# "DERIVATIONAL" PARADIGMS IN MORPHONOLOGY. 

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## INTRODUCTION.

Traditionally, paradigms were used to deal with inflection in inflectionally rich languages. Only recently (Calder, 1989; Carstairs-McCarthy, 1988, 1992) paradigms have been the object of a far-reaching investigation covering their formal and computational properties. This investigation has highligthed the significance of a paradigm-based treatment of morphonological phenomena and its theoretical implications. In this paper, we show how derivational processes in Morphology can be treated paradigmatically by using a morphonological network. The approach is not only theoretical speculation but has been subjected to the practical test of a computer implementation. This implementation leads, in our opinion, to a conceptually and computationally cleaner treatment of Morphonology.

## 1 THE PROBLEM.

There are two basic ways to relate a pair of morphonological representations derivationally: 1) to take either of them as basic, and derive the other from it via a process of rule-governed phonological change (Fig. 1 below); 2) to assume a hird representation (somewhat intermediate between the two) as underlying, and make the other two derive from it either by substitution of some phonological segments, or by filling in an underspecified phonological representation (Fig. 2 below).


Fig. 1 base-derivative relation in Morphonology
Hercafter, we will refer to both 1) and 2) as derivational accounts of morphonological relations. Usually, solution 1 stores the basic form only in the lexicon, while the derivative is, as it were, cranked out
on demand by rule application ${ }^{1}$. On the other hand, solution 2 requires that only one underlying, abstract representation be stored in the lexicon: the two related forms are yielded from their common lexical source by rules. If $b$ and c are the morphonological representations to relate, the two approaches can be illustrated as shown in Figg. 1 and 2.

In Fig. I, b and $c$ are taken to be on a diliferent footing: the form at the top is more basic than the one at the bottom, the arrow indicating a derivational relation. The following assumption is made: given two forms to relate, it is always possible to specily the direction of the arrow.


Fig. 2 abstract representations and morphonological relations

This assumption stumbles upon a number of difficulties. Let us consider a small but crucial portion of English segmental Phonology as classically analysed since Chomsky and Halle (1968). First, schwa is well known to alternate with full vowels within the Phonology of English. Derivational series such as in Fig. 3 helow show that full vowels under stress correspond to sehwas in unstressed positions.

## ['fowtograef] / [fowto'grafik] / [fa'to gre fi]

Fig. 3 derivational alternations
This alternation is captured by a rule of vowel reduction: full vowels are reduced to schwa in unstressed position (c.g., /ad/ > schwa in photography). Another systematic phonological atternation in English involves derivational pairs such as sane-sanity (['scjn]/|'seniti]), which strongly suggest a derivational rule like ej $->\boldsymbol{x}$. However, other alternations appear to go in the opposite direction. For example in a triple like marginal

[^0]/marginality/ marginglia, the following allemation in the underlined vowel emerges: schwa/e/ej. If we posit /e/ as underlying, then we end up having to set up an la/ $\rightarrow>/ \mathrm{ej} /$ change, which is the miror-image of the $/ \mathrm{cj} /->/ \mathrm{a} /$ relation posited for the derivational pair ['sejn]/['seniti] (inore on this in Durand, 1990).

The solution illustrated in Fig. 2 above is a way to solve this apparent paradox. A third abstract segment /a:/ is assumed to be basic relative to /schwa/a/ej/. This means that/schwa/e/ej/ can be derived from /e:/ through application of some phonological rules. A derivational chain of this sort can be mather complex, since /a:/ and /ej/ are, phonologically, far removed from each other, and many intermediate changes can be needed (as in ['se:n] -> |'se:n] $\rightarrow$ |'se:jn| $\rightarrow$ |'sejn|; see Halle and Mohanan, (1985) for more examples). More reservations on chains of this sort have been expressed recently in a series of psycholinguistic experiments, amed at probing the reality of the derivational assumptions (Jaeger, 1986; Wang and Derwing, 1986).

In the literature, an altogether different approach from both derivationat accounts 1) and 2) above has been suggested (Vennemann, 1974): band e should simply be listed in the Lexicon, one beside the other, on a par:


Fig. 4 morphonological relations and lexical listing
Formulated in this way, the relation in Iig. 4 is always "true on the surface", since there is no abstract representation involved in this accoum. Moreover, no rule ordering problems arise (i.e., concerning the direction of the arrow). If the solution in Fig. 4 is adopted, however, it is not at all clear what type of lexical architecture one is suggesting: i.e., it is moot whether $b$ and $c$ are somehow related in the lexicon, or they are simply listed together. More worringly, the notion "true on the surface" is of little theoretical help for explaining some well-known cases of alternation. Take, for example, the opposition between the American Paglish pronunciation of writer and rider, respectively /raj $\Gamma$ ed and /raj $\Gamma^{-1}$ ed, where both $/ / /$ and / $/ /$ have been turned into a flap ([ [] ). If the only dilierence between the two phonological realizations is the surface-true
 relation between vowel length and the verbat bases of the two derivatives, a relation that represents an important, productive generalization within the American English phonological system (Durand, 1990). An American English speaker, when asked to derive a new agentive in eer lrom verbs ending in $/ 4$, will produce flapping with no lengthening. In contrast, (s) he will produce both a lengthened vowel and a llap if the base is a verb ending in/d/. Derivational accounts capture this generalization in an elegant way, through rule ordering: vowel lengthening takes place before llapping does, in the context "vowel followed by a voiced consonant", so that when either $/ / /$ or $/ \mathrm{d} /$ disappears, lengthening has already applied (or failed to). In contast, accounts based on lexical listing are clearly incapable of grasping this significant hidden relation, since the opposition between $/ / /$ and $/ / / /$ is no longer true
on the surface in pairs such as /ail er os /rajle ent, where the opposition is neutralized by a flap.

To sum up, derivational accounts of morphonological altermations face a number of theoretical and practical problems. In what follows, we will illustrate the working of a sel of analogy-based principles and the design of a general parallel arehitecture for their implementation. These principles dispense with both rule ordering and surface untrue representations by using paradigms of alternations instead of derivational chains. The implemented architecture proves to be accurate and computationally eflicient.

## 2 THE GENERAL MODEL.

In this section the idea is illustrated that redundancies among linguistic data can be used to convey interesting lingnistic generalizations if data are stored in an incremental network. I ct us consider the general case first, exemplified by the following list of abstract cases and their categorial classification:

| 137 | $x$ |
| :--- | :--- |
| 037 | $x$ |
| 337 | $x$ |

Suppose that the sequence of numerals 137 represents the form of a linguistic object (say a word); $x$ is its category. We can represent these data by exploiting the redundancies that they show at both the formal and categorial level of description as follows:


## Fig. 5 a formal core and its category

The idea is to intercomeet all forms chassified the same way by letting them share a common formal core if there is any (for a rigorous definition of the notion of Formal core, see Pitrelli, 1993). In lig.5, - 37 is the formal core. $A$ core with its eategory ( $x$ in the example at hand) is called a nucleus. The graph in rig. 5 can be seen as a network of nodes. Nodes which are linked through a solid line have been witnessed in inpul as co-occurring in the same form. Nodes which are not linked do not co-oceur. Moreover, if two nodes allemate, that is if they are in complementary distribution with respect to a shared core, they oceupy the same column in the figure. In other words, nodes on the same column in Fig. 5 are mutually exclusive, paradigmatically related alternations.

Let us consider now how this network can be used to associate loms with categorics. Assume that more dita have been stored in the network so that the configuration shown in Fig. 6 overleat is built up, In Fig. 6 o is another possible category (different from $x$ ), and $38<=>$ o another mucleus. Given a network like this, network cores are activated by an input string if they are contained by it. The network output will then be the catcgory associated with the activated core.


Fig. 6 rival cores in a multicategory network
More concretely, if a certain form, say 437, is given as input to the network, the system tries to guess the right category on the basis of the amalogy of 4.37 (called the target string) with already stored items (called base strings). This is carried out through the following steps. Network cores are activated by 437: this is done through a simple string-matching routine ${ }^{2}$. For example, 37 will be activated, and its category $x$ is a candidate response of the system for the inpu4 437. What happens when more than one core gets activated by the same input token? If the activated cores have the same category, the corresponding multiple responses would reinforce each other: the only category aclivated is given as output. The case of multiple responses with different categories (and thus potentially differem outputs) is more complex. We can distinguish two calses:

1) there is no core which is fully activated
2) there is at least one fully activated core.

A core is fully activated when it is entirely contained by the input string: in the example above 437 fully activates the core -37 . This contrasts with partial activation, when the core is only partially contained by the input string: for example, 437 partially activates the core -38 of Fig. 6 above, since it contains 3 in the second position, but not 8 in the third. Let us consider case 1) above first. If there is no core which is fully activated, then the system goes through the following two steps: 1a) for each candidate response, the system gauges an Activation Ratio:
number of numerals of the
activated core contained in input
total number of numerals in the activated core

The activation ratio $(\operatorname{AcR})$ is then $0<\operatorname{AcR} \leq 1$. The case of full activation ( $\mathrm{AcR}=1$ ) is dealt with in 2 ); 1 b ) the core with the highest AcR wins out over the others.

Let us consider now case 2). If there exists at least one fully activated core, then two further subcases need be distinguished: 2a) there is only one core which is fully activated: the category borne out by that core is

[^1]then picked up; 2b) there are at least two cores which are fully activated. 2a) can be seen as a degenerate case of 1) above, when $A \subset R=1$. As to 2b), in this case the activation ratio is clearly no longer conclusive. One needs to gatuge a further ratio, called Analogy Ratio, whose detinition follows:

$\frac{\text { total number of numerals in the }}{\text { activated core }}$ total number of numerals | in input |
| :---: |

Again, the analogy ratio (AnR) is $0<\operatorname{AnR} \leq 1^{3}$.
To sum up, a certain pattern is analogically activated if the following conclitions are met in this order:

1) it is activated by an input pair
2) it has got the highest activation ratio
3) it has got the highest analogy ratio

So far, we have been assuming that the network produces cores incermentally as more data are input. In fact, the network progressively extracts reduced cores. lach full form is already a core in its own right, otherwise it would never get activated. The extraction of smaller cores represents the process of acquiring generalizations on the basis of the analogy between data (redundancies). In the network, an exception is simply an isolated case, that is a nueleus which is fully activated only when it is witnessed in input in its entirety ( $\mathrm{AnR}=1$ ).

## 3 AN ANALOGY-BASED NETWORK FOR THE SYNTHESIS OF MORPHONOLOGICAL ALTERNATIONS.

How is it possible to model the synthesis of the set of systematic alternations illustrated in section 1 by means of a network such as the one in Fig.6? Fig.7-a) overleal illustrates the result of storing four phonological representations, namely ['vejn] (vane), |'sejn| (same), ['vieniti] (vamity) and [i'neeniti| (inamity), phis an (abstract) categorial feature string (instead of an atom) for each of them: respectively $x o$, yo, $x j$ and $z j$. Fach categorial feature string is supposed to contain lexico-semantic information (eg., a capsule representation of the meaning of the relevant lemma) and morphosyntactic information (such as grammatical category, gender, number, tense ete.): the content of the feature string, however, will be relatively neglected here. The machinery of core reduction outlined above obtains For categorial feature strings as well as for their forms. [aniti] and [ejn] are formal cores; $\mathbf{x}, \mathbf{i}$ and $o$ are categorial cores.

In lig.7-b) the arrows between [s-] and [-aenili], and $y$ and $j$, pictures an instance of paradigm extension.

[^2]Paradigm extension is based on an intuitive idear if same shares with vane one nucleus, then it is expected to share all other paradigmatically-related nuclei.


Fig. 7 morphonological alternations and paradigm extension

This may not always be true, but is certainly a governing principle in the theory of paradigms. For example, when faced with an unknown oending adjectival form such as obsoleto (linglish 'obsolete'), an Italian speaker would also prediet that obsolefa is feminine singular, obsoleti masculine plural, obsolete feminine pharal, according to the paradigm of four-way adjectives in Italian (Mathews, 1992). By the same token, the extension in lig. $7-\mathrm{b}$ ) above represents the expectation that the nominalization of same is ['satniti|, by paradigmatic amalogy with l'vanitil. Computationally, this extension is implemented as a continuous path of inter-node connections (saly from $|s|$ to [aniti], through [cjn] and [v] in Fig. $7-1$ ).
i)

ii)


Fig. 8 rival paradigms in a morphonological network

Plapping and lengthening, in the American linglish pronunciation of writer and rider, can be represented in analogical terms by the two diagrams in Fig.8. There, we have represented the pronunciation of writer and rider in two separate analogical patterns, respectively i) (without lengthening), and ii) (with lengthening). In lact, i) and ii) should to merged into the same larger pattern. However, it quickly becomes impossible to pieture mutidimensional links on a page. Fig. 8 -i is the result of the exposure of the network to the following four word forms: [rajt (write), |raj|"er| (witer), |haj] cer| (fighter) and |lajt| (light). Bach word form is given with its categorial feature string: xk for [mith, wo for |rajl" er|, $y o$ for [fajl'er] and wh for [tajt]. P'ig. 8 -ii is what the system yields when it comes across the following three word forms: \{ga:j1 er| (guider), |ga:jd\} (gute) and \{ra:jd] (ride). Again, forms are given with their categorial string: jo for [ga:j| erl], $j k$ for lga:jd| and $z k$ for |ra:jd||.

The reader will note that formal cores are parasitic on phonological redundancies, since cores are extracted on the basis of systematic surface-Irue analogies between morphonological representations. The difference between suppletion and (semi)regular altermations is casily captured: (semi)regular atternations exploit cores more systematieally than do suppletive allernations. Moreover, the structure of the amalogical network makes it possible to express hidden phonological constames as paradigms of phonological allemations. This allows the system to avoid the questionable use of surface untrue, underlying phonological representarions, typical of derivational accounts (as in lig. 2 above).

To make the last two points clearer, let us turn to a concrete instance of word synthesis by anatogy. $A$ typical ohjection levelled at representations which treat alternations by listing them, is that crode lists of stored items do not make a clear distinction between regular alternations and irregular ones. Given a raw list of cases, it is objeceed, nothing can tre predicted from such a list, in much the same waty as nothing can be predieted from - Say - the suppletive alternation go/went.
i)

ii)


Fig. 9 word symhesis through morphonological paradigms

However, paradigmatic extension accounts for the fact that flapping is a productive alternation in American English.

Let us suppose that the system has to produce the agentive nominalization (lighter) of ['lajt], whose surface form and lexical content has been already stored in the network (Fig.9-i above). A flap (with no lengthening) would then automatically appear in the place of surface $[-t]$, according to the following steps: a) the input conditions are represented by the lexical content of the verb light (w in Fig.9-i), and the categorial information "agentive nominalization" ( $o$ in Fig.9); b) $w$ activates the [1] of [laj! in the paradigm i) of Fig. 9 above; c) the activated core o triggers the thap alternation $[-\mathrm{aj} \Gamma \mathrm{er}]$ of word-final $[-\mathrm{aj} j]$ in $\mathrm{Fig} .9-\mathrm{i}$, and the alternation [a:jГer] of word final [-a:jd] in 「ig.9-ii; d) the form ["ajГ $\Gamma$ er] is thus produced, since there is a path of pradigmatic links between [I] and [aj $\Gamma$ er], white there being no such a path linking [ $[$ ] and the alternation [a:j $\left.{ }^{-1} \mathrm{Cer}\right]$ by paradigm extension.

It should be noted that only (semi)regular alternations share some (sub)core(s) in common. Suppletions such as go/went simply do not. Nevertheless, no clear-cut distinction is drawn here between minor alternations and irregular forms, since all of them are simply stored in an analogy-based network. Their difference is accounted for in terms of a gradation, defined by the fact that regular alternations overlap with other forms more extensively than do suppletions. We believe that this solution is empirically superior to the Anaximander's principle invoked by Hudson (1974), to the elfect that, since there exists no clear-cut distinction between suppletions and systematic alternations, all of them should be listed in the lexicon.

## 4 LIMITS OF TIIE MODEL AND FURTIIER IMPROVEMENTS.

The network has been implemented in C, and proved to be $95 \%$ accurate in amalysis after a training on 20,000 Italian word forms, and $75 \%$ accurate in synthesis, as reported in Pirrelli and Federici (1991). These performances have been obtained by using the simplified model illustrated here.

It should be noted, however, that this model works well for the Morphology of those languages (such as Italian and English) where alfixation is commonly realized through a concatenative operation (sulfixation or prefixation). In these cases, string-matching is a fairly simple head-and-ail operation. Clearly, this model is far from having a universal, cross-linguistic validity though. For example, it does not work well with cases of circumfixation (known also as parasynthesis), let alone the Morphology of nonconcatenative languages. Nevertheless, we contend that the set of analogy-based principles illustrated here hold for a wider spectrum of languages than purely concatenative ones: by making string-matching a more flexible and powerful operation, we can successtully adapt our model to the requirements of noncatenative languages such as Arabic, or to the treatment of discontinuous affixation. What follows sketchily illustrates this line of development.

Given two strings of characters/phonemes to match (called the base and the target string), the new stringmatching algorithm (discontinuous stringmatching) we are currently experimenting on is, informally:
start from the left corner of both the target and base string and scan them rightwards; extract, down the way, all characters/phonemes which appear in both, and in the same order.

Take the Italian word forms [inve'k:jare] (invecchiare, English 'to age' a parasynthetic verbal derivative of the adjective vecchio, 'otd ${ }^{14}$ ) and [intimi'dire] (intimidire, English 'to make shy, intimidate', a parasynthetic derivalive of timido, 'timid, shy'), or the Arabic pair |kulayb] ('little dog') and [kalb] ('dog') in the diagrams in Fig. 10. In the Arabic example, the shared portion of meaning (DOG) triggers the extraction of a tentative core (a stem). By using a discontinuous string-matching, the meaning DOG is associated with the match $k_{-} l i$. The remaining portions of morpholexical leatures of the two word forms are respectively associated with the substrings left out of the mateli. Note that the two $a$ 's which are linked by a dotted line will not be extracted in the same pattern as $k_{-} l b$, since they are ordered differently relative to the position of $I$ (in the top string, a follows $l$, while in the botom string, a precedes it). In the Italian example, the shared morphological feature infinitive triggers the extraction of the circumfix [in__re].


Fig. I0 the use of discontinuous string-matehing in Italian and Arabic.

Discontinuous string-matching captures an important range of phenomena which would be treated clumsily by using a simple head-and-tail matching. A further advantage of this routine over even more unconstrained conceivathe routines is that it reduces considerably the number of candidate mateles. On the more negative side, we are not able to find matches whose order in the base string is interchanged relative to the order in the target, as in English un-re-do and re-un-pack in Fig.11-a) overleaf. This by no means implies that phenomena such as so-called inversion or metathesis, as in the Rotuman example of Fig. 11-b) overleaf, are beyond the reach of our approach. The idea is that a mateh is extracted only when a base and a target string show the same order of interchangeable characters, as in Fig. $11-\mathrm{c}$ ) overleal. The productive morphological relation between, say, pat and ap in the word 'pigeon' in Rotuman is accounted for paradigmatically, as explained in section 3 of this paper. Intuitively, we do not saly that a sequence $p a$ is transformed into ap under

[^3]particular circumstances. Rather, the sequence pa alternates with the sequence ap within a certain paradigm.
a)

b)


Fig. 11 discontinuous string-matehing does not allow for cross-matehes.

## 5 CONCLUSIONS.

The arehitecture illustated here can be looked at as a model of the morphonological competence of a native speaker, and functions both in analysis and generation. At this point, a question maturally arises: is it a lexicom or a grammar? In our opinion, it is both: a selfmodelling lexicon which extracts generalizations on the basis of the analogies between already stored items, and uses these generalizations as repair strategies for lack of direct evidence provided by an already stored item. This interpenetration of lexicon and grammar offers a few advantages in dealing with the problem at hand:

- phonological concreteness of texical representations: known lexical items are given a lull surface phonological representation in the lexical network: no abstract phonological segrnemts such as ate: in the phonological representation of profound in l"g. 2 are needed;
- alternations vs deletions and inversions: changes in the phonological structure of a given entry are always expressed as alternations, never as deletions; this has the obvious implication that all athernationg segments are encoded in the network and can be retrieved at any time: e.g., one does not say that flapping makes a dental disappear, bet that flapping can appear only in those paradigmatic contexts where a dental is also present; this limits the computational power of the required rule set considerably, since deletive rules are computationally most costly; moreover, by treating cases of metathesis paradigmatically, the system further spares the computationat price of a transfomational operation such as inversion.
- unordered rules: the context for a given phonological change to take place can be specified in terms of a whole paradigm; this formulation has the immediate advantage of avoiding the need for ruleordering: for example, the fact that writer in the American-English pronunciation has no lengthened |aj| is traditionally accounted for by ordering vowel lengthening before flapping; this move is no longer
needed as long as one can restrict the application of vowel lengthening to the paradigin of those nuthei which present [a:j] in the base form of a verb, as we showed above;
phonological concreteness of extracted generalizations: phonological generalizations are expressed in terms of extracted nuelei; nuctei represent what is shared by two (or more) stored items; it lollows that no phonological features appear in extracted nuctei other than those which occur in the surface representations from which nuelei are derived;
- use of direct evidence: as we saw, smaller nuclei (morphemes) come into play as repair strategies only; that is, if and only if there exists no whole lexical representation (an already known word) which matches either the input (in analysis) or the ouput (in generation) in its entirety; otherwise, bigger nuclei always override smaller ones; this accounts for phenomena of lexieal blocking (Aronoff, 1976), when say - the word business is never interpreted as the 'guality of being busy'.

From a more dynanic perspective the network illustrated above can be seen as an abstract model of the gradual learning of morphonological phenomena by a speaker. In fact, the principles illustrated above were originally developed as principles informing machine language learning as such (Federici, 1990), and tested in dealing with some complex cases of unsupervised acpuisition of particular linguistic capabilities (c.g., in tasks of bi-lingual translation). Research carried out in this paper proves that morphonological phenomena are within the grasp of these learning principles. This represents an important a-posteriori confirmation of the validity of the integration between models of machine learning and computational models of linguistic competence, an integration that has already shown its merits in cognitive approaches to language learning and linguistic theorizing (Pinker, 1989) Carstairs-McCarthy and Stemberger, 1988).

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Lexicon


[^0]:    ${ }^{1}$ Alternatively, both representations can be stored in the Lexicon, and related through the statement of some redundancy lexical rule (Jackendoff, 1975).

[^1]:    ${ }^{2}$ More on string-matehing will be said in section 4 of this paper.

[^2]:    ${ }^{3}$ We assume that AnR is calculated only for those cores which have been fully activated ( $\Lambda c R=1$ ). Thus, acti;ated cores cannot comain more numerals than the input does.

[^3]:    ${ }^{4}$ We depart, here, from Scalise's analysis of invecchiare as the prodere of the sequential application of a suffix 1 are |and a prefix lin-l in this order (Scalise, 1983).

