

Learning Numeral Embedding

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Abstract

Word embedding is an essential building block for deep learning methods for natural language processing. Although word embedding has been extensively studied over the years, the problem of how to effectively embed numerals, a special subset of words, is still under-explored. Existing word embedding methods do not learn numeral embeddings well because there are an infinite number of numerals and their individual appearances in training corpora are highly scarce. In this paper, we propose two novel numeral embedding methods that can handle the out-of-vocabulary (OOV) problem for numerals. We first induce a finite set of prototype numerals using either a self-organizing map or a Gaussian mixture model. We then represent the embedding of a numeral as a weighted average of the prototype number embeddings. Numeral embeddings represented in this manner can be plugged into existing word embedding learning approaches such as skip-gram for training. We evaluated our methods and showed its effectiveness on four intrinsic and extrinsic tasks: word similarity, embedding numeracy, numeral prediction, and sequence labeling.

1 Introduction

Word embeddings have become an essential building block for deep learning approaches to natural language processing (NLP). The quality of pre-trained word embeddings has been shown to significantly impact the performance of neural approaches to a variety of NLP tasks. Over the past two decades, significant progress has been made in the development of word embedding techniques (Lund and Burgess, 1996; Bengio et al., 2003; Bullinaria and Levy, 2007; Mikolov et al., 2013b; Pennington et al., 2014). However, existing word embedding methods do not handle numerals

adequately and cannot directly encode the numeracy and magnitude of a numeral Naik et al. (2019). Most methods have a limited vocabulary size and therefore can only represent a small subset of the infinite number of numerals. Furthermore, most numerals have very scarce appearances in training corpora and therefore are more likely to be out-of-vocabulary (OOV) compared to non-numerical words. For example, numerals account for 6.15% of all unique tokens in English Wikipedia, but in GloVe (Pennington et al., 2014) which is partially trained on Wikipedia, only 3.79% of its vocabulary is numerals.

Previous work (Spithourakis et al., 2016) also shows that the numeral OOV problem is more severe when learning word embeddings from corpora with abundant numerals such as clinical reports. Even if a numeral is included in the vocabulary, its scarcity in the training corpus would negatively impact the learning accuracy of its embedding. The inadequate handling of numerals in existing word embedding methods can be problematic in scenarios where numerals convey critical information. For instance,

- “Jeff is **190**, so he should wear size XXL.” (190 is a reasonable height for size XXL. If we replace 190 with 160, the sentence becomes unreasonable.)
- “Jeff is **10**, so he should wear size XS.” (10 is an age instead of a height.)

If the numerals in the example are OOV or their embeddings are not accurately learned, then it becomes impossible to judge the categories of the numerals or the reasonableness of the sentences. In this paper, we propose two novel methods that can produce reasonable embeddings for any numerals. The key idea is to represent the embedding of a numeral as a weighted average of a small set

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of prototype number embeddings induced from the training corpus using either a self-organizing map (Kohonen, 1990) or a Gaussian mixture model. The weights are computed based on the differences between the target numeral and the prototype numerals, reflecting the inductive bias that numerals with similar quantities are likely to convey similar semantic information and thus should have similar embeddings. Numeral embeddings represented in this manner can then be plugged into a traditional word embedding method for training. We empirically evaluate our methods on four tasks: word similarity, embedding numeracy, numeral prediction, and sequence labeling. The results show that our methods can produce high-quality embeddings for both numerals and non-numerical words and improve the performance of downstream tasks.

2 Related Work

Word Embedding Word embeddings are vector representations of words that carry semantic meanings implicitly and are trained without supervision. Most existing word embedding training methods can be divided into two classes. The first class of methods (Lund and Burgess, 1996; LeBret and LeBret, 2013) extract word co-occurrence statistics from the training corpus, compute a word-word matrix based on measures such as PPMI, and then apply dimension reduction techniques such as principle component analysis to produce a low-dimensional representation for each word. The second class of methods (Bengio et al., 2003; Collobert and Weston, 2008; Mikolov et al., 2013a,b) use a simple neural network to model the relation between a word and its context within a sliding window in the training corpus. GloVe (Pennington et al., 2014) has been proposed as a method that combines the advantages of both classes. All the above methods have a finite vocabulary size and use a ‘UNK’ symbol to represent OOV words. Recent work (Naik et al., 2019) shows that these popular methods do not handle numerals adequately. Wallace et al. (2019) shows that existing word embedding methods can encode numeracy implicitly for high-frequency numerals, but the embedding’s numeracy for OOV numerals is not investigated. Our goal is to design numeral embedding methods that can be integrated into traditional word embedding methods and handle the OOV problem for numerals.

Numeracy in natural language Numeral understanding has been found important in textual entailment (Lev et al., 2004; De Marneffe et al., 2008; Roy et al., 2015) and information extraction (Intxaurreto et al., 2015; Madaan et al., 2016), but existing systems often use manually defined task-specific features and logic rules to identify numerals, which is hard to generalize to other tasks. A lot of research has been done trying to solve math problems, using either manually designed features and rules (Roy et al., 2015; Upadhyay et al., 2016) or sequence-to-sequence neural networks (Wang et al., 2017), but the quantity of numerals is not important in this task and hence existing methods often replace numerals by dummy symbols such as n_1 and n_2 . Spithourakis and Riedel (2018) studied different strategies to better model numerals in language models. Chen et al. (2019) created Numeracy-600K dataset and studied the ability of neural network models to learn numeracy. Our work differs from previous work in that we aim to produce general-purpose numeral embeddings that can be employed in any neural NLP approach.

3 Methods

Given a training corpus C , we first extract all the numerals using regular expressions and form a dataset X containing all the numbers represented by these numerals. A number (e.g., 2000) may appear for multiple times in X if its corresponding numerals (e.g., ‘2000’, ‘2,000’, etc.) appear for multiple times in C . We then induce a finite set \mathbb{P} of typical numerals (i.e., prototypes) from X using a self-organizing map (Kohonen, 1990) or a Gaussian mixture model. We also define a function $\text{sim}(n_1, n_2)$ outputting the similarity between two arbitrary numbers n_1 and n_2 . Now we represent the embedding of any target numeral n as a weighted average of the prototype number embeddings with the weights computed by the similarity function:

$$e(n) = \sum_{p \in \mathbb{P}} \alpha \cdot \text{sim}(n, p) \cdot e(p) \quad (1)$$

We use $e(\cdot)$ to denote the embedding of a number, α is the normalization factor where $\sum_{p \in \mathbb{P}} \alpha \cdot \text{sim}(n, p) = 1$. This formulation satisfies the intuition that numerals with similar quantities are likely to convey similar semantic information and should have similar embeddings.

Our numeral embeddings can be integrated into traditional word embedding methods such as skip-

gram for training. During training, we back-propagate the error gradient to update the prototype embeddings. In this way, the prototype embeddings (and hence all the numeral embeddings) are learned jointly with non-numerical word embeddings.

3.1 Squashing numbers to log-space

Inspired by psychological evidence that our brain compresses large quantities nonlinearly using a logarithmic scale on the mental number line (Nieder and Miller, 2003; Dehaene, 2011), we design the following squashing function to transform all the numbers in X into the log-space before prototype induction. Alternatively, we can apply the function only in the similarity function. Squashing is also necessary for our methods to avoid overflow during training when there are very large numbers such as 10^{15} in the training corpus.

$$f(x) = \begin{cases} \log(x) + 1, & \text{if } x > 1 \\ x, & \text{if } x \in [-1, 1] \\ -\log(-x) - 1, & \text{if } x < -1 \end{cases} \quad (2)$$

3.2 Prototype Induction

We develop two methods for inducing a small set P of m prototypes from the number dataset X .

Self-Organizing Map A self-organizing map (SOM) (Kohonen, 1990) is a neural network that can be viewed as a clustering method. After training a SOM on the dataset X , we regard each cluster centroid as a prototype. One advantage of using a SOM in comparison with traditional clustering methods is that it distributes prototypes more evenly on the number line and may assign prototypes to number ranges with few training samples, which we expect would lead to better generalizability.

Gaussian Mixture Model Inspired by psychological study of the mental number line (Dehaene et al., 2003) and previous work on language modeling (Spithourakis and Riedel, 2018), we train a Gaussian mixture model (GMM) to induce number prototypes. A GMM is defined as follows.

$$\begin{aligned} p(U = n) &= \sum_{k=1}^m P(Z = k)P(U = n|Z = k) \\ &= \sum_{k=1}^m \pi_k \mathcal{N}(n; \mu_k, \sigma_k^2) \end{aligned} \quad (3)$$

where Z is a latent variable representing the mixture component for random variable U , and \mathcal{N} is

the probability density function of a normal distribution, and $\pi_k, \mu_k, \sigma_k \in \mathbb{R}$ represent the mixing coefficient, mean and standard deviation of the k -th Gaussian component. We train a GMM on the number dataset X using the expectation-maximization (EM) or hard-EM algorithm and regard the means of the learned Gaussian components as prototypes $\mathbb{P} = \{\mu_1, \dots, \mu_m\}$. We use three GMM initialization methods described in Appendix A.

3.3 Similarity Function

For SOM-induced prototypes, we define the following similarity function:

$$\text{sim}(p, n) = |g(p) - g(n)|^{-\beta}, \quad \beta > 0, \quad p \in \mathbb{P} \quad (4)$$

where function g is equal to the squashing function f defined in Eq. 2 if we do not apply log transformation before prototype induction and is the identity function I otherwise. β is a hyper-parameter set to 1.0 by default.

For GMM-induced prototypes, we can naturally use the posterior probability of the component assignment to define the similarity function, for all $p_k \in \mathbb{P}$,

$$\begin{aligned} \text{sim}(p_k, n) &\propto P(Z = k|U = n) \\ &= \frac{\pi_k \mathcal{N}(n; \mu_k, \sigma_k^2)}{\sum_{k=1}^m \pi_k \mathcal{N}(n; \mu_k, \sigma_k^2)} \end{aligned} \quad (5)$$

3.4 Embedding Training

We now describe how to integrate our numeral embeddings into traditional word embedding methods for training. We choose skip-gram with negative sampling (Mikolov et al., 2013b) as the word embedding method here, but many other word embedding methods such as CBOW (Mikolov et al., 2013a), HAL (Lund and Burgess, 1996) and GloVe (Pennington et al., 2014) can be used as well. Skip-gram is a word embedding method based on the idea of context word prediction. The training corpus C is regarded as a sequence of words (x_1, \dots, x_T) . For token x_t , we define the preceding and following c tokens as the context of x_t . Skip-gram aims to maximize $p(x_{t+j}|x_t)$ ($-c \leq j \leq c$), the probability of a context word given the center word x_t . To formulate $p(x_{t+j}|x_t)$, skip-gram associates each word x_i with two vector representations: the input embedding $v_{x_t}^i$ for being a center word and the output embedding $v_{x_t}^o$ for being a context word. The input and output embeddings of all the words in the vocabulary \mathbb{V} constitute matrices $E_I \in \mathbb{R}^{D \times |\mathbb{V}|}$ and $E_O \in \mathbb{R}^{D \times |\mathbb{V}|}$ respectively,

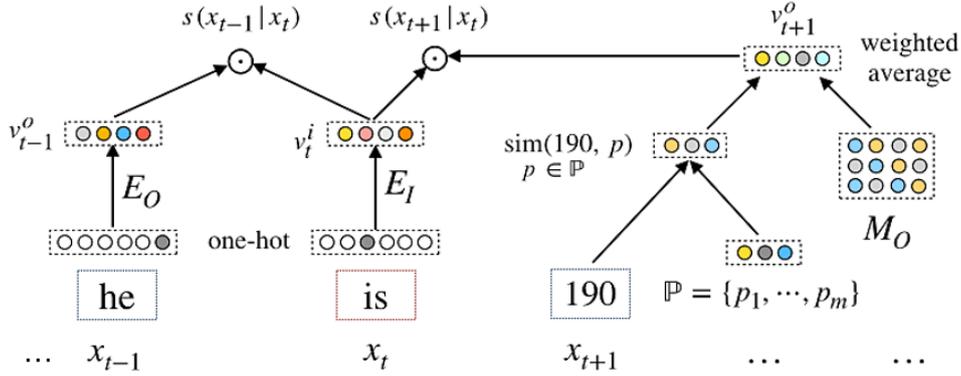


Figure 1: The computational graph when the center word is ‘is’ and the context words are ‘he’ and the numeral ‘190’. We look up the embedding vectors of non-numerical words directly from the embedding matrices and use the weighted average of prototype embeddings as the numeral embedding. Negative sampling is not shown in the figure.

where D is the embedding dimension. The conditional probability $p(x_{t+j}|x_t)$ is then defined to be based on the dot product $s(x_{t+j}|x_t) = \mathbf{v}_{x_t}^i \cdot \mathbf{v}_{x_{t+j}}^o$. Negative sampling is used to approximate the normalization factor for the conditional probability.

$$\log p(x_{t+j}|x_t) \approx \log \sigma(\mathbf{v}_{x_{t+j}}^o \cdot \mathbf{v}_{x_t}^i) + \sum_{i=1}^k \mathbb{E}_{x_i \sim P_n(x)} [\log \sigma(-\mathbf{v}_{x_i}^o \cdot \mathbf{v}_{x_t}^i)] \quad (6)$$

where σ denotes the sigmoid function, and $P_n(x)$ is the sampling distribution used to draw k negative word samples. We modify skip-gram by computing numeral embeddings differently from non-numerical word embeddings. We associate each prototype number with an input embedding and an output embedding. The input and output embeddings of all the prototypes constitute matrices $M_I \in \mathbb{R}^{D \times |\mathbb{P}|}$ and $M_O \in \mathbb{R}^{D \times |\mathbb{P}|}$ respectively. For any numeral, we can compute its input and output embeddings by taking a weighted average of the prototype input and output embeddings respectively based on Eq.1 and use them in exactly the same way as the embeddings of non-numerical words to compute the learning objective (Eq.6). When drawing negative samples, we first set the ratio of numerals and non-numerical words to their actual ratio in the training corpus, to guarantee a sufficient number of numeral negative samples. Then we sample numerals and non-numerical words separately from their respective distributions in the training corpus raised to the power of $\frac{3}{4}$. During training, we optimize the objective function Eq.6 by back-propagating the gradient of the error to update both the non-numerical word embed-

ding matrices E_I , E_O and the prototype number embedding matrices M_I , M_O . In this way, the embeddings of non-numerical words and numerals are learned jointly in the same space. We show an example in Figure 1.

4 Experiments and Results

We evaluate our methods on four intrinsic and extrinsic tasks: word similarity, embedding numeracy, numeral prediction, and sequence labeling. We report the results of our methods based on SOM and GMM separately. We choose the hyper-parameters (e.g., the number of prototypes, GMM initialization and training methods) using validation sets and report the best hyper-parameters for each experiment in Appendix.B.

4.1 Baselines

NumAsTok This baseline treats numerals and non-numerical words in the same way, which is very similar to the original skip-gram. The vocabulary includes both high-frequency words and high-frequency numerals. OOV non-numerical words are replaced with symbol UNK_{word} and OOV numerals are replaced with symbol UNK_{num} .

D-LSTM Character-level RNNs are often used to encode OOV words (Graves, 2013). Here we apply an LSTM (Hochreiter and Schmidhuber, 1997) to the digit sequence of a numeral and use the last hidden state of the LSTM as the embedding of the numeral. We use the embedding to compute the skip-gram objective function and propagate the gradients back to update the LSTM. The vocabulary of digits is: $\{0-9, ‘.’, ‘+’, ‘-’, ‘e’\}$.

	Non-numerical Word Vocabulary	Numeral Vocabulary
SOM, GMM, D-LSTM, Fixed	{In-vocab words} UNK _{word}	all numerals
NumAsTok	{In-vocab words} UNK _{word}	{In-vocab nums} UNK _{num}

Table 1: Vocabularies of different methods.

Methods	WS353	MEN	SIM999
SOM	64.40	71.79	36.09
GMM	64.90	71.89	36.29
NumAsTok	65.30	71.83	35.85
D-LSTM	63.60	71.82	34.58
Fixed	64.35	72.17	36.27
SG GoogleNews-100B	70.00	74.10	44.20
GloVe Wiki-6B	52.20	73.70	37.10

Table 2: Results on word similarity tasks trained on Wiki-1B. For reference, we also show the results of the official skip-gram and GloVe trained on larger corpora.

Fixed This baseline fixed embeddings for numerals with no training. We define the embedding a numeral with value n as $[f(n); \mathbf{1}]/Z$ where f is the squashing function defined in Eq.2, $\mathbf{1} \in \mathbb{R}^{D-1}$ is an all-ones vector, and Z is a constant used to keep the vector norm close to those of non-numerical words and is set to $2 \times D$ by default.

We compare the vocabularies of different methods in Table 1. Our methods, D-LSTM, and Fixed have finite non-numerical vocabularies but infinite numeral vocabularies. In contrast, the NumAsTok baseline has a finite numeral vocabulary and treats all the OOV numerals as UNK_{num}.

4.2 Word Similarity for Non-numerical Words

To ensure that our methods can still generate high quality embeddings for non-numerical words, we evaluate our trained embeddings on classical intrinsic word similarity tasks, including WordSim-353, (Finkelstein et al., 2001), MEN (Bruni et al., 2014) and Simplex-999 (Hill et al., 2014). We train 300-dimensional word embeddings on the 1B Wikipedia dump and set the context window size to 5, the number of negative samples to 5, and the vocabulary size to 3×10^5 . We use the evaluation tools¹ provided by Jastrzebski et al. (2017). Note that while the training data contains numerals, the evaluation tasks do not involve numerals and are only designed to evaluate the quality of

¹<https://github.com/kudkudak/word-embeddings-benchmarks>

non-numerical word embeddings. The results are shown in Table 2.

It can be seen that our methods can achieve scores comparable to those of the baselines. The performance of SG trained on 100B GoogleNews is much better than all the other methods probably because of its much larger training corpus. The results show that adding our numeral embedding methods into skip-gram does not harm the quality of non-numerical word embeddings. We also show some examples of prototypes and their nearest non-numerical words in Table 3, and some additional results of our methods in Appendix.C. The results show that our embedding method learns the semantic of numerals. We use the embedding trained by the SOM model with 200 prototypes on Wikipedia-1B.

Prototype	Most Related Non-numerical Words
8186446.58	million, billion, total, budget, funding, dollars
10372.49	approximately, thousands, millions, roughly
2000.06	millennium, decade, internet, twentieth, worldwide, latest
1598.79	renaissance, giovanni, dutch, baroque, vii, shakespeare
10.00	ten, six, eleven, pm, seconds, eight

Table 3: Examples of prototypes and their nearest non-numerical words.

4.3 Magnitude and Numeration of Embeddings

Naik et al. (2019) propose a framework for evaluating the ability of numeral embeddings to capture magnitude and numeration. Given a target numeral, its embedding is evaluated against a set of numerals using the **OVA (One-vs-All)**, **SC (Strict Contrastive)** and **BC (Broad Contrastive)** tests:

OVA: The embedding vector distance between the target and its nearest neighbor on the number line should be smaller than that between the target and any other numeral in the set.

SC: The embedding vector distance between the target and its nearest neighbor on the number line should be smaller than that between the target and its second nearest neighbors on the number line.

BC: The embedding vector distance between the target and its nearest neighbor on the number line should be smaller than that between the target and its furthest neighbors on the number line.

We follow the settings described by Naik et al. (2019): for the magnitude evaluation, we run the tests using a set of 2342 numerals that are most frequent in Wikipedia-1B, whose embeddings are well learned by all the methods; and for the numer-

ation evaluation, we run the tests using 113 English words that represent numbers (e.g., ‘three’, ‘billion’) sampled from the same corpus and we measure the distance between the target numeral embedding and the word embeddings of these words. We report the accuracy of various embedding models on these three tests, along with the average rank (denoted as **AVGR**) of the target numeral’s nearest neighbor among all the candidates based on their vector distances to the target. We use the embeddings trained on Wikipedia-1B.

Table 4 shows the results. The Fixed baseline has the best performance in the magnitude evaluation, which is unsurprising because the numeral embedding vector explicitly contains the (squashed) magnitude. NumAsTok performs very well in the numeration evaluation, which is because the number-representing words used in the evaluation are high-frequency words and their embeddings are adequately trained. Except for these two special cases, our methods can be seen to outperform the baselines with a large margin.

Wallace et al. (2019) recently show that classic embeddings of numerals may contain magnitude information that can be extracted by neural networks. Following their methodology, we conduct a nonlinear decoding test on our 2342 numerals. We first randomly sample 80% of the numerals for training and 20% for test. Then we train an MLP with 2 hidden layers to predict the value of a numeral given its embedding by minimizing the mean squared error. The root mean squared error (RMSE) result on the test set is shown in the last column of Table 4, which shows that our embeddings are better at capturing the magnitude information non-linearly.

4.4 Numeral Prediction

To evaluate the quality of numeral embeddings, we design a new numeral prediction task: choosing the right numeral from a set of candidates given the context of the numeral in a sentence. We randomly sample 2000 sentences containing numerals from a subset of Wikipedia that is not used in training, with 600 for validation and 1400 for testing. For each sentence, we use the five words preceding and following the target numeral as its context. An example is shown below, where the ten bold words are the context and 2.31 is the target numeral.

In Hollywood, **the average household size was [2.31] and the average family size was 3.00.**

We use all the 1400 numerals in the test set as the candidates from which one has to select the right numeral for each test sentence. Given the learned word and numeral embeddings, we define two score functions to rank candidate numerals given the context. Following the skip-gram model, we first define the score of center numeral n predicting context word c_j as $s(c_j|n) = \mathbf{v}_{c_j}^o T \mathbf{v}_n^i$ and the score of context word c_j predicting the center numeral n as $s(n|c_j) = \mathbf{v}_n^o T \mathbf{v}_{c_j}^i$. Our first candidate-ranking score function \mathbf{S}_A is the sum of log probabilities of center numeral n predicting each context word c_j . We use softmax here to calculate the probability.

$$\begin{aligned} \mathbf{S}_A(n) &= \sum_j \log p(c_j|n) \approx \sum_j \log \frac{e^{s(c_j|n)}}{\sum_{c_k \in \mathbb{V}_t} e^{s(c_k|n)}} \\ &= \sum_j s(c_j|n) - \sum_j \log Z(n) \end{aligned} \quad (7)$$

where \mathbb{V}_t is the vocabulary of non-numerical words and $Z(n)$ is the normalization factor. The other candidate-ranking score function \mathbf{S}_B is the sum of log probabilities of each context word c_j predicting center numeral n .

$$\begin{aligned} \mathbf{S}_B(n) &= \sum_j \log p(n|c_j) \approx \sum_j \log \frac{e^{s(n|c_j)}}{\sum_{n_k \in \mathbb{V}_n} e^{s(n_k|c_j)}} \\ &= \sum_j s(n|c_j) - \text{Constant} \end{aligned} \quad (8)$$

where \mathbb{V}_n is the set of numerals in the dataset. There are a few other possible score functions, but we find that they lead to results similar to \mathbf{S}_A and \mathbf{S}_B .

We use three metrics to evaluate numeral prediction (Spithourakis and Riedel, 2018). **MdAE** is the median of the absolute errors between the predicted and true numerals, **MdAPE** is the median of the absolute percentage errors between the predicted and true numerals, and **AVGR** is the average rank of the true numeral among the candidates.

We train embeddings on Wikipedia-1B and report the evaluation results in the left part of Table 5. Our methods significantly outperform the NumAsTok and Fixed baselines on all three metrics. D-LSTM also performs well but needs more parameters and computing time than our methods.

For reference, we also test the mixture-of-Gaussians numerate language model² (Spithourakis and Riedel, 2018) on the same task. Although the numerate language model does not learn

²<https://github.com/uclnlp/numerate-language-models>

Metrics	Magnitude				Numeration				Non-linear Decoding
	OVA	SC	BC	AVGR	OVA	SC	BC	AVGR	RMSE
SOM	67.72	71.86	99.40	15.91	3.54	62.83	100.00	28.98	2724.12
GMM	57.86	58.63	100.00	1.75	4.42	65.49	100.00	25.97	678.78
NumAsTok	12.17	51.02	95.99	144.13	7.08	61.95	99.12	27.08	14878.73
D-LSTM	7.26	51.79	92.83	158.82	1.77	54.87	89.38	53.55	20949.66
Fixed	83.90	78.22	100.00	1.17	0.89	49.56	99.12	56.00	5550.97

Table 4: Magnitude, numeration, and non-linear decoding results for our methods and baselines. Accuracies of OVA, SC and BC are expressed as percentages. Lower AVGR indicates better performance. Numbers indicating top-2 performance are highlighted.

numeral embeddings, it is shown to produce accurate numeral prediction. We use a smaller vocabulary size (3×10^4) for the model compared with our methods and the baselines (3×10^5) because we find it requires unacceptable GPU memory and training time with a large vocabulary size. The default prediction method of the model predicts a numeral from its preceding context and the predicted numeral may not belong to the candidate set (hence no **AVGR** result). A second prediction method is to use the log-likelihood of the whole sentence computed by the model to score and rank the candidates. As shown in the last row of table 5, the numerate language model reaches slightly better **MdAE** but worse **MdAPE** and **AVGR** than our methods.

We also conduct a slightly different numeral prediction task on the recently released Numeracy-600K dataset (the Article Title part) (Chen et al., 2019). This dataset contains 600k sentences with numerals and in each sentence, a numeral is selected and tagged with its order of magnitude. There are eight possible orders of magnitude and the goal is to predict the correct one for the target numeral from its context. To solve this classification problem, we sample 100 numerals for each magnitude order and use the mean of their numeral embeddings to create a ‘meta’ embedding; we then use these ‘meta’ embeddings to replace the numeral embeddings in the score functions S_A and S_B and the highest-scoring order of magnitude is returned. We split the dataset to 450k sentences for training, 50k for validation and 100k for testing. We use micro-F1 and macro-F1 in addition to **AVGR** as the evaluation metrics. The result is shown in the right part of Table 5. The result shows that our methods achieve much better performance compared to the baselines.

4.5 Sequence Labeling on Customer Service Data

To verify the effectiveness of our methods in practice, we evaluate our methods with a sequence labeling task on a dataset of customer service chat logs from an online apparel shopping website. This dataset contains a large number of numerals related to height, weight, foot length, etc., and therefore is a good testbed for evaluating numeral embeddings. The task is to assign a label to each word or numeral in the dataset indicating its information type. We shows two examples below:

W O H O O O O O W H O O O
82 kg 177 cm what size shall I choose 82 177 what size ?

W, H, O are labels representing weight, height and ordinary word respectively. We show the statistics of the dataset in Appendix.E. To better evaluate the generalizability, we create two additional test sets. The first one is created by ‘augmenting’ the original test set with new sentences containing slightly perturbed numerals. For example, we can create new sentences by replacing ‘177’ in the above example with ‘176’ and ‘178’. The second one contains ‘hard’ sentences from the original test set that do not have explicit cues for label prediction. For example, the first sentence above contains ‘kg’ and ‘cm’ that can greatly facilitate the prediction of W and H, but the second sentence above does not contain such cues and hence is a ‘hard’ sentence. Finally, we also test the low-resource settings in which only 30% or 10% of the training set is used. We described the augmented and hard test set Appendix.D more detailedly.

We learn embeddings from the training set using our methods and the baselines and use a validation set to do model selection. We plug the learned embeddings into the Neural-CRF model (Yang and Zhang, 2018)³ to do sequence labeling without using part-of-speech and character-level features

³<https://github.com/jiesutd/NCRFpp>

Metrics	Wikipedia-1B, dim 300						Numeracy-600k, dim 300					
	AVGR	MdAE	MdAPE	AVGR	MdAE	MdAPE	AVGR	Mi-F1	Ma-F1	AVGR	Mi-F1	Ma-F1
	S_A			S_B			S_A			S_B		
SOM	381.41	825.79	0.9836	455.01	1184.60	0.9880	2.91	37.99	13.50	2.02	42.74	13.66
GMM	343.50	1184.85	0.9450	444.15	1081.50	0.9866	2.19	41.86	18.47	2.02	44.07	13.77
NumAsTok	600.17	1918.00	0.9965	600.28	32772.50	19.07	4.21	9.74	5.47	6.16	24.28	4.88
D-LSTM	357.45	1310.65	0.9369	466.81	1080.5	0.9908	3.98	27.98	8.80	4.49	16.49	8.42
Fixed	685.58	50371.50	42.82	672.47	50525.00	61.59	3.23	0.00	0.01	3.23	0.00	0.00
	Default			Likelihood Scoring								
Numerate-LM	-	795.00	0.9923	571.37	890.00	0.9937						

Table 5: The results of the numeral prediction tasks. Numerate-LM represents the language model of Spithourakis and Riedel (2018), shown here for reference.

		Original				Augmented				Hard			
		Acc	P	R	F1	Acc	P	R	F1	Acc	P	R	F1
100%	GMM	97.12	91.19	90.46	90.83	97.02	91.28	90.18	90.72	96.19	86.66	85.91	86.28
	SOM	97.04	90.74	90.45	90.60	97.03	91.19	90.43	90.81	96.06	86.18	85.93	86.06
	D-LSTM	96.72	89.84	88.80	89.32	96.72	90.40	88.99	89.69	95.52	84.19	83.30	83.74
	Fixed	95.75	86.19	87.42	86.80	95.86	87.13	87.65	87.39	93.97	78.39	80.18	79.27
	NumAsTok	96.88	91.37	89.29	90.32	96.36	90.99	87.39	89.15	96.00	87.11	85.12	86.10
30%	GMM	96.21	89.55	86.07	87.78	95.92	89.07	85.33	87.16	95.27	84.42	81.62	82.99
	SOM	96.20	89.50	86.18	87.81	95.88	89.12	85.29	87.16	95.23	84.44	81.50	82.94
	D-LSTM	95.55	86.83	83.88	85.33	95.30	86.22	83.13	84.64	94.32	80.10	78.17	79.12
	Fixed	94.67	83.51	82.69	83.10	94.48	83.40	82.02	82.71	92.92	75.03	75.18	75.10
	NumAsTok	95.58	89.18	83.55	86.27	94.57	88.39	79.94	83.95	94.65	84.42	79.06	81.65
10%	GMM	93.43	82.36	75.01	78.51	92.78	81.48	72.85	76.92	93.19	80.26	72.71	76.30
	SOM	93.48	82.13	75.11	78.46	92.87	80.96	73.22	76.89	93.24	79.47	73.04	76.11
	D-LSTM	92.53	77.71	71.45	74.45	91.99	76.24	69.96	72.96	92.10	73.26	68.72	70.92
	Fixed	91.90	75.39	71.41	73.34	91.48	73.96	70.20	72.02	91.06	69.50	67.47	68.46
	NumAsTok	92.31	81.98	70.51	75.81	90.77	80.10	64.95	71.73	92.00	79.64	67.95	73.32

Table 6: The results of sequence labeling. We report the accuracy, precision, recall, F1 score for the original, augmented, and harder test sets with different training data sizes. Accuracy is in the token level and the other metrics are in the entity level. All the results are very stable and their standard deviations are often much smaller than the differences between our methods and the baselines.

and embedding fine-tuning.

The results are shown in Table 6. We also include the table with standard deviation in Appendix.F. Our methods consistently outperform all the baselines on the Accuracy, Recall, and F1 metrics in different configurations. NumAsTok trained with 100% training samples has the highest precision on the original and hard test sets probably because it learns high-quality embeddings for high-frequency numerals included in its vocabulary; but its recall is lower than that of our methods, most likely because of its numeral OOV problem. Comparing the results on the original and augmented test sets, we see that NumAsTok shows a more significant drop in performance than the other methods, which suggests that NumAsTok does not generalize well because of the numeral OOV problem. In the low-resource settings, the advantage of our methods over the baselines becomes even larger, indicating better generalizability and less annotation required for our methods to achieve a promising performance.

5 Conclusion

In this paper, we propose two novel numeral embedding methods that represent the embedding of a numeral as a weighted average of a set of prototype numeral embeddings. The methods can be integrated into traditional word embedding approaches such as skip-gram for training. We evaluate our methods on four intrinsic and extrinsic tasks, including word similarity, embedding numeracy, numeral prediction, and sequence labeling, and show that our methods can improve the performance of numeral-related tasks and has better generalizability. Our code and sample data can be found at <https://github.com/jeffchy/Learning-Numeral-Embeddings>.

An important future direction is to handle numeral polysemy. For example, the numeral “2019” may denote either a year or an ordinary number. One potential method is to assign a different embedding to each sense of a numeral. In this way, “2019” would have one embedding for representing a year and another for representing an ordinary quantity.

The similarity function would treat different senses of a numeral differently. For example, the year sense of “2019” would be similar to the year sense of “19” but dissimilar to the sole sense of “2019.5”, while the quantity sense of “2019” would be similar to that of “2019.5”. Our methods also have the potential to apply to contextual word embedding methods, so this would be another future direction.

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A GMM Initialization

Both EM and hard-EM are sensitive to initialization and we use the initialization methods described in (Blömer and Bujna, 2013). We first initialize the mean μ_k of the k -th Gaussian component using one of the following three strategies:

Random initialization choose μ_k from X randomly. This is suitable when X contains a wide range of numbers, e.g., numbers collected from Wikipedia.

SOM-based initialization initialize μ_k to $p_k \in \mathbb{P}$ produced by the SOM method.

K-means initialization run randomly initialized k-means on X and then use k-means centroids to initialize μ_k .

We then assign the data samples to their closest means. The standard deviation of the data samples assigned to the k -th mean becomes σ_k .

B Hyper-parameters

We list all of the important hyper-parameters we tune for each model.

General hyper-parameters embedding dimension, context window size, SGD learning rate, batch size, vocabulary size, etc.

SOM hyper-parameters number of prototypes, stage of applying the log-squashing function (stage 1: before prototype induction; stage 2: only in the similarity function).

GMM hyper-parameters number of prototypes, whether we apply the log-squashing function to the numerals, EM initialization (from SOM, random initialization, or k-means initialization), type of EM (hard-EM or soft-EM).

We show the values of the SOM and GMM hyper-parameters in Table 7 and the values of the general hyper-parameters of all the methods in Table 8. We find that the general hyper-parameters influence the performance of our methods and the baselines in the same way, so in most cases, these hyper-parameters are set to be identical for all the methods. For large training corpora (Wiki1B, Numeracy-600k), we use 2048 as the batch size for D-LSTM, because D-LSTM consumes much more GPU memory. We set the batch size of the other methods to 4096. For the sequence labeling tasks, because the data is relatively small and confined to a very specific domain (chat log from online apparel shops), we set a small vocabulary size of 500 for all the methods except NumAsTok and set the vocabulary size of NumAsTok to 550 to ensure that different methods have similar numbers of parameters for word embedding training. Consequently, our methods have $(500 + |\mathbb{P}|) \times D$ parameters for word embedding training and NumAsTok has $550 \times D$ parameters, where \mathbb{P} is the prototype set, whose size is typically smaller than 50, and D is the embedding dimension.

Table 7 also shows that the optimal number of prototypes is around 200–500 for the Wiki1B corpus and 10–25 for the much smaller sequence labeling dataset. As a rule of thumb, we suggest setting the number of prototypes to $(\log N)^2$, where N is the number of distinct numerals in the training corpus.

C More Results on Wikipedia-1B

We show the histograms of numerals in the Wikipedia-1B dataset and the prototypes learned by SOM and GMM in Fig.2. It can be seen that the prototypes induced by our methods have a similar distribution compared to the original numerals.

In addition, we select several typical numerals and non-numerical words and project their embeddings to 2D using t-SNE (Maaten and Hinton, 2008) (Figure 3). We use embeddings learned on

	SOM		GMM			
	prototype number	log transform stage	prototype number	log transform	initialization	EM
Word similarity (Wiki1B)	200	dataset	200	True	random	hard
Magnitude (Wiki1B)	200	dataset	300	True	random	soft
Numeration (Wiki1B)	300	similarity function	500	True	random	soft
Numeral Prediction (Wiki1B)	300	similarity function	300	False	random	hard
Numeral Prediction (Numeracy-600k)	50	dataset	200	False	random	hard
Sequence Labeling 100 %	15	dataset	30	False	random	soft
Sequence Labeling 30 %	10	dataset	15	False	k-means	soft
Sequence Labeling 10 %	25	similarity function	20	False	from-som	soft

Table 7: Hyper-parameter values for GMM and SOM based methods for each experiment.

	embed dim	context window	negative samples	epoch	batch size	learning rate	vocabulary size
Word similarity (Wiki1B)	300	5	5	1	4096, 2048	5×10^{-3}	3×10^5
Magnitude (-MAG) (Wiki1B)	300	5	5	1	4096, 2048	5×10^{-3}	3×10^5
Numeration (-NUM) (Wiki1B)	300	5	5	1	4096, 2048	5×10^{-3}	3×10^5
Numeral Prediction (Wiki1B)	300	5	5	1	4096, 2048	5×10^{-3}	3×10^5
Numeral Prediction (Numeracy-600k)	300	2	5	10	4096, 2048	5×10^{-3}	1×10^5
Sequence Labeling 100% 30% 10%	50	2	5	10	50	5×10^{-2}	500, 550

Table 8: Values of general hyper-parameters for each experiment.

Wikipedia-1B corpus using the SOM and GMM methods. The examples and the figures show that our model does capture some semantic relations between numeral quantities and normal words.

We show the training speed of each embedding method on the Wikipedia-1B dataset in Table 9. The batch size is set to 2048 for all the methods. Our methods are slower than NumAsTok but are faster than D-LSTM.

D Augmented and Hard Test Sets in Sequence Labeling

The augmented test set is created by reasonably perturbing the numerals in a sentence. For example, for a numeral ‘173’ that describes height, we generate new samples by changing ‘173’ to ‘174’ or ‘175’ while keeping the other non-numerical words in the sentence unchanged. For a decimal such as ‘1.7 meters’, we change it to ‘1.6’ or ‘1.8’. The perturbation will not change the decimal places of numerals and will only change the quantity slightly, which makes the generated sentences reasonable.

The hard test set is created by manually collect ‘hard’ samples in the original test set. Hard samples do not have explicit patterns, meaning that a numeral’s tag cannot be easily inferred by its adjacent words. For example, tags of numerals followed by units like ‘cm’, ‘m’, ‘kg’, ‘years’ and ‘feet’ can be figured out easily, so we exclude them from the hard test set. Customers are very likely to use ambiguous expressions like: ‘I’m 16.5, can I buy 24?’, where 16.5 is about foot length and 24 is the shoe

size. These ambiguous sentences are included in the hard test set.

E Statistics of Sequence Labeling Dataset

We show the statistics of the customer-service dataset in the Table 10. The vocabulary is small because the dataset is confined to a specific domain: online customer service chat log about apparel purchase. In this dataset, most of the sentences are about sizes of various kinds of clothes and are very short and ambiguous.

F Sequence labeling result with standard deviation.

We also show the sequence labeling result with standard deviation in Table 11. The standard deviation is small, so the result is stable.

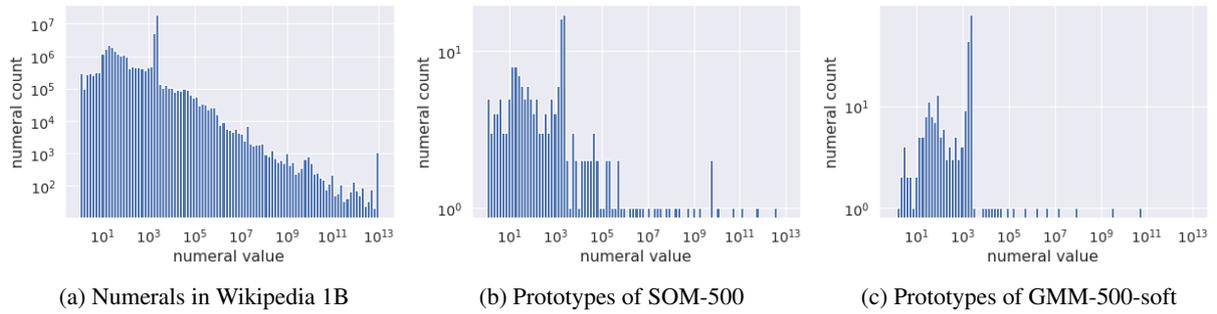


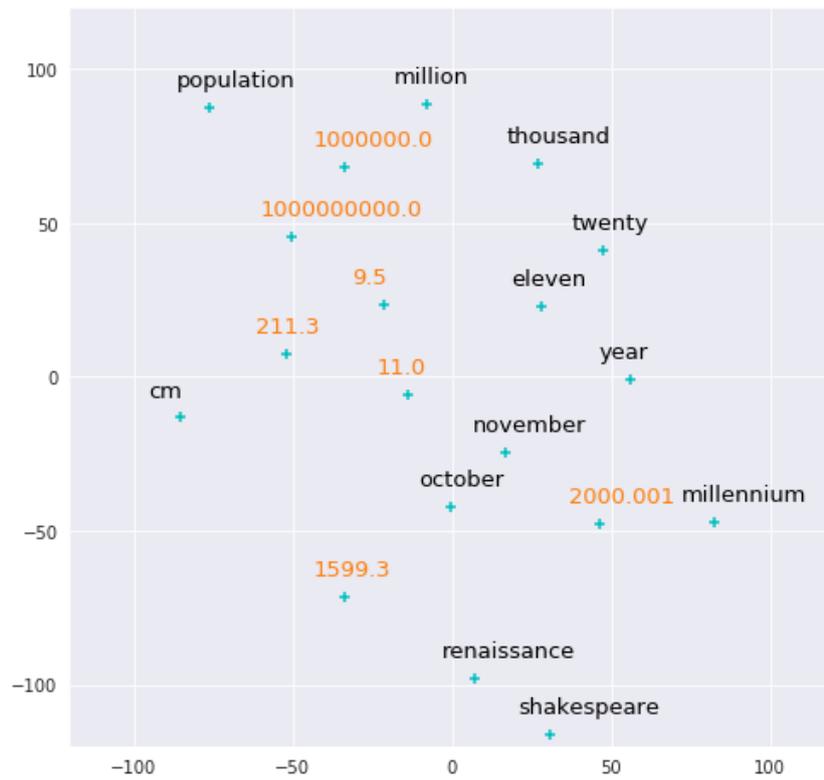
Figure 2: Histograms of numerals and learned prototypes that range from 0 to 10^{13} . The horizontal axis represents the numeral quantity and the vertical axis represents the number of occurrences, ‘500’ means the number of prototypes, ‘soft’ means soft-EM.

Method	SOM	GMM	NumAsTok	D-LSTM	Fixed
Speed (sent/s)	13590.93	12691.18	22907.97	8421.66	13055.08

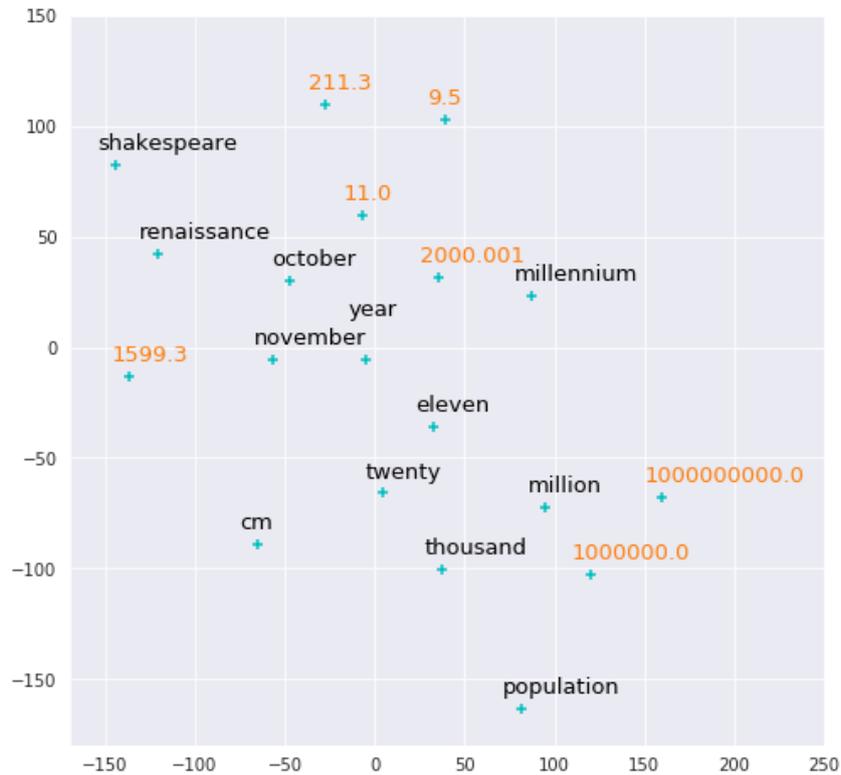
Table 9: Training speed for each methods.

Number of Sentences				
Train	Dev	Original Test	Augmented Test	Hard Test
1389	793	1802	8052	726
Statistics of Training Set				
Token Vocab	Numeral Vocab	Avg sent length	Numeral Ratio	labels
505	234	10.42	15.89 %	21

Table 10: Statistics of customer-service dataset.



(a) t-SNE plot for embedding trained by the SOM-based method with 200 prototypes.



(b) t-SNE plot for embedding trained by the GMM-based method with 300 prototypes, random initialization and soft-EM training.

Figure 3: 2D t-SNE results for the SOM-based and GMM-based methods.

		Original				Augmented				Hard			
		Acc	P	R	F1	Acc	P	R	F1	Acc	P	R	F1
100%	GMM	97.12	91.19	90.46	90.83	97.02	91.28	90.18	90.72	96.19	86.66	85.91	86.28
		± 0.05	± 0.11	± 0.17	± 0.14	± 0.06	± 0.17	± 0.19	± 0.18	± 0.05	± 0.13	± 0.36	± 0.24
	SOM	97.04	90.74	90.45	90.60	97.03	91.19	90.43	90.81	96.06	86.18	85.93	86.06
		± 0.04	± 0.15	± 0.10	± 0.12	± 0.03	± 0.14	± 0.11	± 0.13	± 0.09	± 0.14	± 0.32	± 0.23
	D-LSTM	96.72	89.84	88.80	89.32	96.72	90.40	88.99	89.69	95.52	84.19	83.30	83.74
		± 0.06	± 0.26	± 0.24	± 0.25	± 0.07	± 0.29	± 0.23	± 0.26	± 0.14	± 0.66	± 0.55	± 0.60
	Fixed	95.75	86.19	87.42	86.80	95.86	87.13	87.65	87.39	93.97	78.39	80.18	79.27
		± 0.11	± 0.38	± 0.21	± 0.29	± 0.10	± 0.25	± 0.28	± 0.26	± 0.16	± 0.46	± 0.43	± 0.45
	NumAsTok	96.88	91.37	89.29	90.32	96.36	90.99	87.39	89.15	96.00	87.11	85.12	86.10
		± 0.07	± 0.40	± 0.09	± 0.21	± 0.05	± 0.41	± 0.09	± 0.20	± 0.10	± 0.52	± 0.03	± 0.26
30%	GMM	96.21	89.55	86.07	87.78	95.92	89.07	85.33	87.16	95.27	84.42	81.62	82.99
		± 0.07	± 0.15	± 0.32	± 0.24	± 0.09	± 0.32	± 0.40	± 0.36	± 0.13	± 0.41	± 0.47	± 0.43
	SOM	96.20	89.50	86.18	87.81	95.88	89.12	85.29	87.16	95.23	84.44	81.50	82.94
		± 0.03	± 0.17	± 0.29	± 0.08	± 0.08	± 0.16	± 0.41	± 0.13	± 0.02	± 0.30	± 0.22	± 0.09
	D-LSTM	95.55	86.83	83.88	85.33	95.30	86.22	83.13	84.64	94.32	80.10	78.17	79.12
		± 0.08	± 0.29	± 0.36	± 0.32	± 0.12	± 0.41	± 0.50	± 0.46	± 0.07	± 0.33	± 0.39	± 0.35
	Fixed	94.67	83.51	82.69	83.10	94.48	83.40	82.02	82.71	92.92	75.03	75.18	75.10
		± 0.06	± 0.21	± 0.18	± 0.12	± 0.08	± 0.23	± 0.26	± 0.17	± 0.05	± 0.06	± 0.38	± 0.17
	NumAsTok	95.58	89.18	83.55	86.27	94.57	88.39	79.94	83.95	94.65	84.42	79.06	81.65
		± 0.03	± 0.25	± 0.31	± 0.10	± 0.07	± 0.40	± 0.16	± 0.21	± 0.03	± 0.39	± 0.23	± 0.10
10%	GMM	93.43	82.36	75.01	78.51	92.78	81.48	72.85	76.92	93.19	80.26	72.71	76.30
		± 0.12	± 0.17	± 0.52	± 0.21	± 0.03	± 0.25	± 0.36	± 0.14	± 0.04	± 0.41	± 0.09	± 0.19
	SOM	93.48	82.13	75.11	78.46	92.87	80.96	73.22	76.89	93.24	79.47	73.04	76.11
		± 0.11	± 0.26	± 0.41	± 0.21	± 0.10	± 0.25	± 0.37	± 0.19	± 0.10	± 0.07	± 0.49	± 0.30
	D-LSTM	92.53	77.71	71.45	74.45	91.99	76.24	69.96	72.96	92.10	73.26	68.72	70.92
		± 0.19	± 0.38	± 0.82	± 0.61	± 0.26	± 0.40	± 0.11	± 0.80	± 0.16	± 0.26	± 0.70	± 0.40
	Fixed	91.90	75.39	71.41	73.34	91.48	73.96	70.20	72.02	91.06	69.50	67.47	68.46
		± 0.05	± 0.46	± 0.58	± 0.17	± 0.12	± 0.64	± 0.73	± 0.40	± 0.06	± 0.78	± 0.27	± 0.25
	NumAsTok	92.31	81.98	70.51	75.81	90.77	80.10	64.95	71.73	92.00	79.64	67.95	73.32
		± 0.12	± 0.44	± 0.56	± 0.29	± 0.14	± 0.65	± 0.66	± 0.23	± 0.06	± 0.64	± 0.38	± 0.20

Table 11: The results of sequence labeling. We report the accuracy, precision, recall, F1 score for the original, augmented, and harder test sets with different training data sizes. Accuracy is in the token level and the other metrics are in the entity level.