Learning to Rank in the Age of Muppets: Effectiveness–Efficiency Tradeoffs in Multi-Stage Ranking

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Abstract

It is well known that rerankers built on pretrained transformer models such as BERT have dramatically improved retrieval effectiveness in many tasks. However, these gains have come at substantial costs in terms of efficiency, as noted by many researchers. In this work, we show that it is possible to retain the benefits of transformer-based rerankers in a multi-stage reranking pipeline by first using feature-based learning-to-rank techniques to reduce the number of candidate documents under consideration without adversely affecting their quality in terms of recall. Applied to the MS MARCO passage and document ranking tasks, we are able to achieve the same level of effectiveness, but with up to 18× increase in efficiency. Furthermore, our techniques are orthogonal to other methods focused on accelerating transformer inference, and thus can be combined for even greater efficiency gains. A higher-level message from our work is that, even though pretrained transformers dominate the modern IR landscape, there are still important roles for "traditional" LTR techniques, and that we should not forget history.

1 Introduction

Pretrained transformers such as BERT (Devlin et al., 2019) have dramatically increased retrieval effectiveness in many tasks across a multitude of domains (Lin et al., 2020a). Nevertheless, in a standard "retrieve-then-rerank" setup, the application of pretrained transformer-based rerankers incurs large computational costs and long query latencies, making those rerankers unrealistic for many real-world applications. For example, according to the ColBERT paper (Khattab and Zaharia, 2020), reranking 1000 hits from the MS MARCO passage dataset takes 32.9 seconds per query. Other researchers have noted the computational costs of transformer-based rankers (Hofstätter and Hanbury, 2019), and this realization has compelled the field to explore other approaches, for example, simplified models (Hofstätter et al., 2020; Soldaini and Moschitti, 2020; Mitra et al., 2020; MacAvaney et al., 2020; Gao et al., 2020; Jiang et al., 2020) and learned dense representations (Xiong et al., 2020; Lin et al., 2020b).

We are also motivated by the desire to reduce the computational costs of ranking with transformers, but from a different perspective. Based on the observation that neural networks in general (and transformers in particular) have largely supplanted feature-based learning to rank (LTR) in modern information retrieval, we ask the question: What, if anything, does "traditional" feature-based learning to rank have to offer in the age of muppets?¹ The subtext of this question is that we, as a field, should not forget our own history.

There are two obvious approaches to try and answer this question. The first is to simply consider transformer-based features (e.g., BERT score, ColBERT score, etc.) as yet another feature within a learning-to-rank framework-for example, with gradient boosted decision trees (Wang et al., 2020). This is not the route that we take, because this approach has less bearing on our desire to increase the efficiency of transformer-based models. Instead, we take the alternative approach of using learningto-rank techniques as a "filtering" stage in a multistage ranking architecture to reduce the number of candidates under consideration by BERT. More concretely, we find that a design based on this idea achieves the same level of effectiveness as a standard retrieve-and-rerank approach using BERT, but is up to $18 \times$ faster. Other effectiveness–efficiency tradeoffs are possible, giving developers a rich design space to build systems tailored to different application scenarios.

The contribution of this work is to demon-

¹Muppets being a whimsical way to refer to BERT and related

transformer models.

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strate that by inserting a "filtering" learning-to-rank stage prior to BERT-based reranking, we can control effectiveness–efficiency tradeoffs in a manner that makes deployments in real-world applications more practical. We emphasize that this work is orthogonal to other methods that directly attempt to accelerate inference, e.g., via knowledge distillation, early exits, model simplifications, etc. It is likely that our gains are cumulative with respect to these enhancements.

2 Methods

2.1 Multi-Stage Ranking

We adopt a standard formulation of multi-stage ranking, which comprises a candidate generation stage H_0 (also called first-stage retrieval), followed by a pipeline of rerankers, denoted H_1 to H_N . Candidate generation is typically accomplished via keyword search against an inverted index, which retrieves k_0 hits from the corpus. Each subsequent stage H_n receives a ranked list R_{n-1} comprising k_{n-1} candidates from the previous stage, reranks these candidates, and then passes the results to the next stage. The output of the last stage serves as the final ranked list, e.g., to be shown to the user or to be evaluated using standard tools.

In this work, we compare two designs of multistage ranking architectures:

BoW + BERT As a baseline, we consider the retrieve-and-rerank approach originally proposed by Nogueira and Cho (2019), which has emerged as the standard architecture for applying pretrained transformers to ranking. We notate a specific configuration of this design as $BoW(k_0) + BERT$, where k_0 denotes the number of candidates from bag-of-words retrieval that are then reranked by BERT. A commonly used default is BoW(1000) + BERT (Nogueira and Cho, 2019).

In addition, we also examine the docTTTTTquery document expansion technique (Nogueira et al., 2019b; Nogueira and Lin, 2019) based on predicting queries for which a text would be relevant (henceforth, just d2q for short). The predicted queries are concatenated to the end of the original text; this greatly improves BoW retrieval. We call this variant BoW_{d2q} and denote the corresponding pipeline BoW_{d2q}(1000) + BERT.

BoW + LTR + BERT This represents our proposed design of introducing a filtering stage before BERT to reduce the number of candidates under consideration. We notate a specific configuration of this design as $BoW(k_0) + LTR(k_1) + BERT$, where k_0 denotes the number of candidates from bag-ofwords retrieval. Our LTR stage then reranks these k_0 hits to generate a new ranking of k_1 hits that are passed to the BERT stage. Similar to BoW_{d2q} , the LTR variant that extracts features from the document expansions is called LTR_{d2q}.

Given this setup, our research question then becomes an effectiveness–efficiency exploration of BoW + BERT vs. BoW + LTR + BERT (including d2q variants). We want to know, given effectiveness parity as a requirement, what degree of latency reduction we can achieve. To answer this question, we adopt the standard setting of LTR as supervised machine learning, where our objective is to maximize recall. We use features extracted from our LTR module to train a model and then apply inference on candidates from the BoW stage, passing on only the most promising ones for (expensive) neural reranking.

2.2 Learning-to-Rank Features

Our LTR features fall into four categories: term-based, score-based, proximity-based, and translation-based. These features are inspired by previous studies on LTR (Qin and Liu, 2013; Gallagher et al., 2020) and summarized in Table 1. An enumeration of all features is presented in Appendix A.

Term-based features Following previous work, we compute different term statistics including term frequency (TF), inverse document frequency (IDF), log term probability, and inverse collection term frequency. Furthermore, existing retrieval models such as BM25 are used to compute the relevance score of a term, and these scores can also be used as term-based features combining different types of statistics. To aggregate term-based statistics for all terms in a query, a number of different aggregation functions are used, e.g., max, min, sum, mean, median, and the ratio between max and min.

Score-based features Term-based statistics are not sufficient as document-level statistics such as document length are also crucial for retrieval effectiveness. Traditional BoW retrieval models (e.g., BM25, Query Likelihood, Divergence From Randomness) have proposed effective ways of combining term-based and document-based statistics, so we also include the retrieval scores of these models

Feature Category	#	Examples
Term-based	54	Max of IDF, Max of TF
Score-based	14	BM25, DFR
Proximity-based	15	Co-occurrences, BM25-TP
Translation-based	4	translation probability

Table 1: Summary of LTR features.

as features. Note that when we use sum as the aggregation function for term-based statistics, we are essentially computing the retrieval model score.

Proximity-based features Traditional retrieval models assume terms are independent and ignore their relationships, but the proximity among query terms often serves as an important relevance signal. Thus, we include features that directly capture the proximity of query terms, such as the counts of ordered and unordered co-occurrence of bigrams within different window sizes. We compute the scores of proximity-based retrieval functions, such as SDM (Metzler and Croft, 2005; Gallagher et al., 2020) and BM25-TP (Lu et al., 2015; Gallagher et al., 2020), as our features.

Translation-based features Capturing semantic relationships between a query and a document is also crucial to improving retrieval accuracy. To incorporate such features, we can use a translation model (Boytsov and Nyberg, 2020; Boytsov and Kolter, 2021) to measure the log translation probability between queries and documents. The conditional probability we need $p(q|d_n)$ is generated by the IBM Model 1 translation model, and the final query–document feature is the sum of all individual conditional query probabilities.

The extraction of all LTR features is performed at the level of tokens. In particular, both queries and documents are tokenized into a multi-field representation. They include: (1) the raw field, which consists of the original tokens; (2) the stemmed field, which includes the stemmed tokens; (3) the subword field, which breaks tokens into subwords; and (4) the d2q field, which includes the stemmed tokens from the concatenated docTTTTTquery predictions (for the d2q variants). For each querydocument pair, feature extraction is repeated over all applicable fields. In total, there are 83 different features (per field) plus four translation-based features that are only available in the raw and subword fields. Table 1 summarizes our features and provides examples for each feature category.

3 Experimental Setup

Data We use the MS MARCO passage ranking dataset (Bajaj et al., 2018) for training and testing. The training set contains \sim 500K queries while the development and test sets contain \sim 7K queries each. On average, each query has only one positive example; negative examples are taken from BM25 results that are not otherwise judged as relevant. Since it is inefficient to use all the negative samples, we downsample to 20 negative examples per query and combine them with all the positive examples to arrive at the training data.

We additionally test on the MS MARCO document ranking task (Bajaj et al., 2018) in a zeroshot manner. For this, we segment each document into multiple passages as the neural models cannot process long documents. Specifically, we use the sliding window strategy of Pradeep et al. (2021), where the window length is ten sentences with a stride of five sentences. Retrieval is performed at the passage level, and the document score is computed based on the highest relevance score among its passages.

Implementation We use Anserini (Yang et al., 2018), an open-source IR toolkit built on Lucene, to build the indexes and retrieve top-ranked candidate passages. For first-stage retrieval, we use BM25, with parameters ($k_1 = 0.82$ and b = 0.68) based on the authors' recommendations to optimize for recall@1000. The retrieved candidate passages are then sent to feature extraction through Anserini's Python interface, Pyserini (Lin et al., 2021).²

For our LTR module, we use the LambdaMART algorithm implemented in LightGBM³ as our model. The hyperparameters are tuned to achieve the highest recall@200 on the development set. Specifically, num_leaves is 200, learning_rate is 0.1, min_data_in_leaf is 50, max_bin is 255. We fix early stopping patience to 200 and use up to 1000 trees. Finally, we utilize batch processing and multi-threading to accelerate the processing. This helps us leverage contemporary multi-core CPUs.

For the final-stage neural reranker, we experiment with BERT-large and T5-base in the PyGaggle library fine-tuned on the MS MARCO passage data.⁴ We simply use checkpoints provided by the library, as our work is not specifically focused

²https://github.com/castorini/pyserini

³https://github.com/microsoft/LightGBM

⁴https://github.com/castorini/pygaggle

Configuration	N	MRR@10	NDCG@10	Lat	ency
BoW(1k) + BERT	1000	0.379	0.441	9.63s	
BoW(10k) + LTR(100) + BERT	100	0.381	0.443	1.32s	(7×)
$BoW(10k) + LTR_{d2q}(20) + BERT$	20	0.382	0.442	0.53s	(18×)
BoW(1k) + T5	1000	0.380	0.443	5.60s	
BoW(10k) + LTR(100) + T5	100	0.382	0.445	0.92s	$(6\times)$
$BoW(10k) + LTR_{d2q}(20) + T5$	20	0.382	0.444	0.46s	(12×)
$BoW_{d2q}(1k) + BERT$	1000	0.389	0.454	9.63s	
$BoW_{d2q}(10k) + LTR_{d2q}(50) + BERT$	50	0.389	0.454	0.83s	(12×)
$BoW_{d2q}(1k) + T5$	1000	0.386	0.453	5.60s	
$BoW_{d2q}(10k) + LTR_{d2q}(50) + T5$	50	0.388	0.454	0.63s	(9×)

Table 2: The effectiveness and efficiency of different pipeline configurations on the MS MARCO passage ranking task. The effectiveness of the pipelines with additional LTR modules are statistically indistinguishable from the baselines without the LTR modules.

on final-stage neural reranking. Previous evaluations (Nogueira and Cho, 2019; Nogueira et al., 2020; Pradeep et al., 2021) have already verified that these two models serve as competitive baselines. We pad all the token sequences in the batch to have the same length and truncate them if their lengths exceed 512 tokens.

Latency Measurements When measuring latency, we used two different servers. The latency of first-stage retrieval and the LTR filtering module is measured on a server equipped with 2 Intel Xeon Platinum 8160 CPUs. The index is located on a local SSD partition. The neural model latency is measured using a 6 core server with a single Tesla V100 GPU. All latency measurements exclude the time to load data and models. Component results are summed to yield end-to-end query latency, which we normalize into a speedup value when comparing different conditions.

4 Results and Analysis

4.1 Results on Passage Ranking

Evaluation results on MS MARCO passage ranking are shown in Table 2 for the various pipeline configurations based on the notation introduced in Section 2. N represents the number of candidates reranked by the final neural reranker, which consumes most of the query time. Note that in these experiments, our goal is to obtain effectiveness parity (i.e., same level of effectiveness) while accelerating inference (i.e., reducing query latency).

The first row in each block of the table represents a baseline configuration, with N set to the common value of 1000. We present six LTR pipelines, where we choose the smallest N (and different k's) that can reach MRR@10 parity with the baseline. We conduct two-tailed paired t-tests to confirm that there are no significant effectiveness differences between results before and after inserting LTR as the filtering stage. Depending on the pipeline setup, we only need to perform neural inference on 20 to 100 candidates-precisely because of our LTR filtering. We report the per-query latency for each configuration and compute a speedup by normalizing against the latency of each baseline. Based on which neural model we use and whether we use d2q, we observe speedups ranging from $6 \times$ to $18 \times$. That is, we can achieve comparable effectiveness with these increases in speed. Note that our baseline BoW + BERT latency is already more than $3 \times$ faster than the values reported by Khattab and Zaharia (2020) (\sim 33s) using the same configuration, primarily due to batch tokenization and other engineering optimizations, so the LTR pipelines are compared against a well-optimized baseline.

Table 3 shows the query latency breakdown for a few representative models. Note that latency is dominated by final-stage neural reranking latency, which scales linearly, so smaller N values (in Table 2) are more desirable. However, this is balanced by the introduction of LTR overhead, both feature extraction as well as the prediction latency itself. Nevertheless, this is a worthwhile tradeoff as we observe large speedups overall. Since T5-base is faster than BERT-large, the effect of the LTR overhead is relatively larger and thus the speedup is lower. We can see that increasing the initial k_0 for BoW from 1k to 10k is acceptable as LTR overhead remains modest.

The most time-consuming step in LTR is feature extraction, and within that, loading the forward in-

Model	Retrieval	Feature Extraction	LTR Prediction	Neural Reranking	Total
BoW(1k) + BERT $BoW(10k) + LTR(100) + BERT$	15 120	- 180	40	9610 980	9630 1320
BoW(1k) + T5 BoW(10k) + LTR(100) + T5	15 120	- 180	40	5580 584	5600 920

Table 3: Detailed breakdown of latency (ms/query) for a few representative pipeline configurations on the MS MARCO passage ranking task.



Figure 1: MRR@10 as a function of N, the number of candidates reranked by the final neural reranker, on the MS MARCO passage ranking task.

dex for each document is the most expensive single step. Our experiments show that the number of features does not affect latency substantially because we only need to load the document once; once in cache, individual feature extraction is very fast. Note that we have not spent much effort optimizing feature extraction (which is relatively inefficient Java code) and that more engineering effort, for example, optimizations proposed by Asadi and Lin (2013), are likely to further increase speedups.

Figure 1 shows the MRR@10 for our five models as a function of N (number of candidates reranked by the final neural reranker), shown on the x-axis (log scale). Effectiveness of the BoW + BERT baseline at N = 1000 is represented as the horizontal line—the effectiveness level we are targeting. Note that for some configurations, we needed to adjust the k_1 for the LTR stage in order to meet the desired N. We can see that our pipelines reach the target MRR@10 with much smaller values of N; reducing expensive neural reranking is where most of our speedups come from. After adding d2q predictions, we are able to achieve our target MRR@10 with an even smaller value of N.

Figure 2 shows the trade-offs between MRR@10 and query latency (the x-axis). Each curve repre-



Figure 2: MRR@10 vs. reranking latency on the MS MARCO passage ranking task.

sents a sweep over N values; we only focus on the case when N is relatively small (< 300). We can see that BoW + LTR + BERT is not helpful if the desired per-query latency is less than 0.5s, because the LTR system itself introduces overhead and leaves little time for neural reranking. For reference, without neural reranking, BoW + LTR only reaches 0.25 MRR@10 while consuming 0.34s; in contrast, spending 0.43s with BoW + BERT achieves 0.28 MRR@10. Between 0.5s and 2s, the effectiveness gap between BoW + BERT and BoW + LTR + BERT increases.

Until now, we have focused on targeting effectiveness parity. What if we're willing to sacrifice effectiveness? Figure 3 uses the BoW + LTR + BERT configuration as an example to show possible speedups and corresponding MRR@10 values if we accept lower effectiveness. We use the latency of BoW(1000) + BERT as our reference point to calculate speedups. For example, in one setting, we can achieve 0.36 MRR@10 using only 20 candidates (N = 20) and enjoy 17× speedup without using d2q (see Table 2).

We also conduct ablation experiments to investigate the importance of the four feature categories used in our LTR module. We use BoW(10k) + LTR(100) + BERT as our base model and assess



Figure 3: MRR@10 vs. speedup for different N, the number of candidates reranked by the final neural reranker, on the MS MARCO passage ranking task.

Configuration	Recall@100	MRR@10
Full Model	0.781	0.382
- Score-based	0.780 (-0.09%)	0.381 (-0.24%)
- Term-based	0.771 (-1.27%)	0.379 (-0.74%)
- Proximity-based	0.767 (-1.76%)	0.379 (-0.96%)
- Translation-based	0.743 (-4.82%)	0.371 (-3.01%)

Table 4: Feature importance ablation results on the MS MARCO passage ranking task.

feature importance by removing each category of features from the LTR module and measuring the effectiveness of the ablated reranker. Table 4 shows the absolute scores and relative differences in terms of recall@100 and MRR@10.

From these results, we can see that the scorebased features appear to be the least important category of features in our model, likely because there is a lot of redundant information between scorebased and term-based features. They use different arithmetic formulas to manipulate the same raw signals: term frequency, document frequency, etc. Compared with term-based features, score-based features are fewer in number. Removing scorebased features has much less impact than removing term-based features.

Translation-based features appear to be the most important feature category: they make the biggest difference in effectiveness with the smallest number of features. The translation model bridges the query–document gap by modeling alternative expressions of query terms and enables a document to match query terms that are not present in the document (i.e., semantic matching).

We also evaluate each feature's importance by the total number of splits and the total gain of splits using a built-in feature in the LightGBM library. We find that all translation-based features rank in the top 10 features with the highest number of splits. This again confirms that matching alternative expressions is an important factor of why our method works. The GL2 model from the Divergence From Randomness family of scoring functions ranks first in terms of total gain of splits, suggesting that traditional bag-of-words retrieval models still form the backbone of learning to rank.

4.2 **Results on Document Ranking**

To explore the generality of our LTR approach, we also conduct experiments on the MS MARCO document ranking task. We emphasize here that all experiments are conducted in a zero-shot manner, over paragraph extracts from the collection, what is commonly known as the MaxP approach (Bendersky and Kurland, 2009; Dai and Callan, 2019; Akkalyoncu Yilmaz et al., 2019; Sheetrit et al., 2020). Both the final-stage neural reranker and our LTR module are trained on MS MARCO *passage* data only. However, comparing our effectiveness results with the official leaderboard reveals that our configurations are competitive compared to other single-stage rerankers.

Results are shown in Table 5, organized in the same manner as Table 2. Recall again that the goal here is also to retain effectiveness parity with respect to the reference reranker (T5 in this case). We conduct two-tailed paired *t*-tests to confirm that there are no statistically significant effectiveness differences between all model configurations. We see that in a zero-shot setting, speedups of nearly $3 \times$ can be observed.

We have a few explanations of why the speedups here are not as impressive as in the passage ranking case. First, because we are not training a corpusspecific model, the power of the LTR module is weaker, and hence the pipeline needs to consider more candidates—larger N means more time in final-stage neural reranking, and hence less savings. Additionally, input to the neural models are on average much longer than the candidates from the passage corpus. This means that there is more text and richer signals for the transformers to extract, which correspondingly means that LTR is more impoverished. Furthermore, longer documents translate into more time spent on feature extraction in LTR. Taken together, all of these issues result in smaller speedups.

Configurlation	N	MRR@100	NDCG@10	Late	ency
$BoW(1k) + T5BoW(10k) + LTR(550) + T5BoW(10k) + LTR_{d2q}(750) + T5$	1000 550 750	$0.405 \\ 0.406 \\ 0.405$	0.470 0.474 0.470	18.2s 10.0s 13.7s	(1.8×) (1.4×)
$\begin{array}{c} BoW_{d2q}(1k) + T5 \\ BoW_{d2q}(1k) + LTR_{d2q}(350) + T5 \end{array}$	1000 350	0.409 0.409	0.476 0.476	18.2s 6.4s	(2.8×)

Table 5: The effectiveness and efficiency of different pipeline configurations on the MS MARCO document ranking task. The effectiveness of the pipelines with additional LTR modules are statistically indistinguishable from the baselines without the LTR modules.

5 Related Work

At a high level, the entire premise of our work is the point of multi-stage ranking, in that the architecture evolved to achieve a good balance between effectiveness and efficiency in end-to-end retrieval. Motivated by the observation, dating back more than a decade, that effective techniques are often computationally expensive, multi-stage retrieval architectures control latency by applying expensive techniques over only the most promising candidates (Wang et al., 2011). This is often operationalized as optimizing for recall in the earlier stages of the pipeline. Specifically in the context of transformers, multi-stage neural pipelines have been explored in the past by many researchers (Nogueira et al., 2019a; Soldaini and Moschitti, 2020; Matsubara et al., 2020; Pradeep et al., 2021). The key difference in our work is the (re-)introduction of "traditional" feature-based learning-to-rank approaches alongside neural models. This aligns with our broader goal of investigating how learning to rank might contribute to modern retrieval approaches dominated by neural models.

The computational costs associated with ranking using pretrained transformers can be reduced in various ways. We can accelerate inference using smaller or simpler models. Gao et al. (2020) use distillation to transfer knowledge captured in a larger model into a smaller model, achieving substantial speedups with minimal effectiveness loss. Hofstätter et al. (2020) propose a simpler transformer model to capture contextual information that trades effectiveness for much faster inference. Additional examples of this approach include Mitra et al. (2020) and MacAvaney et al. (2020). An alternative is to introduce early-exit optimizations, as in Soldaini and Moschitti (2020) and Xin et al. (2020). Further speedups can be gained by making modifications to the backbone transformer model, as in Sanh et al. (2020). The key point is that our

proposed LTR filtering module achieves speedups in a manner that is orthogonal to the methods discussed here, which focus on directly accelerating transformer inference. Thus, these approaches can be combined with our method for even greater efficiency gains.

6 Conclusions

The "retrieve-then-rerank" approach with transformers has been demonstrated to be effective in many IR tasks, but poor efficiency makes it less attractive for real-world applications. Our goal is to increase the efficiency of the entire pipeline but at the same time maintain the same level of effectiveness: this is achieved by a feature-based learning-to-rank module that filters candidates prior to neural reranking. On the MS MARCO passage ranking task, we observe up to $18 \times$ speedup without degradation in terms of MRR@10. In a zeroshot setting on the MS MARCO document ranking task, we can achieve $3 \times$ speedup. These results demonstrate that in this age of muppets dominated by transformers and other neural models, learningto-rank techniques can still be useful. Despite LTR "falling out of fashion", we should not "throw the baby out with the bath water".

One key point that bears emphasis, and one promising direction for future research is that our work can be combined with other approaches that directly accelerate inference in neural models. We expect speedups to be cumulative since we tackle efficiency issues from an orthogonal perspective.

Acknowledgements

The research conducted at the University of Waterloo was supported in part by the Canada First Research Excellence Fund and the Natural Sciences and Engineering Research Council (NSERC) of Canada; computational resources were provided by Compute Canada. The research conducted at the University of Delaware was supported as part of the Center for Plastics Innovation, an Energy Frontier Research Center, funded by the U.S. Department of Energy (DOE), Office of Science, Basic Energy Sciences (BES), under Award Number DE-SC0021166.

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A Appendix

A.1 Full List of LTR Features

Term-based				
				Sum of ICTF
Average of BM25	Average of DFR_GL2	Average of DFR_in_expB2	Average of DPH	Average of ICTF
Median of BM25	Median of DFR_GL2	Median of DFR_in_expB2	Median of DPH	Median of ICTF
Max of BM25	Max of DFR_GL2	Max of DFR_in_expB2	Max of DPH	Max of ICTF
Min of BM25	Min of DFR_GL2	Min of DFR_in_expB2	Min of DPH	Min of ICTF
MaxMinRatio of BM25	MaxMinRatio of DFR_GL2	MaxMinRatio of DFR_in_expB2	MaxMinRatio of DPH	MaxMinRatio of ICTF
Sum of IDF		Sum of Normalized TF	Sum of TF	
Average of IDF	Average of LMDir	Average of Normalized TF	Average of TF	Average of TFIDF
Median of IDF	Median of LMDir	Median of Normalized TF	Median of TF	Median of TFIDF
Max of IDF	Max of LMDir	Max of Normalized TF	Max of TF	Max of TFIDF
Min of IDF	Min of LMDir	Min of Normalized TF	Min of TF	Min of TFIDF
MaxMinRatio of IDF	MaxMinRatio of LMDir	MaxMinRatio of Normalized TF	MaxMinRatio of TF	MaxMinRatio of TFIDF
Score-based				
SCS	Probablity Sum	Doc Size	Query Length	Query Coverage Ratio
Unique Term Count in Query	Matching Term Count	Normalized TFIDF	BM25	LMDir
DFR_GL2	DFR_in_expB2	DPH	TFIDF	
Proximity-based				
UnorderedSequentialPairs with gap 3	OrderedSequentialPairs with gap 3	UnorderedQueryPairs with gap 3	OrderedQueryPairs with gap 3	BM25-TP
UnorderedSequentialPairs with gap 8	OrderedSequentialPairs with gap 8	UnorderedQueryPairs with gap 8	OrderedQueryPairs with gap 8	Proximity
UnorderedSequentialPairs with gap 15	OrderedSequentialPairs with gap 15	UnorderedQueryPairs with gap 15	OrderedQueryPairs with gap 15	TP distance
Translation-based				
title IBM Model1(raw field)	url IBM Model1(raw field)	body IBM Model1(raw field)	body IBM Model (subword field)	