Similarity-Based Estimation of Word Cooccurrence Probabilities

Ido Dagan Fernando Pereira AT&T Bell Laboratories 600 Mountain Ave. Murray Hill, NJ 07974, USA dagan@research.att.com pereira@research.att.com

Abstract

In many applications of natural language processing it is necessary to determine the likelihood of a given word combination. For example, a speech recognizer may need to determine which of the two word combinations "eat a peach" and "eat a beach" is more likely. Statistical NLP methods determine the likelihood of a word combination according to its frequency in a training corpus. However, the nature of language is such that many word combinations are infrequent and do not occur in a given corpus. In this work we propose a method for estimating the probability of such previously unseen word combinations using available information on "most similar" words.

We describe a probabilistic word association model based on distributional word similarity, and apply it to improving probability estimates for unseen word bigrams in a variant of Katz's back-off model. The similarity-based method yields a 20% perplexity improvement in the prediction of unseen bigrams and statistically significant reductions in speech-recognition error.

Introduction

Data sparseness is an inherent problem in statistical methods for natural language processing. Such methods use statistics on the relative frequencies of configurations of elements in a training corpus to evaluate alternative analyses or interpretations of new samples of text or speech. The most likely analysis will be taken to be the one that contains the most frequent configurations. The problem of data sparseness arises when analyses contain configurations that never occurred in the training corpus. Then it is not possible to estimate probabilities from observed frequencies, and some other estimation scheme has to be used.

We focus here on a particular kind of configuration, word cooccurrence. Examples of such cooccurrences include relationships between head words in syntactic constructions (verb-object or adjective-noun, for example) and word sequences (*n*-grams). In commonly used models, the probability estimate for a previously unseen cooccurrence is a function of the probability estiLillian Lee Division of Applied Sciences Harvard University 33 Oxford St. Cambridge MA 02138, USA llee@das.harvard.edu

mates for the words in the cooccurrence. For example, in the bigram models that we study here, the probability $P(w_2|w_1)$ of a conditioned word w_2 that has never occurred in training following the conditioning word w_1 is calculated from the probability of w_2 , as estimated by w_2 's frequency in the corpus (Jelinek, Mercer, and Roukos, 1992; Katz, 1987). This method depends on an independence assumption on the cooccurrence of w_1 and w_2 : the more frequent w_2 is, the higher will be the estimate of $P(w_2|w_1)$, regardless of w_1 .

Class-based and similarity-based models provide an alternative to the independence assumption. In those models, the relationship between given words is modeled by analogy with other words that are in some sense similar to the given ones.

Brown et al. (1992) suggest a class-based *n*-gram model in which words with similar cooccurrence distributions are clustered in word classes. The cooccurrence probability of a given pair of words then is estimated according to an averaged cooccurrence probability of the two corresponding classes. Pereira, Tishby, and Lee (1993) propose a "soft" clustering scheme for certain grammatical cooccurrences in which membership of a word in a class is probabilistic. Cooccurrence probabilities of words are then modeled by averaged cooccurrence probabilities of word clusters.

Dagan, Markus, and Markovitch (1993) argue that reduction to a relatively small number of predetermined word classes or clusters may cause a substantial loss of information. Their similarity-based model avoids clustering altogether. Instead, each word is modeled by its own specific class, a set of words which are most similar to it (as in *k*-nearest neighbor approaches in pattern recognition). Using this scheme, they predict which unobserved cooccurrences are more likely than others. Their model, however, is not probabilistic, that is, it does not provide a probability estimate for unobserved cooccurrences. It cannot therefore be used in a complete probabilistic framework, such as *n*-gram language models or probabilistic lexicalized grammars (Schabes, 1992; Lafferty, Sleator, and Temperley, 1992).

We now give a similarity-based method for estimating the probabilities of cooccurrences unseen in training. Similarity-based estimation was first used for language modeling in the *cooccurrence smoothing* method of Essen and Steinbiss (1992), derived from work on acoustic model smoothing by Sugawara et al. (1985). We present a different method that takes as starting point the back-off scheme of Katz (1987). We first allocate an appropriate probability mass for unseen cooccurrences following the back-off method. Then we redistribute that mass to unseen cooccurrences according to an averaged cooccurrence distribution of a set of most similar conditioning words, using relative entropy as our similarity measure. This second step replaces the use of the independence assumption in the original back-off model.

We applied our method to estimate unseen bigram probabilities for *Wall Street Journal* text and compared it to the standard back-off model. Testing on a held-out sample, the similarity model achieved a 20% reduction in perplexity for unseen bigrams. These constituted just 10.6% of the test sample, leading to an overall reduction in test-set perplexity of 2.4%. We also experimented with an application to language modeling for speech recognition, which yielded a statistically significant reduction in recognition error.

The remainder of the discussion is presented in terms of bigrams, but it is valid for other types of word cooccurrence as well.

Discounting and Redistribution

Many low-probability bigrams will be missing from any finite sample. Yet, the aggregate probability of all these unseen bigrams is fairly high; any new sample is very likely to contain some.

Because of data sparseness, we cannot reliably use a maximum likelihood estimator (MLE) for bigram probabilities. The MLE for the probability of a bigram (w_1, w_2) is simply:

$$P_{ML}(w_1, w_2) = \frac{c(w_1, w_2)}{N} \quad , \qquad (1)$$

where $c(w_1, w_2)$ is the frequency of (w_1, w_2) in the training corpus and N is the total number of bigrams. However, this estimates the probability of any unseen bigram to be zero, which is clearly undesirable.

Previous proposals to circumvent the above problem (Good, 1953; Jelinek, Mercer, and Roukos, 1992; Katz, 1987; Church and Gale, 1991) take the MLE as an initial estimate and adjust it so that the total probability of seen bigrams is less than one, leaving some probability mass for unseen bigrams. Typically, the adjustment involves either *interpolation*, in which the new estimator is a weighted combination of the MLE and an estimator that is guaranteed to be nonzero for unseen bigrams, or *discounting*, in which the MLE is decreased according to a model of the unreliability of small frequency counts, leaving some probability mass for unseen bigrams.

The back-off model of Katz (1987) provides a clear separation between frequent events, for which observed frequencies are reliable probability estimators, and lowfrequency events, whose prediction must involve additional information sources. In addition, the back-off model does not require complex estimations for interpolation parameters.

A back-off model requires methods for (a) discounting the estimates of previously observed events to leave out some positive probability mass for unseen events, and (b) redistributing among the unseen events the probability mass freed by discounting. For bigrams the resulting estimator has the general form

$$\hat{P}(w_2|w_1) = \begin{cases} P_d(w_2|w_1) & \text{if } c(w_1, w_2) > 0\\ \alpha(w_1)P_r(w_2|w_1) & \text{otherwise} \end{cases} , (2)$$

where P_d represents the discounted estimate for seen bigrams, P_r the model for probability redistribution among the unseen bigrams, and $\alpha(w)$ is a normalization factor. Since the overall mass left for unseen bigrams starting with w_1 is given by

$$\tilde{\beta}(w_1) = 1 - \sum_{w_2: c(w_1, w_2) > 0} P_d(w_2|w_1)$$

the normalization factor required to ensure $\sum_{w_2} \hat{P}(w_2|w_1) = 1$ is

$$\begin{aligned} \alpha(w_1) &= \frac{\tilde{\beta}(w_1)}{\sum_{w_2:c(w_1,w_2)=0} P_r(w_2|w_1)} \\ &= \frac{\tilde{\beta}(w_1)}{1 - \sum_{w_2:c(w_1,w_2)>0} P_r(w_2|w_1)} \end{aligned}$$

The second formulation of the normalization is computationally preferable because the total number of possible bigram types far exceeds the number of observed types. Equation (2) modifies slightly Katz's presentation to include the placeholder P_r for alternative models of the distribution of unseen bigrams.

Katz uses the Good-Turing formula to replace the actual frequency $c(w_1, w_2)$ of a bigram (or an event, in general) with a discounted frequency, $c^*(w_1, w_2)$, defined by

$$c^*(w_1, w_2) = (c(w_1, w_2) + 1) \frac{n_{c(w_1, w_2)+1}}{n_{c(w_1, w_2)}}, \quad (3)$$

where n_c is the number of different bigrams in the corpus that have frequency c. He then uses the discounted frequency in the conditional probability calculation for a bigram:

$$P_d(w_2|w_1) = \frac{c^*(w_1, w_2)}{c(w_1)} \qquad . \tag{4}$$

In the original Good-Turing method (Good, 1953) the free probability mass is redistributed uniformly among all unseen events. Instead, Katz's back-off scheme redistributes the free probability mass non-uniformly in proportion to the frequency of w_2 , by setting

$$P_r(w_2|w_1) = P(w_2) . (5)$$

Katz thus assumes that for a given conditioning word w_1 the probability of an unseen following word w_2 is proportional to its unconditional probability. However, the overall form of the model (2) does not depend on this assumption, and we will next investigate an estimate for $P_r(w_2|w_1)$ derived by averaging estimates for the conditional probabilities that w_2 follows words that are distributionally similar to w_1 .

The Similarity Model

Our scheme is based on the assumption that words that are "similar" to w_1 can provide good predictions for the distribution of w_1 in unseen bigrams. Let $\mathcal{S}(w_1)$ denote a set of words which are most similar to w_1 , as determined by some similarity metric. We define $P_{\text{SIM}}(w_2|w_1)$, the similarity-based model for the conditional distribution of w_1 , as a weighted average of the conditional distributions of the words in $\mathcal{S}(w_1)$:

$$P_{\text{SIM}}(w_2|w_1) = \sum_{w_1' \in \mathcal{S}(w_1)} P(w_2|w_1') \frac{W(w_1',w_1)}{\sum_{w_1' \in \mathcal{S}(w_1)} W(w_1',w_1)} \quad , \quad (6)$$

where $W(w'_1, w_1)$ is the (unnormalized) weight given to w'_1 , determined by its degree of similarity to w_1 . According to this scheme, w_2 is more likely to follow w_1 if it tends to follow words that are most similar to w_1 . To complete the scheme, it is necessary to define the similarity metric and, accordingly, $S(w_1)$ and $W(w'_1, w_1)$.

Following Pereira, Tishby, and Lee (1993), we measure word similarity by the *relative entropy*, or *Kullback-Leibler (KL) distance*, between the corresponding conditional distributions

$$D(w_1 \parallel w_1') = \sum_{w_2} P(w_2 \mid w_1) \log \frac{P(w_2 \mid w_1)}{P(w_2 \mid w_1')} .$$
(7)

The KL distance is 0 when $w_1 = w'_1$, and it increases as the two distribution are less similar.

To compute (6) and (7) we must have nonzero estimates of $P(w_2|w_1)$ whenever necessary for (7) to be defined. We use the estimates given by the standard back-off model, which satisfy that requirement. Thus our application of the similarity model averages together standard back-off estimates for a set of similar conditioning words.

We define $S(w_1)$ as the set of at most k nearest words to w_1 (excluding w_1 itself), that also satisfy $D(w_1 \parallel w'_1) < t$. k and t are parameters that control the contents of $S(w_1)$ and are tuned experimentally, as we will see below.

 $W(w'_1, w_1)$ is defined as

$$W(w'_1, w_1) = \exp{-\beta D(w_1 \parallel w'_1)}$$

The weight is larger for words that are more similar (closer) to w_1 . The parameter β controls the relative contribution of words in different distances from w_1 : as the value of β increases, the nearest words to w_1 get relatively more weight. As β decreases, remote words get a larger effect. Like k and t, β is tuned experimentally.

Having a definition for $P_{\text{SIM}}(w_2|w_1)$, we could use it directly as $P_r(w_2|w_1)$ in the back-off scheme (2). We found that it is better to smooth $P_{\text{SIM}}(w_2|w_1)$ by interpolating it with the unigram probability $P(w_2)$ (recall that Katz used $P(w_2)$ as $P_r(w_2|w_1)$). Using linear interpolation we get

$$P_r(w_2|w_1) = \gamma P(w_2) + (1-\gamma)P_{\text{SIM}}(w_2|w_1) , \quad (8)$$

where γ is an experimentally-determined interpolation parameter. This smoothing appears to compensate for inaccuracies in $P_{\text{SIM}}(w_2|w_1)$, mainly for infrequent conditioning words. However, as the evaluation below shows, good values for γ are small, that is, the similarity-based model plays a stronger role than the independence assumption.

To summarize, we construct a similarity-based model for $P(w_2|w_1)$ and then interpolate it with $P(w_2)$. The interpolated model (8) is used in the back-off scheme as $P_r(w_2|w_1)$, to obtain better estimates for unseen bigrams. Four parameters, to be tuned experimentally, are relevant for this process: k and t, which determine the set of similar words to be considered, β , which determines the relative effect of these words, and γ , which determines the overall importance of the similarity-based model.

Evaluation

We evaluated our method by comparing its perplexity¹ and effect on speech-recognition accuracy with the baseline bigram back-off model developed by MIT Lincoln Laboratories for the *Wall Street Journal* (WSJ) text and dictation corpora provided by ARPA's HLT program (Paul, 1991).² The baseline back-off model follows closely the Katz design, except that for compactness all frequency one bigrams are ignored. The counts used in this model and in ours were obtained from 40.5 million words of WSJ text from the years 1987-89.

For perplexity evaluation, we tuned the similarity model parameters by minimizing perplexity on an additional sample of 57.5 thousand words of WSJ text, drawn from the ARPA HLT development test set. The best parameter values found were $k = 60, t = 2.5, \beta = 4$ and $\gamma = 0.15$. For these values, the improvement in perplexity for unseen bigrams in a held-out 18 thousand word sample, in which 10.6% of the bigrams are unseen, is just over 20%. This improvement on unseen

¹The perplexity of a conditional bigram probability model \hat{P} with respect to the true bigram distribution is an information-theoretic measure of model quality (Jelinek, Mercer, and Roukos, 1992) that can be empirically estimated by $\exp -\frac{1}{N} \sum_{i} \log \hat{P}(w_i|w_{i-1})$ for a test set of length N. Intuitively, the lower the perplexity of a model the more likely the model is to assign high probability to bigrams that actually occur. In our task, lower perplexity will indicate better prediction of unseen bigrams.

²The ARPA WSJ development corpora come in two versions, one with verbalized punctuation and the other without. We used the latter in all our experiments.

	k	t	$\boldsymbol{\beta}$	γ	training reduction (%)	test reduction (%)
	60	2.5	4	0.15	18.4	20.51
	50	2.5	4	0.15	18.38	20.45
	40	2.5	4	0.2	18.34	20.03
	30	2.5	4	0.25	18.33	19.76
	70	2.5	4	0.1	18.3	20.53
	80	2.5	4.5	0.1	18.25	20.55
1	00	2.5	4.5	0.1	18.23	20.54
	90	2.5	4.5	0.1	18.23	20.59
	20	1.5	4	0.3	18.04	18.7
	10	1.5	3.5	0.3	16.64	16.94

Table 1: Perplexity Reduction on Unseen Bigrams for Different Model Parameters

bigrams corresponds to an overall test set perplexity improvement of 2.4% (from 237.4 to 231.7). Table 1 shows reductions in training and test perplexity, sorted by training reduction, for different choices in the number k of closest neighbors used. The values of β , γ and t are the best ones found for each k.³

From equation (6), it is clear that the computational cost of applying the similarity model to an unseen bigram is O(k). Therefore, lower values for k (and also for t) are computationally preferable. From the table, we can see that reducing k to 30 incurs a penalty of less than 1% in the perplexity improvement, so relatively low values of k appear to be sufficient to achieve most of the benefit of the similarity model. As the table also shows, the best value of γ increases as k decreases, that is, for lower k a greater weight is given to the conditioned word's frequency. This suggests that the predictive power of neighbors beyond the closest 30 or so can be modeled fairly well by the overall frequency of the conditioned word.

The bigram similarity model was also tested as a language model in speech recognition. The test data for this experiment were pruned word lattices for 403 WSJ closed-vocabulary test sentences. Arc scores in those lattices are sums of an acoustic score (negative log likelihood) and a language-model score, in this case the negative log probability provided by the baseline bigram model.

From the given lattices, we constructed new lattices in which the arc scores were modified to use the similarity model instead of the baseline model. We compared the best sentence hypothesis in each original lattice and in the modified one, and counted the word disagreements in which one of the hypotheses is correct. There were a total of 96 such disagreements. The similarity model was correct in 64 cases, and the back-off model in 32. This advantage for the similarity model is statistically significant at the 0.01 level. The overall reduction in error rate is small, from 21.4% to 20.9%, because the number of disagreements is small compared with the overall number of errors in our current recognition setup.

Table 2 shows some examples of speech recognition disagreements between the two models. The hypotheses are labeled 'B' for back-off and 'S' for similarity, and the bold-face words are errors. The similarity model seems to be able to model better regularities such as semantic parallelism in lists and avoiding a past tense form after "to." On the other hand, the similarity model makes several mistakes in which a function word is inserted in a place where punctuation would be found in written text.

Related Work

The cooccurrence smoothing technique (Essen and Steinbiss, 1992), based on earlier stochastic speech modeling work by Sugawara et al. (1985), is the main previous attempt to use similarity to estimate the probability of unseen events in language modeling. In addition to its original use in language modeling for speech recognition, Grishman and Sterling (1993) applied the cooccurrence smoothing technique to estimate the likelihood of selectional patterns. We will outline here the main parallels and differences between our method and cooccurrence smoothing. A more detailed analysis would require an empirical comparison of the two methods on the same corpus and task.

In cooccurrence smoothing, as in our method, a baseline model is combined with a similarity-based model that refines some of its probability estimates. The similarity model in cooccurrence smoothing is based on the intuition that the similarity between two words wand w' can be measured by the *confusion* probability $P_C(w'|w)$ that w' can be substituted for w in an arbitrary context in the training corpus. Given a baseline probability model P, which is taken to be the MLE, the confusion probability $P_C(w'_1|w_1)$ between conditioning words w'_1 and w_1 is defined as

$$\frac{P_C(w_1'|w_1) =}{\frac{1}{P(w_1)} \sum_{w_2} P(w_1|w_2) P(w_1'|w_2) P(w_2)} , \quad (9)$$

the probability that w_1 is followed by the same context words as w'_1 . Then the bigram estimate derived by

³Values of β and t refer to base 10 logarithms and exponentials in all calculations.

В	commitments from leaders felt the three point six billion dollars				
S	commitments from leaders fell to three point six billion dollars				
В	followed by France the US agreed in Italy				
S	followed by France the US Greece Italy				
В	he whispers to made a				
S	he whispers to an aide				
В	the necessity for change exist				
S	the necessity for change exists				
B	without additional reserves Centrust would have reported				
B	withoutadditional reserves Centrust would have reported withoutadditional reserves of Centrust would have reported				

Table 2: Speech Recognition Disagreements between Models

cooccurrence smoothing is given by

$$P_{S}(w_{2}|w_{1}) = \sum_{w'_{1}} P(w_{2}|w'_{1}) P_{C}(w'_{1}|w_{1})$$

Notice that this formula has the same form as our similarity model (6), except that it uses confusion probabilities where we use normalized weights.⁴ In addition, we restrict the summation to sufficiently similar words, whereas the cooccurrence smoothing method sums over all words in the lexicon.

The similarity measure (9) is symmetric in the sense that $P_C(w'|w)$ and $P_C(w|w')$ are identical up to frequency normalization, that is $\frac{P_C(w'|w)}{P_C(w|w')} = \frac{P(w)}{P(w')}$. In contrast, D(w || w') (7) is asymmetric in that it weighs each context in proportion to its probability of occurrence with w, but not with w'. In this way, if w and w' have comparable frequencies but w' has a sharper context distribution than w, then D(w' || w) is greater than D(w || w'). Therefore, in our similarity model w' will play a stronger role in estimating w than vice versa. These properties motivated our choice of relative entropy for similarity measure, because of the intuition that words with sharper distributions are more informative about other words than words with flat distributions.

$$P_{S}(w_{2}|w_{1}) = \sum_{w_{1}',w_{2}'} P(w_{2}|w_{1}')P(w_{1}'|w_{2}')P(w_{2}'|w_{1})$$

They also consider other definitions of confusion probability and smoothed probability estimate, but the one above yielded the best experimental results. Finally, while we have used our similarity model only for missing bigrams in a back-off scheme, Essen and Steinbiss (1992) used linear interpolation for all bigrams to combine the cooccurrence smoothing model with MLE models of bigrams and unigrams. Notice, however, that the choice of back-off or interpolation is independent from the similarity model used.

Further Research

Our model provides a basic scheme for probabilistic similarity-based estimation that can be developed in several directions. First, variations of (6) may be tried, such as different similarity metrics and different weighting schemes. Also, some simplification of the current model parameters may be possible, especially with respect to the parameters t and k used to select the nearest neighbors of a word. A more substantial variation would be to base the model on similarity between conditioned words rather than on similarity between conditioning words.

Other evidence may be combined with the similaritybased estimate. For instance, it may be advantageous to weigh those estimates by some measure of the reliability of the similarity metric and of the neighbor distributions. A second possibility is to take into account negative evidence: if w_1 is frequent, but w_2 never followed it, there may be enough statistical evidence to put an upper bound on the estimate of $P(w_2|w_1)$. This may require an adjustment of the similarity based estimate, possibly along the lines of (Rosenfeld and Huang, 1992). Third, the similarity-based estimate can be used to smooth the maximum likelihood estimate for small nonzero frequencies. If the similarity-based estimate is relatively high, a bigram would receive a higher estimate than predicted by the uniform discounting method.

Finally, the similarity-based model may be applied to configurations other than bigrams. For trigrams, it is necessary to measure similarity between different conditioning bigrams. This can be done directly,

⁴This presentation corresponds to model 2-B in Essen and Steinbiss (1992). Their presentation follows the equivalent model 1-A, which averages over similar conditioned words, with the similarity defined with the preceding word as context. In fact, these equivalent models are symmetric in their treatment of conditioning and conditioned word, as they can both be rewritten as

by measuring the distance between distributions of the form $P(w_3|w_1, w_2)$, corresponding to different bigrams (w_1, w_2) . Alternatively, and more practically, it would be possible to define a similarity measure between bigrams as a function of similarities between corresponding words in them. Other types of conditional cooccurrence probabilities have been used in probabilistic parsing (Black et al., 1993). If the configuration in question includes only two words, such as P(object|verb), then it is possible to use the model we have used for bigrams. If the configuration includes more elements, it is necessary to adjust the method, along the lines discussed above for trigrams.

Conclusions

Similarity-based models suggest an appealing approach for dealing with data sparseness. Based on corpus statistics, they provide analogies between words that often agree with our linguistic and domain intuitions. In this paper we presented a new model that implements the similarity-based approach to provide estimates for the conditional probabilities of unseen word cooccurrences.

Our method combines similarity-based estimates with Katz's back-off scheme, which is widely used for language modeling in speech recognition. Although the scheme was originally proposed as a preferred way of implementing the independence assumption, we suggest that it is also appropriate for implementing similaritybased models, as well as class-based models. It enables us to rely on direct maximum likelihood estimates when reliable statistics are available, and only otherwise resort to the estimates of an "indirect" model.

The improvement we achieved for a bigram model is statistically significant, though modest in its overall effect because of the small proportion of unseen events. While we have used bigrams as an easily-accessible platform to develop and test the model, more substantial improvements might be obtainable for more informative configurations. An obvious case is that of trigrams, for which the sparse data problem is much more severe.⁵ Our longer-term goal, however, is to apply similarity techniques to linguistically motivated word cooccurrence configurations, as suggested by lexicalized approaches to parsing (Schabes, 1992; Lafferty, Sleator, and Temperley, 1992). In configurations like verb-object and adjective-noun, there is some evidence (Pereira, Tishby, and Lee, 1993) that sharper word cooccurrence distributions are obtainable, leading to improved predictions by similarity techniques.

Acknowledgments

We thank Slava Katz for discussions on the topic of this paper, Doug McIlroy for detailed comments, Doug Paul

.

for help with his baseline back-off model, and Andre Ljolje and Michael Riley for providing the word lattices for our experiments.

References

- Black, Ezra, Fred Jelinek, John Lafferty, David M. Magerman, David Mercer, and Salim Roukos. 1993.
 Towards history-based grammars: Using richer models for probabilistic parsing. In 30th Annual Meeting of the Association for Computational Linguistics, pages 31-37, Columbus, Ohio. Ohio State University. Association for Computational Linguistics, Morristown, New Jersey.
- Brown, Peter F., Vincent J. Della Pietra, Peter V. deSouza, Jenifer C. Lai, and Robert L. Mercer. 1992. Class-based n-gram models of natural language. Computational Linguistics, 18(4):467-479.
- Church, Kenneth W. and William A. Gale. 1991. A comparison of the enhanced Good-Turing and deleted estimation methods for estimating probabilities of English bigrams. Computer Speech and Language, 5:19-54.
- Dagan, Ido, Shaul Markus, and Shaul Markovitch. 1993. Contextual word similarity and estimation from sparse data. In 30th Annual Meeting of the Association for Computational Linguistics, pages 164– 171, Columbus, Ohio. Ohio State University, Association for Computational Linguistics, Morristown, New Jersey.
- Essen, Ute and Volker Steinbiss. 1992. Coocurrence smoothing for stochastic language modeling. In *Pro*ceedings of ICASSP, volume I, pages 161-164. IEEE.
- Good, I. J. 1953. The population frequencies of species and the estimation of population parameters. *Biometrika*, 40(3):237-264.
- Grishman, Ralph and John Sterling. 1993. Smoothing of automatically generated selectional constraints. In *Human Language Technology*, pages 254–259, San Francisco, California. Advanced Research Projects Agency, Software and Intelligent Systems Technology Office, Morgan Kaufmann.
- Jelinek, Frederick, Robert L. Mercer, and Salim Roukos. 1992. Principles of lexical language modeling for speech recognition. In Sadaoki Furui and M. Mohan Sondhi, editors, Advances in Speech Signal Processing. Mercer Dekker, Inc., pages 651-699.
- Katz, Slava M. 1987. Estimation of probabilities from sparse data for the language model component of a speech recognizer. *IEEE Transactions on Acoustics*, Speech and Signal Processing, 35(3):400-401.
- Lafferty, John, Daniel Sleator, and Davey Temperley. 1992. Grammatical trigrams: aa probabilistic model of link grammar. In Robert Goldman, editor, AAAI

⁵For WSJ trigrams, only 58.6% of test set trigrams occur in 40M of words of training (Doug Paul, personal communication).

Fall Symposium on Probabilistic Approaches to Natural Language Processing, Cambridge, Massachusetts. American Association for Artificial Intelligence.

- Paul, Douglas B. 1991. Experience with a stack decoder-based HMM CSR and back-off n-gram language models. In Proceedings of the Speech and Natural Language Workshop, pages 284-288, Palo Alto, California, February. Defense Advanced Research Projects Agency, Information Science and Technology Office, Morgan Kaufmann.
- Pereira, Fernando C. N., Naftali Z. Tishby, and Lillian Lee. 1993. Distributional clustering of English words. In 30th Annual Meeting of the Association for Computational Linguistics, pages 183–190, Columbus, Ohio. Ohio State University, Association for Computational Linguistics, Morristown, New Jersey.
- Rosenfeld, Ronald and Xuedong Huang. 1992. Improvements in stochastic language modeling. In *DARPA Speech and Natural Language Workshop*, pages 107–111, Harriman, New York, February. Morgan Kaufmann, San Mateo, California.
- Schabes, Yves. 1992. Stochastic lexicalized treeadjoining grammars. In Proceeedings of the 14th International Conference on Computational Linguistics, Nantes, France.
- Sugawara, K., M. Nishimura, K. Toshioka, M. Okochi, and T. Kaneko. 1985. Isolated word recognition using hidden Markov models. In *Proceedings of ICASSP*, pages 1-4, Tampa, Florida. IEEE.