i, r_i)\}; \end{array} 
                  if \mathcal{D}_{pos} \neq \emptyset and \mathcal{D}_{neg} \neq \emptyset then
                          (\mathbf{y}_c, r_c) \sim \mathcal{D}_{pos};
                         (\mathbf{y}_l, r_l) \sim \mathcal{D}_{\text{neg}};

\mathcal{D}_t \leftarrow \mathcal{D}_t \cup \{(\mathbf{x}, \mathbf{y}_c, \mathbf{y}_l, r_c, r_l)\};
         Compute averge reward M = \frac{1}{|\mathcal{D}_t|} \sum_{(r_c, r_l) \in \mathcal{D}_t} r_c (1 - r_l);
         for data sample (\mathbf{x}, \mathbf{y}_c, \mathbf{y}_l, r_c, r_l) \in \mathcal{D}_t do
                   Compute adaptive \tilde{\beta} = 1 + \gamma (r_c(1 - r_l) - M);
                   Perform Consistent DPO Training via Equation (3);
```

A.3 Data Collection

We construct the dataset \mathcal{D}_{SFT} where each sample (\mathbf{x}, \mathbf{y}) is a tuple of (content, query). The construction procedure of \mathcal{D}_{SFT} mainly includes the following steps:

- Core Metric Aggregation. We first aggregate behavioral signals (page views, clicks) at the contentquery level through temporal summation, with the time spans one year. This initial phase establishes baseline engagement metrics and computes derived indicators including CTR. A minimum exposure threshold eliminates statistically insignificant observations.
- Multi-Dimensional Filtering. The raw dataset undergoes successive quality filters:
 - Lexical constraints: Remove short/non-compliant queries through length thresholds and regex pattern matching.
 - Engagement thresholds: Eliminate low-CTR entries through percentile-based cutoffs
 - Commercial term exclusion: Filter queries containing promotional phrases via predefined blocklists
 - Semantic redundancy checks: Exclude queries exhibiting high similarity to shop names through normalized Levenshtein distance calculations
- **Diversity-Preserving Sampling.** To ensure categorical diversity and prevent domain dominance in the training corpus, we implement a stratified sampling strategy grounded in content taxonomy. The dataset is first partitioned by content categories. Within each categorical partition, entries are ranked



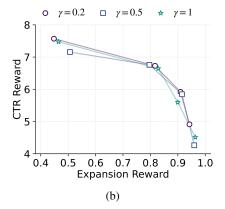


Figure 7: (a) The Pareto Front of CMAQ under different query sample times $k \in [2, 4, 6, 8]$. (b) The Pareto Front of CMAQ under different scaling coefficient γ in obtaining $\tilde{\beta}$, where $\gamma \in [0.2, 0.5, 1]$.

through a composite scoring metric prioritizing CTR while considering auxiliary quality signals. A maximum cap of 10,000 samples per category is enforced to prevent the bias of prevalent domains.

Finally, we collected \mathcal{D}_{SFT} for both quality style alignment and consistent multi-objective alignment processes. The size of \mathcal{D}_{SFT} is 1,292,031.

A.4 Detailed Experiment Settings

For all fine-tuning experiments in each iteration, we utilize PyTorch 2.1.0¹ (Paszke et al., 2019) in conjunction with HuggingFace's TRL framework². Experiments are executed on eight A100 GPUs, with each iteration requiring approximately 10 GPU hours, including query generation, rewarding and training. We employ the AdamW optimizer (Loshchilov and Hutter, 2019) with a learning rate of 1e-5 and a cosine learning rate schedule incorporating 20 warmup steps. The temperature is set to 1.5 in generation k queries to ensure the diversity for iterative DPO training. The training process spans 1 epochs with a global batch size of 32. For LoRA training, we set the rank r = 32, and the $\alpha = 8$. For online inference, we utilize vLLM³ (Kwon et al., 2023) for speed-up.

A.5 Supplementary Experimental Results

We conducted additional experiments to investigate the impact of the sampling number k and the scaling coefficient γ in Equation (3) on the performance.

The impact of sample times k Figure 7a illustrates that the performance of CMAQ improves as k increases, suggesting that additional sampling instances contribute to more diverse information during training. As the number of sample times rises with k, we select k=8 for our final model, balancing the trade-off between performance and efficiency.

Parameter sensitivity of γ Figure 7b indicates that CMAQ exhibits robustness across various values of γ . This suggests that the method maintains its effectiveness despite changes in the hyperparameter settings, making it adaptable to different conditions.

¹https://pytorch.org/

²https://github.com/huggingface/trl

³https://github.com/vllm-project/vllm