# **Supplementary Material**

# Variables Summary

Variable	Domain	Description
$\overline{n}$	$\mathbb{N}_+$	sentence length
r	$\mathbb{N}_+$	number of semantic roles
m	$\mathbb{N}_+$	number of senses
T	$\mathbb{N}_+$	number of refinement iterations
j	$\mathbb{N}_+$	position of the given predicate
R	$\Delta_{r-1}^n$	semantic roles probability
Р	$\Delta_{m-1}$	senses probability
П	$\mathbb{R}^{m  imes d_{\pi}}$	predicate senses embedding
$x^{\mathrm{w}}$	$\mathbb{R}^{n  imes d_w}$	sentence tokens embeddings
$x^{\mathrm{dep}}$	$\mathbb{R}^{n  imes d_{\delta}}$	dependency labels embeddings
$x^{\mathrm{pos}}$	$\mathbb{R}^{n  imes d_p}$	part-of-speech tags embeddings
x	$\mathbb{R}^{n \times (d_w + d_\pi + d_p)}$	concatenated representation
Baseline Model		
h	$\mathbb{R}^{n  imes d_h}$	encoded sentence representation
$\mathrm{h}^{ ho_0}$	$\mathbb{R}^{n  imes d_{ ho_0}}$	argument feature for null role logits
$\mathrm{h}^{ ho_1}$	$\mathbb{R}^{n \times d_{\rho_1}}$	argument feature for other roles logits
$\mathrm{h}^{arrho_0}$	$\mathbb{R}^{d_{ ho_0}}$	predicate feature for null role logits
$\mathrm{h}^{\varrho_1}$	$\mathbb{R}^{d_{ ho_1}}$	predicate feature for other roles logits
$\mathrm{I}^{ ho_0}$	$\mathbb{R}^{n}$	null role logits
$\mathrm{I}^{ ho_1}$	$\mathbb{R}^{n \times (r-1)}$	other roles logits
$\mathrm{I}^{lpha}$	$\mathbb{R}^{n  imes r}$	roles logits
$\mathrm{h}^{\pi}$	$\mathbb{R}^{d_{\pi}}$	predicate feature for sense disambiguation
$\mathrm{I}^{\pi}$	$\mathbb{R}^m$	sense logits
Refinement Network		
g	$\mathbb{R}^{n  imes d_g}$	encoded sentence representation
$\mathrm{g}^{lpha}$	$\mathbb{R}^{n  imes d_{lpha}}$	argument feature
$\mathrm{g}^{\pi}$	$\mathbb{R}^{d_{\pi}}$	predicate feature
$\mathrm{o}_i$	$\mathbb{R}^{r-1}$	sum of other roles
$\mathrm{z}_i^lpha$	$\mathbb{R}^{2r-1+2d_g+d_\pi}$	input to role refinement network
$ {M}^{lpha}$	$\mathbb{R}^{n  imes r}$	refinement role logits to be added with $I^{\alpha}$
$\mathrm{r}_{\pi}$	$\mathbb{R}^{r-1}$	sum of all roles
$\mathbf{z}^{\pi}$	$\mathbb{R}^{2r-1+2d_g+d_\pi}$	input to sense refinement network
$M^{\pi}$	$\mathbb{R}^{m}$	refinement sense logits to be added with $I^{\pi}$

Table 1: Variables domain and description

#### Networks

Network	Description
BiLSTM	3 layers stacked highway BiLSTM
MLP	1 layer MLP with exponential linear units

Table 2: Networks for all languages at all occurrence in the main text. Note that the input and output dimensions of MLP and BiLSTM can be decided by the other hyper-parameters at each occurrence.

### **Hyper-Parameters**

Hyper-parameter	Value	2	Description
	English	Others	
p	0.3		dropout rate for all neural modules
$p_r$	0.3		recurrent dropout rate for BiLSTMs
$d_w$	1024	300	tokens embedding dimension
$d_{\delta}$	64		dependency label embedding dimension
$d_p$	64		part-of-speech tags embedding dimension
$d_h$	500	428	BiLSTM hidden state dimension in one direction
$d_{ ho_0}$	300		dimension for feature for null role logits
$d_{ ho_1}$	128		dimension for feature for other role logits
$d_g$	200		dimension for feature for refinement networks
$d_r$	200		hidden dimension of refinement networks
$\lambda_g^\pi$	50		multiplier of Gumbel noise for sense logits
$\lambda_g^{lpha}$	5		multiplier of Gumbel noise for role logits

Table 3: Hyper-parameters value and description. Note that the input and output dimensions of MLP and BiLSTM can be decided by the other hyper-parameters at each occurrence.

## References

- Djork-Arné Clevert, Thomas Unterthiner, and Sepp Hochreiter. 2016. Fast and accurate deep network learning by exponential linear units (elus). In 4th International Conference on Learning Representations, ICLR 2016, San Juan, Puerto Rico, May 2-4, 2016, Conference Track Proceedings.
- Yarin Gal and Zoubin Ghahramani. 2016. A theoretically grounded application of dropout in recurrent neural networks. In Proceedings of the 30th International Conference on Neural Information Processing Systems, NIPS'16, pages 1027–1035, USA. Curran Associates Inc.
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