

MEMORY CAPACITY AND SENTENCE PROCESSING

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ABSTRACT

The limited capacity of working memory is intrinsic to human sentence processing, and therefore must be addressed by any theory of human sentence processing. This paper gives a theory of garden-path effects and processing overload that is based on simple assumptions about human short term memory capacity.

1 INTRODUCTION

The limited capacity of working memory is intrinsic to human sentence processing, and therefore must be addressed by any theory of human sentence processing. I assume that the amount of short term memory that is necessary at any stage in the parsing process is determined by the syntactic, semantic and pragmatic properties of the structure(s) that have been built up to that point in the parse. A sentence becomes unacceptable for processing reasons if the combination of these properties produces too great a load for the working memory capacity (*cf.* Frazier 1985):

(1)

$$\sum_{i=1}^n A_i x_i > K$$

where:

K is the maximum allowable processing load (in processing load units or PLUs),

x_i is the number of PLUs associated with property i ,

n is the number of properties,

A_i is the number of times property i appears in the structure in question.

Furthermore, the assumptions described above provide a simple mechanism for the explanation of common psycholinguistic phenomena such as garden-path effects and preferred readings for ambiguous sentences. Following Fodor (1983), I assume that the language processor is an automatic device that uses a greedy algorithm: only the best of the set of all compatible representations for an input string are locally maintained from word to word. One way to make this idea explicit is to assume that restrictions on memory allow at most one representation for an input string at any time (see, for example, Frazier and Fodor 1978; Frazier 1979; Marcus 1980; Berwick and Weinberg 1984; Pritchett 1988). This hypothesis, commonly called the serial

hypothesis, is easily compatible with the above view of processing load calculation: given a choice between two different representations for the same input string, simply choose the representation that is associated with the lower processing load.

The serial hypothesis is just one way of placing local memory restrictions on the parsing model, however. In this paper I will present an alternative formulation of local memory restrictions within a parallel framework.

There is a longstanding debate in the psycholinguistic literature as to whether or not more than one representation for an input can be maintained in parallel (see, for example, Kurtzman (1985) or Gorrell (1987) for a history of the debate). It turns out that the parallel view appears to handle some kinds of data more directly than the serial view, keeping in mind that the data are often controversial. For example, it is difficult to explain in a serial model why relative processing load increases as ambiguous input is encountered (see, for example, Fodor *et al.* 1968; Rayner *et al.* 1983; Gorrell 1987). Data that is normally taken to support for the serial hypothesis includes garden-path effects and the existence of preferred readings of ambiguous input. However, as noted above, limiting the number of allowable representations is only one way of constraining parallelism so that these effects can also be accounted for in a parallel framework.

As a result of the plausibility of a parallel model, I propose to limit the *difference in processing load* that may be present between two structures for the same input, rather than limit the *number* of structures allowed in the processing of an input (*cf.* Gibson 1987; Gibson and Clark 1987; Clark and Gibson 1988). Thus I assume that the human parser prefers one structure over another when the processing load (in PLUs) associated with maintaining the first is markedly lower than the processing load associated with maintaining the second. That is, I assume there exists some arithmetic preference quantity P corresponding to a processing load, such that if the processing loads associated with two representations for the same string differ by load P , then only the representation associated with the smaller of the two loads is pursued.¹ Given the existence of a

¹It is possible that the preference factor is a *geometric* one rather than an *arithmetic* one. Given a geometric preference factor, one structure is preferred over another when the ratio of their processing loads reaches a threshold value. I explore only the arithmetic possibility in this paper; it is possible that the geometric alternative gives results that are as good, although I leave this issue for future research.

preference factor P , it is easy to account for garden-path effects and preferred readings of ambiguous sentences. Both effects occur because of a local ambiguity which is resolved in favor of one reading. In the case of a garden-path effect, the favored reading is not compatible with the whole sentence. Given two representations for the same input string that differ in processing load by at least the factor P , only the less computationally expensive structure will be pursued. If that structure is not compatible with the rest of the sentence and the discarded structure is part of a successful parse of the sentence, a garden-path effect results. If the parse is successful, but the discarded structure is compatible with another reading for the sentence, then only a preferred reading for the sentence has been calculated. Thus if we know where one reading of a (temporarily) ambiguous sentence becomes the strongly preferred reading, we can write an inequality associated with this preference:

$$(2) \quad \sum_{i=1}^n A_i x_i - \sum_{i=1}^n B_i x_i > P$$

where:

- P is the preference factor (in PLUs),
- x_i is the number of PLUs associated with property i ,
- n is the number of properties,
- A_i is the number of times property i appears in the unpreferred structure,
- B_i is the number of times property i appears in the preferred structure.

Given a parsing algorithm together with n properties and their associated processing loads $x_1 \dots x_n$, we may write inequalities having the form of (1) and (2) corresponding to the processing load at various parse states. An algebraic technique called *linear programming* can then be used to solve this system of linear inequalities, giving an n -dimensional space for the values of x_i as a solution, any point of which satisfies all the inequalities.

In this paper I will concentrate on syntactic properties:² in particular, I present two properties based on the θ -Criterion of Government and Binding Theory (Chomsky 1981).³ It will be shown that these properties, once associated with processing loads, predict a large array of garden-path effects. Furthermore, it is demonstrated that these properties also make de-

²Note that I assume that there also exist semantic and pragmatic properties which are associated with significant processing loads, but which are not discussed here.

³In another syntactic theory, similar properties may be obtained from the principles that correspond to the θ -Criterion in that theory. For example, the completeness and coherence conditions of Lexical Functional Grammar (Bresnan 1982) would derive properties similar to those derived from the θ -Criterion. The same empirical effects should result from these two sets of properties.

sirable predictions with respect to unacceptability due to memory capacity overload.

The organization of this paper is given as follows: first, the structure of the underlying parser is described; second, the two syntactic properties are proposed; third, a number of locally ambiguous sentences, including some garden-paths, are examined with respect to these properties and a solution space for the processing loads of the two properties is calculated; fourth, it is shown that this space seems to make the right predictions with respect to processing overload; conclusions are given in the final section.

2 THE UNDERLYING PARSER

The parser to which the memory limitation constraints apply must construct representations in such a way so that incomplete input will be associated with some structure. Furthermore, the parsing algorithm must, in principle, allow more than one structure for an input string, so that the general constraints described in the previous section may apply to restrict the possibilities. The parsing model that I will assume is an extension of the model described in Clark and Gibson (1988). When a word is input, representations for each of its lexical entries are built and placed in the *buffer*, a one cell data structure that holds a set of tree structures. The parsing model contains a second data structure, the *stack-set*, which contains a set of stacks of buffer cells. The parser builds trees in parallel based on possible attachments made between the buffer and the top of each stack in the stack-set. The buffer and stack-set are formally defined in (3) and (4).

(3) A *buffer cell* is a set of structures $\{ S_1, \dots, S_n \}$, where each S_i represents the same segment of the input string. The *buffer* contains one buffer cell.

(4) The *stack-set* is a set of stacks of buffer cells, where each stack represents the same segment of the input string:

$$\left\{ \left(\begin{array}{l} \{ S_{1,1,1}, S_{1,1,2}, \dots, S_{1,1,n_{1,1}} \}, \\ \{ S_{1,2,1}, S_{1,2,2}, \dots, S_{1,2,n_{1,2}} \}, \dots \\ \{ S_{1,m_1,1}, S_{1,m_1,2}, \dots, S_{1,m_1,n_{1,m_1}} \} \end{array} \right) \right. \\ \dots \\ \left. \left(\begin{array}{l} \{ S_{p,1,1}, S_{p,1,2}, \dots, S_{p,1,n_{p,1}} \}, \\ \{ S_{p,2,1}, S_{p,2,2}, \dots, S_{p,2,n_{p,2}} \}, \dots \\ \{ S_{p,m_p,1}, S_{p,m_p,2}, \dots, S_{p,m_p,n_{p,m_p}} \} \end{array} \right) \right\}$$

where:

- p is the number of stacks;
- m_i is the number of buffer cells in stack i ;
- and $n_{i,j}$ is the number of tree structures in the j th buffer cell of stack i .

The motivation for these data structures is given by the desire for a completely unconstrained parsing algorithm upon which constraints may be placed: this algorithm should allow all possible parser operations to occur at each parse state. There are exactly two parser operations: attaching a node to another node and

pushing a buffer cell onto a stack. In order to allow both of these operations to be performed in parallel, it is necessary to have the given data structures: the buffer and the stack-set. For example, consider a parser state in which the buffer is non-empty and the stack-set contains only a single cell stack:

(5)
 Stack-set: $\{ \{ \{ S_1, \dots, S_n \} \} \}$
 Buffer: $\{ B_1, \dots, B_m \}$

Suppose that attachments are possible between the buffer and the single stack cell. The structures that result from these attachments will take up a single stack cell. Let us call these resultant structures A_1, A_2, \dots, A_k . If all possible operations are to take place at this parser state, then the contents of the current buffer must also be pushed on top of the current stack. Thus two stacks, both representing the same segment of the input string will result:

(6)
 Stack 1: $\{ \{ \{ A_1, \dots, A_k \} \} \}$
 Stack 2: $\{ \{ \{ B_1, \dots, B_m \} \{ S_1, \dots, S_n \} \} \}$

Since these two stacks break up the same segment of the input string in different ways, the stack-set data structure is necessary.

3 TWO SYNTACTIC PROPERTIES DERIVABLE FROM THE θ -CRITERION

Following early work in linguistic theory, I distinguish two kinds of categories: *functional* categories and *thematic* or *content* categories (see, for example, Fukui and Speas (1986) and Abney (1987) and the references cited in each). Thematic categories include nouns, verbs, adjectives and prepositions; functional categories include determiners, complementizers, and inflection markers. There are a number of properties that distinguish functional elements from thematic elements, the most crucial being that functional elements mark grammatical or relational features while thematic elements pick out a class of objects or events. I will assume as a working hypothesis that only those syntactic properties that have to do with the thematic elements of an utterance are relevant to preferences and overload in processing. One principle of syntax that is directly involved with the thematic content of an utterance in a Government-Binding theory is the θ -Criterion:

(7) Each argument bears one and only one θ -role (thematic role) and each θ -role is assigned to one and only one argument (Chomsky 1981:36).

I hypothesize that the human parser attempts to locally satisfy the θ -Criterion whenever possible. Thus given a thematic role, the parser prefers to assign that role, and given a thematic element, the parser prefers to assign a role to that element. These assumptions are made explicit as the following properties:

(8) The Property of Thematic Reception (PTR): Associate a load of x_{TR} PLUs of short term memory to each thematic element that is in a position that can receive a thematic role in some co-existing structure, but whose θ -assigner is not unambiguously identifiable in the structure in question.

(9) The Property of Thematic Assignment (PTA): Associate a load of x_{TA} PLUs of short term memory to each thematic role that is not assigned to a node containing a thematic element.

Note that the Properties of Thematic Assignment and Reception are stated in terms of *thematic* elements. Thus the Property of Thematic Reception doesn't apply to functional categories, whether or not they are in positions that receive thematic roles. Similarly, if a thematic role is assigned to a functional category, the Property of Thematic Assignment does not notice until there is a thematic element inside this constituent.

4 AMBIGUITY AND THE PROPERTIES OF THEMATIC ASSIGNMENT AND RECEPTION

Consider sentence (10) with respect to the Properties of Thematic Assignment and Reception:

(10) John expected Mary to like Fred.

The verb *expect* is ambiguous: either it takes an NP complement as in the sentence *John expected Mary* or it takes an IP complement as in (10).⁴ Consider the state of the parse of (10) after the word *Mary* has been processed:

(11) a. $[_{IP} [_{NP} \text{John}] [_{VP} \text{expected} [_{NP} \text{Mary}]]]$
 b. $[_{IP} [_{NP} \text{John}] [_{VP} \text{expected} [_{IP} [_{NP} \text{Mary}]]]]]$

In (11a), the NP *Mary* is attached as the NP complement of *expected*. In this representation there is no load associated with either of the Properties of Thematic Assignment or Reception since no thematic elements need thematic roles and no thematic roles are left unassigned. In (11b), the NP *Mary* is the specifier of a hypothesized IP node which is attached as the complement of the other reading of *expected*.⁵ This representation is associated with at least x_{TR} PLUs since the NP *Mary* is in a position that can be associated with a thematic role, the subject position, but whose θ -assigner is not yet identifiable. No load is associated with the Property of Thematic Assignment, however, since both thematic roles of the verb *expected* are assigned to nodes that contain thematic elements. Since

⁴Following current notation in GB Theory, IP (Inflection Phrase) = S and CP (Complementizer Phrase) = S' (Chomsky 1986).

⁵I assume some form of hypothesis-driven node projection so that noun phrases are projected to those categories that they may specify. Motivation for this kind of projection algorithm is given by the processing of Dutch (Frazier 1987) and the processing of certain English noun phrase constructions (Gibson 1989).

there is no difficulty in processing sentence (10), the load difference between these two structures cannot be greater than P PLUs, the preference factor in inequality (2). Thus the inequality in (12) is obtained:

$$(12) x_{TR} \leq P$$

Since the load difference between the two structures is not sufficient to cause a strong preference, both structures are maintained. Note that this is an important difference between the theories presented here and the theory presented in Frazier and Fodor (1978), Frazier (1979) and Pritchett (1988). In each of these theories, only one representation can be maintained, so that either (11a) or (11b) would be preferred. In order to account for the lack of difficulty in parsing (10), Frazier and Pritchett both assume that reanalysis in certain situations is not expensive. No such stipulation is necessary in the framework given here: it is simply assumed that *all* reanalysis is expensive.⁶

Consider now sentence (13) with respect to the Properties of Thematic Assignment and Reception:

(13) John expected her mother to like Fred.

Consider the state of the parse of (13) after the word *her* has been processed. In one representation the NP *her* will be attached as the NP complement of *expected*:

$$(14) [IP [NP John] [VP expected [NP her]]]$$

In this representation there is no load associated with either of the Properties of Thematic Assignment or Reception since no thematic objects need thematic roles and no thematic roles are left unassigned. In another representation the NP *her* is the specifier of a hypothesized NP which is pushed onto a substack containing the other reading of the verb *expected*:

$$(15) \left\{ \begin{array}{l} [IP [NP John] [VP expected [IP e]]] \\ [NP [NP her]] \end{array} \right\}$$

This representation is associated with at least x_{TA} PLUs since the verb *expected* has a thematic role to assign. However, no load is associated with the genitive NP specifier *her* since its θ -assigner, although not yet present, is unambiguously identified as the head of the NP to follow (Chomsky (1986a)).⁷ Thus the total load associated with (15) is x_{TA} PLUs. Since there is no difficulty in processing sentence (10), the load difference

⁶See Section 4.1 for a brief comparison between the model proposed here and serial models such as those proposed by Frazier and Fodor (1978) and Pritchett (1988).

⁷Note that specifiers do not always receive their thematic roles from the categories which they specify. For example, a non-genitive noun phrase may specify any major category. In particular, it may specify an IP or a CP. But the specifier of these categories may receive its thematic role through chain formation from a distant θ -assigner, as in (16):

(16) John appears to like beans.

Note that there is no NP that corresponds to (16) (Chomsky (1970)):

(17) * John's appearance to like beans.

between these two structures cannot be greater than P PLUs. Thus the second inequality, (18), is obtained:

$$(18) x_{TA} \leq P$$

Now consider (19):⁸

(19) # I put the candy on the table in my mouth.

This sentence becomes ambiguous when the preposition *on* is read. This preposition may attach as an argument of the verb *put* or as a modifier of the NP *the candy*:

$$(20) \text{ a. } I [VP [V' [V put] [NP the candy] [PP on]]] \\ \text{ b. } I [VP [V' [V put] [NP the candy] [PP on]]]$$

At this point the argument attachment is strongly preferred. However, this attachment turns out to be incompatible with the rest of the sentence. When the word *mouth* is encountered, no pragmatically coherent structure can be built, since tables are not normally found in mouths. Thus a garden-path effect results. Consider the parse state depicted in (20) with respect to the Properties of Thematic Assignment and Reception. The load associated with the structure resulting from argument attachment is x_{TA} PLUs since, although the θ -grid belonging to the verb *put* is filled, the thematic role assigned by the preposition *on* remains unassigned. On the other hand, the load associated with the modifier attachment is $2 * x_{TA} + x_{TR}$ PLUs since 1) both the verb *put* and the preposition *on* have thematic roles that need to be assigned and 2) the PP headed by *on* receives a thematic role in the argument attachment structure, while it receives no such role in the structure under consideration. Thus the difference between the loads associated with the two structures is $x_{TA} + x_{TR}$ PLUs. Since the argument attachment structure is strongly preferred over the other structure, I hypothesize that this load is greater than P PLUs:

$$(21) x_{TA} + x_{TR} > P$$

Now consider the the well-known garden-path sentence in (22):

(22) # The horse raced past the barn fell.

The structure for the input *the horse raced* is ambiguous between at least the two structures in (23):

$$(23) \text{ a. } [IP [NP the horse] [VP raced]] \\ \text{ b. } [IP [NP the [N' [N' horse]] [CP O_i raced]]]$$

Structure (23a) has no load associated with it due to either the PTA or the PTR. Crucially note that the verb *raced* has an intransitive reading so that no load is required via the Property of Thematic Assignment. On the other hand, structure (23b) requires a load of $2 * x_{TR}$ PLUs since 1) the noun phrase *the horse* is in a position that can receive a thematic role, but currently does not and 2) the operator O_i is in a position that may be associated with a thematic role, but is not yet

⁸I will prefix sentences that are difficult to parse because of memory limitations with the symbol "#". Hence sentences that are unacceptable due to processing overload will be prefixed with "#", as will be garden-path sentences.

associated with one.⁹ Thus the difference between the processing loads of structures (23a) and (23b) is $2 * x_{TR}$ PLUs. Since this sentence is a strong garden-path sentence, it is hypothesized that a load difference of $2 * x_{TR}$ PLUs is greater than the allowable limit, P PLUs:

$$(24) 2 * x_{TR} > P$$

A surprising effect occurs when a verb which *optionally* subcategorizes for a direct object, like *race*, is replaced by a verb which *obligatorily* subcategorizes for a direct object, like *find*:

(25) The bird found in the room was dead.

Although the structures and local ambiguities in (25) and (22) are similar, (22) causes a garden-path effect while, surprisingly, (25) does not. To determine why (25) is not a garden-path sentence we need to examine the local ambiguity when the word *found* is read:

- (26) a. [_{IP} [_{NP} the bird] [_{VP} [_{V'} [_V found] [_{NP}]]]]
 b. [_{IP} [_{NP} the [_{N'} [_{N'} bird_i]] [_{CP} *O_i* found]]]

The crucial difference between the verb *found* and the verb *raced* is that *found* requires a direct object, while *raced* does not. Since the θ -grid of the verb *found* is not filled in structure (26a), this representation is associated with x_{TA} PLUs of memory load. Like structure (23b), structure (26b) requires $2 * x_{TR}$ PLUs. Thus the difference between the processing loads of structures (26a) and (26b) is $2 * x_{TR} - x_{TA}$ PLUs. Since no garden-path effect results in (25), I hypothesize that this load is less than or equal to P PLUs:

$$(27) 2 * x_{TR} - x_{TA} \leq P$$

Furthermore, these results correctly predict that sentence (28) is not a garden-path sentence either:

(28) The bird found in the room enough debris to build a nest.

Hence we have the following system of inequalities:

- (29) a. $x_{TR} \leq P$
 b. $x_{TA} \leq P$
 c. $x_{TA} + x_{TR} > P$
 d. $2 * x_{TR} > P$
 e. $2 * x_{TR} - x_{TA} \leq P$

This system of inequalities is consistent. Thus it identifies a particular solution space. This solution space is depicted by the shaded region in Figure 1.

Note that, pretheoretically, there is no reason for this system of inequalities to be consistent. It could have been that the parser state of one of the example sentences forced an inequality that contradicted some previously obtained inequality. This situation would have had one of three implications: the properties being considered might be incorrect; the properties being considered might be incomplete; or the whole approach

⁹In fact, this operator will be associated with a thematic role as soon as a gap-positioning algorithm links it with the object of the passive participle *raced*. However, when the attachment is initially made, no such link yet exists: the operator will initially be unassociated with a thematic role.

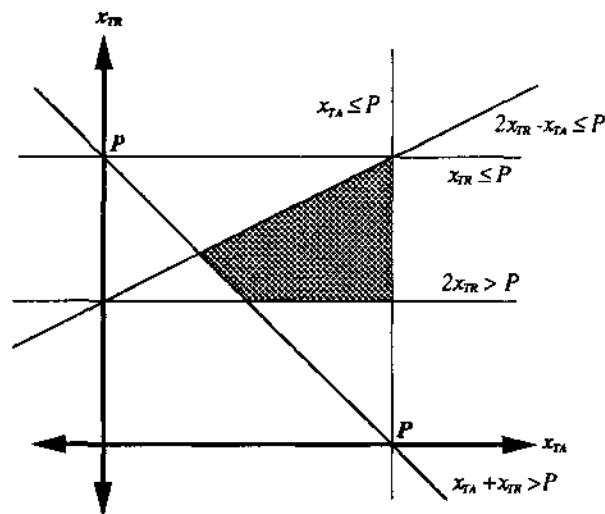


Figure 1: The Solution Space for the Inequalities in (29)

might be incorrect. Since this situation has not yet been observed, the results mutually support one another.

4.1 A COMPARISON WITH SERIAL MODELS

Because serial models of parsing can maintain at most one representation for any input string, they have difficulty explaining the lack of garden-path effects in sentences like (10) and (25):

(10) John expected Mary to like Fred.

(25) The bird found in the room was dead.

As a result of this difficulty Pritchett (1988) proposes the Theta Reanalysis Constraint:¹⁰

(30) Theta Reanalysis Constraint (TRC): Syntactic reanalysis which interprets a θ -marked constituent as outside its current θ -Domain and as within an existing θ -Domain of which it is not a member is costly.

(31) θ -Domain: α is in the γ θ -Domain of β iff α receives the γ θ -role from β or α is dominated by a constituent that receives the γ θ -role from β .

As a result of the Theta Reanalysis Constraint, the necessary reanalysis in each of (10) and (25) is not expensive, so that no garden-path effect is predicted. Furthermore, the reanalysis in sentences like (22) and (19) violates the TRC, so that the garden-path effects are predicted.

However, there are a number of empirical problems with Pritchett's theory. First of all, it turns out that the

¹⁰Frazier and Rayner (1982) make a similar stipulation to account for problems with the theory of Frazier and Fodor (1978). However, their account fails to explain the lack of garden-path effect in (25). See Pritchett (1988) for a description of further problems with their analysis.

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