Enhancing Fact Verification with Causal Knowledge Graphs and Transformer-Based Retrieval for Deductive Reasoning

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Abstract

The ability to extract and verify factual information from free-form text is critical in an era where vast amounts of unstructured data are available, yet unreliable sources abound. This paper focuses on enhancing causal deductive reasoning, a key component of factual verification, through the lens of accident investigation, where determining the probable causes of events is paramount.

Deductive reasoning refers to the task of drawing conclusions based on a premise. While some deductive reasoning benchmarks exist, none focus on causal deductive reasoning and are from real-world applications. Recently, large language models (LLMs) used with prompt engineering techniques like retrievalaugmented generation (RAG) have demonstrated remarkable performance across various natural language processing benchmarks. However, adapting these techniques to handle scenarios with no knowledge bases and to different data structures, such as graphs, remains an ongoing challenge. In our study, we introduce a novel framework leveraging LLMs' decent ability to detect and infer causal relations to construct a causal Knowledge Graph (KG) which represents knowledge that the LLM recognizes. Additionally, we propose a RoBERTa-based Transformer Graph Neural Network (RoTG) specifically designed to select relevant nodes within this KG. Integrating RoTG-retrieved causal chains into prompts effectively enhances LLM performance, demonstrating usefulness of our approach in advancing LLMs' causal deductive reasoning capabilities.

1 Introduction

Large language models (LLMs) have shown impressive performance on some language tasks, however, their ability to plan and reason on complex tasks remains an ongoing challenge (Wei et al., 2022; Valmeekam et al., 2023). In Psychology, the standard test for deductive reasoning consists of giving people premises and asking them to draw conclusions (Evans, 2005; Rips, 1994; Johnson-Laird, 2010). In natural language processing (NLP), RuleTaker (Clark et al., 2020) and ProofWriter (Tafjord et al., 2021) are datasets that challenge models to assign True or False labels to statements about a probable implication. However, there are no NLP benchmarks on causal deductive reasoning, where the premise are facts about an outcome and the statement is about a probable cause. Furthermore, Huang and Chang (2023); Valmeekam et al. (2022) find that current benchmarks do not truly investigate the reasoning capabilities of LLMs, because the tasks are not meaningfully applied in the real-world.

Researchers have proposed prompt engineering techniques to improve few-shot and zero-shot task performance (Reynolds and McDonell, 2021), like using role-play (Kong et al., 2023; Wang et al., 2023), in-context learning (Xie et al., 2022; Min et al., 2022), and retrieval-augmented generation (RAG) (Lewis et al., 2020; Shao et al., 2023). Recent work has explored using LLMs to retrieve a task-relevant knowledge sub-graph to support reasoning (Li et al., 2024). However, extending these techniques to handle cases where no explicit

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knowledge base is available, or and how to best use knowledge graphs (KGs) in a RAG-based LLM system remains an open area for research.

This paper focuses on the causal deductive reasoning task performed by Accident Investigators. When an accident occurs, investigators conduct thorough investigations, and come up with a probable cause for the accident. Our main contributions can be summarized as follows:

- We present a task (Section 2) and dataset (Section 3) comprising 631 reports with 11,422 statements. This dataset is curated from original reports written by humans and processed using rules and Claude 2.1. It will be made publicly available.
- We introduce a framework (Figure 1) employing LLMs such as Mistral-Instruct 7B to identify causal relations for constructing a causal KG. Additionally, we trained a RoBERTabased Transformer Graph Neural Network (RoTG) to select relevant nodes, leveraging deductive reasoning labels as an auxiliary task. (Section 4)
- We observe that incorporating causal relations retrieved from the LLM-constructed KG improves the LLM's causal deductive reasoning performance. (Section 5)

2 Causal Deductive Reasoning

Given an input context C, the goal is to identify the likelihood of a statement s_i being a probable cause of accident a. This likelihood is represented by $y_i \in (0,1)$, where $y_i = 1$ if s_i is a probable cause and $y_i = 0$ if not. The task is to determine $P(y_i|C)$ for each potential cause s_i within a report context C. Since we have multiple reports in our dataset, the objective extends to calculating $P(y_{it}|C_t)$, where t denotes the report ID. We define $G_t = F_{extract}(C_t)$ as the set of causal relations mentioned in context C_t . The function $F_{extract}(.)$ extracts causal relations from the context. The aggregated set of all extracted relations from the dataset is denoted as G, representing the repository of causal relations of our dataset. Each relation in G_t is represented by a cause and effect pair, denoted as (s_i, s_j) .

If a causal chain $x_{it} = (s_i, s_{j1}), (s_{j1}, s_{j2}), ..., (j_k, k) \notin G_t$, then $y_i = 0$. However, if $x_{it} \in G_t$, the rank of y_{it} relative to other potential causes y_{jt} must be considered. Only the top z rank of most important causes can be the probable cause of an accident a. In the case where we only consider the top cause (z = 1) as the probable cause, then the probability of $P(y_{it})$ can be reformulated into:

$$P(y_{it} = 0) = P(y_{it} | x_{it} \notin G_t) + P(y_i | x_{it} \in G_t, P(y_{jt} = 1) > P(y_{it} = 1))$$

$$P(y_{it} = 1) = P(y_{it} | x_{it} \in G_t)$$

$$(1)$$

$$P(y_{it} = 1) = P(y_i | x_{it} \in G_t, P(y_{it} = 1) > P(y_{jt} = 1))$$
(2)

Since the task is a binary classification task, every example s_{it} is not aware of the other possible s_{jt} for the same report t. Therefore, s_{jt} are causes the model implicit tracks and has to rank against for the current task. Our causal deductive task can be re-framed into two sub-challenges: (1) extracting x_{it} and identifying $x_{it} \in G_t$, and (2) implicitly ranking $P(y_{it} = 1) > P(y_{jt} = 1)$ or not.

Hypothesis 1: Generalizing causal chain to outof-context In the first challenge, extracting x_{it} and identifying $x_{it} \in G_t$, restricting the knowledge source to a report results in a high chance for there to be gaps in the causal chain. All else fixed, $P(y_{it}|x_{it} \notin G_t)$ will be overestimated (i.e., model predicts more 0s than 1s). If are willing to relax our criteria to check if $s_i \in C_t$ and $x_{it} \in G$, then we are allowing our model to generalize to its own knowledge base, to recognize more valid causal chains, and therefore, increase the probability of predicting $P(y_{it} = 1)$. When working with LLMs, therefore, we could inject causal relations outside of G_t but semantically part of x_{it} to improve prediction.

Hypothesis 2: Ranking importance of cause within context If the LLM is exposed to too many relevant causal relations in the prompt, it would hallucinate and start to always view s_i as the most important probable cause (over other possible options in C_t). However, we do not know z. In some reports, there are a few probable causes. One approach is to explicitly expose the LLM to the available causes in the report, so that we re-ground the response, and in some way, a ranking based on context is encouraged.

3 Dataset & Task Creation

We wish to investigate the LLMs' ability to perform a real-world causal deductive reasoning task.



Figure 1: Overview of our proposed methodology. Detailed infographic is available in Appendix Figure 4.

Given an accident description (<CONTEXT>), the model must determine if a sentence about the probable cause of the accident (<STATEMENT>) is *True* or *False*. To facilitate our research, we leverage on reasoning-rich investigation reports from the National Transportation Safety Board (NTSB)¹. NTSB publishes Accident Reports that provides details about an accident, analysis of the factual data, conclusions and the probable cause of the accident, and the related safety recommendations. There can be one or multiple probable cause(s). We downloaded reports published after Year 2000, across all reported categories (Aviation, Hazardous Materials, Highway, Marine, Pipeline and Railroad).

Report pre-processing Pre-processing was done to convert the PDF reports to JSON, and subsequently, we removed information like headers, page numbers, and table of contents. We identified the probable cause of the accident by searching for the title "Probable Cause". We discarded reports where this match was impossible. Any text before this section is defined as the <CONTEXT>. In our experiments, we constrained our coverage to 157 reports where the context length is $\leq 2,000$ words.

Extracting *True* **statements** Trailing descriptions in the probable cause were removed. ² We used Anthropic's Claude 2.1^3 to convert the para-

¹https://www.ntsb.gov/investigations/ AccidentReports/Pages/Reports.aspx graphs into a list of probable causes. Prompt 1 in Appendix outlines the one-shot prompt template that we used. We manually annotated four examples to measure the extraction performance, of which we found ROUGEL score of 87.46 and BLEU4 score of 75.02. When evaluating by semantic match⁴ with a threshold of ≥ 0.7 as a match, Claude 2.1 scored 100% for Recall, 72.92% for Precision, and 84.34% for F1. To summarize, the high scores for the evaluated sample provides us with the confidence to reliably use the extracted probable causes as *True* instances for our main causal deductive task.

CONTEXT	
The P. B. Shah captain erred when he initiated a port-to-port (one whistle) pas the radio with the Dewey R captain. He had meant to arrange a starboard-to (two-whistle) passing, but the captain was distracted by the many tasks ass with preparing for his arrival at the Ingram facility. This included having a cell conversation with the boat store to discuss a grocery delivery and meeting with to discuss upcoming tasks, both around the same time the passing arrangement	starboard sociated phone the mate
made with the Dewey R. "Sliding underneath the point" is an action described by	y pilots
made with the Dewey R. "Sliding underneath the point" is an action described by STATEMENT The probable cause of the accident was	/ pilots
STATEMENT The probable cause of the accident was the impact of distraction upon the decision making and recollection of the	LABEL
STATEMENT The probable cause of the accident was the impact of distraction upon the decision making and recollection of the captain of the P. B. Shah.	LABEL True
STATEMENT The probable cause of the accident was the impact of distraction upon the decision making and recollection of the captain of the P. B. Shah. the distraction of the captain on the Loretta G. Cenac from safety-critical	LABEL True False

Figure 2: An example report from our dataset.

Generating *False* **statements** False examples were generated by two methods: (1) rule-based, and (2) LLM-based methods. For rule-based, each

²E.g. Descriptions unrelated to the cause (E.g. "*The National Transportation Safety Board determines that the*") were removed.

³We intentionally used an LLM different from Mistral when creating our dataset to avoid cases where the LLM rec-

ognizes its own phrasing or terms.

⁴We encoded each probable cause item into an embedding using the princeton-nlp/sup-simcse-roberta-large encoder (Gao et al., 2021) that was pre-trained on the Natural Language Inference task. Link to their repository: https: //github.com/princeton-nlp/SimCSE.

Processing	#Docs	#Statement	#True	#False	True %
Total NTSB	631	11,422	1300	10,122	11.38%
≤ 2000 words	157	2,523	243	2,280	9.63%
Success CRE	133	1,677	155	1,522	9.24%

Table 1: Data sizes at each filtering stage. The last row represents the working dataset for this paper after successful causal relation extraction (CRE). Our experiments are conducted using 10-folds CV, and the test data sizes per fold are provided in Appendix Table 6.

True statement was matched to three similar-butnot-too-similar statements are generated as negative examples. The degree of similarity between the *False* examples and the *True* statement was controlled to ensure that false examples are plausible but distinct from the true statement, with similarity scores ranging from 0.5 to 0.75. This approach aims to provide a challenging set of false examples for participants to evaluate. For LLM-based, we used Claude 2.1 (See Prompt 2 in the Appendix) to generate a list of 10 possible causes or contributing causes investigated within the context that are not stated as the final true probable cause.

Our task aims to provide a comprehensive evaluation of participants' ability to perform the challenging causal deductive reasoning task. Table 1⁵ presents the statistics for our dataset. After keeping examples that we could extract causal relations described in the next section, our main dataset comprises of 133 reports and 1,677 statements. Of which, 155 are *True* while the remaining 1,522 are *False* probable cause statements. An example report is shown in Figure 2.

3.1 Evaluation Metrics

For each experiment, we report Macro F1, Micro F1 and the accuracy scores for each class label and label source. Since our dataset is small, we used a 10-fold cross validation (split by report ID) to train and generate predictions for the full dataset. Therefore, our evaluation metrics are first computed at the fold level, then averaged, where both the mean and standard deviations of each metric are reported. When making comparisons between two models, P-values are indicated by: * < 0.15, ** < 0.10, *** < 0.05.

4 Causal KG RAG with LLM

We mentioned in Section 2 that we wish to help the LLM recognize generalized $(j_a, j_b) \in D$ by injecting relevant causal relations outside of G_t . However, we do not have a knowledge base for G. We also do not have any annotations for the intermediate causal chains that might be relevant given a probable cause i and accident a. To work around these problems, we constructed our knowledge base using the LLM itself. Afterwhich, we designed a novel graph-based retriever model, trained on the auxiliary binary classification task, to select relevant nodes.

4.1 Step 1. Mining LLM's Latent Causal KG

We wish to investigate properties regarding Equations 1 and 2. However, we do not have a knowledge base. Therefore, we separately tasked the LLM to mine the causal relations it recognizes and understands. Specifically, we mined two types of causal relations:

Extracted causal relations We tasked the LLM to extract all causal relations expressed within the <CONTEXT>. Prompt 3 in the Appendix outlines our zero-shot prompt, with only instructions about the desired output format.

Inferred causal relations We tasked the LLM to infer the chain of causal relations that could possibly link the cause stated within the \langle STATEMENT \rangle to the accident stated within the \langle CONTEXT \rangle . Prompt 4 in the Appendix outlines our zero-shot prompt, with only instructions about the desired output format. The causal chains from this step can be viewed as the LLM's hallucinated version of x_{it} .

Causal KG To maximize the size of our knowledge store, we constructed our heterogeneous causal knowledge based on a slightly larger dataset of 157 reports and 2,523 statements, which provided us with 4,128 extracted cause-effect pairs and 22,685 inferred cause-effect pairs. Reports with contexts longer than 2,000 words did not fit into our models' input context, so we did not explore the full dataset, although it would be an important future work to extend the size of the knowledge store further.

Our KG G = (V, E) is a collection of nodes $V = \{(v_1, v_2, ..., v_n)\}$ and directed edges $E = \{(v_1, v_2), (v_2, v_3), ...\}$. The edges are directed, and comprises of three possible types: extracted, inferred, or similar. For extracted and inferred relations, a directed edge (v_x, v_y) represents the presence of causality between the two nodes, where v_x is the cause argument and v_y is the effect ar-

⁵We will release the full dataset of 11,422 statements to the community.

gument. To prevent a sparse graph, prior causal KG research employ various clustering (Tan et al., 2023) or generalization (Radinsky et al., 2012) methods to group semantically similar arguments together. For us, we opted for a simple (and shown to be effective in Section 5.1) approach by adding bidirectional edges between two nodes v_x and v_y , weighted by the similarity score ss, for all node pairs with similarity score ss > 0.7. Overall, our final G is a collection of 16,675 nodes and 23,493 edges. The distribution of edge types are: 1,822 extracted, 11,399 inferred, and 10,272 similar.

4.2 Step 2. Node Selection over Causal KG

We re-frame our retrieval task as a node classification task: Given a causal KG, we wish to extract the most important and relevant nodes (arguments) to include in our downstream prompt. Since we have no labels as to what helps the LLM learn, we used the the binary classification task (to classify if a <STATEMENT> is *True* or *False*) as an auxiliary task to train our model. The model is encouraged to learn from the KG, and at inference, we discard the classification head and keep top-E nodes with highest node weights as pointers to obtain information for RAG.

Our retriever module uses a RoBERTa-based Transformer GNN (RoTG) framework. Since a traditional RoBERTa model (Liu et al., 2019)'s input token limit of 512 is too small for our reports, we designed a workaround that does not require the long <CONTEXT> sequences as inputs. Our model is trained only by the following inputs: (1) Encoded <STATEMENT> (r_i represents the [CLS] token vector with *e* features) and (2) A one-hot encoded vector (*oh*) assigned to each node if the span does appear in the extracted or inferred causal relations (1 if appear, 0 otherwise).

Node classification module Our initial node features were represented by Q_1 , an attended representation of Q'_1 . Q'_1 is a concatenation of the RoBERTa-encoded frozen embeddings for each node description s (R is a $n \times e$ matrix comprising of n nodes, an input that does not change over training) and the two one-hot vectors (oh_{extr}, oh_{inf}) indicating if the node was extracted or inferred based on the context and target statement or not. The attention mechanism then computes the attention weights between the node features Q'_1 and the target statement embedding r_i to generate the cross-attended node feature matrix Q. Since our graph is heterogeneous, we require message passing across edge features. Hence, we employed the Transformer (Vaswani et al., 2017) Graph Convolutional Network (TransformerGCN) (Shi et al., 2021), which helps to incorporate edge features into the multi-head attention for graph learning. The architecture of TransformerGCN is outlined in Appendix Section D.1.

$$r_i = \text{RoBERTa}(s_i) \tag{3}$$

$$R = \text{RoBERTa}(S) \tag{4}$$

$$Q'_1 = [R, oh_{\text{extr}}, oh_{\text{inf}}]$$
(5)

$$Q_1 = \text{Attention}(Q'_1, r_i, r_i) \tag{6}$$

$$pw_i = \text{TransformerGCN}(G_{(Q_1,E)})$$
 (7)

Auxiliary task training We multiplied the local graph weights ow_i onto the global node embeddings R, obtaining our node embeddings Q_2 that are now customized for our inputs. We proceeded with another round of message passing using TransformerGCN over our global graph, and obtained a vector representing the scores each node contributes (nw_i). We incorporated a skip-connection by concatenating nw_i with the original statement embedding r_i and applied dropout and layer normalization layers to get o_i . Subsequently, we ran o_i through multiple rounds of Linear layers, with LeakyReLU in between. In the last layer, we used a Linear layer with output dimension of 2 to obtain logits for our binary classification task.

$$ow'_i = \text{topKGating}(ow_i)$$
 (8)

$$Q_2 = ow_i' R \tag{9}$$

$$iw_i = \text{TransformerGCN}(G_{(Q_2,E)})$$
 (10)

$$o_i = \text{LayerNorm}(\text{Dropout}([r_i, nw_i]))$$
 (11)

$$o_i^{(l+1)} = W^{(l)}o_i^{(l)} + b^{(l)}$$
(12)

Each model was trained for 8 epochs, with an effective batch size of 8. Since our dataset is extremely unbalanced (9% *True* only), we also balanced class labels by oversampling *True* examples, such that the ratio is 1:2 for *True:False*, then included the post-oversampling class weights into the CrossEntropyLoss function. Model specifics are provided in Appendix Section B.

4.3 Step 3. Prompt Engineering with LLM

During inference, we selected the top-E nodes with the highest scores based on node weights, ow_i . Subsequently, we obtained the nodes' original reports' extracted or inferred causal chains, then kept

	Macro F1	Micro F1		Accuracy	
		WIICIO I'I	True	False (Rules)	False (LLM)
All	55.43 (6.09)	83.96 (9.07)	31.01 (31.19)	67.44 (34.41)	99.45 (0.86)
Similarity Only	56.97 (6.05)	82.75 (8.39)	34.70 (26.65)	66.77 (25.59)	98.14 (5.22)
Causality Only	56.90 (6.62)	81.48 (9.35)	39.56 (30.79)	60.62 (30.83)	97.92 (5.63)

Table 2: RoTG classification performance when trained over different edges types in G. Highest score per column is in bold. All scores are not statistically significant from the first row.

Relations	Macro F1	Micro F1		Accuracy	
Retrieved	Iviació I'i	WIICIO I'I	True	False (Rules)	False (LLM)
None	70.36 (7.07)	90.30 (1.78)	46.53 (13.21)	92.23 (3.66)	95.69 (1.86)
Semantic	72.50 (6.37)	91.24 (1.40)	48.72 (11.04)	92.99 (2.48)	96.54 (1.93)
RoTG	73.19 (7.01)	91.65 (1.42)**	49.49 (13.47)	94.31 (3.49)	96.37 (1.37)

Table 3: Mistral Instruct with *None*, Semantic, and RoTG (Ours) retrieval-augmented relations. Highest score per column is in bold. P-values against *None* scores indicated by: * < 0.15, ** < 0.10, *** < 0.05.

all chains that contain the node span. We investigated 9 distinct prompt formats (see Prompts 5 to 13 in the Appendix), incorporating variations of retrieved, extracted, and inferred causal relations. Our best-performing prompt format (Prompt 10) consists of retrieved information that were presented as a multi-turn prompt: Initially, retrieved relations were introduced to the model. Next, we set the models' response to be "*Yes I understand*.". Finally, a description of the task followed in the subsequent reply. We found that including the retrieved information in the same responses as the task description led to poor performance.

All relations underwent post-processing to remove similar causal chains, defined by a Levenshtein ratio ≥ 0.8 , with duplicates resolved by retaining only the first instance. Additionally, we limited each relation type to the first 10 rows of causal chains. Subsequent experiments revealed that such cleaning procedures enhanced the model's F1 scores. We categorized a model response as *False* if the word "False" appeared in any part of the response, and *True* otherwise. Due to the length of the reports, particularly when utilizing Mistral as our LLM, in-context learning was not feasible. Consequently, all experiments were conducted in a zero-shot manner.

5 Experimental Findings

This paper focuses the investigation on the Mistral-Instruct 7B LLM (Jiang et al., 2023). We used Mistral to extract and infer causal relations for our KG as described in Section 4.1, then trained RoTG over this KG as described in Section 4.2. Finally, we tested Mistral on the causal deductive reasoning task as described by Section 4.3.

5.1 Auxiliary Task Performance

Investigating RoTG's performance on the causal deductive task serves as a proxy of how helpful would the LLM's latent causal KG be for this task. From the first row of Table 2, we notice that RoTG achieves reasonable Macro F1 score of 55.43%. The model performs very well on identifying LLMgenerated False statements, but struggle with semantically similar False statements. We wish to understand if our task can be performed without understanding causality in the first place. To investigate this, we destroyed all causal edges in G, and retrained the model on the task. Interestingly, we find that all scores decline from the initial baseline, but not by too much. This suggests that while causal edges are still important to the task, as long as some understanding of similarity between events in a KG exists, models can still perform the task. Conversely, we wish to understand the importance of our similarity edges. When we destroyed similartype edges, we noticed a significant increase in the accuracy for the True prediction (along with the fall in accuracy for False prediction). Without similarity edges, the model focuses only on causal edges and in return, over-weighs the probability of a causal statement. To conclude this subsection, RoTG demonstrates that we can perform the causal deductive task reasonably well by only relying on extracted and inferred causal relations from LLM. This presents us with a lower bound of what the LLM can understand. In Appendix Section D.3, we investigated RoTG's performance across different K values. We found that a concave relationship across top-K and F1 scores, but the differences are not statistically significant when comparing

K = 4,096 to K = 8,192 or more.

5.2 LLM's Deductive Reasoning Performance

In this section, we directly test the LLM on the causal deductive reasoning task. Table 3 presents the main findings while the full findings are available in Appendix Table 8. Our proposed RoTG method (73.19% Macro F1 and 91.65% Micro F1) outperforms the baseline (70.36%) Macro F1 and 90.30% Micro F1) and also improved the LLM's accuracy for all class labels. The improvement for Micro F1 is statistically significant with P-value < 0.10. To provide an alternative baseline, we retrieved semantically similar causal relations for every causal relation extracted or inferred in a report. We encoded arguments (Cause span and Effect span) using sentence-transformers/all-mpnet-base-v2 then did vector embedding search using FaissSearcher (Douze et al., 2024). Similar truncation and cleaning procedures were done as per RoTG. Mistral's performance also improves when we inject these semantic causal relations, however, the improvement is slightly smaller than ours and unlike ours, is not statistically significant.

5.2.1 Which types of causal relations help?

In Hypothesis 1 of Section 2, we hypothesized that injecting causal relations outside of G_t but semantically part of x_{it} would improve prediction, or at least increase the likelihood of predicting *True*. Apart from exposing the model to semantic or RoTG relations, which both increased accuracy of *True* (46.53% (Row 1) compared to 48.72% (Row 5) and 49.49% (Row 7) in Table 4), we could also inject the inferred causal relations in the prompt. As expected, the accuracy for *True* in the baseline model increases to 55.99% (Row 3).

However, consistent with Hypothesis 2 of Section 2, accuracy for *False* falls significantly. This fall is slightly mitigated if we inject the extracted causal relations alongside the inferred causal relations (Row 4), supporting our grounding hypothesis. With either semantic or RoTG retrieved relations, injecting extracted relations have a negligible effect, suggesting when relations out of G_t are shown, hallucination is less of an issue, and grounding is unnecessary.

Overall, we find that we need to expose the LLM to relevant causal relations outside of the report's relations G_t to increase accuracy of *True* predictions (Hypothesis 1). However, if the inferred relations

are included (relations partially in G_t , partially not), LLMs might take the provided causal chains to be the truth, and so grounding becomes helpful (Hypothesis 2). The best balance between the two would be to incorporate retrieved relations (relations $\notin G_t$), so that the model can better focus on learning about causality instead of being confused by the truthfulness of the given chain.

5.2.2 Does the number and quality of RoTG relations matter?

We described our post-processing steps for causal relations in Section 4.3. In Table 5, we investigate if we do not truncate to first 10 causal relations (No truncate), and if we do not post-process at all (No cleaning). In general, we did not find lower statistically significantly different scores. For the RoTG relations only prompt, the LLM performed best with truncation and de-duplication. For the RoTG and extracted relations prompt, the LLM performed best if we do not clean the RoTG relations. This again suggests that ensuring more retrieved relations outside of C_t , as opposed to re-exposing the model to relations from C_t , are more helpful.

5.2.3 Investigating the generation probability

We investigated the generation probabilities of the model by tracking the logits of the "True" and "False" token at the first utterance of the "True" / "False" token. We comparing the model with and without our RoTG relations, and notice that for the 1446 examples where both models correctly predicted False, our RoTG model returned an average False probability of 3.39%, while the baseline model had a probability of 2.07%. Meanwhile, for the 69 examples where both models correctly predicted True, our RoTG model returned an average True probability of 47.02%, while the baseline model had a probability of 35.60%. There are two interesting findings from here: (1) Apart from returning a higher F1, incorporating RoTG-relations helps the model become more confident in its predictions for the overlapping correct examples. (2) On average, we found that it takes the model a much higher probability to generate the True token than it takes for it to generate the False token. When models generate True, the next most likely word is almost always False. Meanwhile, for False predictions, the probabilities are small and more spread across all possible tokens in the models' dictionary. More investigation is needed to explain why this is the case.

S/N		Relatio	ns	Macro F1	Micro F1		Accuracy	
5/19	Extract	Infer	Retrieved		WIICIO I'I	True	False (Rules)	False (LLM)
1			None	70.36 (7.07)	90.30 (1.78)	46.53 (13.21)	92.23 (3.66)	95.69 (1.86)
2	\checkmark		None	72.42 (7.19)	90.59 (2.52)	52.62 (13.79)	91.73 (4.22)	95.60 (2.06)
3		\checkmark	None	63.97 (4.87)***	83.15 (2.85)***	55.99 (11.38)*	78.56 (4.79)***	89.03 (4.35)***
4	\checkmark	\checkmark	None	63.66 (5.31)***	84.10 (2.53)***	50.36 (12.18)	80.12 (4.66)***	90.65 (3.38)***
5			Semantic	72.50 (6.37)	91.24 (1.40)	48.72 (11.04)	92.99 (2.48)	96.54 (1.93)
6	\checkmark		Semantic	70.97 (4.69)	90.67 (2.11)	45.54 (7.10)	91.70 (4.21)	96.91 (1.89)
7	\checkmark	\checkmark	Semantic	64.48 (6.02)***	86.83 (2.27)***	41.81 (12.63)	86.19 (4.56)***	93.59 (2.44)***
8			RoTG	73.19 (7.01)	91.65 (1.42)	49.49 (13.47)	94.31 (3.49)	96.37 (1.37)
9	\checkmark		RoTG	71.15 (6.40)	91.09 (2.14)	44.07 (10.02)	93.43 (3.89)	97.02 (1.63)
10	\checkmark	\checkmark	RoTG	64.21 (7.89)***	87.28 (3.23)***	37.98 (13.90)**	87.21 (4.02)***	94.46 (2.79)**

Table 4: Mistral Instruct with various relations included into prompt. Highest score per column is in bold. P-values against scores from the first row per line-separated section is indicated by: * < 0.15, ** < 0.10, *** < 0.05.

Retrieved	Relations	Macro F1	Micro F1		Accuracy	
Processing	Extracted	Macio Fi	MICIO FI	True	False (Rules)	False
		73.19 (7.01)	91.65 (1.42)	49.49 (13.47)	94.31 (3.49)	96.37 (1.37)
No truncate		72.92 (6.43)	91.60 (1.11)	48.87 (12.59)	93.75 (3.24)	96.66 (1.04)
No cleaning		71.93 (5.57)	91.19 (1.37)	46.53 (8.61)	94.01 (3.72)	96.38 (1.03)
	\checkmark	71.15 (6.40)	91.09 (2.14)	44.07 (10.02)	93.43 (3.89)	97.02 (1.63)
No truncate	\checkmark	70.96 (6.69)	90.95 (2.07)	44.50 (11.16)	93.43 (3.89)	96.73 (1.70)
No cleaning	\checkmark	71.52 (5.94)	91.12 (2.16)	45.04 (9.33)	93.28 (4.17)	97.13 (1.38)

Table 5: Mistral Instruct with RoTG retrieval-augmented relations post-processed using three strategies: (1) With truncation (first 10) and de-duplication, (2) Without truncation but with de-duplication, (3) Without truncation and without de-duplication. Highest score per column is in bold.

6 Related Work

Our dataset and task is most relevant to the deductive reasoning NLP literature, like efforts by Rule-Taker (Clark et al., 2020) and ProofWriter (Tafjord et al., 2021). Different from them, our dataset is a real-world deductive reasoning task about accident investigations, and dive deep into the causal aspect. Huang and Chang (2023); Valmeekam et al. (2022) stated that current reasoning benchmarks are not meaningfully applied in the real-world. Thus, we hope that our dataset and work allievates this gap in the literature.

Our methodology is relevant to literature on RAG for LLMs (Gao et al., 2024). However, due to the nature of causal relations in our task, we focus on retrieval techniques over a graph. Thus, we were also inspired by prior research on retrieval on KGs (Liu et al., 2018; Reinanda et al., 2020) and on node classification (Shi et al., 2021; Xiao et al., 2022). Since encoding graph structured data for LLMs is also an ongoing research (Fatemi et al., 2023; Per-ozzi et al., 2024), more investigations on how to best present the causal chains in the prompts are needed. Different from previous works, we investigate how to leverage on knowledge already present in the dataset (extract) and within the LLMs (infer) to improve performance, instead of relying on

external databases that many RAG methodologies focus on.

7 Conclusion

Our study addresses the challenging task of causal deductive reasoning, particularly within the context of real-world Accident Investigation reports. Firstly, we introduced a framework that constructs a causal KG based on what LLMs' can extract and infer. Secondly, we proposed RoTG, trained to select relevant nodes, utilizing deductive reasoning labels as an auxiliary task. Our experiments demonstrate that incorporating RoTG relations into the prompt enhances the performance of LLMs (from 70.36% (90.30%) to 73.19% (91.65%) Macro (Micro) F1), highlighting the effectiveness of integrating graph-based retrieved relations in improving LLMs' causal deductive reasoning abilities. Lastly, our dataset will be released and will be a valuable resource for researchers. Overall, our study advances the understanding and application of deductive reasoning tasks in NLP, specifically in the domain of KG-based RAG for LLMs.

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A Limitations & Ethics Statement

Our investigations are confined to findings derived from Mistral-Instruct, as such, the generalizability of our results to other LLMs may be limited. Future research should aim to explore a broader range of LLM architectures to gain a more comprehensive understanding of the phenomena under investigation. All datasets are attributed to the National Transportation Safety Board (NTSB), "Courtesy: National Transportation Safety Board."

B Experimental Details

Claude 2.1 inference

- Model = anthropic.claude-v2:1
- Max tokens to sample = 1000 for extracting causes as a list, 1800 for generating *False* statements
- Temperature = 0.5

RoTG training

- Encoder = roberta-base
- Local graph node dim = 770
- Global graph node dim = 768
- Num layers in GNN = 4
- Top-K = 4096
- Dropout = 0.1
- Post-GNN to Auxiliary Clf Layers:
 - Linear1 Out Dim = 128
 - Linear2 Out Dim = 64
 - Linear3 Out Dim = 2
- CrossEntropyLoss with class weights, reduction='mean'
- Top-E = 3

Mistral-Instruct inference

- Model = Mistral-7B-Instruct-v0.1
- Max new tokens = 1500
- Temperature = 0.5

C Dataset & Task Creation

C.1 Prompts

Prompt 1: Prompt for extracting probable causes into a list.

INSTRUCTIONS

Please help to extract the key Causes into point forms based on a paragraph bounded by [START_CONTEXT] and [END_CONTEXT].

Fold#	#Statements	#True	#False
1	159	10	149
2	169	15	154
3	191	14	177
4	179	15	164
5	185	18	167
6	169	11	158
7	151	16	135
8	138	16	122
9	168	26	142
10	168	14	154

Table 6: Count of examples per fold by class labels.

Do not add any explanations, or leading or trailing descriptions. Add as many bullet points as needed to exhaustively extract all stated Causes.

EXAMPLE

[START_CONTEXT]

The probable cause of the employee fatality at the Dyno Nobel facility was a result of the conductor being impacted by the moving railcars during a shoving movement while located in an area with insufficient walking space available for the employee to perform trackside duties. [END_CONTEXT]

Expected Output:

```
[START_CAUSES]
```

 Conductor impacted by the moving railcars during a shoving movement
 Accident was located in area with insufficient walking space available for the employee to perform trackside duties [END_CAUSES]

TASK

Prompt 2: Prompt for generating negative causal examples.

Based on the following accident investigation bounded by <CONTEXT> delimiters, the true probable cause(s) are provided within <CAUSES> delimiters. Given these information, provide a list



Figure 3: First page of an NTSB report in PDF.

of 10 possible causes or contributing causes investigated within the context that is not stated as a final true probable cause. Your output should only contain a list of 10 enumerated statements/sentences with no explanation. <CAUSES> {causes} </CAUSES>

<CONTEXT> {context} </CONTEXT>

D Mining Causal Knowledge in LLMs

Figure 4 provides a detailed outline of our proposed methodology, corresponding to the descriptions in Section 4.

D.1 TransformerGCN architecture

We introduced the overall structure of our RoTG model in Section 4.2. This section outlines the detailed model architecture for TransformerGCN (Shi et al., 2021).

Our initial node features are represented by Q,

an attended representation of Q'. Q' is a concatenation of the RoBERTa-encoded embeddings for each node description s and the two one-hot vectors $(oh_{\text{extr}}, oh_{\text{inf}})$ indicating if the node is extracted or inferred to the target statement s_i or not. The attention mechanism then computes the attention weights between the node features Q' and the target statement embedding r_i to generate the crossattended node feature matrix Q.

$$r_i = \text{RoBERTa}(s_i) \tag{13}$$

$$R = \text{RoBERTa}(S) \tag{14}$$

$$Q' = [R, oh_{\text{extr}}, oh_{\text{inf}}]$$
(15)

$$Q = \text{Attention}(Q', r_i, r_i) \tag{16}$$

Our graph G is equivalently represented by the adjacency matrix $A = [a_{ij}] \in \mathbb{R}^{n \times n}$. The diagonal degree matrix is denoted by D =diag (d_1, d_2, \ldots, d_n) , where $d_i = \sum_j a_{ij}$ is the degree of node *i*. A normalized adjacency matrix is defined as $D^{-1}A$ or $D^{-\frac{1}{2}}AD^{-\frac{1}{2}}$.

A typical GCN transforms and propagates node features across the graph by several layers to build the approximation of the mapping of input to output. In other words, the feature propagation scheme



Figure 4: Detailed outline of our proposed methodology.

K Value	Macro F1	Micro F1		Accuracy	
		MICIO I'I	True	False (Rules)	False (LLM)
2048	54.12 (6.55)	79.99 (9.80)*	34.46 (29.03)	57.20 (35.58)*	97.78 (4.44)
4096	55.43 (6.09)	83.96 (9.07)	31.01 (31.19)	67.44 (34.41)	99.45 (0.86)
8192	56.06 (6.53)	86.17 (6.09)	24.10 (20.63)	77.03 (21.26)	99.82 (0.38)
All ∽16K	53.98 (5.79)	83.75 (10.40)	28.27 (32.49)	68.04 (37.25)	99.65 (0.84)

Table 7: Mean (Std) F1 and Accuracy across different K values for Top-K Gating. Highest score per column is in bold. P-values against K=8192 scores indicated by: * < 0.15.

of GCN in layer l is:

$$H^{(l+1)} = \sigma \left(D^{-1} A H^{(l)} W^{(l)} \right)$$
 (17)

$$Y = f_{\text{out}}(H^{(L)}) \tag{18}$$

where σ is an activation function, $W^{(l)}$ is the trainable weight in the *l*-th layer, and $H^{(l)}$ is the *l*-th layer representations of nodes. $H^{(0)}$ is equal to node input features Q. Finally, an f_{out} output linear layer is applied on the final representation to make predictions Y for each node.

However, since our graph is heterogenous, we require message passing across edge features too. Therefore, TGCN helps by incorporating edge features into the multi-head attention for graph learning. Given node features $H^{(l)} = \{h_1^{(l)}, h_2^{(l)}, \ldots, h_n^{(l)}\}$, multi-head attention for each

edge j to i is computed as follows:

$$q_{c,i}^{(l)} = W_{c,q}^{(l)} h_i^{(l)} + b_{c,q}^{(l)}$$
(19)

$$k_{c,j}^{(l)} = W_{c,k}^{(l)} h_j^{(l)} + b_{c,k}^{(l)}$$
(20)

$$e_{c,ij} = W_{c,e}e_{ij} + b_{c,e}$$
 (21)

$$\alpha_{c,ij}^{(l)} = \frac{\exp(q_{c,i}^{(l)} \cdot k_{c,j}^{(l)} + e_{c,ij})}{\sum_{u \in N(i)} \exp(q_{c,i}^{(l)} \cdot k_{c,u}^{(l)} + e_{c,iu})}$$
(22)

where $h_{q,k}^{(l)} = \exp\left(\frac{q_{c,i}^{(l)} \cdot k_{c,j}^{(l)}}{\sqrt{d}}\right)$ is the exponential scale dot-product function and d is the hidden size of each head. For the c-th head attention, we transform the source feature $h_i^{(l)}$ and distant feature $h_j^{(l)}$ into query vector $q_{c,i}^{(l)} \in \mathbb{R}^d$ and key vector $k_{c,j}^{(l)} \in \mathbb{R}^d$ respectively using different trainable parameters $W_{c,q}^{(l)}, W_{c,k}^{(l)}, b_{c,q}^{(l)}, b_{c,k}^{(l)}$. The provided edge

features e_{ij} are encoded and added into the key vector as additional information for each layer.

After obtaining the graph multi-head attention, message passing and aggregation from the distant j to the source i is computed by:

$$v_{c,j}^{(l)} = W_{c,v}^{(l)} h_j^{(l)} + b_{c,v}^{(l)}$$
(23)

$$\hat{h}_{i}^{(l+1)} = \sum_{j \in N(i)} \alpha_{c,ij}^{(l)} (v_{c,j}^{(l)} + e_{c,ij}) \qquad (24)$$

where k is the concatenation operation for C head attention. This multi-head attention matrix replaces the original normalized adjacency matrix in Equation 17 as the transition matrix for message passing.

Finally, we apply a linear transformation to the last layer of node features $h_i^{(l)}$, obtaining a representation of local node weights (ow_i) , trained to represent how important this node is to the downstream task.

$$ow_i = W_{c,v}^{(l)} h_i^{(l)} + b_{c,v}^{(l)}$$
(25)

D.2 Prompts

Prompt 3: Prompt for extracting causal relations Extract all the causal events in this report:

{context}

```
Format the extracted Cause and Effect
events into a list, like:

1. Engineer's inattentiveness to signal
indications --> Engineer failed to
operate train in accordance with signal
indications and speed restriction -->
Train collided with another train

2. Lack of positive train control
system --> Train A not stopped before
red signal --> Train A passed red
signal --> Collision between Train A
and Train B
...
where "-->" represents "causes", so
"Cause Event --> Effect Event".
```

Answer:

Prompt 4: Prompt for inferring causal relations Based on your knowledge, suggest the series of Cause and Effect events that explain how the cause within the STATEMENT could have led to the accident in the CONTEXT. <STATEMENT> {statement} </STATEMENT> <CONTEXT> {context} </CONTEXT>

Format the suggested Cause and Effect events into a list, like: - Engineer's inattentiveness to signal indications --> Engineer failed to operate train in accordance with signal indications and speed restriction --> Train collided with another train (Accident) where "-->" represents "causes", so "Cause Event --> Effect Event".

Answer:

Prompt 5: Prompt V1 for causal deductive reasoning task.

Based on an accident investigation bounded by <CONTEXT> delimiters, answer if the statement within <STATEMENT> delimiters about the probable cause(s) of the accident is True or False. Your answer must be based on the investigation facts and details within <CONTEXT>.

```
<CONTEXT>
{context}
</CONTEXT>
```

Is this statement True or False?
<STATEMENT>
{statement}
</STATEMENT>

Answer:

Prompt 6: Prompt V2 for causal deductive reasoning task.

<s>[INST] You have a fair understanding of causal relations, where "-->" represents "causes". [/INST] Yes, I understand.</s> [INST] Based on an accident investigation bounded by <CONTEXT> delimiters, answer if the statement within <STATEMENT> delimiters about the probable cause(s) of the accident is True or False. Your answer must be based on the investigation facts and details within <CONTEXT>.

<CONTEXT> {context} </CONTEXT>

Is this statement True or False?
<STATEMENT>
{statement}
</STATEMENT> [/INST]

Answer:

Prompt 7: Prompt V3 for causal deductive reasoning task.

<s>[INST] You have a fair understanding of causal relations, where "-->" represents "causes". [/INST] Yes, I understand.</s> [INST] Based on an accident investigation bounded by <CONTEXT> delimiters, answer if the statement within <STATEMENT> delimiters about the probable cause(s) of the accident is True or False. Your answer must be based on the investigation facts and details within <CONTEXT>.

<CONTEXT> {context} </CONTEXT>

<RELATIONS> Relations extracted from <CONTEXT>: {extracted} </RELATIONS>

Is this statement True or False? <STATEMENT> {statement} </STATEMENT> [/INST]

Answer:

Prompt 8: Prompt V4 for causal deductive reasoning task.

<s>[INST] You have a fair understanding of causal relations, where "-->" represents "causes". [/INST] Yes, I understand.</s> [INST] Based on an accident investigation bounded by <CONTEXT> delimiters, answer if the statement within <STATEMENT> delimiters about the probable cause(s) of the accident is True or False. Your answer must be based on the investigation facts and details within <CONTEXT>.

<CONTEXT> {context} </CONTEXT>

<RELATIONS> Possible relations linking probable cause in <STATEMENT> to accident: {inferred} </RELATIONS>

Is this statement True or False?
<STATEMENT>
{statement}
</STATEMENT> [/INST]

Answer:

Prompt 9: Prompt V5 for causal deductive reasoning task.

<s>[INST] You have a fair understanding of causal relations, where "-->" represents "causes". [/INST] Yes, I understand.</s> [INST] Based on an accident investigation bounded by <CONTEXT> delimiters, answer if the statement within <STATEMENT> delimiters about the probable cause(s) of the accident is True or False. Your answer must be based on the investigation facts and details within <CONTEXT>.

<CONTEXT> {context} </CONTEXT>

<RELATIONS> Relations extracted from <CONTEXT>: {extracted} Possible relations linking probable cause in <STATEMENT> to accident: {inferred} </RELATIONS>

Is this statement True or False?
<STATEMENT>
{statement}
</STATEMENT> [/INST]

Answer:

Prompt 10: Prompt V6 for causal deductive reasoning task.

<s>[INST] You have a fair understanding of causal relations, where "-->" represents "causes", such as: {retrieved} [/INST] Yes, I understand.</s> [INST] Based on an accident investigation bounded by <CONTEXT> delimiters, answer if the statement within <STATEMENT> delimiters about the probable cause(s) of the accident is True or False. Your answer must be based on the investigation facts and details within <CONTEXT>.

<CONTEXT> {context} </CONTEXT>

Is this statement True or False?
<STATEMENT>
{statement}
</STATEMENT> [/INST]

Answer:

Prompt 11: Prompt V7 for causal deductive reasoning task.

<s>[INST] You have a fair understanding of causal relations, where "-->" represents "causes", such as: {retrieved} [/INST] Yes, I understand.</s> [INST] Based on an accident investigation bounded by <CONTEXT> delimiters, answer if the statement within <STATEMENT> delimiters about the probable cause(s) of the accident is True or False. Your answer must be based on the investigation facts and details within <CONTEXT>.

<CONTEXT> {context} </CONTEXT>

<RELATIONS> Relations extracted from <CONTEXT>: {extracted} </RELATIONS>

Is this statement True or False?
<STATEMENT>
{statement}
</STATEMENT> [/INST]

Answer:

Prompt 12: Prompt V8 for causal deductive reasoning task.

<s>[INST] You have a fair understanding of causal relations, where "-->" represents "causes", such as: {retrieved} [/INST] Yes, I understand.</s> [INST] Based on an accident investigation bounded by <CONTEXT> delimiters, answer if the statement within <STATEMENT> delimiters about the probable cause(s) of the accident is True or False. Your answer must be based on the investigation facts and details within <CONTEXT>.

<CONTEXT> {context} </CONTEXT>

<RELATIONS> Relations extracted from <CONTEXT>: {extracted}

Possible relations linking probable cause in <STATEMENT> to accident: {inferred} </RELATIONS>

Is this statement True or False? <STATEMENT> {statement}
</STATEMENT> [/INST]

Answer:

Prompt 13: Prompt V9 for causal deductive reasoning task.

<s>[INST] You have a fair understanding of causal relations, where "-->" represents "causes", such as: <RELATIONS> Historical relations: {retrieved}

Relations extracted from <CONTEXT>: {extracted}

Possible relations linking probable cause in <STATEMENT> to accident: {inferred} </RELATIONS> [/INST] Yes, I understand.</s> [INST] Based on an accident investigation bounded by <CONTEXT> delimiters, answer if the statement within <STATEMENT> delimiters about the probable cause(s) of the accident is True or False. Your answer must be based on the investigation facts and details within <CONTEXT>.

<CONTEXT> {context} </CONTEXT>

Is this statement True or False?
<STATEMENT>
{statement}
</STATEMENT> [/INST]

Answer:

D.3 RoTG Findings

Our RoTG model includes a gating framework to focus on top-K nodes. Table 7 presents scores from RoTG across different K values. In terms of Macro and Micro F1, K=8192 returns the best performance. We notice a slight concave pattern of F1 against K values, suggesting an optimal amount of gating is needed. However, the findings did not show statistically significant differences across K=4096 to when all nodes were allowed to be differentiated against.

D.4 LLM Findings

Findings from all experiments with Mistral-Instruct are available in Table 8. The first column indicates the corresponding Prompt number used, while the next four columns indicate the additional information included in the prompt, or if any different processing method was used.

D.5 Qualitative Examples

Table 9 shows the output response from Mistral-Instruct across the three main prompt versions, corresponding to Table 3. The last two columns details the retrieved relations that were included in the prompt.

Dromot #		Relations	SU	Other Tmonle	Macro F1	Micro E1		Accuracy	
nulut #	Extract	Infer	Retrieved	OUICI INCARS	INIACIO L'I		True	False (Rules)	False (LLM)
5			None		70.36 (7.07)	90.30 (1.78)	46.53 (13.21)	92.23 (3.66)	95.69 (1.86)
9			None	Role-play	71.04 (5.99)	89.64 (0.87)	53.82 (12.26)	91.12 (2.76)	$94.00(1.63)^{***}$
٢	>		None		72.42 (7.19)	90.59 (2.52)	52.62 (13.79)	91.73 (4.22)	95.60 (2.06)
8		>	None		63.97 (4.87)***	83.15 (2.85)***	55.99 (11.38)*	78.56 (4.79)***	89.03 (4.35)***
6	>	>	None		63.66 (5.31)***	84.10 (2.53)***	50.36 (12.18)	80.12 (4.66)***	90.65 (3.38)***
10			Semantic		72.50 (6.37)	91.24 (1.40)	48.72 (11.04)	92.99 (2.48)	96.54 (1.93)
11	>		Semantic		70.97 (4.69)	90.67 (2.11)	45.54 (7.10)	91.70(4.21)	96.91 (1.89)
12	>	>	Semantic		64.48 (6.02)**	86.83 (2.27)***	41.81 (12.63)	86.19 (4.56)***	93.59 (2.44)***
10			RoTG		73.19 (7.01)	91.65 (1.42) **	49.49 (13.47)	94.31 (3.49)	96.37 (1.37)
11	>		RoTG		71.15 (6.40)	91.09 (2.14)	44.07 (10.02)	93.43 (3.89)	97.02 (1.63)*
12	>	>	RoTG		64.21 (7.89)**	87.28 (3.23)***	37.98 (13.90)	87.21 (4.02)***	94.46 (2.79)
10			RoTG	No cleaning	71.93 (5.57)	91.19 (1.37)	46.53 (8.61)	94.01 (3.72)	96.38 (1.03)
10			RoTG	No truncate	72.92 (6.43)	91.60 (1.11)	48.87 (12.59)	93.75 (3.24)	96.66 (1.04)
11	>		RoTG	No cleaning	71.52 (5.94)	91.12 (2.16)	45.04 (9.33)	93.28 (4.17)	97.13 (1.38)**
11	>		RoTG	No truncate	70.96 (6.69)	90.95 (2.07)	44.50 (11.16)	93.43 (3.89)	96.73 (1.70)
13	>	>	RoTG	Rels before Task	64.55 (6.48)**	$86.58 (1.80)^{***}$	42.85 (11.72)	87.09 (2.66)***	92.74 (2.00)***

Table 8: Mistral Instruct with various relations included into prompt. Highest score per column is in bold. P-values against scores from the *None* scores in the first row is indicated by: * < 0.15, ** < 0.10, *** < 0.05.

	Base	Semantic	RoTG	Semantic_Rels	RoTG_Rels
	Answer:	Answer:	Answer:	- BART's simple approval process allowed access	
	E			along the right-of-way without protection from mov-	
	The statement is True.	False.	False.	ing trains -> Safety issues and concerns identified	 Errant control signals sent to power systems -> Unoccu-
				during the NLSB accident investigation	
e	Explanation:	The probable cause of the accident was	Explanation:	- Workers were not able to properly protect them-	
		the P. B. Shah captain's error in initiating a		selves from moving trains -> Accident occurred.	driver's medical history, sleep opportunity, sleep quality,
dent able	The accident occurred due	port-to-port (one whistle) passing on the radio	The probable cause of the accident was not insuffi-	NTSB accident investigation -> Major findings	sleep schedule, and time awake, it is unlikely that he was
was cause	to a miscommunication be-	with the Dewey R captain, who had meant to	cient communication between the captains after the	identified safety issues and concerns	fatigued at the time of the collision -> Based on evidence
insuf- of the	tween the captains of the two	arrange a starboard-to-starboard (two-whistle)	passing arrangement was changed. The investigation	- Identification of safety issues and concerns -> New	and statements regarding the float driver's medical history,
ficient acci-	vessels regarding the passing	passing. The P. B. Shah captain was distracted	found that the P. B. Shah captain misunderstood the	safety regulations and requirements	sleep opportunity, sleep quality, sleep schedule, and time
	arrangement The P B Shah	hv the many tasksassociated with menaring	initial nassing agreement and believed he was pronosing a	_	awake it is unlikely that he was farioned at the time of the
		for his arrival at the Ingram facility including	starboard to starboard messare while the Daward Domain	_	
			starboard-to-starboard passage, while the Dewey is captain		
=	starboard-to-starboard passing	naving a cell phone conversation with the boat	Delieved he was proposing a poin-to-poin passage. The	pie approvais -> Access to the right-of-way must	
	arrangement, but the Dewey	store and meeting with the mate to discuss			
	R captain misunderstood and	upcoming tasks. The Dewey R captain made a	_		
the cap- upon	believed it was a port-to-port	mistake by not following the inland navigation	arrival at the Ingram facility, and the Dewey R captain	cedures -> Workers were not able to properly protect	that he was fatigued at the time of the collision.
tains the	passing arrangement. The	rules and should have assessed the risk of	doubting his understanding of the original agreement. The	themselves from moving trains	- There is no evidence that the float driver was experiencing
after decision-	Dewev F	collision presented by the two alternative	-	_	stress or had a health, hearing, or visual condition that af-
		meeting arrangements chosen the ontion that			fected his shility to nerreive the grade crossing warnings
passing and	or the river in an attempt to	did not include passing in front of the P. B.	should have assessed the risk of collision presented by	_	
recol-	conduct a two-whistle pass,	Shah tow, and then used his privilege as the	the two alternative meeting arrangements and chosen the	_	
range- lection	which resulted in a collision with	downbound vessel to overrule the P. B. Shah	option that did not include passing in front of the P. B. Shah	fatalities -> Identification of safety issues and con-	
ment of the	the P. B. Shah tow. The miscom-	captain's change to a two-whistle meeting	tow.	cerns	time awake, it is unlikely that he was fatigued at the time of
was captain	munication and confusion about	arrangement.		- BART's simple approval process allowed access	the collision.
har	the receipe arrangement lad to			along the right of way that did not arouids work-	- Reced on avidance and statements recording the float
Ч.	the accident.			ers with protection from moving trans -> BART is-	
Shah.")				sued General Order 175 (GO 175) to govern roadway	
-				WOLKEL PLOTECHOLITOL TAIL HAIISH WOLKELS III CALIFOL	Jauguca at the tille of the collision> The glade crossing
				nia, prohibiting the type of access that was allowed	warning system provided 20 seconds of warning as required
-				under BART's simple approval process.	by federal regulations.
-				DADT assistant shine transmission officer dis	The float defines new not distructed by the use of in which
				DAINI assistant cinet transportation officer dis-	- The hoat univer was not distracted by the use of the venicle
				tributed a memorandum immediately prohibiting sim-	electronic devices -> The float driver was not distracted
				nle approvale -> Acress to the right-of-way must	by electronic devices which could have contributed to the
				pre approvais -> Access to the right-of-way inter-	
				provide the work crew with protection from moving	accident.
				trains	
The False	Answer:	Answer:	Answer:	- Pedestrian's decision to run across the multilane	- Defective control system in unoccupied cars -> Errant
prob- (True				roadwav in front of the oncoming car -> Driver's	control signals sent to power systems
	Tere	The statement is Taxe	Edina	docidion to mole a laft trum from the laft trum land	Event control clands cont to nonce surfame > Il noor
	True.	The scalement is true.	raise.		- Erran control signals sent to power systems -> Unoccu-
cause ment:				onto eastbound Leesburg Pike	pied cars moved and stopped
of the "The	The investigation found that	The investigation found that the accident was	The probable cause of the accident was not the cur-	- Driver failed to see nedestrian -> Driver applied	- Conductor was ninched between the knuckle of the sta-
	And mycsugation round unit		_		
acci- prob-	the accident was caused by	caused by the intermittent submersion of	rent conditions contributing to intermittent submersion	brakes and attempted to steer left, colliding with	tionary car and the drawbar carrier of the free-rolling car ->
dent able	the intermittent submersion of	wastage holes on the starboard stern quarter of	of wastage holes. The investigation found that the two	nedestrian (Accident)	
					D
	wastage notes on the stat total	the MISS MOSIVIL due to the capital pushing	wastage holes and a machined wern at the main new to		- Dy-passed couplets on the 1/11 and 1000 cars -> raid
current of the	stern quarter of the Miss Roslyn	against the tow at a 9000b0 angle to the	the starboard steering void were not watertight, and the		accident
condi- acci-	due to the cantain nushing	hank for 2.5 to 3 hours. The current likely	cantain was assisting in making up a tow, which required		- Train movement hefore soing between cars to nerform
		lowered and submerged the noies, allowing	mm to push against the tow at a 900000 angle to the		work on cars -> ratat accident
con- was the	to the bank for 2.5 to 3 hours.	continuous water ingress to the starboard	bank for 2.5 to 3 hours. This action likely lowered and		 Violation of these rules escalated the discipline policy by
tribut- com-	The current likely lowered and	steering void for about 3 hours. Once the hull	intermittently submerged the wastage and fracture holes		one step -> Fatal accident
	and the holes offening	Acceled the worked cards lower increase	on the storboard stars cuestar allowing continuous metar		Douth of the medeataion > Eated accident
	subilicized the noise, anowing	HOUNDLY, LIK VESSEL SAILY LOWEL, HILLEASHIE	on the stationard stern quarter, anowing continuous water		
inter- lack	continuous water ingress to the	the rate of flooding through the holes to	ingress to the starboard steering void for about 3 hours. The		 Fatal accident -> Accident Number: HWY16SH023, Acci-
mittent of ef-	starboard steering void for about	the starboard steering void, resulting in the	aft steering void was partially flooded, which likely caused		dent Type: Fatal pedestrian collision with car. Location: 9th
	3 hours Orea the hull flooded	observed starboard list. The nort flanking void	the observed storboard list Once the hull flooded the		Streat and D Streat NW Workington DC Data and Time-
	2 HOURS. OTKE UK HUILHOURD,	ODSELVED STATEO ALL INC. THE POLLIAIRNING VOID	LIE ODSELVEU SLAIDOATU IISI. OTKE LIE IIUII HOOUEU, LIE		Succi and F Succi IN W, Washington, DC, Date and Inne
sion of hull	the vessel sank lower, increasing	eventually flooded, causing the vessel to lose	vessel sank lower, increasing the rate of flooding through		August 18, 2016, about 2:20 a.m. eastern daylight time, Ve-
wastage inspec-	the rate of flooding through the	stability and cansize.	the holes to the starboard steering void, thus increasing the		hicle: 2000 Mercedes-Benz CLK 320. Driver: 31-vear-old
	a minute based and a state of a	J 6	a standard become and a second on the local becomes		family Dadaction, 44 years old male Established 1
	TIOLES TO THE STAT DOAL O STEELING		Starboard IRCT and Subfillerging the starboard buiwark and		ICILIAIE, FEUESUTAIL: 44-YEAL-ON ILLAIE, FAUALILIES: 1
and	void, resulting in the observed		stern deck. The port flanking void flooded, resulting in the		 Coding error in the software upgrade -> Acceleration and
mainte-	starboard list. The port flanking		vessel's loss of stability and capsizing. The severe wastage		deceleration of the train
" anna "	void avantually flooded concing		found throughout the vascal in the nost excident survey		Acceleration and deceleration of the train ~ Initial of
I IIIII	VOID CVCIIIUMILY INCOUCH, CAUSING				
	the vessel's loss of stability and		indicates that the Miss Kostyn was poorly maintained. The		passengers
	capsizing.		company did not have an effective maintenance program on		
			board the vessel so holes in and fractures to the hull and		
-			all the well and a feature in the part of the second s		
-			deck went underected and utilitately ted to moduling write		

Table 9: Qualitative examples from Mistral-Instruct across the three different prompts. (Base (No additional relations in prompt), Semantic, and RoTG causal relations in prompt).