A Feature Induction Algorithm with Application to Named Entity Disambiguation

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Abstract

The performance of NLP classifiers largely depends on the quality of the features considered for prediction (feature engineering). However, as the number of features increases, the more likely overfitting becomes and performance decreases. Also, due to the very large number of features, only slimple linear classifiers are considered, thus disregarding potentially predictive non-linear combinations of features. Here we propose an automated method for feature induction, which selects and includes in the model features and feature combinations which are likely to be useful for the prediction. The resulting model relies on a smaller feature set, is non-linear and is more accurate than the baseline, which is the model trained on the entire feature set. The method uses a greedy filtering approach based on various univariate measures of feature relevance and it is very fast in practice. Also, our feature induction method is independent of the classifier used: we applied it together with Naïve Bayes and Perceptron models.

1 Introduction

NLP classification tasks are characterized by a very large number of features. When the number of available samples is smaller (for example several orders of magnitude less samples), overfitting can occur, leading to poor performance. In order to avoid overfitting, *feature selection* is commonly applied. In (Guyon and Elisseeff, 2003), the main approaches to feature selection are summarized: *filter*, *wrapper* and *embedded* methods. Filters use some scoring measure to quantify the predictivity of each feature independently. Then,

features are ranked and only the top scoring ones are kept in the final model. The most popular measures for feature predictivity are Mutual Information (Lewis, 1992; Taira and Haruno, 1999), Information Gain (Uguz, 2011; Yang and Pedersen, 1997), Kullback-Leibler divergence (Lee and Lee, 2006; Schneider, 2004; Lee et al., 2011), Chi-squared statistics (Yang and Pedersen, 1997; Mesleh, 2007), Fisher statistics, Pearson correlation, etc. In (Yang and Pedersen, 1997) and (Forman, 2003), comparisons of the most popular methods are presented. Filter methods are computationally fast, but the univariate scoring can lead to the elimination of features that are useful only in combinations (Guyon and Elisseeff, 2003). Wrapper methods (Kohavi and John, 1997) can score subsets of features directly, by evaluating the performance of the classifier on the respective subset. A strategy of iteratively updating the subset of features is used, with the goal of finding a (close to) optimal subset. Forward selection, backward elimination, branch-and-bound (Narendra and Fukunaga, 1977), simulated annealing (Ekbal et al., 2011), genetic algorithms (Yang and Honavar, 1998) are among the most popular strategies. Wrapper methods tend to be slow in practice, because a classifier needs to be trained at each iteration. Embedded methods are explicitly optimizing an objective function that incorporates feature selection. In general, the objective is an expression of the trade-off between the goodness of fit and the number of variables that participate in the model. For example, l_1 penalties (Haffner et al., 2005) are combined with the likelihood objective in maximum entropy models in order to keep the number of predictors small.

For most NLP classification tasks, the number of features is very large. If no experts are available for selecting the most promising features for a specific task, the choice is really vast. In (Kamolvilassatian, 2002), the authors systemati-



Figure 1: Classifier models used for a) document classification and b) named entity recognition. Linear models are represented with gray bars and non-linear models with black.

cally list of all features (with parameters), such as for example n-grams (n is a parameter), context of words, part of speech, lemmas, stems, etc. Owing to the very large number of features, linear (or log-linear) classifiers are preferred, because they are robust and can be trained fast. Simple search in Google Scholar shows that most frequently used models for document classification are Naive Bayes, linear SVMs (Cortes and Vapnik, 1995), Perceptrons (Rosenblatt, 1957) and Maximum Entropy (Berger et al., 1996) (Figure 1a). In contrast, non-linear models such as non-linear SVMs and Random Forest (Breiman, 2001) and Classification trees (Breiman et al., 1984) are significantly under-represented. For Named Entity Recognition, Maximum Entropy and CRFs (Lafferty, 2001) are mostly used, but other linear models like Perceptron, Naive Bayes and linear SVMs are employed (Figure 1b). Non-linear models are significantly less frequent. Feature induction can be used to efficiently introduce non-linearity in large models, in the form of feature conjunctions. As the space of all conjunctions of arbitrary length is very large (2^{#features}), a greedy search approach is applied for selecting the most promising conjunctions with reasonable computational cost. In (McCallum, 2003), a method for inducing features and conjunctions especially tailored to CRF models is proposed. Iteratively, the most promising feature or conjunction to be added to the model is identified. To this end, a gain function is defined, for evaluating the improvement of the likelihood target upon the addition of the feature. Conjunctions are considered only among the top scoring feature candidates and the features already included in the model. In (Vens and Costa, 2011), the authors use random forests to form feature conjunctions, by traversing the trees from the root to the leaves.

In this article we present a method for feature selection and feature induction. The strengths of our method are fast running time and generality, in the sense that it can be used as preprocessing step to any classifier the user may choose.

2 Methods

Given are N pairs of observations and labels $(X_1, Y_1), (X_2, Y_2), ..., (X_N, Y_N)$. The observations X_i are over a set of p binary predicates (or terms) $T_1, ..., T_p$, which we call *atomic features*. For example, an atomic feature is an indicator of presence or absence of a particular word in a document. The class label can take the values from the set $\{c_1, c_2, ..., c_K\}$. In this article. we use the notion of 'features' to denote predicates, and not the classical feature functions $f(X_i, c_i)$ commonly used in NLP tasks. The reason is that we wish to be consistent with the established notions of 'feature selection' and 'feature induction', which otherwise would have to be called 'predicate selection' and 'predicate induction'.

The purpose of our method is to find a set of features consisting of atomic features or conjunctions of atomic features which can predict the class variable with high accuracy. The classification model is the user's choice.

Our algorithm is entitled Fast ITerative Selection and Induction (FITSI) and is a greedy heuristic search through the space of the atomic features and conjunctions. The main steps are described in Algorithm 1. A feature selection step and a feature induction step alternate in an iterative process. At each iteration, we rank the features according to some score σ that measures the univariate relevance of each feature w.r.t. the class variable. The choices for σ are described in Section 2.1. We keep only the top k features, where k is a generic parameter which can be either a percentage of the total number of features, or the number of features with scores larger than a threshold. Then, we add to the features set conjunctions between atomic features larger than a certain rank l and features or conjunctions from the entire list. The algorithm runs for *m* iterations, allowing for conjunctions of length up to m to be generated. Below we discuss in detail the two key ingredients of our algorithm: measures of feature relevance and the algorithm for generation of conjunctions.

2.1 Feature ranking and filtering

For ranking and filtering features (σ parameter in Algorithm 1), we implemented several measures: mutual information (MI), information gain (IG), symmetrical uncertainty (SU) and Fisher tests (FT). Each measure returns a score, which is an estimate of the predictive power of each feature w.r.t. the class variable. In a multi-class setting, there are several ways to compute scores: either globally, trying to capture the overall association of the feature with the class variable, or separately, computing a relevance score w.r.t. each class and then summing the scores. We prefer the later approach because it is equally fair to small and large classes. We summarize the class-specific scores by taking either the sum or their maximum value.

In what follows, we denote with Y_i the indicator

Algorithm 1 Fast Iterative Selection and Induction					
Require: $\{T_1,, T_p\}, \sigma, k, l, m$					
1:	Initialize feature list $\Phi \leftarrow [T_1,, T_p]$				
2:	2: for $i \in \{1,, m-1\}$ do				
3:	Feature selection:				
4:	$\Phi \leftarrow \operatorname{sort}(\Phi, \sigma) \triangleright \operatorname{Sort}$ the list according to σ scores				
5:	$\Phi \leftarrow \Phi[1k] $ \triangleright Keep only the top k features				
6:	Feature induction:				
7:	$\Gamma \leftarrow \text{generateConjunctions}(\Phi, l)$				
8:	if $\Phi == \Phi \bigcup \Gamma$ then \triangleright No new conjunctions				
9:	break				
10:	else				
11:	$\Phi \leftarrow \Phi \bigcup \Gamma \qquad \qquad \triangleright \operatorname{Append} \Gamma \text{ to } \Phi$				
12:	end if				
13:	end for				
14:	return Φ				

Algorithm 2 generateConjunctions(Φ , l)					
1: $\Gamma \leftarrow \emptyset$	▷ Initialize with empty list				

2:	for $i \in \{1,, l\}$ do	1.5
3:	if $\Phi[i]$ is atomic then	
4:	for $j \in \{i+1,, \text{length}\}$	$\Phi)\}$ do
5:	$\Gamma \leftarrow \Gamma \bigcup \{\Phi[i]\&\Phi[j]\}$	Add conjunction
6:	end for	
7:	end if	
8:	end for	
9:	return Γ	

variable of class c_i : $Y_i[k] = 1$, if $Y[k] = c_i$ and 0, otherwise.

Mutual information

Mutual information (Hamming, 1986) between a feature T and an indicator variable Y_i of class c_i is a quantity $MI(T, Y_i)$ that measures the dependence between the two variables. It is calculated as:

$$MI(T, Y_i) = \sum_{t \in \{0, 1\}} \sum_{y \in \{0, 1\}} Pr(t, y) \log \left(\frac{Pr(t, y)}{Pr(t) Pr(y)} \right)$$

where the joint probability Pr(t, y) and the marginals Pr(t) and Pr(y) are estimated using relative frequencies. $MI(T, Y_i)$ is a positive quantity, with a value of zero if T and Y_i are independent. A large $MI(T, Y_i)$ score indicates that T is predictive for class c_i .

Information gain

The information gain of feature T with respect to Y_i measures the decrease in entropy when the feature T is present versus absent from the set of features. We evaluate the information gain of feature T with respect to class c_i as in (Yang and Pedersen, 1997):

$$\begin{aligned} \text{IG}(T, Y_i) &= -\Pr(Y_i = 1) \log(\Pr(Y_i = 1)) \\ &+ \Pr(T) \Pr(Y_i = 1 | T) \log(\Pr(Y_i = 1 | T)) \\ &+ \Pr(\bar{T}) \Pr(Y_i = 1 | \bar{T}) \log(\Pr(Y_i = 1 | \bar{T})) \end{aligned}$$

Symmetric uncertainty

Symmetric uncertainty between term T and class indicator variable Y_i is a normalized mutual information score, computed as follows:

$$SU(T, Y_i) = \frac{2MI(T, Y_i)}{H(T) + H(Y_i)}$$

where by H(X) we denote the entropy of variable X, computed in practice as $H(X) = \sum_{x \in X} -\Pr(x)\log(\Pr(x))$.

Fisher test

Fisher's exact test (Fisher, 1928) is used to examine the significance of association between two binary variables. We apply it to the contingency table between feature T and class indicator Y_i and retrieve the significance p-value, which expresses the probability of the observed values of the table under the assumption of independence between the variables. If the probability is very small (i.e. p-value is small), then the independence assumption is rejected. We define the Fisher test score for feature selection as: $FT(T, Y_i) = 1 - p$ -value. $FT(T, Y_i)$ always has values between 0 and 1. A typical threshold for significance is p-value < 0.05 or, more conservatively, p-value < 0.01.

2.2 Induction (generating conjunctions)

We include in the model feature conjunctions of maximum length m, which is a parameter of our method. At each iteration, the conjunctions are formed between atomic features that exceed some relevance threshold and any other feature or conjunction still present in the list of features.

Before adding a conjunction $T_i\&T_j$ to the the set Φ , we check if it has not been introduced already, for example as $T_j\&T_i$. If at a certain step all conjunctions that are generated are already in Φ , the algorithm stops (see step 8, Algorithm 1).

In typical applications, it is unlikely that very long conjunctions have a great impact on the classification performance. Therefore we suggest that m is kept small in practice, a value up to 3 should be sufficient for most applications.

2.3 Complexity of the algorithm

As we already argued in the introduction, computational complexity is one important bottleneck of feature selection and induction algorithms. Despite this, our method is fast. We run once through all samples in order to build the necessary data structures for evaluation of MI, IG, SU and FT scores, which takes $\mathcal{O}(pKN)$ time. The data structures esentially store the counts of samples in each class, for each feature. Thereafter, the complexity of scoring the set of p features and the sorting take place in $\mathcal{O}(pK)$ time, which is run mtimes. The overall time is thus $\mathcal{O}(pKm + pKN)$, which is $\mathcal{O}(pKN)$, in most applications. In practice the algorithm can become even faster by using sparse vectors to represent features.

2.4 Model training and evaluation

We use the FITSI Algorithm for generating a set Φ of atomic features and conjunctions of length up to m = 2. We use these features to represent the data and train a model \mathcal{M} , which in our experiments can be a Perceptron or a Naive Bayes model. The performance of the algorithm clearly depends on the parameters used for the feature induction and selection: σ , k and l.

If we exclude the scoring measure σ , which can be chosen by the user based on some subjective criteria, our algorithm has two numerical hyper parameters that can be estimated from data, in a way that the resulting model has optimal performance. We use B-fold cross-validation for this purpose. We first split the data into two subsets, for parameter selection and for testing. The part that is used for parameter selection is split into B bins (5 in our experiments). For each combination of parameters, we use B - 1 bins for feature induction and model training and we evaluate the performance of the classifier on the remaining bin. In consequence, for each combination of parameters, a set of B performance estimates are obtained, which allows to compute mean and standard deviation. We identify the model with largest mean performance and select the simplest model (smallest k) that has the mean within one standard deviation from the best model. This is known as the one-standard-error rule, proposed by (Breiman et al., 1984). The parameters of this model are the optimal parameters k_{opt} and l_{opt} . We test this model on the excluded samples and report a test performance.

We compare the performance of our model to that of a baseline model. To this end, we repeat the cross validation described above, but we do not perform any feature induction.

For evaluating the performance of a classifier, we use the F_1 measure, which is the harmonic mean of precision and recall.

3 Data

PA data: The "PA" dataset was developed by the Press Association¹ to enable the implementation of a system for recognition and semantic disambiguation of named entities in press releases. Given certain metadata for a number of overlapping candidate entities, an array of features derived from the textual context of their oc-

¹http://www.pressassociation.com/

currence, and additional document-level metadata, the model recognizes which (if any) of the candidate entities is the one referenced in the text.

The corpus is annotated with respect to people, organization and location mentions; a special "negative" label denotes the candidates that can be considered irrelevant in the given context. In all cases, at most one of the overlapping candidates is annotated as positive. The dataset comprises a total of 2539 manually curated documents, and a total of 85602 concept mentions (this number represents the total of all candidate instances, including those annotated as non-entities).

For this dataset, the domain of the press releases is an important factor during classification, and specific features that express the belonging of a press release to a particular domain or category are also available. The dataset comprises articles from two domains: "General News" and "Olympics".

We remove non-location entity candidates, thus reducing the problem to the binary classification task of discerning locations from non-entities. We split the corpus into a training set (2369 documents) and a held-out test set (160 documents). As a result of this preprocessing, we have 2 classes (Location and Negative), 46273 instances, and a target to irrelevant instance counts ratio of 0.17.

From the training document set, we extracted 50455 atomic features.

As performance measure we report the F1 score of the positive class (i.e. 'Location').

4 Results

We performed feature induction using in turn all the measures of feature relevance mentioned in Section 2.1, followed by training Naive Bayes and Perceptron classifiers. The parameters k and l(l > k) of the feature induction step were iteratively selected from the set:

$$\{0.1\%, 0.25\%, 0.5\%, 0.75\%, 1\%, 2.5\%, 5\%, 7.5\%, 10\%, 25\%$$

of the total number of features p.

We used 5-fold cross-validation for selection of the optimal parameters k_{opt} and l_{opt} , as explained in section 2.4. Figure 2 illustrates the cross-validation search grid for the particular combination of feature induction with MI score and a Perceptron classifier. The intensity of the shade of gray is proportional to the average F1 measure over the 5 folds. The standard deviation for each combination of parameters is not shown in



Figure 2: Parameter grid search by cross-validation.

	NB	Perc
MI	0.70	0.83
IG	0.70	0.83
SU	0.70	0.80
FT	0.75	0.83
Baseline	0.54	0.79

 Table 1: Performance on the test dataset of classification models using various measures of feature relevance and comparison with the baseline.

the image. The largest average F1 is 0.825 and is achieved for k = 25% and l = 0.75% of p.The standard deviation of this model is 0.009, estimated based on the 5 cross-validation folds. A simpler model, with k = 25% and l = 0.1%has average performance of 0.824, which is within one standard deviation from the maximum performance, hence there is no statistically significant difference between the two models. We thus chose the simpler model as optimal.

In Table 1, we show the performance of the optimal models (determined by cross validation). The models that we investigated are various combinations of feature scoring measures (as rows) and classifiers (as columns). We compare to a Baseline model (last row), which is either a Naive Bayes or Perceptron, without any feature induction. Clearly, all our models outperform the Baseline, by a large margin: up to 20% in the case of Naive Bayes models and up to 4% for Perceptrons. In general, Naive Bayes classifiers are worse than the Perceptron. Fisher test ranking appears to work best for Naive Bayes classifiers, whereas for Perceptron models achieve similar performance for most of the scoring measures (apart from Symmetrical Uncertainty).

Table 2 shows for each model the optimal parameters k_{opt} and l_{opt} that were selected via cross

	NB (k_{opt}, l_{opt})	Perc (k_{opt}, l_{opt})
MI	25%, 0.25%	1000000000000000000000000000000000000
	/	,
IG	25%, 0.25%	25%, 0.1%
SU	25%, 0.1%	10%, 0.1%
FT	25%, 0.1%	10%, 0.25%

Table 2: Parameters of the resulting models.

validation. In general many atomic features are included in the model, indicated by the large values of k_opt , which are in general 25%. Only two models select 10% features, namely the Perceptron with FT and SU. The most common values for l_{opt} are 0.25% and 0.1%, which means that the useful conjunctions are those that comprise at least one high scoring atomic feature (from top 0.01% or 0.25%). In contrast, a larger l_{opt} would mean that the model benefits from conjunctions between two low scoring atomic features, which is not the case, according to our results.

5 Analysis of conjunctions

The purpose of feature induction is to generate useful combinations of features without the help of an expert in the domain of the application. Below we comment on interesting (types) of conjunctions that rank high ccording to the Perceptron model using the MI criterion for feature ranking, which showed highest performance.

http://www.geonames.org/ontology#P.PPLC
 & ANNIES=location`city

The Geonames ontology² indicates that the candidate is a capital and Gate's ANNIE³ suggests that the instance is a city. Therefore, the conjunction reinforces the recommendation for a location. The conjunction is very informative.

- PrevWord = "in" & MOST PROBABLE=true

If the word preceding the candidate is 'in' and Location is most probable label of the entity, then there is a strong indication that the entity is indeed a Location.

- PrevWord = "in" & NoCandidates=1

The conjunction between previous word being 'in' and the absence of other candidates at the specific location is a strong indicator for Location. This is a linguistic pattern that most experts would add to the model. Our algorithm automatically generates this pattern. ANNIES=location country & pacategory:Olympics

A very interesting domain-specific conjunction is formed by the indication of ANNIE to a country and the category of the document being Olympics. Even though ANNIE points to a country, the fact that the document belongs to the Olympics category makes the Location less likely, because the candidate is most probably referring to a team. Such conjunctions are specific to domain adaptation tasks and our algorithm generates it automatically, without defining a domain adaptation problem explicitly. Only adding atomic domain features allows for generating of domain specific-conjunctions.

- multiple conjunctions including the domain name

Our algorithm ranks high various conjunctions that include the domain of the document. As commented already above, our approach seems to implicitly perform domain adaptation, by adding conjunctions between features that play different roles in different domains and the respective domain features (very similar to the approach of (Daumé, 2009)).

6 Discussion

We introduced a greedy heuristic for feature selection and induction. The method is applied as a preprocessing step, prior to model fitting, therefore it is independent from the classifier chosen by the user. It is very fast in practice, having all the advantages of the filter-based methods over complex wrappers and embedded methods.

We applied the method on a custom dataset from Press Association, for named entity disambiguation. In particular, we recognized Locations from negative entities. The results, presented in the form of F1 measure corresponding to the Location class, show great improvements over the baseline.

We provided with a qualitative analysis of some of the highest ranking conjunctions and they appear to be strong predictors for Location, that a domain expert would also consider adding to the model.

²www.geonames.org

³http://gate.ac.uk/

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