Efficiently Parsable Extensions to Tree-Local Multicomponent TAG

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Abstract

Recent applications of Tree-Adjoining Grammar (TAG) to the domain of semantics as well as new attention to syntactic phenomena have given rise to increased interested in more expressive and complex multicomponent TAG formalisms (MCTAG). Although many constructions can be modeled using tree-local MCTAG (TL-MCTAG), certain applications require even more flexibility. In this paper we suggest a shift in focus from constraining locality and complexity through treeand set-locality to constraining locality and complexity through restrictions on the derivational distance between trees in the same tree set in a valid derivation. We examine three formalisms, restricted NS-MCTAG, restricted Vector-TAG and delayed TL-MCTAG, that use notions of derivational distance to constrain locality and demonstrate how they permit additional expressivity beyond TL-MCTAG without increasing complexity to the level of set local MCTAG.

1 Introduction

Tree-Adjoining Grammar (TAG) has long been popular for natural language applications because of its ability to naturally capture syntactic relationships while also remaining efficient to process. More recent applications of TAG to the domain of semantics as well as new attention to syntactic phenomena such as scrambling have given rise to increased interested in multicomponent TAG formalisms (MC-TAG), which extend the flexibility, and in some cases generative capacity of the formalism but also have substantial costs in terms of efficient processing. Much work in TAG semantics makes use of tree-local MCTAG (TL-MCTAG) to model phenomena such as quantifier scoping, Wh-question formation, and many other constructions (Kallmeyer and Romero, 2004; Romero et al., 2004). Certain applications, however, appear to require even more flexibility than is provided by TL-MCTAG. Scrambling is one well-known example (Rambow, 1994). In addition, in the semantics domain, the use of a new TAG operation, flexible composition, is used to perform certain semantic operations that seemingly cannot be modeled with TL-MCTAG alone (Chiang and Scheffler, 2008) and in work in synchronous TAG semantics, constructions such as nested quantifiers require a set-local MCTAG (SL-MCTAG) analysis (Nesson and Shieber, 2006).

In this paper we suggest a shift in focus from constraining locality and complexity through restrictions that all trees in a tree set must adjoin within a single tree or tree set to constraining locality and complexity through restrictions on the derivational distance between trees in the same tree set in a valid derivation. We examine three formalisms, two of them introduced in this work for the first time, that use derivational distance to constrain locality and demonstrate by construction of parsers their relationship to TL-MCTAG in both expressivity and complexity. In Section 2 we give a very brief introduction to TAG. In Section 3 we elaborate further the distinction between these two types of locality restrictions using TAG derivation trees. Section 4 briefly addresses the simultaneity requirement present in MCTAG formalisms but not in Vector-



Figure 1: An example of the TAG operations **substitution** and **adjunction**.

TAG formalisms and argues for dropping the requirement. In Sections 5 and 6 we introduce two novel formalisms, restricted non-simultaneous MC-TAG and restricted Vector-TAG, respectively, and define CKY-style parsers for them. In Section 7 we recall the delayed TL-MCTAG formalism introduced by Chiang and Scheffler (2008) and define a CKY-style parser for it as well. In Section 8 we explore the complexity of all three parsers and the relationship between the formalisms. In Section 9 we discuss the linguistic applications of these formalisms and show that they permit analyses of some of the hard cases that have led researchers to look beyond TL-MCTAG.

2 Background

A tree-adjoining grammar consists of a set of elementary tree structures of arbitrary depth, which are combined by operations of **adjunction** and **substitution**. **Auxiliary trees** are elementary trees in which the root and a frontier node, called the **foot node** and distinguished by the diacritic *, are labeled with the same nonterminal A. The adjunction operation entails splicing an auxiliary tree in at an internal node in an elementary tree also labeled with nonterminal A. Trees without a foot node, which serve as a base for derivations and may combine with other trees by substitution, are called **initial trees**. Examples of the adjunction and substitution operations are given in Figure 1. For further background, refer to the survey by (Joshi and Schabes, 1997).

Shieber et al. (1995) and Vijay-Shanker (1987) apply the Cocke-Kasami-Younger (CKY) algorithm first introduced for use with context-free grammars in Chomsky normal form (Kasami, 1965; Younger, 1967) to the TAG parsing problem to generate parsers with a time complexity of $O(n^6|G|^2)$. In

order to clarify the presentation of our extended TL-MCTAG parsers below, we briefly review the algorithm of Shieber et al. (1995) using the inference rule notation from that paper. As shown in Figure 2, items in CKY-style TAG parsing consist of a node in an elementary tree and the indices that mark the edges of the span dominated by that node. Nodes, notated $\alpha @a^\circ$, are specified by three pieces of information: the identifier α of the elementary tree the node is in, the Gorn address a of the node in that tree¹, and a diacritic, \circ , indicating that an adjunction or substitution is still available at that node or \bullet , indicating that one has already taken place.

Each item has four indices, indicating the left and right edges of the span covered by the node as well as any gap in the node that may be the result of a foot node dominated by the node. Nodes that do not dominate a foot node will have no gap in them, which we indicate by the use of underscores in place of the indices for the gap. To limit the number of inference rules needed, we define the following function $i \cup j$ for combining indices:

$$i \cup j = \begin{cases} i & j = -\\ j & i = -\\ i & i = j\\ \text{undefined otherwise} \end{cases}$$

The side conditions $lnit(\alpha)$ and $Aux(\alpha)$ hold if α is an initial tree or an auxiliary tree, respectively. Label($\alpha@a$) specifies the label of the node in tree α at address a. Ft(α) specifies the address of the foot node of tree α . Adj($\alpha@a, \beta$) holds if tree β may adjoin into tree α at address a. Subst($\alpha@a, \beta$) holds if tree β may substitute into tree α at address a. These conditions fail if the adjunction or substitution is prevented by constraints such as mismatched node labels.

Multi-component TAG (MCTAG) generalizes TAG by allowing the elementary items to be sets of trees rather than single trees (Joshi and Schabes, 1997). The basic operations are the same but all trees in a set must adjoin (or substitute) into another tree or tree set in a single step in the derivation.

An MCTAG is **tree-local** if tree sets are required to adjoin within a single elementary tree (Weir,

¹A Gorn address uniquely identifies a node within a tree. The Gorn address of the root node is ε . The *j*th child of the node with address *i* has address *i* · *j*.

Goal Item:	$\langle \alpha @ \varepsilon^{\bullet}, 0, _, _, n \rangle$	$\begin{array}{l} \operatorname{Init}(\alpha) \\ \operatorname{Label}(\alpha @ \varepsilon) = S \end{array}$
Terminal Axiom:	$\langle lpha @a^{ullet}, i-1,$, , , , $i angle$	$Label(\alpha @a) = w_i$
Empty Axiom:	$\langle lpha @a^{ullet}, i,$ _, _, _, $i angle$	$Label(\alpha @a) = \varepsilon$
Foot Axiom:	$\langle \alpha @Ft(\alpha)^\circ, p, p, q, q \rangle$	$Aux(\alpha)$
Unary Complete:	$\frac{\langle \alpha @(a \cdot 1)^{\bullet}, i, j, k, l \rangle}{\langle \alpha @a^{\circ}, i, j, k, l \rangle}$	$\alpha @ (a \cdot 2)$ undefined
Binary Complete:	$\frac{\langle \alpha @ (a \cdot 1)^{\bullet}, i, j, k, l \rangle, \langle \alpha @ (a \cdot 2)^{\bullet}, l, j', k', m \rangle}{\langle \alpha @ a^{\circ}, i, j \cup j', k \cup k', m \rangle}$	
Adjoin:	$\frac{\langle \beta @ \varepsilon^{\bullet}, i, p, q, l \rangle, \langle \alpha @ a^{\circ}, p, j, k, q \rangle}{\langle \alpha @ a^{\bullet}, i, j, k, l \rangle}$	$Adj(\alpha@a,\beta)$
No Adjoin:	$rac{\langle lpha @a^\circ, i, j, k, l angle}{\langle lpha @a^ullet, i, j, k, l angle}$	
Substitute:	$rac{\langleeta@arepsilon^ullet,i,,,l angle}{\langlelpha@a^ullet,i,,,l angle}$	$Subst(\alpha @a,\beta)$

Figure 2: The CKY algorithm for TAG

1988). Although tree-local MCTAG (TL-MCTAG) has the same generative capacity as TAG (Weir, 1988), the conversion to TAG is exponential and the TL-MCTAG formalism is NP-hard to recognize (Søgaard et al., 2007). An MCTAG is **set-local** if tree sets required to adjoin within a single elementary tree set (Weir, 1988). Set-local MCTAG (SL-MCTAG) has equivalent expressivity to linear context-free rewriting systems and recognition is provably PSPACE complete (Nesson et al., 2008).

3 Domains of Locality and Derivation Trees

The domains of locality of TL-MCTAG and SL-MCTAG (and trivially, TAG) can be thought of as lexically defined. That is, all locations at which the adjunction of one tree set into another may occur must be present within a single lexical item. However, we can also think of locality derivationally. In a derivationally local system the constraint is on the

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relationships allowed between members of the same tree set in the derivation tree.

TAG derivation trees provide the information about how the elementary structures of the grammar combine that is necessary to construct the derived tree. Nodes in a TAG derivation tree are labeled with identifiers of elementary structures. One elementary structure is the child of another in the derivation tree if it adjoins or substitutes into it in the derivation. Arcs in the derivation tree are labeled with the address in the target elementary structure at which the operation takes place.

In MCTAG the derivation trees are often drawn with identifiers of entire tree sets as the nodes of the tree because the lexical locality constraints require that each elementary tree set be the derivational child of only one other tree set. However, if we elaborate the derivation tree to include a node for each tree in the grammar rather than only for each tree set we can see a stark contrast in the derivational



Figure 3: An example SL-MCTAG grammar that generates the language *ww* and associated derivation tree that demonstrating an arbitrarily long derivational distance between the trees of a given tree set and their nearest common ancestor. Note that if this grammar is interpreted as a TL-MCTAG grammar only two derivations are possible (for the strings *aa* and *bb*).

locality of these two formalisms. In TL-MCTAG all trees in a set must adjoin to the same tree. This means that they must all be siblings in the derivation tree. In SL-MCTAG, on the other hand, it is possible to generate derivations with arbitrarily long distances before the nearest common ancestor of two trees from the same elementary tree set is reached. An example SL-MCTAG grammar that can produce an arbitrarily long derivational distance to the nearest common ancestor of the trees in a given tree set is given in Figure 3.

Chiang and Scheffler (2008) recently introduced one variant of MCTAG, delayed Tree-Local MC-TAG (delayed TL-MCTAG) that uses a derivational notion of locality. In this paper we introduce two additional derivationally local TAG-based formalisms, restricted non-simultaneous MCTAG (restricted NS-MCTAG) and restricted Vector TAG (restricted V-TAG) and demonstrate by construction of parsers how each gives rise to a hierarchy of derivationally local formalisms with a well-defined efficiency penalty for each step of derivational distance permitted.

4 The Simultaneity Requirement

In addition to lexical locality constraints the definition of MCTAG requires that all trees from a set adjoin simultaneously. In terms of well-formed derivation trees, this amounts to disallowing derivations in which a tree from a given set is the ancestor of a tree from the same tree set. For most linguistic applications of TAG, this requirement seems natural and is strictly obeyed. There are a few applications, including flexible composition and scrambling in free-word order languages that benefit from TAG-based grammars that drop the simultaneity requirement (Chiang and Scheffler, 2008; Rambow, 1994). From a complexity perspective, however, checking the simultaneity requirement is expensive (Kallmeyer, 2007). As a result, it can be advantageous to select a base formalism that does not require simultaneity even if the grammars implemented with it do not make use of that additional freedom.

5 Restricted Non-simultaneous MCTAG

The simplest version of a derivationally local TAGbased formalism is most similar to non-local MC-TAG. There is no lexical locality requirement at all. In addition, we drop the simultaneity requirement. Thus the only constraint on elementary tree sets is the limit, d, on the derivational distance between the trees in a given set and their nearest common ancestor. We call this formalism restricted nonsimultaneous MCTAG. Note that if we constrain d to be one, this happens to enforce both the derivational delay limit and the lexical locality requirement of TL-MCTAG.

A CKY-style parser for restricted NS-MCTAG with a restriction of d is given in Figure 4. The items of this parser contain d lists, $\Lambda^1, \ldots, \Lambda^d$, called **his**tories that record the identities of the trees that have already adjoined in the derivation in order to enforce the locality constraints. The identities of the trees in a tree set that have adjoined in a given derivation are maintained in the histories until all the trees from that set have adjoined. Once the locality constraint is checked for a tree set, the Filter side condition expunges those trees from the histories. A tree is recorded in this history list with superscript *i*, where i is the derivational distance between the location where the recorded tree adjoined and the location of the current item. The locality constraint is enforced at the point of adjunction or substitution where the

$$\frac{\langle \alpha_x @a^{\bullet}, i, _, _, l, \Lambda^1, \dots, \Lambda}{\langle \alpha_x @a^{\bullet}, i, _, _, l, \Lambda^1, \dots, \Lambda}$$

No Adjoin:

$$\frac{\langle \alpha_x @a^{\circ}, i, j, k, l, \Lambda^1, \dots, \Lambda^d \rangle}{\langle \alpha_x @a^{\bullet}, i, j, k, l, \Lambda^1, \dots, \Lambda^d \rangle}$$

Figure 4: Axioms and inference rules for the CKY algorithm for restricted NS-MCTAG with a restriction of d.

history at the limit of the permissible delay must be empty for the operation to succeed.

6 **Restricted V-TAG**

A Vector-TAG (V-TAG) (Rambow, 1994) is similar to an MCTAG in that the elementary structures are sets (or vectors) of TAG trees. A derivation in a V-TAG is defined as in TAG. There is no locality requirement or other restriction on adjunction except that if one tree from a vector is used in a derivation, all trees from that vector must be used in the derivation. The trees in a vector may be connected by dominance links between the foot nodes of auxiliary trees and any node in other trees in the vector. All adjunctions must respect the dominance relations in that a node η_1 that dominates a node η_2 must appear on the path from η_2 to the root of the derived tree. The definition of V-TAG is very similar to that of non-local MCTAG as defined by Weir (1988) except that in non-local MCTAG all trees from a tree set are required to adjoin simultaneously.

Restricted V-TAG constrains V-TAG in several ways. First, the dominance chain in each elementary tree vector is required to define a total order over the trees in the vector. This means there is a single base tree in each vector. Note also that all trees other than the base tree must be auxiliary trees in order to dominate other trees in the vector. The base tree may be either an initial tree or an auxiliary tree. Second, a restricted V-TAG has a restriction level, d, that determines the largest derivational distance that may exists between the base tree and the highest tree in a tree vector in a derivation. Restricted V-TAG differs from restricted NS-MCTAG in one important respect: the dominance requirements of restricted V-TAG require that trees from the same set must appear along a single path in the derived tree, whereas in restricted NS-MCTAG trees from the same set need not adhere to any dominance relationship in the derived tree.

A CKY-style parser for restricted V-TAG with restriction level d is given in Figure 5. Parsing is similar to delayed TL-MCTAG in that we have a set of histories for each restriction level. However, because of the total order over trees in a vector, the parser only needs to maintain the identity of the highest tree from a vector that has been used in the derivation along with its distance from the base tree from that vector. The Filter side condition accordingly expunges trees that are the top tree in the dominance chain of their tree vector. The side conditions for the Adjoin non-base rule enforce that the dominance constraints are satisfied and that the derivational distance from the base of a tree vector to its currently highest adjoined tree is maintained accurately. We note that in order to allow a non-total ordering of the trees in a vector we would simply have to record all trees in a tree vector in the histories as is done in the delayed TL-MCTAG parser.

7 Delayed TL-MCTAG

Chiang and Scheffler (2008) introduce the delayed TL-MCTAG formalism which makes use of a derivational distance restriction in a somewhat different way. Rather than restricting the absolute distance between the trees of a set and their nearest common ancestor, given a node α in a derivation tree, delayed TL-MCTAG restricts the number of tree sets that are not fully dominated by α . Borrowing directly from Chiang and Scheffler (2008), Figure 7 gives two examples.

Parsing for delayed TL-MCTAG is not discussed by Chiang and Scheffler (2008) but can be accomplished using a similar CKY-style strategy as in the two parsers above. We present a parser in Figure 6. Rather than keeping histories that record derivational distance, we keep an active delay list for each item that records the delays that are active (by recording the identities of the trees that have adjoined) for the tree of which the current node is a part. At the root of each tree the active delay list is filtered using the Filter side condition to remove all tree sets that are fully dominated and the resulting



Figure 7: Examples of 1-delay (top) and 2-delay (bottom) taken from Chiang and Scheffler (2008). The delays are marked with dashed boxes on the derivation trees.

list is checked using the Size to ensure that it contains no more than d distinct tree sets where d is the specified delay for the grammar. The active delays for a given tree are passed to its derivational parent when it adjoins or substitutes.

Delayed TL-MCTAG differs from both of the previous formalisms in that it places no constraint on the length of a delay. On the other hand while the previous formalisms allow unlimited short delays to be pending at the same time, in delayed TL-MCTAG, only a restricted number of delays may be active at once. Similar to restricted V-TAG, there is no simultaneity requirement, so a tree may have another tree from the same set as an ancestor.

8 Complexity

The complexity of the restricted NS-MCTAG and restricted V-TAG parsers presented above depends on the number of possible histories that may appear in an item. For each step of derivational distance permitted between trees of the same set, the corresponding history permits many more entries. History Λ^1 may contain trees that have adjoined into the same tree as the node of the current item. The number of entries is therefore limited by the number of adjunction sites in that tree, which is in turn limited by the number of nodes in that tree. We will call the maximum number of nodes in a tree in the grammar t. Theoretically, any tree in the grammar could adjoin at any of these adjunction sites, meaning that the number of possible values for each entry in the history is bounded by the size of the grammar |G|. Thus the size of Λ^1 is $O(|G|^t)$. For Λ^2 the enUnary Complete

$$\frac{\langle \alpha_x @ (a \cdot 1)^{\bullet}, i, j, k, l, \Lambda^1, \dots, \Lambda^d \rangle}{\langle \alpha_x @ a^{\circ}, i, j, k, l, \Lambda^1, \dots, \Lambda^d \rangle}$$

 $\alpha_x @(a \cdot 2)$ undefined

 $\mathsf{Filter}(\Lambda^1_2\cup\{\beta_1\},\Lambda^2_2\cup\Lambda^1_1,$

 $\begin{aligned} \mathsf{Filter}(\Lambda_{2'}^1,\Lambda_{2'}^2\cup\Lambda_1^1,\ldots,\\ \Lambda_{2'}^d\cup\Lambda_1^{d-1}) = \\ \Lambda^1,\ldots,\Lambda^d \end{aligned}$

 $\begin{array}{c} \dots, \Lambda_2^d \cup \Lambda_1^{d-1}) = \\ \Lambda^1, \dots, \Lambda^d \end{array}$

 $\operatorname{Adj}(\alpha_x @a, \beta_1)$

 $\operatorname{Adj}(\alpha_x @a, \beta_u)$

Binary Complete

$$\frac{\langle \alpha_x @(a \cdot 1)^{\bullet}, i, j, k, l, \Lambda_1^1, \dots, \Lambda_1^d \rangle \langle \alpha_x @(a \cdot 2)^{\bullet}, l, j', k', m, \Lambda_2^1, \dots, \Lambda_2^d \rangle}{\langle \alpha_x @a^{\circ}, i, j \cup j', k \cup k', m, \Lambda_1^1 \cup \Lambda_2^1, \dots, \Lambda_1^d \cup \Lambda_2^d \rangle}$$

Adjoin base:

$$\frac{\langle \beta_1 @ \varepsilon^{\bullet}, i, p, q, l, \Lambda_1^1, \dots, \Lambda_1^{d-1}, \emptyset \rangle \langle \alpha_x @ a^{\circ}, p, j, k, q, \Lambda_2^1, \dots, \Lambda_2^d \rangle}{\langle \alpha_x @ a^{\bullet}, i, j, k, l, \Lambda^1, \dots, \Lambda^d \rangle}$$

Adjoin non-base:

$$\begin{array}{c} \underline{\langle \beta_y @ \varepsilon^{\bullet}, i, p, q, l, \Lambda_1^1, \dots, \Lambda_1^{d-1}, \emptyset \rangle \langle \alpha_x @ a^{\circ}, p, j, k, q, \Lambda_2^1, \dots, \Lambda_2^d \rangle} \\ \overline{\langle \alpha_x @ a^{\bullet}, i, j, k, l, \Lambda^1, \dots, \Lambda^d \rangle} \\ \text{for unique } \Lambda_2^i \text{ s.t. } \beta_{y-1} \in \Lambda_2^i, \Lambda_{2'}^i = (\Lambda_2^i \cup \Lambda_1^{i-1} \cup \{\beta_y\}) - \{\beta_{y-1}\} \\ \text{ for } \Lambda_2^i \text{ s.t. } \beta_{y-1} \notin \Lambda_2^i, \Lambda_{2'}^i = \Lambda_2^i \cup \Lambda_1^{i-1} \end{array}$$

Substitute:

$$\frac{\langle \beta_1 @ \varepsilon^{\bullet}, i, _, _, l, \Lambda_1^1, \dots, \Lambda_1^{d-1}, \emptyset \rangle}{\langle \alpha_x @ a^{\bullet}, i, _, _, l, \Lambda^1, \dots, \Lambda^d \rangle}$$
Subst $(\alpha_x @ a, \beta_1)$
Filter $(\{\beta_1\}, \Lambda_1^1, \dots, \Lambda_1^{d-1})$

$$= \Lambda^1, \dots, \Lambda^d$$

No Adjoin:

$$\frac{\langle \alpha_x @ a^{\circ}, i, j, k, l, \Lambda^1, \dots, \Lambda^d \rangle}{\langle \alpha_x @ a^{\bullet}, i, j, k, l, \Lambda^1, \dots, \Lambda^d \rangle}$$

Figure 5: Inference rules for the CKY algorithm for restricted V-TAG with a restriction of d. Item form, goal item and axioms are omitted because they are identical to those in restricted NS-MCTAG parser.

tries correspond to tree that have adjoined into a tree that has adjoined into the tree of the current item. Thus, for each of the t trees that may have adjoined at a derivational distance of one, there are t more trees that may have adjoined at a derivational distance of two. The size of Λ^2 is therefore $|G|^{t^2}$. The combined size of the histories for a grammar with a delay or restriction of d is therefore $O(|G|\sum_{i=1}^{d} t^d)$. Replacing the sum with its closed form solution, we have $O(|G|^{\frac{t^{d+1}-1}{t-1}-1})$ histories.

Using the reasoning about the size of the histories given above, the restricted NS-MCTAG parser presented here has a complexity of $O(n^6 |G|^{1+\frac{t^{d+1}-1}{t-1}})$, where t is as defined above and d is the limit on delay of adjunction. For a tree-local MCTAG, the complexity reduces to $O(n^6 |G|^{2+t})$. For the linguistic applications that motivate this chapter no delay greater than two is needed, resulting in a complexity of $O(n^6 |G|^{2+t+t^2})$.

The same complexity analysis applies for re-

stricted V-TAG. However, we can provide a somewhat tighter bound by noting that the **rank**, r, of the grammar—how many tree sets adjoin in a single tree—and the **fan out**, f of the grammar—how many trees may be in a single tree set—are limited by t. That is, a complete derivation containing $|\mathcal{D}|$ tree sets can contain no more than $t |\mathcal{D}|$ individual trees and also no more than $rf |\mathcal{D}|$ individual trees. In the restricted V-TAG algorithm we maintain only one tree from a tree set in the history at a time, so rather than maintaining O(t) entries in each history, we only need to maintain the smaller O(r) entries.

The complexity of the delayed TL-MCTAG parser depends on the number of possible active delay lists. As above, each delay list may have a maximum of t entries for trees that adjoin directly into it. The restriction on the number of active delays means that the active delay lists passed up from these child nodes at the point of adjunction or substitution can have size no more than d. This results in an additional td(f - 1) possible entries in the active de-

No Adjoin:

$$\frac{\langle \alpha_x @a^{\circ}, i, j, k, l, \Lambda \rangle}{\langle \alpha_x @a^{\bullet}, i, j, k, l, \Lambda \rangle}$$

Figure 6: Axioms and inference rules for the CKY algorithm for delayed TL-MCTAG with a delay of d.

lay list, giving a total number of active delay lists of $O(|G|^{t(1+d(f-1))})$. Thus the complexity of the parser is $O(n^6 |G|^{2+t(1+d(f-1))})$.

9 Conclusion

Each of the formalisms presented above extends the flexibility of MCTAG beyond that of TL-MCTAG while maintaining, as we have shown herein, complexity much less than that of SL-MCTAG. All three formalisms permit modeling of flexible composition (because they permit one member of a tree set to be a derivational ancestor of another tree in the same set), at least restricted NS-MCTAG and restricted V-TAG permit analyses of scrambling, and all three permit analyses of the various challenging semantic constructions mentioned in the introduction. We conclude that extending locality by constraining derivational distance may be an effective way to add flexibility to MCTAG without losing computational tractability.

 $\operatorname{Size}(\Lambda'_{\beta}) \leq d$

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