A Unified Neural Network Model for Readability Assessment with Feature Projection and Length-Balanced Loss

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Abstract

For readability assessment, traditional methods mainly employ machine learning classifiers with hundreds of linguistic features. Although the deep learning model has become the prominent approach for almost all NLP tasks, it is less explored for readability assessment. In this paper, we propose a BERT-based model with feature projection and length-balanced loss (BERT-FP-LBL) for readability assessment. Specially, we present a new difficulty knowledge guided semi-supervised method to extract topic features to complement the traditional linguistic features. From the linguistic features, we employ projection filtering to extract orthogonal features to supplement BERT representations. Furthermore, we design a new length-balanced loss to handle the greatly varying length distribution of data. Our model achieves state-of-theart performances on two English benchmark datasets and one dataset of Chinese textbooks, and also achieves the near-perfect accuracy of 99% on one English dataset. Moreover, our proposed model obtains comparable results with human experts in consistency test.

1 Introduction

Readability assessment is to automatically determine the difficulty level of a given text, aiming to recommend suitable reading materials to readers. There are wide applications of readability assessment, such as automating readers' advisory (Pera and Ng, 2014), clinical informed consent forms (Perni et al., 2019) and internet-based patient education materials (Sare et al., 2020).

Comparing with other natural language processing (NLP) tasks, readability assessment is less explored. In the early days, researchers exploit linguistic features to develop various readability formulas, such as Flesch (Flesch, 1948), Dale-Chall (Dale and Chall, 1948) and SMOG (Mc Laughlin, 1969). Later, the mainstream research (Deutsch et al., 2020; Hansen et al., 2021; Lee et al., 2021) is to employ machine learning models to classify a text, by designing a large number of linguistic features. There are also works that treat it as a regression task (Sheehan et al., 2010) or a ranking task (Lee and Vajjala, 2022).

Recently, unlike other NLP tasks, the introduction of deep neural networks for readability assessment does not achieve overwhelming advantages over traditional machine learning methods. Employing neural network models for readability assessment, there are several challenges:

(1) The scale of the dataset for readability assessment is small, which restricts the performance of deep neural network models.

(2) The deep neural network model is mainly based on characters or words and the extracted features are often at a shallow level. As a result, words with similar functions or meanings, such as "man" and "gentleman", are mapped into close vectors although their reading difficulties are different (Jiang et al., 2018).

(3) The linguistic features designed by researchers and continuous features extracted by neural network models are from two different semantic spaces. If two kinds of features are simply concatenated, it will bring redundant information or even harmful effects to model performance.

(4) Unlike other NLP data whose length follows a normal distribution, a notable problem with the data for readability assessment is that the text length varies greatly. The texts with low difficulty are usually shorter, while texts with high difficulty are usually longer. For example, as shown in Table 1, in ChineseLR the average length of Level 1 is only 266 characters, while the average length of Level 5 is 3,299 characters. As a result, when experimented with deep learning networks, shorter texts tend to converge much faster than those longer ones thus harm the overall performance.

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In order to solve the above problems, we propose a **BERT**-based model with Feature Projection and Length-Balanced Loss (**BERT-FP-LBL**). With the pre-trained BERT as the backbone, we employ feature projection to integrate linguistic features into the neural model, and design a new length-balanced loss function to guide the training. Concretely:

- We leverage BERT and a mixed-pooling mechanism to obtain text representations, which take advantage of the powerful representative ability of pre-trained model, and thus overcome the data-sparsity problem.
- Beyond traditional features, we extract a set of topic features enriched with difficulty knowledge, which are high-level global features. Specifically, based on a graded lexicon, we exploit a clustering algorithm to group related words belonging to the same difficulty level, which then serve as anchor words to guide the training of a semi-supervised topic model.
- Rather than simple concatenation, we project linguistic features to the neural network features to obtain orthogonal features, which supplement the neural network representations.
- We introduce a new length-balanced loss function to revise the standard cross entropy loss, which balances the varying length distribution of data for readability assessment.

We conduct experiments on three English benchmark datasets, including WeeBit (Vajjala and Meurers, 2012), OneStopEnglish (Vajjala and Lučić, 2018) and Cambridge (Xia et al., 2019), and one Chinese dataset collected from school textbooks. Experimental results show that our proposed model outperforms the baseline model by a wide margin, and achieves new state-of-the-art results on WeeBit and Cambridge.

We also conduct test to measure the correlation coefficient between the BERT-FP-LBL model's inference results and three human experts, and the results demonstrate that our model achieves comparable results with human experts.

2 Related Work

Traditional Methods. Early research efforts focused on various linguistic features as defined by linguists. Researchers use these features to create various formulas for readability, including Flesch (Flesch, 1948), Dale-Chall (Dale and Chall, 1948) and SMOG (Mc Laughlin, 1969). Although the readability formula has the advantages of simplicity and objectivity, there are also some problems, such as the introduction of fewer variables during the development, and insufficient consideration of the variables at the discourse level.

Machine Learning Classification Methods. (Schwarm and Ostendorf, 2005) develop a method of reading level assessment that uses support vector machines (SVMs) to combine features from statistical language models (LMs), parse trees, and other traditional features used in reading level assessment. Subsequently, (Petersen and Ostendorf, 2009) present expanded results for the SVM detectors. (Qiu et al., 2017) designe 100 factors to systematically evaluate the impact of four levels of linguistic features (shallow, POS, syntactic, discourse) on predicting text difficulty for L1 Chinese learners and further selected 22 significant features with regression. (Lu et al., 2019) design experiments to analyze the influence of 88 linguistic features on sentence complexity and results suggest that the linguistic features can significantly improve the predictive performance with the highest of 70.78% distance-1 adjacent accuracy. (Deutsch et al., 2020; Lee et al., 2021) evaluate the joint application of handcrafted linguistic features and deep neural network models. The handcrafted linguistic features are fused with the features of neural networks and fed into a machine learning model for classification.

Neural Network Models. (Jiang et al., 2018) provide the knowledge-enriched word embedding (KEWE) for readability assessment, which encodes the knowledge on reading difficulty into the representation of words. (Azpiazu and Pera, 2019) present a multi-attentive recurrent neural network architecture for automatic multilingual readability assessment. This architecture considers raw words as its main input, but internally captures text structure and informs its word attention process using other syntax and morphology-related datapoints, known to be of great importance to readability. (Meng et al., 2020) propose a new and comprehensive framework which uses a hierarchical selfattention model to analyze document readability. (Qiu et al., 2021) form a correlation graph among features, which represent pairwise correlations between features as triplets with linguistic features as nodes and their correlations as edges.

3 Methodology

The overall structure of our model is illustrated in Figure 1. We integrate difficulty knowledge to extract topic features using the Anchored Correlation Explanation (CorEx) (Gallagher et al., 2017), and fuse linguistic features with neural network representations through projection filtering. Further, we propose a new length-balanced loss function to deal with the unbalanced length distribution of the readability assessment data.

3.1 Traditional Features

Many previous studies have proved that shallow and linguistic features are helpful for readability assessment. For Chinese traditional features, we develop a Chinese toolkit **zhfeat** to extract character, word, sentence and paragraph features. Please refer to **Appendix A** for detailed descriptions. For English traditional features, we extract discourse, syntactic, lexical and shallow features, by directly implementing the **lingfeat** (Lee et al., 2021) toolkit. We denote the traditional features as f_{α} .

3.2 Topic Features with Difficulty Knowledge

Background. Besides the above lexical and syntactic features, topic features provide high-level semantic information for assessing difficulty level. (Lee et al., 2021) also leverage topic features, but they train the topic model in a purely unsupervised way without considering difficulty knowledge. Inspired by the work of Anchored Correlation Explanation (CorEx) (Gallagher et al., 2017), which allows integrating domain knowledge through anchor words, we introduce word difficulty knowledge to guide the training of topic model, thus obtaining difficulty-aware topic features.

First, we introduce the concept of information bottleneck (Tishby et al., 2000), which aims to achieve a trade-off between compressing feature X into representation Y and preserving as much information as possible with respect to the label Z. Formally, the information bottleneck is expressed as:

$$\max_{p(y|x)} \xi I(Z:Y) - I(X:Y) \tag{1}$$

$$I(X_1:X_2) = H(X_1) + H(X_2) - H(X_1,X_2)$$
(2)

where $I(X_1 : X_2)$ is the mutual information of random variables X_1 and X_2 , H(X) represents the entropy of the random variable X, and ξ represents the Lagrange multiplier.

In CorEx, if we want to learn representations that are more relevant to specific keywords, we can anchor a word type X_i to topic Y_j , and control the strength of anchoring by constraining optimization $\xi \ge 1$. The optimization objective is:

$$\max_{\xi_{i,j}, p(y_i|x)} \sum_{j=1}^{u} \left(\sum_{i=1}^{v} \xi_{i,j} I(X_i : Y_j) - I(X : Y_j) \right)$$
(3)

where u represents the number of topics, v is the number of words corresponding to the topic, and $\xi_{i,j}$ represents the anchoring strength of the word i to the topic j.

Extracting difficulty-aware Topic Features. We utilize a lexicon containing words of varying difficulty levels to extract anchor words. Let $\Omega = \{L_1, L_2, ..., L_k\}$ be a graded lexicon, where L_i is the set of words with difficulty level *i*. C is the corpus for pre-training the topic model. First, we select out some high frequent words of each level in the corpus C:

$$W_i = L_i \cap \mathcal{C} \tag{4}$$

where \cap represents the intersection operation.

For each level of words, we conduct **KMeans** clustering algorithm to do classification, and then remove isolated word categories (a single word is categorized as a class):

$$W_i^a = \mathrm{KMeans}(W_i) \tag{5}$$

The clustering result of words with the difficulty level *i* is denoted as $W_i^a = \{\{w_{i11}^a, w_{i12}^a, ...\}, \{w_{i21}^a, w_{i22}^a, ...\}, ...\}$. Thus, the final anchor words are:

$$W^{a} = \{W_{1}^{a}, W_{2}^{a}, ..., W_{k}^{a}\}$$
(6)

These anchor words of different difficulty levels serve as domain knowledge to guide the training of topic models:

$$\mathbf{ATM} = \operatorname{CorEx}(\mathcal{C}, anchors = W^a)) \quad (7)$$

where **ATM** represents the anchored topic model. Then, we implement the ATM to obtain a set of topic distribution features involving difficulty information, which are denoted as f_{β} .

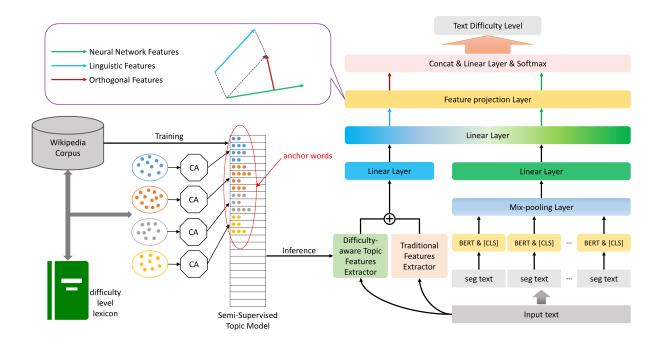


Figure 1: The overall structure of our proposed model for readability assessment. **CA** represents the clustering algorithm. The input color and output color of the feature projection layer represent different types of features.

Combining traditional and topic features, we obtain the overall linguistic features:

$$f_{\gamma} = f_{\alpha} \oplus f_{\beta} \tag{8}$$

where \oplus represents the splicing operation.

3.3 Feature Fusion with Projection Filtering

BERT Representation. We leverage the pretrained BERT model (Devlin et al., 2018) to obtain sentence representation.

The length distribution of data for readability evaluation varies greatly, and texts with higher difficulty are very long, which might exceed the input limit of the model. Therefore, for an input text S, we segment it as $S = (s_1, s_2, ..., s_m)$. For each segment, we exploit BERT to extract its semantic representation: $H_s = (h_{s_1}, h_{s_2}, ..., h_{s_m})$.

Further, we adopt Mixed Pooling (Yu et al., 2014) to extract representations of the entire text:

$$f_{\eta} = \lambda \operatorname{MaxPooling}(H_s) +$$

$$(1 - \lambda) \operatorname{MeanPooling}(H_s)$$
(9)

where λ is a parameter to balance the ratio between max pooling and mean pooling.

Projection Filtering. To obtain better performance, we try to combine BERT representations with linguistic features. As for the method of direct splicing, since two kinds of features come from

different semantic spaces, not only will it introduce some repetitive information, but also it may bring contradictions between some features that will harm the performance. When performing feature fusion, our goal is to obtain additional orthogonal features to complement each other. Inspired by the work (Qin et al., 2020), which uses two identical encoders with different optimization objectives to extract common and differentiated features. Unlike this work, our artificial features and neural features are extracted in different ways, and our purpose is to perform feature complementation. Since the pre-trained model captures more semantic-level features through the contextual co-occurrence relationship between large-scale corpora. This is not enough for readability tasks, and the discrimination of difficulty requires some supplementary features (difficulty, syntax, etc.). So we consider the features extracted by BERT as primary features and linguistic features as secondary ones, and then the secondary features are projected into the primary features to obtain additional orthogonal features.

Concretely, based on the linguistic features f_{γ} and BERT representation f_{η} , we perform dimensional transformation and project them into the same vector space:

$$f_{\gamma} = \tanh(\tanh(f_{\gamma}\mathbf{W}_1 + \mathbf{b}_1))\mathbf{W}_3 + \mathbf{b}_3) \quad (10)$$

$$f_{\eta} = \tanh(\tanh(f_{\eta}\mathbf{W}_2 + \mathbf{b}_2))\mathbf{W}_3 + \mathbf{b}_3) \quad (11)$$

where W_1 , W_2 and W_3 are the trainable parameters, and b_1 , b_2 and b_3 are the scalar biases.

Next, we project the secondary features into primary ones to obtain additional orthogonal features f_o :

$$f_o = f_\gamma - \frac{f_\gamma \cdot f_\eta}{|f_\eta|^2} f_\eta \tag{12}$$

The orthogonal features are further added to the BERT representation to constitute the final text representation:

$$f_{\tau} = f_o \oplus f_{\eta} \tag{13}$$

Finally, we compute the probability that a text belongs to the i - th category by:

$$p_i = \operatorname{Softmax}(f_{\tau} \mathbf{W}_4 + \mathbf{b}_4) \tag{14}$$

where W_4 is the trainable parameters, and b_4 are scalar biases.

3.4 Length Balanced Loss Function

The text length is an important aspect for determining the reading difficulty level. As shown in Table 1, a text with high difficulty level generally contains more tokens than that of low level. For example, on Cambridge dataset, the average length of Level 1 is 141 tokens, while the average length of Level 5 is 751 tokens. When experimented with deep learning methods, texts with short length tend to converge much faster than the texts with long length that influences the final performance.

To address this issue, we revise the loss to handle varying length. Specially, we measure the length distribution by weighting different length attributes, including the average, median, minimum and maximum length:

$$\theta_i = \sum_{j=1}^4 \pi_{ij}, i = 1, 2, \dots, N$$
 (15)

where θ_i represents the length value of the text category *i*, $\pi_{i,1}$, $\pi_{i,2}$, $\pi_{i,3}$ and $\pi_{i,4}$ represent the average, median, minimum and maximum length of the *i*-*th* text, respectively. *N* is the total number of categories.

We normalize the length value to obtain the length coefficient for each category:

$$\kappa_i = \frac{\theta_i}{\sum\limits_{i=1}^N \theta_i} \tag{16}$$

Accordingly, the final loss function for a single sample is defined as:

$$\mathcal{L} = -\sum_{i=1}^{N} \kappa_i^{\rho} y_i \log(p_i) \tag{17}$$

where y_i is the true label of text, ρ is the adjustment factor of length distribution. When $\rho = 0$, it is reduced to the traditional cross entropy loss.

4 Experimental Setup

4.1 Datasets

To demonstrate the effectiveness of our proposed method, we conduct experiments on three English datasets and one Chinese dataset. We split the train, valid and test data according to the ratio of 8:1:1. The statistic distribution of datasets can be found in Table 1.

WeeBit (Vajjala and Meurers, 2012) is often considered as the benchmark data for English readability assessment. It was originally created as an extension of the well-known Weekly Reader corpus. We downsample to 625 passages per class.

OneStopEnglish (Vajjala and Lučić, 2018) is an aligned channel corpus developed for readability assessment and simplification research. Each text is paraphrased into three versions.

Cambridge (Xia et al., 2019) is a dataset consisting of reading passages from the five main suite Cambridge English Exams (KET, PET, FCE, CAE, CPE). We downsample to 60 passages per class.

ChineseLR. ChineseLR is a Chinese dataset that we collected from textbooks of middle and primary school of more than ten publishers. To suit our task, we delete poetry and traditional Chinese texts. Following the standards specified in the *Chinese Curriculum Standards for Compulsory Education*, we category all texts to five difficulty levels.

4.2 Baseline Models

SVM. We employ support vector machines as the traditional machine learning classifier. The input to the model is the linguistic feature f_{γ} . We adopt MinMaxScaler (ranging from -1 to 1) for linguistic

Dataset	W	eeBit	On	eStopE	Can	ıbridge	Chi	neseLR
Level	Passages	Avg.Length	Passages	Avg.Length	Passages	Avg.Length	Passages	Avg.Length
1	625	152	189	535	60	141	814	266
2	625	189	189	678	60	271	1063	679
3	625	295	189	825	60	617	1104	1140
4	625	242	0	0	60	763	762	2165
5	625	347	0	0	60	751	417	3299
All	3125	245	567	679	300	509	4160	1255

Table 1: Statistics of datasets for readability assessment. Avg.Length means the average tokens per passage.

features and use the RBF kernel function. We use the libsvm 1 framework for experiments.

BERT. We utilize f_{η} in Equation 9 followed by a linear layer classifier as our BERT baseline model.

4.3 Training and Evaluation Details

For the selection of the difficulty level lexicon Ω , on the English dataset, we use the lexicon released by Maddela and Xu (2018), where we only use the first 4 levels. On the Chinese dataset, we use the *Compulsory Education Vocabulary* (Su, 2019). The word embedding features of English and Chinese word clustering algorithms are respectively used (Pennington et al., 2014) and (Song et al., 2018). We use the Wikipedia corpus ² for pre-training the semi-supervised topic models. Please refer to **Appendix B** for some other details.

We do experiments using the Pytorch (Paszke et al., 2019) framework. For training, we use the AdamW optimizer, the weight decay is 0.02 and the warm-up ratio is 0.1. The mixing pooling ratio λ is set to 0.5. Other specific parameter settings are shown in Table 2.

For evaluation, we calculate the accuracy, weighted F1 score, precision, recall and quadratic weighted kappa (QWK). We repeated each experiment three times and reported the average score.

Dataset	Batch	MaxLen	Epoch	lr	ρ
WeeBit	8	512	10	3e-5	0.8
OneStopE	8	500×2	10	3e-5	0.4
Cambridge	8	500×2	10	3e-5	0.6
ChineseLR	2	500×8	10	3e-5	0.4

Table 2: Part of the hyperparameter settings, where $500 \times n$ means to split the text into *n* segments with a length of 500 tokens.

5 Results and Analysis

5.1 Overall Results

The experimental results of all models are summarized in Table 3. First of all, it should be noted that there are only a few studies on readability assessment, and there is no unified standard for data division and experimental parameter configuration. This has led to large differences in the results of different research works.

Our BERT-FP-LBL model achieves consistent improvements over the baselines on all four datasets, which validates the effectiveness of our proposed method. In terms of F1 metrics, our method improves WeeBit and ChineseLR by 1.66 and 3.7 compared to the baseline BERT model. Overall, our model achieves state-of-the-art performance on WeeBit and Cambridge. On OneStopEnglish, our model also achieves competitive results compared to previous work (Lee et al., 2021), also achieving near-perfect classification accuracy of 99%.

Comparing the experimental results of SVM and the base BERT, it can be observed that on Cambridge and ChineseLR, SVM outperforms BERT. We believe this benefits from the linguistic features of our design.

5.2 Ablation Study

To illustrate the contribution of each module in our model, we conduct ablation experiments on WeeBit and ChineseLR, and the results are reported in Table 4.

When **AW** is removed, the CorEx changes from semi-supervised to unsupervised. The F1 scores of WeeBit and ChineseLR drop by 0.31 and 0.52, respectively, and when **TFDK** is removed, the corresponding F1 scores drop by 0.61 and 1.27, respectively. This indicates that our topic features incorporating difficulty knowledge indeed contribute to readability assessment.

Furthermore, when **FP** is removed, as described in Section 3.3, the simple splice operation brings

¹https://www.csie.ntu.edu.tw/~cjlin/ libsvm/

²https://dumps.wikimedia.org/

Dataset	Metrics	Qiu-2021	Mar-2021	Lee-2021	SVM	BERT	BERT-FP-LBL
	Accuracy	87.32	85.73	90.50	79.37	91.11	92.70
	F1	-	85.81	90.50	79.27	91.07	92.73
WeeBit	Precision	-	86.58	90.50	79.26	91.42	92.89
	Recall	-	85.73	90.40	79.37	91.11	92.70
	QWK	-	95.27	96.80	93.22	97.36	97.78
	Accuracy	86.61	78.72	99.00	89.47	97.66	99.42
	F1	-	78.88	99.50	89.32	97.66	99.41
OneStopE	Precision	-	79.77	99.50	89.41	97.83	99.44
-	Recall	-	78.72	99.60	89.47	97.66	99.42
	QWK	-	82.45	99.60	92.31	92.98	98.25
	Accuracy	78.52	-	76.30	83.33	82.22	87.78
	F1	-	-	75.20	83.45	81.97	87.73
Cambridge	Precision	-	-	79.20	90.91	82.96	89.46
-	Recall	-	-	75.30	83.33	82.22	87.78
	QWK	-	-	91.90	91.97	94.65	96.87
	Accuracy	-	-	-	76.67	75.16	78.89
	F1	-	-	-	76.53	75.05	78.75
ChineseLR	Precision	-	-	-	76.47	75.95	79.43
	Recall	-	-	-	76.67	75.16	78.89
	QWK	-	-	-	90.60	90.40	91.63

Table 3: Experimental results on both English and Chinese datasets for readability assessment. We compare our method with the recent three works, including Qiu-2021 (Qiu et al., 2021), Mar-2021 (Martine et al., 2021) and Lee-2021 (Lee et al., 2021).

Model	WeeBit	ChineseLR
BERT-FP-LBL	92.73	78.75
-AW	92.42	78.23
-TFDK	92.12	77.48
-FP	92.25	78.27
-LBL	91.76	76.94

Table 4: Ablation study in terms of F1 metric. -AW means to remove the anchor words. -TFDK means remove the difficulty-aware topic features. -FP means that the linguistic features and neural network features are directly spliced without using projection filtering. -LBL means training using the standard cross-entropy loss function ($\rho = 0$).

some duplication or even negative information to the model. The F1 scores of WeeBit and ChineseLR both drop by 0.48.

Finally, when **LBL** is removed, the F1 scores of WeeBit and ChineseLR drop by 0.97 and 1.81, respectively. We believe that the difference in the length distribution of the dataset affects the convergence speed of different categories, which in turn will have an impact on the results. Besides, the drop in F1 metric is much more severe on ChineseLR than on WeeBit, and this result can be attributed to the more severe length imbalance on ChineseLR as shown in Table 1.

5.3 Analysis on the Length-balanced Loss

To explore the effect of length-balanced loss, we set different ρ to conduct experiments. The larger the ρ is, the difference between the loss of different

categories is bigger. The loss difference leads to different convergence rates. When ρ is 0, the loss function is the standard cross entropy loss, and there is no difference in the loss contributed by different categories. The specific results are shown in Figure 2.

For BERT, the optimal value of ρ is relatively large, which means the model needs a relatively big difference in the loss to solve the problem of unbalanced text length. This indicates that there are indeed differences in the convergence speed between different classes, and this difference can be reduced by correcting the loss contributed by different classes. After adding orthogonal features, the optimal value of ρ is relatively small. We think that whether the text is short or long, the number of parameters of its corresponding orthogonal features is fixed and does not require the length-balanced loss to adjust. So, when BERT features are combined with orthogonal features, the optimal value of ρ will be lower than that in BERT alone.

In addition, the optimal value of ρ on WeeBit is 0.8, while the optimal value of ρ on ChineseLR is 0.4. This is perhaps because the WeeBit dataset has a small span of length distribution (maximum 512 truncation), and we need to relatively amplify the differences between different categories. However, the length distribution of the ChineseLR dataset has a large span (500×8), and we need to relatively narrow the differences between different categories.

Of course, the optimal value of ρ is related to the

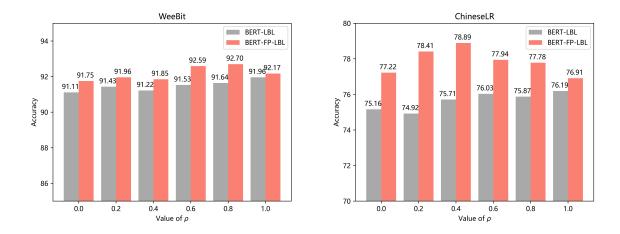


Figure 2: Influences of LBL on classification accuracy.

specific data distribution, which is a parameter that needs to grid search. Generally speaking, when the length difference between different categories is small, we set ρ relatively large, and when the length difference between different categories is large, we set ρ relatively small.

5.4 Analysis on the Difficulty-aware Topic Features

To further explore the impact of topic features with domain knowledge, we visualize the traditional features f_{α} , difficulty-aware topic features f_{β} and combining features f_{γ} . Specifically, On WeeBit and ChineseLR, we randomly selected 50 samples from each level of 1, 3 and 5 for visualization, as shown in Figure 3 and 4.

For texts of completely different difficulty, their traditional features are near in the latent space. This shows that traditional features pay more attention to semantic information rather than reading difficulty. By adding difficulty-aware topic features, texts of different difficulty are better differentiated. Further, the combination of two kinds of features achieves a better ability to distinguish reading difficulty.

5.5 Consistency Test with Human Experts

To judge the difficulty level of a text is also a hard task for humans, and so we conduct experiments to investigate how consistent the model's inference results are with human experts. We collected 200 texts from extracurricular reading materials, and hired three elementary school teachers to do doubleblind labeling. Each text is required to annotate with an unique label 1/2/3, corresponding to the first/second/third level. Our model (denoted as M4) is regarded as a single expert that is equal to the other three human experts (E1/E2/E3). We calculate the Spearman correlation coefficient of annotation results between each pair, and report the results in Table 5.

Rater	E1	E2	E3	M4
E1	1.000	-	-	-
E2	$0.922^{\star\star}$	1.000	-	-
E3	$0.829^{\star\star}$	$0.833^{\star\star}$	1.000	-
M4	$0.836^{\star\star}$	0.820^{**}	0.807^{**}	1.000

Table 5: The Spearman correlation coefficient between four experts, where M4 is our model. ** indicates a significant correlation at the 0.01 level (two-tailed).

On the whole, there is a significant correlation at the 0.01 level between human experts (E1, E2 or E3) and our model. On the one hand, there is still a certain gap between the model and human experts (E1 and E2). On the other hand, the inference results of our model are comparable with the human expert E3. Especially, when E1 is adopted as the reference standard, the consistency of our model prediction is slightly higher than that of E3 (0.836 vs. 0.829). When E2 is regarded as the reference standard, the consistency of our model prediction is slightly lower than that of E3.

Although there is no unified standard for the definition of "text difficulty", which relies heavily on the subject experiences of experts, our model achieves competitive results with human experts.

6 Conclusions

In this paper, we propose a unified neural network model **BERT-FP-LBL** for readability assessment. We extract difficulty-aware topic fea-

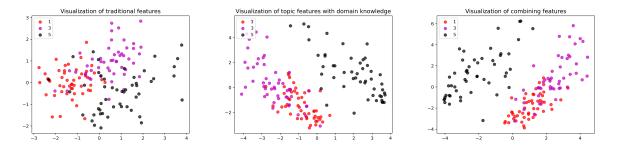


Figure 3: Visualization of different kinds of features on WeeBit.

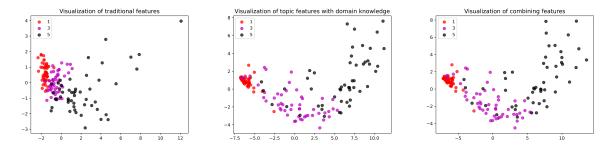


Figure 4: Visualization of different kinds of features on ChineseLR.

tures through the Anchored Correlation Explanation method, and fuse linguistic features with BERT representations via projection filtering. We propose a length-balanced loss to cope with the imbalance length distribution. We conduct extensive experiments and detailed analyses on both English and Chinese datasets. The results show that our method achieves state-of-the-art results on three datasets and near-perfect accuracy of 99% on one English dataset.

Limitations

From the perspective of experimental setup, there is no uniform standard for data division and experimental parameter configuration due to less research on readability assessment. This leads to large differences in the results of different studies (Qiu et al., 2021; Martinc et al., 2021; Lee et al., 2021), and the results of the corresponding experiments are not comparable. Therefore, objectively speaking, our comparison object is only the baseline model, which lacks a fair comparison with previous work.

From the perspective of readability assessment task, since different datasets have different difficulty scales and different length distributions. In order to ensure the performance on the dataset as much as possible, our length-balanced loss parameters are mainly calculated according to the length distribution of the corresponding dataset, and it is impossible to transfer across datasets directly, which is also a major difficulty in this field. In cross-dataset and cross-language scenarios, there is a lack of a unified approach. Without new ways to deal with the difficulty scales of different datasets, or without large public datasets, developing a general readability assessment model will always be challenging.

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A Chinese Traditional Features

Idx	Dim	Feature description			
1	1	Total number of characters			
2	1	Number of character types			
3 4	1	Type Token Ratio (TTR)			
4	1	Average number of strokes			
5	1	Weighted average number of strokes			
6	25	Number of characters with different strokes			
7	25	Proportion of characters with different strokes			
8	1	Average character frequency			
9	1	Weighted average character frequency			
10	1	Number of single characters			
11	1	Proportion of single characters			
12	1	Number of common characters			
13	1	Proportion of common characters			
14	1	Number of unregistered characters			
15	1	Proportion of unregistered characters			
16	1	Number of first-level characters			
17	1	Proportion of first-level characters			
18	1	Number of second-level characters			
19	1	Proportion of second-level characters			
20	1	Number of third-level characters			
21	1	Proportion of third-level characters			
22	1	Number of fourth-level characters			
23	1	Proportion of fourth-level characters			
24	1	Average character level			

Table 6: Character features description.

11Total number of words21Number of word types31Type Token Ratio (TTR)41Average word length51Weighted average word length61Average word frequency71Weighted average word frequency81Number of single-character words91Proportion of single-character words101Number of two-character words111Proportion of two-character words121Number of three-character words131Proportion of three-character words141Number of four-character words151Proportion of four-character words161Number of multi-character words171Proportion of multi-character words181Number of single words201Proportion of single words211Number of first-level words231Number of first-level words241Proportion of first-level words251Number of second-level words261Proportion of third-level words271Number of fourth-level words281Proportion of fourth-level words291Number of fourth-level words301Proportion of fourth-level words311Average word level3257Number of words with different POS <tr <tr="">32</tr>	Idx	Dim	Feature description			
31Type Token Ratio (TTR)41Average word length51Weighted average word length61Average word frequency71Weighted average word frequency81Number of single-character words91Proportion of single-character words101Number of two-character words111Proportion of two-character words121Number of three-character words131Proportion of three-character words141Number of four-character words151Proportion of four-character words161Number of multi-character words171Proportion of multi-character words181Number of single words201Proportion of single words211Number of single words221Proportion of first-level words231Number of first-level words241Proportion of first-level words251Number of second-level words261Proportion of third-level words271Number of fourth-level words281Proportion of fourth-level words301Proportion of fourth-level words311Average word level3257Number of words with different POS	-	1	Total number of words			
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71Weighted average word frequency81Number of single-character words91Proportion of single-character words101Number of two-character words111Proportion of two-character words121Number of three-character words131Proportion of three-character words141Number of four-character words151Proportion of four-character words161Number of multi-character words171Proportion of multi-character words181Number of single words201Proportion of single words211Number of single words221Proportion of first-level words231Number of first-level words241Proportion of first-level words251Number of second-level words261Proportion of third-level words271Number of fourth-level words281Proportion of fourth-level words301Proportion of fourth-level words311Average word level3257Number of words with different POS		1	Weighted average word length			
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101Number of two-character words111Proportion of two-character words121Number of three-character words131Proportion of three-character words141Number of four-character words151Proportion of four-character words161Number of multi-character words171Proportion of multi-character words181Number of single words201Proportion of single words211Number of single words221Proportion of unregistered words231Number of first-level words241Proportion of first-level words251Number of second-level words261Proportion of third-level words271Number of fourth-level words281Proportion of third-level words301Proportion of fourth-level words311Average word level3257Number of words with different POS		1	Number of single-character words			
111Proportion of two-character words121Number of three-character words131Proportion of three-character words141Number of four-character words151Proportion of four-character words161Number of multi-character words171Proportion of multi-character words181Number of single words201Proportion of single words211Number of unregistered words221Proportion of first-level words231Number of first-level words241Proportion of second-level words251Number of third-level words261Proportion of third-level words271Number of fourth-level words291Number of fourth-level words301Proportion of fourth-level words311Average word level3257Number of words with different POS	9	1	Proportion of single-character words			
121Number of three-character words131Proportion of three-character words141Number of four-character words151Proportion of four-character words161Number of multi-character words171Proportion of multi-character words181Number of single words201Proportion of single words211Number of unregistered words221Proportion of first-level words231Number of first-level words241Proportion of second-level words251Number of third-level words261Proportion of third-level words271Number of fourth-level words281Proportion of third-level words301Proportion of fourth-level words311Average word level3257Number of words with different POS	10	1	Number of two-character words			
131Proportion of three-character words141Number of four-character words151Proportion of four-character words161Number of multi-character words171Proportion of multi-character words181Number of idioms191Number of single words201Proportion of single words211Number of unregistered words221Proportion of first-level words231Number of first-level words241Proportion of second-level words251Number of second-level words261Proportion of third-level words271Number of fourth-level words281Proportion of fourth-level words301Proportion of fourth-level words311Average word level3257Number of words with different POS	11	1	Proportion of two-character words			
141Number of four-character words151Proportion of four-character words161Number of multi-character words171Proportion of multi-character words181Number of idioms191Number of single words201Proportion of single words211Number of unregistered words221Proportion of unregistered words231Number of first-level words241Proportion of first-level words251Number of second-level words261Proportion of third-level words271Number of fourth-level words281Proportion of third-level words301Proportion of fourth-level words311Average word level3257Number of words with different POS	12	1	Number of three-character words			
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161Number of multi-character words171Proportion of multi-character words181Number of idioms191Number of single words201Proportion of single words211Number of unregistered words221Proportion of unregistered words231Number of first-level words241Proportion of first-level words251Number of second-level words261Proportion of third-level words271Number of third-level words281Proportion of fourth-level words301Proportion of fourth-level words311Average word level3257Number of words with different POS	14	1	Number of four-character words			
171Proportion of multi-character words181Number of idioms191Number of single words201Proportion of single words211Number of unregistered words221Proportion of unregistered words231Number of first-level words241Proportion of first-level words251Number of second-level words261Proportion of third-level words271Number of third-level words281Proportion of fourth-level words301Proportion of fourth-level words311Average word level3257Number of words with different POS	15	1	Proportion of four-character words			
181Number of idioms191Number of single words201Proportion of single words211Number of unregistered words221Proportion of unregistered words231Number of first-level words241Proportion of first-level words251Number of second-level words261Proportion of second-level words271Number of third-level words281Proportion of fourth-level words291Number of fourth-level words301Proportion of fourth-level words311Average word level3257Number of words with different POS	16	1	Number of multi-character words			
191Number of single words201Proportion of single words211Number of unregistered words221Proportion of unregistered words231Number of first-level words241Proportion of first-level words251Number of second-level words261Proportion of third-level words271Number of third-level words281Proportion of third-level words291Number of fourth-level words301Proportion of fourth-level words311Average word level3257Number of words with different POS	17	1	Proportion of multi-character words			
201Proportion of single words211Number of unregistered words221Proportion of unregistered words231Number of first-level words241Proportion of first-level words251Number of second-level words261Proportion of second-level words271Number of third-level words281Proportion of third-level words291Number of fourth-level words301Proportion of fourth-level words311Average word level3257Number of words with different POS	18	1	Number of idioms			
211Number of unregistered words221Proportion of unregistered words231Number of first-level words241Proportion of first-level words251Number of second-level words261Proportion of second-level words271Number of third-level words281Proportion of third-level words291Number of fourth-level words301Proportion of fourth-level words311Average word level3257Number of words with different POS		1	Number of single words			
221Proportion of unregistered words231Number of first-level words241Proportion of first-level words251Number of second-level words261Proportion of second-level words271Number of third-level words281Proportion of third-level words291Number of fourth-level words301Proportion of fourth-level words311Average word level3257Number of words with different POS		1	Proportion of single words			
221Proportion of unregistered words231Number of first-level words241Proportion of first-level words251Number of second-level words261Proportion of second-level words271Number of third-level words281Proportion of third-level words291Number of fourth-level words301Proportion of fourth-level words311Average word level3257Number of words with different POS	21	1	Number of unregistered words			
241Proportion of first-level words251Number of second-level words261Proportion of second-level words271Number of third-level words281Proportion of third-level words291Number of fourth-level words301Proportion of fourth-level words311Average word level3257Number of words with different POS		1				
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261Proportion of second-level words271Number of third-level words281Proportion of third-level words291Number of fourth-level words301Proportion of fourth-level words311Average word level3257Number of words with different POS		1	Proportion of first-level words			
271Number of third-level words281Proportion of third-level words291Number of fourth-level words301Proportion of fourth-level words311Average word level3257Number of words with different POS		1	Number of second-level words			
281Proportion of third-level words291Number of fourth-level words301Proportion of fourth-level words311Average word level3257Number of words with different POS		1	Proportion of second-level words			
291Number of fourth-level words301Proportion of fourth-level words311Average word level3257Number of words with different POS		1	Number of third-level words			
301Proportion of fourth-level words311Average word level3257Number of words with different POS	28	1				
311Average word level3257Number of words with different POS		1	Number of fourth-level words			
311Average word level3257Number of words with different POS	30	1	Proportion of fourth-level words			
		-				
22 57 Depending of words with different DOS	32	57	Number of words with different POS			
33 37 Proportion of words with different POS	33	57	Proportion of words with different POS			

Table 7: Word features description.

Idx	Dim	Feature description
1	1	Total number of sentences
2	1	Average characters in a sentence
3	1	Average words in a sentence
4	1	Maximum characters in a sentence
5	1	Maximum words in a sentence
6	1	Number of clauses
7	1	Average characters in a clause
8	1	Average words in a clause
9	1	Maximum characters in a clause
10	1	Maximum words in a clause
11	30	Sentence length distribution
12	1	Average syntax tree height
13	1	Maximum syntax tree height
14	1	Syntax tree height <= 5 ratio
15	1	Syntax tree height <= 10 ratio
16	1	Syntax tree height <= 15 ratio
17	1	Syntax tree height >= 16 ratio
18	14	Dependency distribution

Table 8: Sentence features description.

Idx	Dim	Feature description
1	1	Total number of paragraphs
2	1	Average characters in a paragraph
3	1	Average words in a paragraph
4	1	Maximum characters in a paragraph
5	1	Maximum words in a paragraph

Table 9: Sentence features description.

B Semi-supervised Topic Model Related Parameters

Pre-training	English	Chinese
Length range	300~1000	$500 \sim 5000$
Items	209018	180977
Topics	120	160
Anchor topics	60	80
Anchor strength	4	5
First-level word anchor topics	16	15
Second-level word anchor topics	21	36
Third-level word anchor topics	14	18
Fourth-level word anchor topics	9	11

Table 10: Details for pre-training the topic model.

C SVM model Related Hyperparameters

Dataset	с	g
WeeBit	32	0.004
OneStopE	8	0.002
Cambridge	16	0.004
ChineseLR	64	0.032

Table 11: SVM best parameters.

The search range of parameter *c* is [2, 4, 8, 16, 32, 64, 128, 256, 512, 1024, 2048, 4096, 8192, 16384, 32768], and the search range of parameter *g* is [0.002, 0.004, 0.008, 0.016, 0.032, 0.064, 0.128, 0.256, 0.512, 1.024, 2.048, 4.096].