Dorabella Cipher as Musical Inspiration

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Abstract

The Dorabella cipher is an encrypted note written by English composer Edward Elgar, which has defied decipherment attempts for more than a century. While most proposed solutions are English texts, we investigate the hypothesis that Dorabella represents enciphered music. We weigh the evidence for and against the hypothesis, devise a simplified music notation, and attempt to reconstruct a melody from the cipher. Our tools are n-gram models of music which we validate on existing music corpora enciphered using monoalphabetic substitution. By applying our methods to Dorabella, we produce a decipherment with musical qualities, which is then transformed via artful composition into a listenable melody. Far from arguing that the end result represents the only true solution, we instead frame the process of decipherment as part of the composition process.

1 Introduction

The Dorabella cipher (henceforth, simply *Dorabella*) is an encrypted note sent by Edward Elgar, the composer of the "Enigma Variations", to his friend Dora Penny in 1897 (Santa and Santa, 2010). While many cryptography researchers have assumed that the underlying message is an English text, it has also been hypothesized that it may encode music, since Elgar was a composer and a music teacher. This raises several interesting questions. Is it possible to find evidence for or against the music hypothesis? What kind of music notation could be devised with only two dozen possible distinct symbols? How would a musical decipherment compare to the proposed textual decipherments?

In this paper, we attempt to answer these questions in a principled manner, by using n-gram language models derived from collections of transcribed music. However, we also approach musical בשאר הער האש האש האשר שיר הער היי היי איז איז איז איז איז האיז באר האשיע האשר האשיע האשי האשיע האשי האשיע האשי

Figure 1: The Dorabella Cipher.

decipherment as a creative process. We demonstrate this technique on Dorabella, producing a decipherment that has musical qualities, transformed via artful composition into a listenable melody. While prior work typically pursues a single correct decipherment, we instead adopt a creative approach of converting ciphers into music, which might lead to composition of new works.

This paper has the following structure: In Section 2 we provide background on n-grams, perplexity and monoalphabetic substitution ciphers. In Section 3, we discuss prior work. In Section 4, we describe our methodology, including datasets for training language models. In Section 5, we describe our results on encrypted melody samples. In Section 6, our highest-scoring decipherment of Dorabella as a melody is used as inspiration to compose a new work.

2 Background

Substitution ciphers, their properties, and cryptanalysis techniques have been studied for centuries (Singh, 2011). A *monoalphabetic substitution cipher* enciphers a *plaintext* by applying a 1-to-1 mapping of symbols to each character token, producing a *ciphertext* which has a length equal to the length of the plaintext. The symbol mapping function is called the *key*. Given the key, reversing the encipherment process and recovering the plaintext is trivial: simply apply the inverse of the key to each ciphertext when the key is *not* given A2 E3 B2 A3 A1 C2 G1 A3 D1 H2 B3 F2 F1 B1 F2 C3 F2 F2 C2 E3 E3 F2 B1 H1 H2 H1 C1 B3 F3 G1 F2 G1 C2 H1 A3 D1 D2 A3 B2 F2 F2 B2 C2 C1 F1 G1 F2 B3 F2 C2 G2 F3 F1 B1 H1 D1 D1 H1 B3 F3 B2 F3 C2 G2 F3 B2 B1 G2 G3 C1 F3 B2 F2 C2 G2 F1 F3 C1 A3 E3 C1 F3 C2 A3 B1 H1 A3

Figure 2: Our transcription of Dorabella which encodes the orientation and semicircle count of each symbol.

is called *decipherment*. Common measures of the decipherment success are: (1) *decipherment accuracy*, which is the percentage of correctly recovered symbols in the ciphertext; and (2) *key accuracy*, which is the percentage of correctly mapped symbols in the cipher alphabet. Decipherment accuracy is typically higher than key accuracy, because more frequent symbols are more likely to be deciphered correctly.

Computational decipherment methods are based on heuristic search algorithms guided by statistical n-gram language models (Nuhn et al., 2013; Hauer et al., 2014). An n-gram language model estimates the probability of a token in a sequence based on the previous n-1 tokens. If the token is near the beginning of the string, a special start token is used in place of the missing prior tokens. Through repeated applications of this model, the probability of the entire sequence can be estimated. Perplexity is a function of probability, which measures the ability of a statistical model to predict a particular sequence. Lower perplexity indicates that the model is "less surprised" by the data, and so is said to be a better fit. Tokens may be characters or words in natural language, or symbols used in music notation. For compatibility with prior work which models sequences of characters in natural language, we refer to a language model over music notation as a character language model.

3 Prior Work

This section describes prior works that use n-gram models for composition, and prior attempts to solve the Dorabella cipher.

3.1 N-Gram models for composition

N-gram models have been applied to study the structure of music (Manzara et al., 1992) and to compose music. N-gram models in music research and composition range from serial notes, to chords, to pitch and duration pairs (Lo and Lucas, 2006; Wołkowicz et al., 2008), and more complicated structures (McCormack, 1996).

Manzara et al. (1992) investigate the entropy of music from an n-gram perspective. They test how well people can guess the next note, and compare that to n-gram models of Bach's four part *Chorale*. They report that people outperform n-gram models, and that both people and n-gram models have relatively consistent performance.

McCormack (1996) employs n-grams and similar Bayesian structures to compose music. His focus was on Markov chains, which are related to n-gram language models and perplexity estimations.

Lo and Lucas (2006) combine genetic algorithms and n-gram language models to evolve musical sequences. The n-gram models act as fitness functions to guide the creation of musical sequences that have lower perplexity given an n-gram language model. In addition, they use their models to identify composers.

Wołkowicz et al. (2008) also use n-grams to identify composers. They process MIDI files and produce n-grams of pitch and duration tuples. They achieve up to 84% accuracy at identifying composers using a large corpus of 10000 notes of each composer's work, and about 54% accuracy when using only 100 notes, which is at a similar level of accuracy as Lo and Lucas (2006).

3.2 Dorabella Cipher

The earliest computational attempt at solving the Dorabella Cipher that we are aware of is that of Sams (1970). He applies statistical analysis based on character frequencies and brute force cryptanalysis. The work considers the assumptions that the cipher encrypts English text which may be partly phoneticized, is not strictly monoalphabetic, and may involve multiple layers of encryption. The author ultimately proposes the following solution to the cipher: *"Larks! It's chaotic, but a cloak obscures my new letters, a, b. I own the dark makes E. E. sigh when you are too long gone."*

Santa and Santa (2010) provide an overview of Elgar's work on cryptography, focusing on the "enigma" that he implied to be hidden within his musical piece *Variations on a Theme*. They note the connections Elgar made between that piece and Dorabella, neither of which has been conclusively solved. despite this and other "hints" from Elgar. In particular, they raise the possibility of mathematical concepts being used in Dorabella, specifically the constant π , as well as the encoding of scaledegrees with numerical values.

As well-known techniques, such as frequency analysis, have not proven effective on Dorabella, Schmeh (2018) proposes to consider less common techniques. These include vowel detection and a frequency-based consonant identification method. The author applies these techniques both to Dorabella, and on a control plaintext. He does not propose a solution to Dorabella, but demonstrates that these methods can distinguish between vowels and consonants in the control cipher. With the same techniques, he attempts to identify some Dorabella symbols as vowels or consonants. He also notes that certain statistical properties of Dorabella are consistent with English text.

Packwood (2020) proposes a natural language solution to Dorabella. The method is complex, and involves breaking the cipher into discrete blocks, among which patterns can be observed, and an elaborate system of transposition. The author further speculates that the cipher also conceals a musical composition, but makes no attempt at a musical decipherment.

Hauer et al. (2021) experiment with several monoalphabetic substitution cipher solvers to decipher music. They rely on a corpus of Bach and Elgar MIDI files, and try to decipher synthetic music ciphers using a pitch/duration language model, but the results are quite low compared to textual ciphers. They conclude that it is unlikely that Dorabella represents music encoded using an alphabet of pitch and duration.

4 Methodology

In this section, we describe our methodology, including datasets for training language models.

4.1 Transcribing Dorabella

The first step is to render Dorabella into a machinereadable form. In order to establish such a transcription, we compared five different manual transcriptions attempts, including Schmeh (2018), Hartmeier (2017), Pelling (2012), as well as transcriptions by two of the authors of this paper. A majority consensus transcription is shown in Figure 2. It consists of 87 tokens made of an uppercase letter encoding the symbol orientation, followed by the number of semicircles. There are 8 possible orientations (A-H), while the number of semicircles ranges from 1 to 3.

4.2 Pitch-Duration Dataset and Encoding

We use the music dataset created by Hauer et al. (2021). The dataset was created from MIDI files, a form of digitally representing musical composition which encodes pitch, pitch amplitude, and duration over a timeline, usually including metric and tempo information. The files represent music from both Elgar and Bach. The Elgar data consists of 29 files containing a total of 1.2M notes, while the Bach data consists of 295 files containing 3.7M notes. We include the Bach data due to the relatively small size of the Elgar corpus; this increases the total size of our data by a factor of four. Each dataset is divided into training and testing splits. This is done to ensure that experimental results are generalizable to data not used to provide statistical information for the models used by the decipherment algorithms. The test set is further divided into 87-note sequences, the same length as Dorabella.

Hauer et al. (2021) assume that enciphered music must, before encipherment, be represented in some serial, symbolic notation. To this end, they transpose all music into the key of C major, and use only one octave. All symbols except notes (e.g. rests) are removed. All notes are normalized to one of three durations: quarter note, shorter than a quarter note, or longer than a quarter note. Further, all notes were normalized to one of the eight most frequent notes: A, B, C, D, E, F, F[#], and G. Thus, just as each Dorabella cipher symbol has one of three semicircle counts and one of eight orientations, giving a theoretical vocabulary of 24 symbols, the encoding assigns to each symbol one of three durations and one of eight notes, yielding 24 distinct symbols. While there is much more information encoded in musical notation, we are constrained by the 24-symbol alphabet of the cipher. For example, if we assumed that some cipher symbols represent rests, we would need to further reduce the already limited range of notes that the cipher can represent. While this encoding was designed to match the form of the Dorabella cipher, we present a more principled approach in Section 4.4.

4.3 English Dataset

To assess the ability of our statistical models to fit music, we induce models of both music and English, and compare the fitness of our modelling method on different types of data. We use the English language dataset of Hauer et al. (2021), which is a subset of the letters of Jane Austen. This corpus was deemed appropriate since it consists of written epistolary correspondences, which is the hypothesized domain of Dorabella. The text was first processed to remove all non-alphabetic characters, including white space. 300 excerpts from the corpus were selected at random, each consisting of a sequence of 87 characters. We use this set of 300 texts for the perplexity measurement experiment described in Section 5.

4.4 Melody Dataset

We experiment with the CANTUS corpus of folk music (Lacoste, 2012). We conjecture that Elgar would be more likely to create something that reflected contemporary styles of folk music rather than the more complex, and often more chromatically adventurous music of his own. This leads us to consider musical databases that are limited to a single line of music, as well as to simplify the issues around key signature, meter, rhythm, and other factors. Our melody corpus reduces all examples to the common key of C. We also chose to not attempt to model rhythms, dynamics, articulations, and other components, looking mainly at pitch, and assuming 4/4 meter. There are other composition decisions which could have been made. Given the extremely small set of symbols, and the short length of the cipher, we necessarily had to make some simplifying assumptions, and we did so based on our intuitions regarding what setting would produce the most natural-sounding composition.

Our melody dataset is from the CANTUS Database of chants and melodies (Lacoste, 2012; Helsen and Lacoste, 2011), an online searchable database that encodes melodies as sequences of pitches without including their durations.¹ Table 1 shows the sources of melodies in the CANTUS dataset and their average length. The melodies in CANTUS are monophonic, and most include notes in the range of F3 to D6. Since there are only 17 distinct notes in our subset of CANTUS, we interpolate the range from A3 to E6 to yield 24 symbols used to decipher Dorabella: A3, Bb3, B3, F3, G3, A4, Bb4, B4, C4, D4, E4, F4, G4, A5, Bb5, B5, C5, D5, E5, F5, G5, C6, D6, E6. Because of the smaller alphabet and vocabulary of the melody dataset, we expect it to have lower perplexity, which should lead to better results than with the dataset described in Section 4.2.

	Name	Dataset	Melodies	Length
-	Gloria	mbos	102	8.9
	Kyrie	mmel	226	8.7
	Agnus Dei	mscb	267	8.9
	Alleluia	msch	409	34.9
	Hymn	msta	344	49.4
	Sanctus	mtha	228	9.0
		All	1576	

Table 1: Melody datasets extracted from CANTUS (Lacoste, 2012; Helsen and Lacoste, 2011)

Our training corpus is created by randomly sampling 467 melodies without replacement. Our datasets, code, and compositions are released at: https://zenodo.org/record/4764819

4.5 Decipherment

As our decipherment method for enciphered music, we use the solver of Norvig (2009), which we refer to as HILLCLIMBC.² We selected it for its effectiveness on deciphering monoalphabetic substitution ciphers, even when word boundaries are not preserved in the cipher. This is important, as our encoding of music has no analogy to word boundaries, and no such boundaries are indicated in Dorabella. The solver maximizes the probability of the decipherment as estimated by a trigram character language model. Starting from a random initial key, HILLCLIMBC applies a hill climbing algorithm as a heuristic search strategy. At each step, many successor keys are generated by applying permutations to the current key; whichever successor gives the greatest increase in probability (equivalently, the greatest decrease in perplexity) becomes the key in the next iteration. We run the algorithm for 4000 iterations, with 90 random restarts. The decipherment with the lowest perplexity across all iterations is returned.

5 Decipherment Results

Table 2 shows the decipherment results on a test set of 300 distinct melody samples, sampled without replacement from the corresponding training set. Clearly, the results on the melody dataset are much better than those on the pitch/duration datasets, which in turn are better for Bach than for Elgar. The mean key accuracy across all examples in the melody dataset is 50%, that is, half of the key symbols are correct. Approximately half of ciphers

¹An example melody http://cantusindex.org/ melody/msch001

²http://norvig.com/ngrams

Source	Key Acc	Dec Acc
pitch/duration (Elgar)	7.0%	12.0%
pitch/duration (Bach)	26.5%	32.0%
melody (CANTUS)	50.0%	54.5%

Table 2: HILLCLIMBC results on music ciphers of length 20,000.

were deciphered with 70% decipherment accuracy or higher, and nearly one third of ciphers were deciphered entirely correctly. This suggests that our approach is effective for melody decipherment.

One reason for the lower accuracy on the pitch/duration datasets may be their quality. The original MIDI files were created by multiple authors, leading to a low consistency in musical transcription. In addition, the files are polyphonic; even for piano music, they often have separate channels for each hand. On the other hand, our melody dataset is monophonic and consistently transcribed.

Dataset	Average Perplexity
English (Austen)	16.2
pitch/duration (Elgar)	24.4
pitch/duration (Bach)	24.5
melody (CANTUS)	5.6

Table 3: Average perplexity using a trigram character language model.

Another possible explanation for the divergent performance could be the encoding. Table 3 shows the perplexity of different datasets. We used trigram language character models with modified Kneser-Ney smoothing and discounts. The relatively high perplexity values of the pitch/duration datasets suggests that the pitch-only encoding may be better suited to modelling music than the pitch/duration encoding. Indeed, based on these results, predicting the next note of a melody is easier than than predicting the next English character in a sentence.

6 Composition from Decipherment

In this section we apply our algorithm to the Dorabella cipher, and take the resulting melody as a basis for a composition. In particular, we manually analyze the output for musical content, and modify it according to subjective musical tastes. This creative process is guided by the familiarity with the composer's style, and is not itself replicable. E6 B5 A4 B4 B3 F4 D6 B4 E5 F5 G5 G4 C4 C5 G4 A5 G4 G4 F4 B5 B5 G4 C5 D5 F5 D5 Bb4 G5 D4 D6 G4 D6 F4 D5 B4 E5 C6 B4 A4 G4 G4 A4 F4 Bb4 C4 D6 G4 G5 G4 F4 E4 D4 C4 C5 D5 E5 E5 D5 G5 D4 A4 D4 F4 E4 D4 A4 C5 E4 A3 Bb4 D4 A4 G4 F4 E4 C4 D4 Bb4 B4 B5 Bb4 D4 F4 B4 C5 D5 B4

Figure 3: A decipherment of Dorabella as melody.

Figure 3 shows our highest-scoring decipherment of Dorabella assuming 4/4 time. Figure 4 depicts its musical transcription, which was obtained by applying HILLCLIMBC with a language model derived from the melody dataset (467 samples). This decipherment attempt has some interesting musical features. The notes in Figure 4 seem at times to imply logical harmonic progressions. In the second half, there are even moments of motivic repetition, albeit not exact, which evoke a musical composition.

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Figure 4: Note output from Dorabella

After manual analysis we decided to realign the notes from the 4/4 meter to the 3/4 meter, as this appears to fit better the contours and implied harmonic progression. Surprisingly, the melody seems to be match two 16-bar 3/4 phrases, except for a premature end in the second phrase. Considering that we only use quarter-note rhythms, this could be an illusion, but the resulting musical piece is intriguing. In the spirit of the creative process, we also decided to relax the strict matching of the decipherment symbols into notes.

Figure 5 shows the final version of the output in which some notes (shown in red) have been altered or added in order to create a cadential con-



Figure 5: Adjusted output, with chords. Notes which have been modified from the output in Figure 4 are color-coded red.

clusion. Interestingly, our altered 32-bar segment features a highly disjunct first 16-bar phrase, with an altered pitch (B-flat) implying a potential transposition, and a second phrase that is much more lyrical and based on smaller step-wise intervals, complete with the "repeated motive." Upon adding the implied harmonic accompaniment, we can see that in some cases there even seem to be an implied V-I cadences, such as between mm. 16-17, mm. 24-25, and the final added measures. Adding some phrasing and interesting timbres, as well as chords based on the implied harmony, gives us the audio rendering³ shown in Figure 5.

It is important to point out several caveats to this seemingly encouraging result. First and foremost, any analysis of musical composition necessarily has subjective elements. Second, we assume that rhythmic values are not encoded in the cipher, and limit the decipherment to quarter-notes. It is also possible that the score may not be connected to common practice notation or even diatonic pitches at all. For example, these could be referring to a very specific set of church bells, or perhaps some other kind of instrument or sonic contraption, or even just rhythm.

7 Conclusions

Although we do not claim to have solved the mystery of Dorabella, our process produced a listenable melody, which opens up interesting avenues of investigation. In the future, we plan to experiment with different corpora and musical attributes, such as rhythm only. Our approach represents a creative way to generate new forms of musical melodies. What seems certain is that Elgar's intention to confound left us with a tantalizing riddle that invites further speculation in the future.

References

- Daniel Hartmeier. 2017. Clues (or red herrings) to the Dorabella cipher. *benzedrine.ch*. https://www. benzedrine.ch/dorabella.html.
- Bradley Hauer, Colin Choi, Anirudh Sundar, Abram Hindle, Scott Smallwood, and Grzegorz Kondrak. 2021. Experimental analysis of the Dorabella cipher with statistical language models. In *Proceedings of the International Conference on Historical Cryptology (HistoCrypt)*.

- Bradley Hauer, Ryan Hayward, and Grzegorz Kondrak. 2014. Solving substitution ciphers with combined language models. In Proceedings of COL-ING, the 25th International Conference on Computational Linguistics: Technical Papers, pages 2314– 2325, Dublin, Ireland.
- Kate Helsen and Debra Lacoste. 2011. A report on the encoding of melodic incipits in the cantus database with the music font'volpiano'. *Plainsong & Medieval Music*, 20(1):51.
- Debra Lacoste. 2012. The cantus database: Mining for medieval chant traditions. *Digital Medievalist*, 7.
- ManYat Lo and Simon M Lucas. 2006. Evolving musical sequences with n-gram based trainable fitness functions. In 2006 ieee international conference on evolutionary computation, pages 601–608. IEEE.
- Leonard C Manzara, Ian H Witten, and Mark James. 1992. On the entropy of music: An experiment with Bach chorale melodies. *Leonardo Music Journal*, 2(1):81–88.
- Jon McCormack. 1996. Grammar based music composition. In In R. Stocker et al. (Eds.), From Local Interactions to Global Phenomena, Complex Systems 96. ISO Press.
- Peter Norvig. 2009. Natural language corpus data. In Toby Segaran and Jeff Hammerbacher, editors, *Beautiful Data: The Stories Behind Elegant Data Solution*, pages 219–242. O'Reilly Media.
- Malte Nuhn, Julian Schamper, and Hermann Ney. 2013. Beam search for solving substitution ciphers. In Proceedings of the 51st Annual Meeting of the Association for Computational Linguistics, pages 1568– 1576.
- Wayne Packwood. 2020. Elgar as cryptographer tuning and turing. *Musical Opinion Quarterly*, pages 34–37.
- Nick Pelling. 2012. Dorabella cipher. Cipher Mysteries.
- Eric Sams. 1970. Elgar's cipher letter to Dorabella. *The Musical Times*, 111(1524):151–154.
- Charles Richard Santa and Matthew Santa. 2010. Solving Elgar's Enigma. *Current Musicology*.
- Klaus Schmeh. 2018. Examining the Dorabella Cipher with three lesser-known cryptanalysis methods. In Proceedings of the International Conference on Historical Cryptology (HistoCrypt), pages 145–152.
- Simon Singh. 2011. *The code book: the science of secrecy from ancient Egypt to quantum cryptography.* Anchor.
- Jacek Wołkowicz, Zbigniew Kulka, and Vlado Kešelj. 2008. N-gram-based approach to composer recognition. *Archives of Acoustics*, 33(1):43–55.

³https://zenodo.org/record/4764819/ files/fig3.wav?download=1