# LINGMESS: Linguistically Informed Multi Expert Scorers for Coreference Resolution

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## Abstract

Current state-of-the-art coreference systems are based on a single pairwise scoring component, which assigns to each pair of mention spans a score reflecting their tendency to corefer to each other. We observe that different kinds of mention pairs require different information sources to assess their score. We present LINGMESS, a linguistically motivated categorization of mention-pairs into 6 types of coreference decisions and learn a dedicated trainable scoring function for each category. This significantly improves the accuracy of the pairwise scorer as well as of the overall coreference performance on the English Ontonotes coreference corpus and 5 additional datasets.<sup>1</sup>

## 1 Introduction

Coreference resolution is the task of clustering textual mentions that refer to the same discourse entity. This fundamental task requires many decisions. In this work, we argue that different *kinds* of decisions involve different challenges. To illustrate that, consider the following text:

"Lionel Messi has won a record seven Ballon d'Or awards. He signed for Paris Saint-Germain in August 2021. "I would like to thank my family", said the Argentinian footballer. Messi holds the records for most goals in La Liga"

To correctly identify that the pronoun "He" refers to "Lionel Messi", models need to model the discourse, while linking "my" to "I" may rely more heavily on morphological agreement. Likewise, linking "the Argentinian footballer" to "Lionel Messi" requires world knowledge, while linking "Messi" to "Lionel Messi" may be achieved by simple lexical heuristics.



Figure 1: Architecture of our multi expert model. Given two spans "Lionel Messi" and "He", we sum four scores: individual mention scores (black),  $f_m$  ("Lionel Messi"),  $f_m$  ("He"), and pairwise scores, shared antecedent score (white)  $f_a$  ("Lionel Messi", "He") and the relevant "expert" score (blue)  $f_a^{\text{PRON-ENT}}$  ("Lionel Messi", "He").

Indeed, pre-neural coreference resolution works often considered the types of a mention-pair, either by incorporating this information as model features, or by tailoring specific rules or specific models for each mention pair (see related work section).

However, neural-network based coreference models are all based on a *single* pairwise scorer that is shared for all mention pairs, regardless of the different challenges that needs to be addressed by each pair type (Lee et al., 2017, 2018; Joshi et al., 2019; Kantor and Globerson, 2019; Joshi et al., 2020; Xu and Choi, 2020; Xia et al., 2020; Toshniwal et al., 2020; Thirukovalluru et al., 2021; Kirstain et al., 2021; Dobrovolskii, 2021).

In this work, we suggest that modeling different mention pairs by different sub-models (in our case, different learned scoring functions) depending on their types is beneficial also for neural models. We identify a set of decisions: (a) linking compatible

<sup>&</sup>lt;sup>1</sup>The codebase to train and run LINGMESS is available in https://github.com/shon-otmazgin/ lingmess-coref. Also, our recent F-COREF Python package (Otmazgin et al., 2022) includes a simple and efficient implementation of LINGMESS in https: //github.com/shon-otmazgin/fastcoref.

Category	Co-referring example	Non Co-referring example
PRON-PRON-C	A couple of <b>my</b> law clerks were going to and <b>I</b> was afraid <b>I</b> was going to	The Lord God said to <b>my</b> Lord: "Sit by me at <b>my</b> right side , and I will put your enemies "
PRON-PRON-NC	"I made a similar line and I produced it cheaper", he says.	She is my Goddess
ENT-PRON	<b>Spain, Argentina, Thailand and Indonesia</b> were doing too little to prevent across <b>their</b> borders.	Tonight, to kick off <b>the effort</b> , CNN will premiere <b>its</b> first prime - time newscast in years.
Матсн	says Paul Amos, CNN executive vice president for programming. Accordingly, CNN is	Hertz and Avis can not benefit <b>Budget's</b> programs, " said Bob Wilson, <b>Budget's</b> vice president
CONTAINS	He reportedly showed <b>DeLay</b> a videotape that made him weep. <b>Tom DeLay</b> then	Give <b>SEC</b> authority to halt securities trading, (also opposed by new <b>SEC chairman</b> )
OTHER	They also saw <b>the two men who were standing</b> with him. When Moses and Elijah were leaving	<b>The company</b> is already working on its own programming <b>the newspaper</b> said.

Table 1: Example of each category, taken from Ontonotes development set. We define the categories of mention pairs as follows. PRON-PRON-C: compatible pronouns based on their attributes such as gender, number and animacy (see Appendix C for more details), PRON-PRON-NC: incompatible pronouns, ENT-PRON: a pronoun and another span, MATCH: non-pronoun spans with the same content words, CONTAINS: one contains the content words of the other, OTHER: all other pairs. Content words exclude stop words, see Appendix C for the full list of stop words.

pronouns (PRON-PRON-C); (b) linking incompatible pronouns (PRON-PRON-NC); (c) linking pronouns to entities (ENT-PRON); (d) linking entities which share the exact lexical form (MATCH); (e) linking entities where the lexical form of one contains the lexical form of the other (CONTAINS); (f) other cases (OTHER). Each of these classes is easy to identify deterministically, each contains both positive and negative instances, and each could benefit from a somewhat different decision process. Table 1 demonstrates the classes.<sup>2</sup>

We present **Ling**uistically Informed **M**ulti **E**xpert **S**corers (LINGMESS), a coreference model which categorizes each pairwise decision into one of these classes, and learns, in addition to a shared scoring function, also a separate scoring function for each pair type. At inference time, for each pair of mentions being scored, we deterministically identify the pair's type, and use the corresponding scoring function.<sup>3</sup>

Specifically, we extend the recent *s2e*'s model (Kirstain et al., 2021) by adding per-category scoring, but the method is general and may work with other coreference models as well. As illustrated in Figure 1, the final coreference score between two spans is composed—in addition to the individual mention scores—of two pairwise scores: a shared antecedent-compatibility score and an "ex-

pert" antecedent compatibility score which depends on the linguistic-type of the pair.

We show that this significantly improves the coreference performance on Ontonotes (Pradhan et al., 2012) and 5 additional datasets. We also inspect the performance of the model for each category separately, showing that some classes improve more than others. This analysis provides a finer-grained understanding of the models and points out directions for future research.

## **2** Background: the s2e Model

The *s2e* model (Kirstain et al., 2021) achieves the current best coreference scores among all practical neural models.<sup>4</sup>

Given a sequence of tokens  $x_1, \ldots, x_n$ , each mention pair (c, q) is scored using a scoring function  $F_s(c, q)^5$  described below, where c is a "candidate span" and q is a "query span" which appears before c in the sentence. The span encodings are based on contextualized word embeddings obtained by a Longformer encoder, see Kirstain et al. (2021) for details. These pairwise scores are then used to form coreference chains (see "inference" below).

<sup>&</sup>lt;sup>2</sup>More fine-grained distinctions are of course also possible, but we leave exploration of them to future work.

<sup>&</sup>lt;sup>3</sup>For computational efficiency on the GPU, we find it beneficial to compute all the scoring functions and mask away the not needed values.

<sup>&</sup>lt;sup>4</sup>We define "practical models" as those that require a constant number transformer-based document encodings per passage, as opposed to a constant number of document encodings per mention. The CorefQA model (Wu et al., 2020) achieves a substantially higher score, but requires to run a separate BERT inference for each mention, making it highly impractical.

<sup>&</sup>lt;sup>5</sup>S state for SHARED

The scoring function  $F_{\rm S}$  is further decomposed:

$$F_{\rm S}(c,q) = \begin{cases} f_m(c) + f_m(q) + f_a(c,q) & c \neq \varepsilon \\ 0 & c = \varepsilon \end{cases}$$

where  $\varepsilon$  is the null antecedent, and  $f_m$  and  $f_a$  are parameterized functions, scoring each individual span  $(f_m)$  and the pairwise interaction  $(f_a)$ .

For each possible mention q, the learning objective optimizes the sum of probabilities over the true antecedent  $\hat{c}$  of q:

$$L_{\mathsf{S}}(q) = \log \sum_{\hat{c} \in \mathcal{C}(q) \cap \text{GOLD}(q)} P_{\mathsf{S}}(\hat{c} \mid q)$$

where C(q) is the set of all candidate antecedents<sup>6</sup> with a null antecedent  $\varepsilon$ . GOLD(q) is the set of the true antecedents of q.  $P_{s}(c \mid q)$  is computed as a softmax over  $F_{s}(c,q)$  scores for c values in C(q):

$$P_{\mathsf{S}}(\hat{c} \mid q) = \frac{\exp F_{\mathsf{S}}(\hat{c}, q)}{\sum\limits_{c' \in \mathcal{C}(q)} \exp F_{\mathsf{S}}(c', q)}$$

## **3** LINGMESS

Clustering coreferring entities typically involves many different phenomena, which we argue should be addressed in a different manner. Therefore, our core contribution is proposing to allocate a dedicated scorer  $f_a^t(c, q)$  for each phenomenon type t, in addition to the shared pairwise scorer  $f_a(c, q)$ . The overall architecture of our model is shown in Figure 1.

Concretely, we extend the s2e model with six additional antecedent scorers  $f_a^t$  where  $t \in$ {PRON-PRON-C, PRON-PRON-NC, ENT-PRON, MATCH, CONTAINS, OTHER}, the six categories we list in Table 1.

The pairwise scoring function now becomes:

$$F(c,q) = \begin{cases} f_m(c) + f_m(q) + f(c,q) & c \neq \varepsilon \\ 0 & c = \varepsilon \end{cases}$$
$$f(c,q) = f_a(c,q) + f_a^{T(c,q)}(c,q)$$

where T(c,q) is a deterministic, rule-based function to determine the category t of the pair (c,q). The pairwise scoring function f(c,q) scoring c as the antecedent of q, is now composed of a shared scorer  $f_a(c,q)$  and an "expert" scorer  $f_a^t(c,q)$ which differs based on the type of the pair c,q. Each of the seven pairwise scoring functions  $(f_a$  and the six  $f_a^t$ ) is parameterized separately using its own set of matrices. The transformer-based encoder and the mention scorer  $f_m$  are shared between all the antecedent scorers. See Appendix A.2 for full model architecture.

**Training** For each span q, our model optimizes the objective function  $L_{\text{COREF}}$  over the sum of probabilities of all true antecedents of q:

$$L_{\text{COREF}}(q) = \log \sum_{\hat{c} \in \mathcal{C}(q) \cap \text{GOLD}(q)} P(\hat{c} \mid q)$$

Here,  $P(\hat{c} \mid q)$  is a softmax over  $F(\hat{c}, q)$  scores, that is our new score function described in Figure 1.

$$P(\hat{c} \mid q) = \frac{\exp F(\hat{c}, q)}{\sum\limits_{c' \in \mathcal{C}(q)} \exp F(c', q)}$$

This scorer is also the one used in inference. However, this objective does not explicitly push each category ("expert") to specialize. For example, for the PRON-PRON-C cases, it would be useful to explicitly train the model to distinguish between the possible antecedents of that type only (without regarding other antecedents), as well as to explicitly distinguish between a pronoun antecedent and a null antecedent. To this end, we extend the training objective by also training each "expert" separately:

$$L_t(q) = \log \sum_{\hat{c} \in \mathcal{C}_t(q) \cap \text{GOLD}(q)} P_t(\hat{c} \mid q)$$

$$P_t(\hat{c} \mid q) = \frac{\exp F_t(\hat{c}, q)}{\sum\limits_{c' \in \mathcal{C}_t(q)} \exp F_t(c', q)}$$

$$F_t(c,q) = \begin{cases} f_m(c) + f_m(q) + f_a^t(c,q) & c \neq \varepsilon \\ 0 & c = \varepsilon \end{cases}$$

Note that for  $L_t(q)$  we replace C(q) with  $C_t(q)$ , considering only the potential antecedents that are compatible with the span q for the given type. For example, for  $L_{\text{MATCH}}$  and a span q, we will only consider candidates c which appear before q with the exact same content words as q. Our final objective for each mention span q is thus:

$$L(q) = L_{\text{COREF}}(q) + L_{\text{EXPERTS}}(q)$$
$$L_{\text{EXPERTS}}(q) = \sum_{t} L_t(q) + L_s(q)$$

<sup>&</sup>lt;sup>6</sup>All spans before q that passed some pruning threshold.

		MUC			$B^3$		$CEAF_{\phi_4}$ LEA						
	R	Р	F1	R	Р	F1	R	Р	F1	R	Р	F1	Avg. F1
<i>s2e</i> LingMess	<b>85.2</b> 85.1	86.6 <b>88.1</b>	85.9 <b>86.6</b>	77.9 <b>78.3</b>	80.3 <b>82.7</b>	79.1 <b>80.5</b>	75.4 <b>76.1</b>	76.8 <b>78.5</b>	76.1 <b>77.3</b>		78.3 <b>80.9</b>	77.0 <b>78.5</b>	80.3 <b>81.4</b>

Table 2: Performance on the test set of the English OntoNotes 5.0 dataset. The averaged F1 of MUC, B<sup>3</sup>, CEAF<sub> $\phi$ </sub> is the main evaluation metric. Our model outperforms the *s2e* model (Kirstain et al., 2021) by 1.1 CoNLL F1. The performance gain is statistically significant according to a non-parametric permutation test (p < 0.05).

	s2e	LINGMESS
WikiCoref (Ghaddar and Langlais, 2016)	59.7	62.6
GAP (Webster et al., 2018)	88.3	89.6
WinoGender (Rudinger et al., 2018)	70.5	77.3
WinoBias (Zhao et al., 2018)	84.3	85.1
BUG (Levy et al., 2021)	72.2	74.6

Table 3: Performance on the test set of various coreference datasets. The reported metrics are CoNLL F1 for WikiCoref, F1 for GAP and Accuracy for WinoGender, WinoBias and BUG.

		s2e		L	INGME	SS
	Р	R	F1	Р	R	F1
PRON-PRON-C	88.8	71.3	79.1	88.0	85.1	86.5
PRON-PRON-NC	84.2	55.8	67.1	88.3	68.7	77.3
ENT-PRON	78.8	68.7	73.4	80.4	69.8	74.7
MATCH	85.6	90.2	87.8	85.3	93.7	89.3
CONTAINS	72.4	80.9	76.4	77.4	78.9	78.1
OTHER	60.1	70.2	64.7	71.7	64.2	67.7

Table 4: Pairwise performance by category, on the test set of the English OntoNotes 5.0 dataset. LINGMESS surpasses the *s2e* model (Kirstain et al., 2021) for most categories by a substantial margin.

**Inference** At inference time, we compute the score of each mention based on the shared scorer as well as the per-type scorer matching the mention type. We then form the coreference chains by linking each mention q to its most likely antecedent c according to F(c, q). We do not use higher-order inference as it has been shown to have a marginal impact (Xu and Choi, 2020).

## **4** Experiments

Our baseline is the *s2e* model trained on the English OntoNotes 5.0 dataset by its authors (Kirstain et al., 2021). We train LINGMESS also on OntoNotes, and evaluate both models on OntoNotes, Wiki-Coref, GAP, WinoGender, WinoBias and BUG. Implementation details are described in Appendix B.

**Performance** Table 2 presents the performance of LINGMESS on the test set of Ontonotes. LINGMESS achieves 81.4 F1 on Ontonotes, while

the *s2e* baseline achieves 80.3. Our performance gain is statistically significant according to a nonparametric permutation test (p < 0.05). Additionally, Table 3 shows that LINGMESS outperforms the *s2e* model on WikiCoref (+2.9) GAP (+1.3), WinoGender (+6.8), WinoBias (+0.8) and BUG (+2.4), indicating a better out-of-domain generalization.

**Importance of per-category scoring.** To assess that the improvement of LINGMESS is due to the decomposition into our set of categories and not to the added parameters, we do two experiments. First, we train a random baseline, which randomly assigns a category for each pair<sup>7</sup> and obtain similar results as the baseline. Second, we train our model by optimizing only the overall loss  $L_{\text{COREF}}$  and not  $L_{\text{EXPERTS}}$ . This achieves lower results than the baseline, due to low mention recall.

In addition to the standard coreference evaluation, we report pairwise performance for each category. Given a mention-pair (c, q), if F(c, q) is higher than 0, we treat it as a positive prediction, otherwise negative. We then measure precision, recall and F1 based on gold clusters labels. Table 4 shows the pairwise performance of the *s2e* model and LINGMESS. LINGMESS outperforms *s2e* by a significant margin for all categories (e.g +7.4 F1 for PRON-PRON-C, +10.2 F1 for PRON-PRON-NC, etc.).<sup>8</sup> The performance varies across the different categories, suggesting aspects of the coreference problem where future work can attempt to improve.

The importance of the shared scorer. To investigate the role of the shared scorer, we trained the LINGMESS model with only the per-type pairwise scorers, excluding the shared pairwise scorer  $F_s(c,q)$  and its accompanying loss term  $L_s(q)$ .

<sup>&</sup>lt;sup>7</sup>For each pair of mentions (c, q), we take the modulo of the sum of the ASCII code of the last character of the last token of c and q.

<sup>&</sup>lt;sup>8</sup>These gains in this pairwise metric are higher than the CoNLL metrics reported in Table 2, because the CoNLL metrics are based on the final clusters, after aggregation of individual pairwise decisions.

This resulted in a significant decrease in performance (-0.9), specifically in the recall of the mention detection component. However, adding the shared scorer was able to mitigate this degradation by balancing the different "experts" pairwise scorers.

# 5 Related Work

Many pre-neural works consider the various linguistic phenomena involved in coreference resolution as a different challenge. The early coreference system by Zhou and Su (2004) divided the antecedents candidates into distinct coreference categories (e.g., Name Alias, Apposition, Definite Noun, and a few more) and defined tailored rules for each category. Later, Lee et al. (2013) proposed the multi-sieves deterministic model, where each sieve adds coreference links between mention pairs from a specific linguistic category (e.g string match, compatible pronoun, etc.). Haghighi and Klein (2009) performed an error analysis of their coreference model according to different types of antecedent decisions, such as Proper Noun-Pronoun, Pronoun-Pronoun, etc. Based on this analysis, they focus on fixing the pronoun antecedent choices by adding syntactic features. More recently, Lu and Ng (2020) analyze empirically the performance of neural coreference resolvers on various finegrained resolution categories of mentions (e.g gendered pronoun vs. 1st and 2nd pronoun). They find that while models perform well on name and nominal mention pairs with some shared content words, they still struggle with resolving pronouns, particularly relative pronouns.

Early supervised statistical models train a feature-based classifier that incorporates the type of antecedent decision (e.g. pronoun-entity, string match) as features at the mention-pair level (Soon et al., 2001; Bengtson and Roth, 2008; Clark and Manning, 2015, 2016). Subsequently, Denis and Baldridge (2008) demonstrate that training separate classifiers that specialize in particular types of mentions (e.g third person pronouns, speech pronouns, proper names, definite descriptions, and all other) provides significant performance improvements. Lassalle and Denis (2013) took that observation a step further and proposed a more advanced method for model specialization by learning to separate types of mention into optimal classes and their proper feature space.

In our work, we make progress in coreference

systems specialization direction, and show that the incorporation of linguistic information is helpful also in the context of end-to-end neural models.

## 6 Conclusion

We present LINGMESS, a coreference model that significantly improves accuracy by splitting the scoring function into different categories, and routing each scoring decision to its own category based on a deterministic, linguistically informed heuristic. This indicates that while end-to-end training is very effective, linguistic knowledge and symbolic computation can still be used to improve results.

## Limitations

In this paper, we consider a set of 6 linguistic categories of mention pairs, as listed in Table 1. These categories might not be optimal for the task, while a different set of finer-grained categories may result to a higher performance gain. Another aspect that can be considered as a limitation is the computation of the categories for every possible pairs. Although the model considers only the top-scoring spans, this additional computation layer increases training and inference time over the baseline (see Appendix B.3 for the exact time). Our linguistic heuristics could be improved by, e.g., running a parser and considering head words. However, we chose not to do so in this work as this will further increase runtime.

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## A Model Architecture

Given a sequence of tokens  $x_1, ..., x_n$  from an input document, a transformer-based (BERT-like) encoder first forms contextualized representation vectors,  $x_1, ..., x_n$  for each token in the sequence.

#### A.1 The s2e Model

**Mention scorer** Given a span  $q = (\mathbf{x_i}, \mathbf{x_j})$ , represented by its start and end tokens, the score for q being a mention is defined as follow:

$$\mathbf{m}_s(\mathbf{x}) = \operatorname{GeLU}(\mathbf{W}_{\mathbf{m}_s}\mathbf{x}) \qquad \mathbf{m}_e(\mathbf{x}) = \operatorname{GeLU}(\mathbf{W}_{\mathbf{m}_e}\mathbf{x})$$

$$f_m(q) = \mathbf{m}_s(\mathbf{x_i}) \cdot \mathbf{v}_s + \mathbf{m}_s(\mathbf{x_j}) \cdot \mathbf{v}_e$$
$$+ \mathbf{m}_s(\mathbf{x_i}) \cdot \mathbf{B}_m \cdot \mathbf{m}_s(\mathbf{x_j})$$

where  $\mathbf{m}_s(\mathbf{x})$  and  $\mathbf{m}_e(\mathbf{x})$  are two non-linear functions to obtain start and end representations for each token x, and  $f_m(q)$  is a biaffine product over these representations.

Antecedent scorer Given two spans,  $c = (\mathbf{x_i}, \mathbf{x_j})$  and  $q = (\mathbf{x_k}, \mathbf{x_l})$ , represented by their start and end tokens, the score for c being an antecedent of q is computed as follow:

$$\mathbf{a}_s(\mathbf{x}) = \operatorname{GeLU}(\mathbf{W}_{\mathbf{a}_s}\mathbf{x}) \qquad \mathbf{a}_e(\mathbf{x}) = \operatorname{GeLU}(\mathbf{W}_{\mathbf{a}_e}\mathbf{x})$$

$$f_a(c,q) = \mathbf{a}_s(\mathbf{x_i}) \cdot \mathbf{B}_{ss} \cdot \mathbf{a}_s(\mathbf{x_k}) + \mathbf{a}_e(\mathbf{x_j}) \cdot \mathbf{B}_{es} \cdot \mathbf{a}_s(\mathbf{x_k}) + \mathbf{a}_s(\mathbf{x_i}) \cdot \mathbf{B}_{se} \cdot \mathbf{a}_e(\mathbf{x_l}) + \mathbf{a}_e(\mathbf{x_j}) \cdot \mathbf{B}_{ee} \cdot \mathbf{a}_e(\mathbf{x_l})$$

Similar to the mention scorer,  $\mathbf{a}_s(\mathbf{x})$  and  $\mathbf{a}_e(\mathbf{x})$ are two non-linear functions to obtain start/end representations for each token, and  $f_a(c,q)$  is a sum of four bilinear functions over the start and end representations of c and q.

## A.2 LINGMESS

**Mention scorer** Our mention scorer is the same as *s2e* mention scorer implementation.

Antecedent scorer As mentioned in the paper (§3), in addition to the shared antecedent scorer  $f_a(c,q)$ , LINGMESS includes a dedicated antecedent scorer  $f_a^t(c,q)$  for each category  $t \in \{\text{PRON-PRON-C}, \text{PRON-PRON-NC}, \text{ENT-PRON}, \text{MATCH}, \text{CONTAINS}, \text{OTHER}\}$ . The overall score for  $c = (\mathbf{x_i}, \mathbf{x_j})$  being an antecedent of  $q = (\mathbf{x_k}, \mathbf{x_l})$  becomes the sum of the shared scorer and the relevant category "expert" scorer:

$$f(c,q) = f_a(c,q) + f_a^{T(c,q)}(c,q)$$

where T(c,q) is a deterministic function to determine the category t of the pair (c,q).

For each category t, we define two specific nonlinear functions to obtain start and end representations ( $\mathbf{a}_s^t(\mathbf{x})$  and  $\mathbf{a}_e^t(\mathbf{x})$ ) as well as an "expert" antecedent scoring function  $f_a^t(c,q)$ :

$$\begin{split} \mathbf{a}_{s}^{t}(\mathbf{x}) &= \mathrm{GeLU}(\mathbf{W}_{\mathbf{a}_{s}}^{t}\mathbf{x}) \qquad \mathbf{a}_{e}^{t}(\mathbf{x}) = \mathrm{GeLU}(\mathbf{W}_{\mathbf{a}_{e}}^{t}\mathbf{x}) \\ & f_{a}^{t}(c,q) = \mathbf{a}_{s}^{t}(\mathbf{x}_{\mathbf{i}}) \cdot \mathbf{B}_{ss}^{t} \cdot \mathbf{a}_{s}^{t}(\mathbf{x}_{\mathbf{k}}) \\ & + \mathbf{a}_{e}^{t}(\mathbf{x}_{\mathbf{j}}) \cdot \mathbf{B}_{es}^{t} \cdot \mathbf{a}_{s}^{t}(\mathbf{x}_{\mathbf{k}}) \\ & + \mathbf{a}_{s}^{t}(\mathbf{x}_{\mathbf{i}}) \cdot \mathbf{B}_{se}^{t} \cdot \mathbf{a}_{e}^{t}(\mathbf{x}_{\mathbf{l}}) \\ & + \mathbf{a}_{e}^{t}(\mathbf{x}_{\mathbf{j}}) \cdot \mathbf{B}_{ee}^{t} \cdot \mathbf{a}_{e}^{t}(\mathbf{x}_{\mathbf{l}}) \end{split}$$

Overall, our model introduces 6 learnable matrices for each category ( $\mathbf{W}_{\mathbf{a}_s}^t$ ,  $\mathbf{W}_{\mathbf{a}_e}^t$ ,  $\mathbf{B}_{ss}^t$ ,  $\mathbf{B}_{es}^t$ ,  $\mathbf{B}_{ee}^t$ ). The transformer-based encoder and the mention scorer are shared between all the different pairwise scorers.

#### **B** Implementation Details

#### **B.1** Hyperparameteres

We extend the s2e's implementation based on Py-Torch (Paszke et al., 2019) and Transformers (Wolf et al., 2020). We used the same hyperparameters (e.g learning rate, warmup, etc.) as the s2e model except the hidden size of all matrices W and B. As our method introduces a dedicated antecedent scoring function  $f_a^t$  function for each category t, we reduce the size of these matrices from 3072 to 2048 to fit training into memory in our hardware. Similar to the baseline our head method is on top of Longformer-Large (Beltagy et al., 2020), resulting in a total of 590M learnable parameters (the s2e model contains 494M learnable parameters). We used dynamic batching both for training and inference, specifically 5K tokens in a single batch during training and 10K tokens at inference.

	Kirstain et al. (2021)				LINGMESS			
_	Р	R	F1		Р	R	F1	
PRON-PRON-C	91.7	77.5	84.0		91.7	90.2	91.0	
PRON-PRON-NC	88.9	66.2	75.9		90.2	81.3	85.5	
ENT-PRON	82.0	74.1	77.9		81.4	74.7	77.9	
MATCH	88.3	87.5	87.9		88.4	92.0	90.2	
CONTAINS	69.1	77.2	72.9		76.1	73.5	74.8	
OTHER	56.8	67.5	61.7		70.8	64.4	67.5	

Table 5: Pairwise performance by category, on the dev set of the English OntoNotes 5.0 dataset.

	Masc	Fem	Bias	Overall
Kirstain et al. (2021)	90.6	85.8	0.95	88.3
LINGMESS	<b>91.3</b>	<b>87.8</b>	<b>0.96</b>	<b>89.6</b>

Table 6: Performance on the test set of the GAP coreference dataset. The reported metrics are F1 scores.

## **B.2** Evaluation

As mentioned in the paper (§4), we conduct our experiments on the English portion of the OntoNotes corpus (Pradhan et al., 2012). This dataset contains 2802 documents for training, 343 for development, and 348 for test.

We evaluate our model according to the standard coreference metric: MUC (Vilain et al., 1995), B<sup>3</sup> (Bagga and Baldwin, 1998), CEAF<sub> $\phi_4$ </sub> (Luo, 2005), and LEA (Moosavi and Strube, 2016) using the official CoNLL coreference scorer.<sup>9</sup> LINGMESS achieves 81.6 CoNLL F1 on the development set of Ontonotes. Also, Table 5 presents the pairwise performance on the development set for each category. We compute statistical significance with a non-parametric permutation test using Ulmer et al. (2022)'s implementation. Table 6 shows that LINGMESS consistenly outperforms the *s2e* model on GAP.

#### **B.3 Runtime and Memory**

Our model was trained for 129 epochs on a single 32GB NVIDIA Tesla V100 SXM2 GPU. The training took 23 hours. At shown in Table 7, the run-time at inference time in LINGMESS is longer than in the s2e model because of the category selection for every possible pair of mentions. The memory consumption remains quite similar to the baseline.

	Runtime	Memory
Kirstain et al. (2021)	28	5.4
LINGMESS	43	5.9

Table 7: Inference time(Seconds) and memory(GiB) on 343 docs of OntoNotes development set. Using Dynamic batching, 10K tokens in a single batch. Hardware, NVIDIA Tesla V100 SXM2

ID	Pronouns
1	I, me, my, mine, myself
2	you, your, yours, yourself, yourselves
3	he, him, his, himself
4	she, her, hers, herself
5	it, its, itself
6	we, us, our, ours, ourselves
7	they, them, their, themselves
8	that, this

Table 8: List of groups of compatible pronouns, pronouns with the same ID are considered as compatible.

## **C** Determining pair types

Our method routes each pair of spans to their corresponding category scorer. This decision is based on the linguistic properties of the spans. Given a mention-pair (c, q), we defined a rule based function T(c,q) that determines the category of that pair. If c and q are both pronouns, if they are compatible according to gender, number and animacy (see Table 8 for the full list), the metnion pair will be routed to PRON-PRON-C, otherwise PRON-**PRON-NC.** If c is pronoun and q is a non-pronoun span (or vise-versa) we route the mention-pair to PRON-ENT. We route the remaining pairs to their corresponding categories (MATCH, CONTAINS or OTHER) by considering only content words, excluding the following stop words: {'s, a, all, an, and, at, for, from, in, into, more, of, on, or, some, the, these, those]. Accordingly, the mentions "the U.S. and Japan" and "Japan and the U.S." are considered MATCH, "This lake of fire" and "the lake of fire" are considered CONTAINS and "Bill Clinton" and "The President" are considered OTHER.

<sup>&</sup>lt;sup>9</sup>https://github.com/conll/

reference-coreference-scorers.