

Pierce the Mists, Greet the Sky: Decipher Knowledge Overshadowing via Knowledge Circuit Analysis

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Abstract

Large Language Models (LLMs), despite their remarkable capabilities, are hampered by hallucinations. A particularly challenging variant, **knowledge overshadowing**, occurs when one piece of activated knowledge inadvertently masks another relevant piece, leading to erroneous outputs even with high-quality training data. Current understanding of overshadowing is *largely confined to inference-time observations, lacking deep insights into its origins and internal mechanisms during model training*. Therefore, we introduce **PHANTOMCIRCUIT**, a novel framework designed to comprehensively analyze and detect knowledge overshadowing. By innovatively employing knowledge circuit analysis, PHANTOMCIRCUIT dissects the function of key components in the circuit and how the attention pattern dynamics contribute to the overshadowing phenomenon and its evolution throughout the training process. Extensive experiments demonstrate PHANTOMCIRCUIT’s effectiveness in identifying such instances, offering novel insights into this elusive hallucination and providing the research community with a new methodological lens for its potential mitigation. Our code can be found in <https://github.com/halfmorepiece/PhantomCircuit>.

1 Introduction

Large Language Models (LLMs) have witnessed explosive growth in recent years, demonstrating remarkable capabilities across a multitude of domains, including natural language understanding, generation, reasoning, and even cross-modal tasks (Chang et al., 2024; Zhao et al., 2024; Yan et al., 2025a, 2024a; Xun et al., 2025). Their proficiency has catalyzed transformative advancements in various applications. However, a persistent challenge that tempers their widespread adoption and reliability is the phenomenon of hallucination. Broadly,

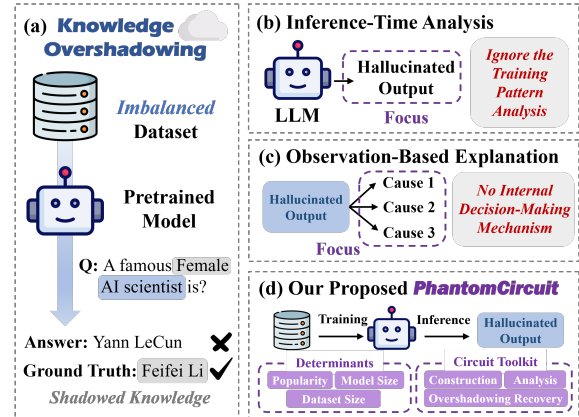


Figure 1: Illustrative comparison of previous research with inference-time analysis (b) and observation-based explanation (c) vs our proposed PHANTOMCIRCUIT (d) on knowledge overshadowing (a).

hallucinations refer to instances where models generate content that is factually incorrect, nonsensical, or unfaithful to the provided source context, despite appearing coherent and fluent (Rawte et al., 2023; Chakraborty et al., 2025; Wang et al., 2025).

While substantial research has been dedicated to understanding the causes and detection of general hallucinations, a specific variant known as “**knowledge overshadowing**” warrants deeper investigation (Zhang et al., 2024b, 2025a). This phenomenon is particularly perplexing because it can manifest even when models are trained on high-quality, meticulously curated pre-training corpora. Current understanding, primarily derived from inference-time observations, characterizes overshadowing as a scenario where, for a given query, one piece of activated knowledge inadvertently “overshadows” another relevant knowledge. This interference ultimately biases the model’s reasoning process, leading to a hallucinatory output, as illustrated in Figure 1 (a).

Nevertheless, existing explorations into knowledge overshadowing suffer from notable limitations. ❶ They *predominantly focus on inference-*

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time analysis, as shown in Figure 1 (b). While valuable for identifying the occurrence of overshadowing, such observations offer a surface-level understanding and often fall short of elucidating how these detrimental patterns are learned during the training phase. ② The explanations for overshadowing are often *speculatively inferred from these observational outcomes* rather than being rigorously investigated through dedicated interpretability tools that can probe the model’s internal decision-making mechanisms, as shown in Figure 1 (c). Consequently, a more comprehensive analytical framework is imperative to dissect this phenomenon from its origins to its manifestation.

To bridge this gap, we introduce **PHANTOMCIRCUIT**, a novel framework designed to comprehensively analyze and detect the knowledge overshadowing phenomenon. Specifically, PHANTOMCIRCUIT facilitates an in-depth examination of the evolution of overshadowing hallucinations throughout the training process, correlating their emergence and prevalence with core factors such as knowledge popularity, model size, and dataset size. Then, by leveraging knowledge circuit analysis as a key interpretability technique, we aim to trace the flow of information and the formation of knowledge representations within attention heads, thereby uncovering the internal mechanisms giving rise to overshadowing. Furthermore, we propose to optimize the number of edges within these circuits, thus alleviating the knowledge overshadowing. As illustrated in Figure 1 (d), our overall work aims to provide a clearer, mechanistic understanding and potential strategies for this elusive type of hallucination.

Our contributions can be summarized as follows:

- We introduce PHANTOMCIRCUIT, the first comprehensive framework designed to systematically analyze and detect knowledge overshadowing, delving into its mechanistic nature and evolution throughout model training.
- We pioneer the use of knowledge circuit analysis to dissect the internal workings of attention heads, specifically elucidating how competing knowledge pathways contribute to the overshadowing phenomenon.
- We conduct extensive experiments to demonstrate PHANTOMCIRCUIT’s efficacy in detecting knowledge overshadowing, offering novel

insights and a new methodological lens for the research community.

2 Related Work

2.1 Hallucination Detection

Factuality hallucination detection, which aims to evaluate whether the output of LLMs aligns with real-world facts, typically involves either external fact-checking or internal uncertainty analysis (Huang et al., 2025; Dang et al., 2024; Zheng et al., 2024; Zou et al., 2024; Zhou et al., 2024; Zhu et al., 2024). For instance, FACTSCORE (Min et al., 2023) decomposes a generation into atomic facts and calculates the proportion that are supported by reliable knowledge sources. FACTOOL (Chern et al., 2023), on the other hand, integrates multiple tools such as Google Search and Google Scholar to gather external evidence and assess the factuality of generated content. In contrast, methods like Chain-of-Verification (Dhuliawala et al., 2023), probability-based assessments (Kadavath et al., 2022; Zhang et al., 2024a), and uncertainty estimation approaches (Varshney et al., 2023; Yao et al., 2023; Luo et al., 2023) rely on LLMs’ internal parametric knowledge or uncertainty signals to predict potential hallucinations. Among these efforts, knowledge overshadowing (Zhang et al., 2025a) offers a novel perspective by modeling hallucination behavior from the perspective of knowledge representation, providing an efficient strategy for proactive prevention.

2.2 Knowledge Circuit Analysis

In the context of mechanistic interpretability (Rai et al., 2024; Huo et al., 2024; Huang et al., 2024a), computations in Transformer-based language models are viewed as a connected directed acyclic graph encompassing components such as MLPs and attention layers (Syed et al., 2023; Conmy et al., 2023; Huang et al., 2024b). A **circuit** refers to a sparse computational subgraph that significantly influences the model’s behavior on a specific task (Olah et al., 2020; Elhage et al., 2021; Wang et al., 2022). Building on this, Yao et al. (2024) introduce the concept of **knowledge circuits**, hypothesizing that cooperation among components reveals implicit knowledge in LLMs. Further, Ou et al. (2025); Zucchet et al. (2025); Hakimi et al. (2025) explore how such circuits evolve during continual pre-training, providing insights into knowledge acquisition. To enable effective knowledge editing, CaKE (Yao

et al., 2024) proposes a Circuit-aware Knowledge Editing method that guides models to activate modified knowledge and form new reasoning pathways. In this paper, we analyze the phenomenon of knowledge overshadowing through the lens of knowledge circuits, contributing new perspectives to LLM hallucination detection.

See more related work in Appendix A.1.

3 Methodology

This section first defines the knowledge overshadowing phenomenon and its quantitative evaluation. Subsequently, we detail the PHANTOMCIRCUIT framework, which encompasses methods for analyzing its training dynamics and for constructing and analyzing knowledge circuits to understand its internal mechanisms¹.

3.1 Knowledge Overshadowing

Knowledge overshadowing refers to a specific type of hallucination where *less prevalent, subordinate knowledge* is suppressed by *high-frequency, dominant knowledge* when both are associated with *common background knowledge* (Zhang et al., 2025a).

As shown in Figure 2, let X_{dom} denote dominant knowledge entities and X_{sub} denote subordinate knowledge entities, both potentially co-occurring with background knowledge X_{bg} . The core idea is that a strong learned pattern $X_{dom} \leftrightarrow X_{bg}$ can "over-generalize" where the model primarily associates X_{dom} with X_{bg} . Consequently, when the model encounters X_{sub} with X_{bg} , denoted as $X_{sub} \leftrightarrow X_{bg}$, it may erroneously favor outputs related to X_{dom} due to the stronger $X_{dom} \leftrightarrow X_{bg}$ pattern.

3.1.1 Knowledge Overshadowing Occurrence

When the input prompt is a knowledge pair composed of background knowledge and dominant knowledge, denoted as $P_{dom} = (X_{bg}, X_{dom})$, and the model correctly generates the answer corresponding to the dominant knowledge, denoted as Y_{dom} , we consider this outcome, represented by the pair (P_{dom}, Y_{dom}) , as a successful recall of dominant knowledge.

When the input prompt is P_{sub} , but the model wrongly generates Y_{dom} , knowledge overshadowing occurs for this query-response instance, resulting in the (P_{sub}, Y_{dom}) . In the case shown in Figure

2, if overshadowing occurs, the model will incorrectly answer "Beijing" to the input prompt "Where is the most important economic center of China?".

3.1.2 Quantitative Indicators

Let N_{dom} be the number of instances of the dominant knowledge prompt P_{dom} and N_{sub} be the number of instances of the subordinate knowledge prompt P_{sub} in a group of data, respectively. In the case shown in Figure 2, N_{dom} and N_{sub} are 2 and 1, respectively. The entire dataset might contain multiple different groups of imbalanced data.

During autoregressive generation tasks performed by the model, let M_{sub} be the number of times when overshadowing instances (P_{sub}, Y_{dom}) occur, and M_{dom} be the number of times (P_{dom}, Y_{dom}) occurs. Then, we can define the absolute extent of the knowledge overshadowing effect, the Absolute Overshadowing rate ($\mathcal{AO}$) and calculate it using M_{sub} and N_{sub} ,

$$\mathcal{AO} = p(Y_{dom}|P_{sub}) = \frac{M_{sub}}{N_{sub}}. \quad (1)$$

To account for the model's inherent performance and potential noise affecting the overshadowing rate, we also introduce R_{dom} for dominant knowledge inputs:

$$R_{dom} = p(Y_{dom}|P_{dom}) = \frac{M_{dom}}{N_{dom}}, \quad (2)$$

which represents the recall rate for P_{dom} query-response instances.

The Relative Overshadowing rate ($\mathcal{RO}$) is then defined as:

$$\mathcal{RO} = \frac{\mathcal{AO}}{R_{dom}} = \frac{p(Y_{dom}|P_{sub})}{p(Y_{dom}|P_{dom})}. \quad (3)$$

3.1.3 Overshadowing Influence Factors

Knowledge Popularity (P) is the fundamental cause of the knowledge overshadowing phenomenon and serves as its primary influencing factor. P is defined as the ratio of N_{dom} to N_{sub} in a group,

$$P = \frac{N_{dom}}{N_{sub}}. \quad (4)$$

In the case of Figure 2, $P = 2$. A higher value of P signifies a more severe data imbalance.

Model Size (M), referring to the number of model parameters, also impacts knowledge overshadowing. A larger M generally implies stronger generalization capabilities, causing the model to

¹Our code will be available upon acceptance.

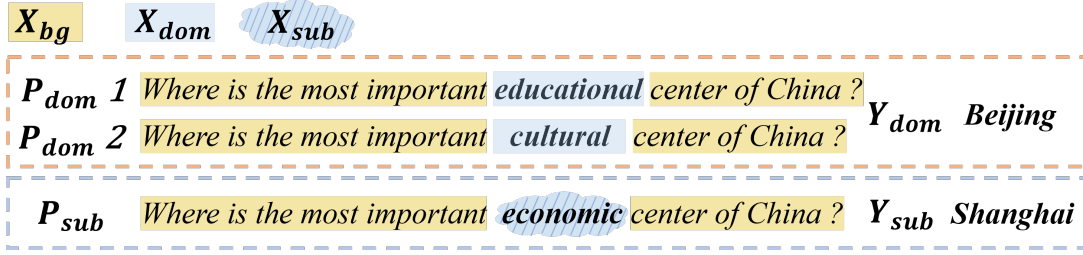


Figure 2: A group of imbalanced natural language data of knowledge overshadowing. The X_{bg} , X_{dom} and X_{sub} are background, dominant and subordinate knowledge respectively. The P_{dom} and P_{sub} are prompt with dominant and subordinate knowledge respectively, their corresponding answers are Y_{dom} and Y_{sub} .

rapidly generalize the $X_{dom} \leftrightarrow X_{bg}$ to instances involving $X_{sub} \leftrightarrow X_{bg}$ and exacerbating overshadowing.

In addition to the factors mentioned in (Zhang et al., 2025a, 2024b), aiming to analyze the dynamic evolution of knowledge overshadowing during the training process, we extend our consideration to total number of tokens, the **Dataset Size (D)** in the training set. Furthermore, the **average loss proportion of subordinate knowledge $\mathcal{LP}$ within an epoch during training** is defined as

$$\mathcal{LP} = \frac{\text{loss}(P_{sub})}{\text{total loss}}, \quad (5)$$

which measures the allocation of the model’s efforts for the optimization of subordinate knowledge and recovery from knowledge overshadowing.

3.2 Analysis Framework PHANTOMCIRCUIT

Our proposed knowledge circuit-based overshadowing analysis framework involves the overshadowing dynamics analysis during training and circuit-based internal mechanism analysis.

3.2.1 Overshadowing Dynamic Analysis

Our framework provides a novel dynamic analysis of knowledge overshadowing during model training. By manipulating P, M, and D, we monitor $\mathcal{RO}$ across epochs. We focus on identifying the onset, duration, and recovery stages of overshadowing to understand their modulation by P, M, and D. Recognizing P as a key factor, we also explore how $\mathcal{LP}$ co-evolves with $\mathcal{RO}$ under these variables, aiming to uncover the role of $\mathcal{LP}$ in explaining overshadowing dynamics.

3.2.2 Knowledge Circuit Construction

We construct the knowledge circuit, a sparse computational subgraph $C \subseteq G$, where $G = (V, E)$ is the directed acyclic graph representation of LLMs. The node set V encompasses input embeddings, attention heads, MLP layers, and output logits. The

edge set E represents the information flow between these components. Our goal is to identify a subgraph C that is critical for recognizing the key component of given input prompt, particularly in knowledge overshadowing, is $\{X_{dom}, X_{sub}\}$, the difference between P_{dom} and P_{sub} . The adapted construction method is similar to Edge Attribution Patching with Integrated Gradients (EAP-IG) (Hanna et al., 2024), which involves:

Paired inputs. For a given X_{bg} , we create a pair of input prompts, the clean input P_{sub} corresponding to our expected output Y_{sub} in the overshadowing case, and the corrupt input P_{dom} serving for the contrast mentioned below.

Activation difference calculation. After running this pair of inputs through the model, we calculate the difference in activation values $\Delta A(v_p), \Delta A(v_c)$ for the parent node v_p and child node v_c of each edge under these distinct inputs, $\Delta A(v_p) = A_{clean}(v_p) - A_{corrupt}(v_p)$, where $A_{clean}(v_p)$ and $A_{corrupt}(v_p)$ are the activations of the parent node for the clean input P_{sub} and the corrupt input P_{dom} , respectively.

Edge score calculation. The importance $S(e)$ of an edge $e = (v_p, v_c)$ is scored based on how patching v_p ’s activation (using $\Delta A(v_p)$) influences a metric $\mathcal{M}$, which assesses the model’s ability to correctly output Y_{sub} rather than Y_{dom} for P_{sub} inputs. Using the Integrated Gradients (IG), $S(e)$ is approximated as:

$$S(e) \approx \text{Exp} \left[\Delta A(v_p) \cdot \frac{\partial \mathcal{M}(Y_{sub}|P_{sub})}{\partial A(v_p)} \right]. \quad (6)$$

Circuit construction. Edges with scores $|S(e)|$ below a threshold τ are pruned. The remaining subgraph forms the knowledge circuit C . See more details about construction in Appendix B.1

Circuit in Knowledge Overshadowing. In the context of knowledge overshadowing, the metric $\mathcal{M}$ is defined as the difference between the output logits of Y_{sub} and Y_{dom} . A positive value

for $\mathcal{M}$ indicates that the model correctly predicts Y_{sub} . Therefore, we can represent the circuit where overshadowing occurs as $C_{overshadowed} = \{V, E\}$ with $\mathcal{M} < 0$ and $S(E|P_{sub}, Y_{dom}) \geq \tau$. Furthermore, the competition between the dominant and subordinate knowledge pairs during circuit construction is quantified by the activation values of different input P_{dom} and P_{sub} , $\Delta A(v_p) = A_{P_{sub}}(v_p) - A_{P_{dom}}(v_p)$.

3.2.3 Circuit-based Analysis

PHANTOMCIRCUIT mainly focuses on the attention heads in C and follows these steps:

Node Attention Analysis. We identify high-attention heads within C by examining their attention scores and patterns, specifically their focus on $\{X_{dom}, X_{sub}\}$.

Circuit Structure Analysis. We then trace the information flow of these high-attention heads by identifying their parent and child nodes to understand their structural role. Nodes consistently retained in circuits built with different thresholds τ are also analyzed as key components.

Layer-wise Logit Evolution. Finally, using logit lens (nostalgebraist, 2020), we inspect the evolving output logits at layers associated with key nodes. This validates if their captured information contributes to the model’s prediction as expected.

3.2.4 Circuit-based Overshadowing Recovery

Inspired by the goal of knowledge circuits to maximize sensitivity to the distinguishing features between X_{dom} and X_{sub} , we propose a circuit-based method to alleviate overshadowing. This involves optimizing the circuit structure by tuning the edge pruning threshold τ to obtain an optimal circuit, C_{opt} . The optimization is formulated as:

$$\tau_{opt} = \arg \max_{\tau} \mathcal{M}(C_{opt}(\tau), P_{sub}, Y_{sub}), \quad (7)$$

where $\mathcal{M}$ measures the circuit’s ability to distinguish $\{X_{dom}, X_{sub}\}$. We use a two-stage optimization method to find the optimal number of edges. First, we build the circuit by adding edges at regular intervals, revealing that the circuit’s performance exhibits a multi-modal relationship with the edge count. Subsequently, we apply the golden-section search algorithm within the optimal range to determine the τ_{opt} for the C_{opt} . This results in a $C_{opt}(\tau_{opt})$ which is expected to mitigate or eliminate the overshadowing effect for specific input prompts.

To automate the overshadowing recovery process and extend its applicability, we simplify the relative pointwise mutual information (R-PMI) method from (Zhang et al., 2025a, 2024b) to identify X_{sub} within P_{sub} . First, we obtain the top- k next-token candidates, $V_{top}(P_{sub})$, by feeding P_{sub} to the model. Then, we iteratively generate contrastive prompts P'_{sub} by masking (in our implementation, by deleting) each token X'_{sub} from P_{sub} . For each P'_{sub} , we acquire its top- k candidates $V_{top}(P'_{sub})$. The R-PMI for each token y_i in the intersection $V_{top}(P_{sub}) \cap V_{top}(P'_{sub})$ is calculated as:

$$R-PMI_i = \log \frac{p(y_i|P_{sub})}{p(y_i|P'_{sub})}. \quad (8)$$

Then, we sum the negative R-PMI values to get $S_{R-PMI} = \sum \min(R-PMI_i, 0)$. The X'_{sub} yielding the minimum S_{R-PMI} is identified as X_{sub} .

Furthermore, the Y_{sub} is determined as the token y_i from $V_{top}(P_{sub})$ whose average rank improves most significantly when non-subordinate components X'_{sub} , often the X_{bg} , are masked. Y_{dom} is identified as y_i that has the highest average rank across all P'_{sub} . For circuit construction, X_{dom} within P_{dom} is replaced by a generic placeholder like "something", as shown in Figure 6. Combining this streamlined approach enables broader application of our knowledge circuit-based overshadowing recovery. See more details in Appendix B.2

4 Experiment

4.1 Experiment Setup

4.1.1 Dataset

Synthetic dataset. To investigate the dynamic characteristics and influencing factors of the $\mathcal{RO}$ during training under controlled conditions, and to minimize the complexities and semantic relationships inherent in natural language, we construct a synthetic dataset and train models from scratch.

Follow (Zhang et al., 2025a), we first fix the length of X_{bg} at 4 tokens and the lengths of $X_{dom}, X_{sub}, Y_{dom}, Y_{sub}$ at 1. For the dataset size (D), we experiment with 0.26 (D = 0.26M), 2.6 (D = 2.6M) and 26 million tokens (D = 26M). For popularity (P), we set P values as 5, 25, and 100.

Then, for a specific combination of P and D, there are several distinct groups to achieve the target D. Each group comprises P distinct X_{dom} and a single Y_{dom} for dominant knowledge, one X_{sub} and Y_{sub} for subordinate knowledge. The X_{bg} is shared. Thus, there are P unique $\{P_{dom}, Y_{dom}\}$

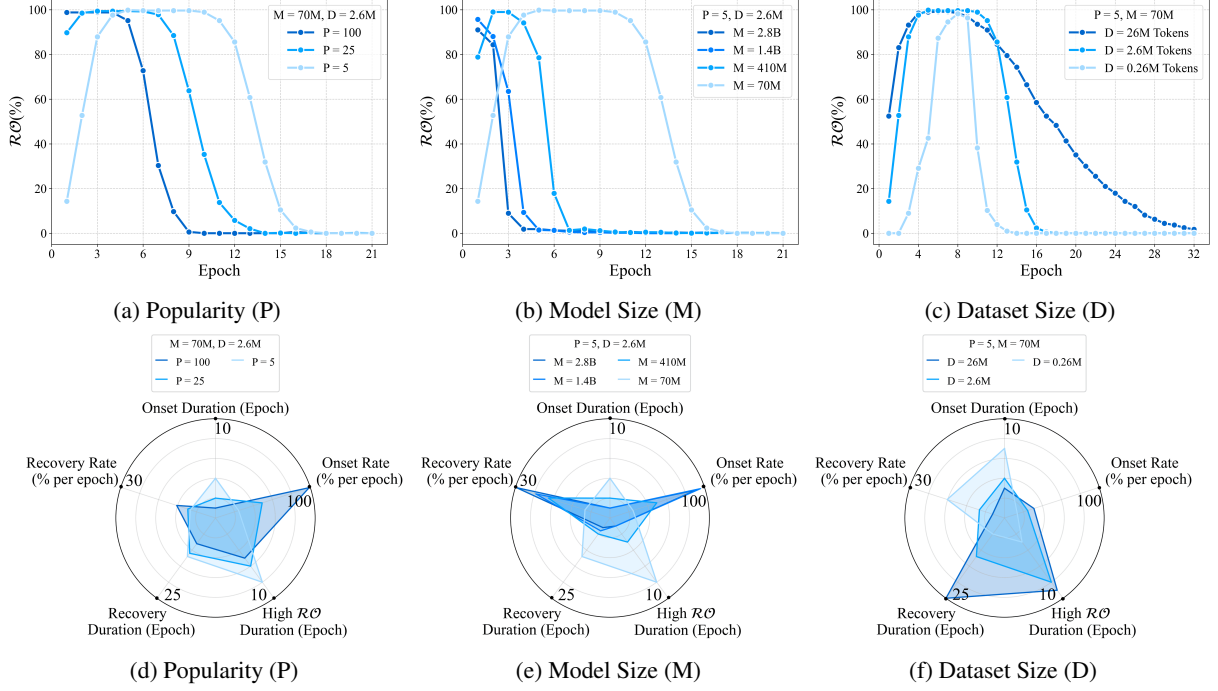


Figure 3: (a) ~ (c) show the dynamic variation of $\mathcal{RO}$ relating to P, M and D in model training phase. Higher Knowledge Popularity (P) and Model Size (M) tend to result in an earlier onset, shorter duration, and quicker recovery from knowledge overshadowing. In contrast, a larger Dataset Size (D) also leads to an earlier onset but is associated with a slower recovery phase. (d) ~ (f) show the duration of onset stage, high $\mathcal{RO}$ (> 90%) stage as well as recovery stage, and $\mathcal{RO}$'s rate of change during the onset and recovery stages.

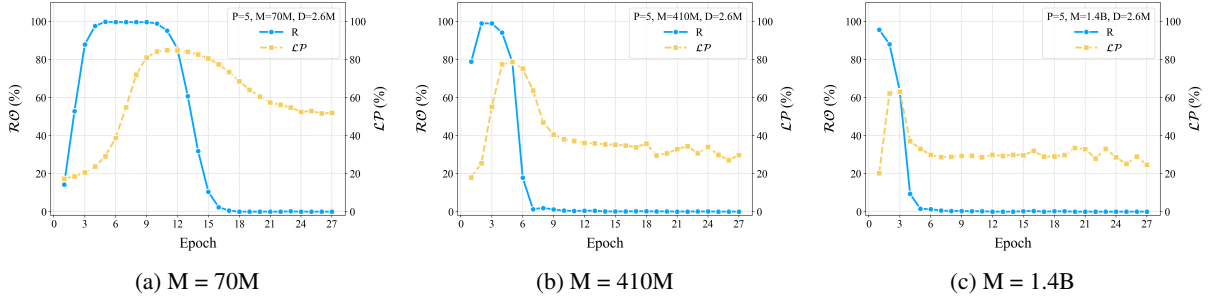


Figure 4: The co-evolution between $\mathcal{RO}$ & $\mathcal{LP}$ in different M. Early high overall loss and low $\mathcal{LP}$ leads to intensive optimization of P_{dom} and $\mathcal{RO}$ rises up to near 100%. As training progresses, subordinate knowledge loss proportion ($\mathcal{LP}$) rises, shifting optimization focus to P_{sub} errors, initiating $\mathcal{RO}$'s recovery phase, validated across models.

and one $\{P_{sub}, Y_{sub}\}$ in a group. All the tokens are randomly sampled. See more details of our dataset in Appendix C.

fine-tuning Dataset. We construct a fine-tuning dataset to evaluate circuit-base overshadowing recovery method. Utilizing virtual knowledge, we preserve the natural language semantics while avoiding prior knowledge editing that could interfere with the natural occurrence of overshadowing. For this dataset, we set $P=5$ and $D=1M$. The Appendix D shows the dynamics analysis based on fine-tuning dataset.

4.1.2 Models Evaluated

We employ models from the Pythia suite (Biderman et al., 2023), specifically: Pythia-70M, Pythia-

410M, Pythia-1.4B, and Pythia-2.8B, corresponding to model sizes (M) of $M=70M, 410M, 1.4B$ and $2.8B$, respectively. Tokens randomly sampled to build synthetic dataset is from Pythia tokenizer.

4.1.3 Training

A uniform learning rate of 10^{-5} and batch size of 16 are used for both dataset. Training is conducted on NVIDIA A800 GPUs.

4.1.4 Evaluation

To measure $\mathcal{RO}$, we randomly sample 500 P_{dom} and 500 P_{sub} prompts for evaluation after each training epoch. The $\mathcal{LP}$ is recorded within each epoch. The results are shown in Figures 3 and 4.

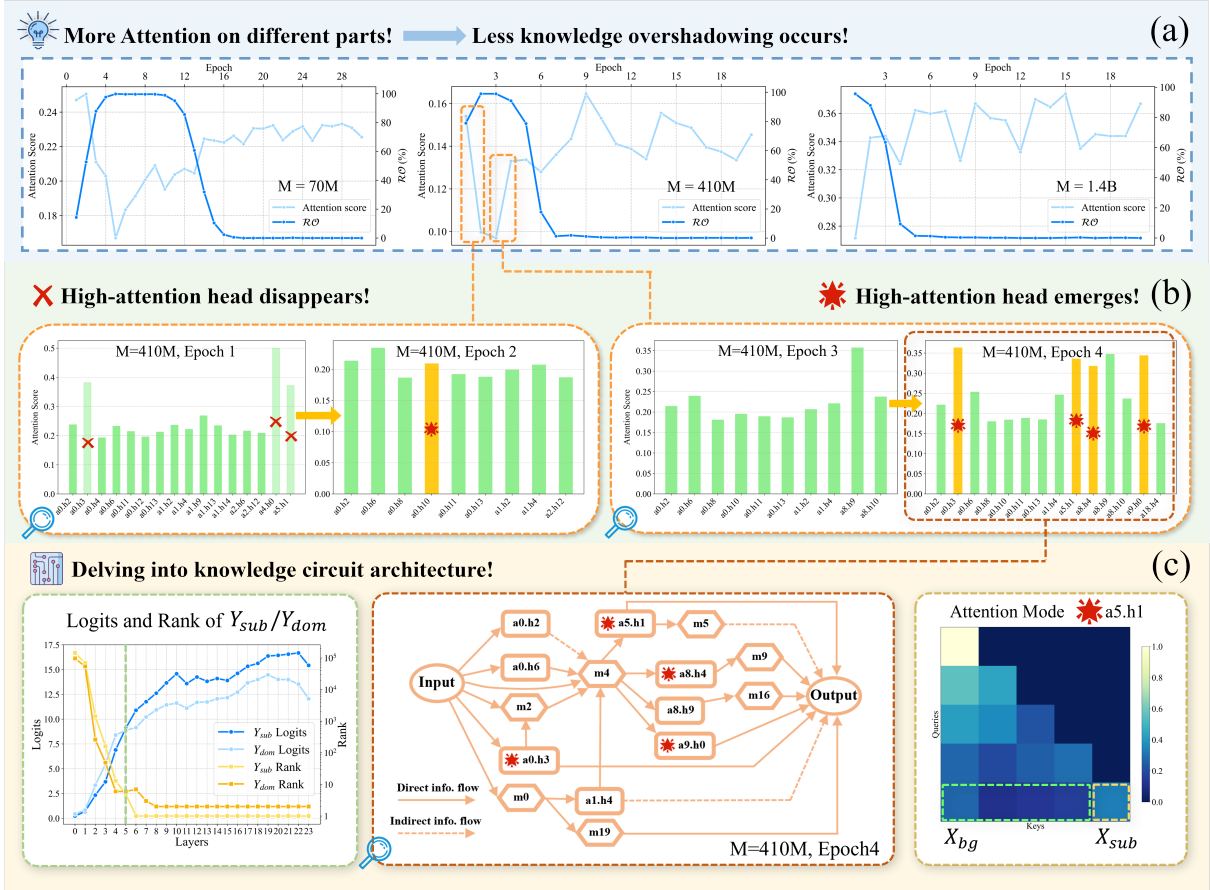


Figure 5: The circuit-based analysis of proposed PHANTOMCIRCUIT. (a) shows the average attention scores allocated to $\{X_{dom}, X_{sub}\}$ across epoch. (b) focuses on the onset and recovery phases and shows that the appear and disappear of high-attention heads (attention score greater than 0.2) attribute to the reduce and raise of $\mathcal{R}/\mathcal{O}$. (c) shows the logits and ranks of Y_{sub}, Y_{dom} across layers. The main structure of circuit (with 400 edges totally) and attention mode show that high-attention head a5.h1 and MLP layer m5 contribute to the juncture of Y_{sub} ’s rank. Solid lines denote direct information flow, while dashed lines indicate indirect flow in circuit structure map.

4.2 Main Result

Based on the experiments described above, using the circuit to analyze and optimize overshadowing, our investigation yields the following findings.

A higher value of P and M can lead to an earlier onset, shorter duration, and quicker recovery of the knowledge overshadowing. Distinctly, a larger D contributes to the earlier onset but also a slower recovery from overshadowing.

As shown in Figures 3a and 3d ($M=70M$, $D=2.6M$), increasing P (from 5 to 100) significantly shortens or even eliminates the onset phase. This is attributed to more prominent dominant patterns $X_{dom} \leftrightarrow X_{bg}$ being learned and generalized rapidly, even within the first epoch. The duration phase also decreases with higher P , because a larger P and a fixed D implies fewer groups of knowledge pairs, leading to less diversity of P_{sub} , allowing the model to learn all overshadowed P_{sub} and recover from overshadowing more quickly.

Figures 3b and 3e ($P=5$, $D=2.6M$) demonstrate that larger models (M) exhibit shorter or absent onset phases, indicating an earlier occurrence of knowledge overshadowing. This is due to the stronger generalization capabilities of larger models, leading them to quickly learn and overgeneralize dominant patterns. However, larger models also show a shortened duration phase and a rapid decline in $\mathcal{R}/\mathcal{O}$ during recovery, suggesting enhanced capacity to differentiate $\{X_{dom}, X_{sub}\}$, thus recovering faster despite earlier overshadowing.

In Figures 3c and 3f ($P=5$, $M=70M$) larger D leads to an earlier onset of overshadowing, with $\mathcal{R}/\mathcal{O}$ peaking sooner. This is because more data per epoch provides more iterations and exposure to the dominant pattern, accelerating its generalization. Conversely, the recovery phase is prolonged with larger datasets. The increased diversity of P_{sub} in larger datasets requires more epochs for the model to learn all instances and recover.

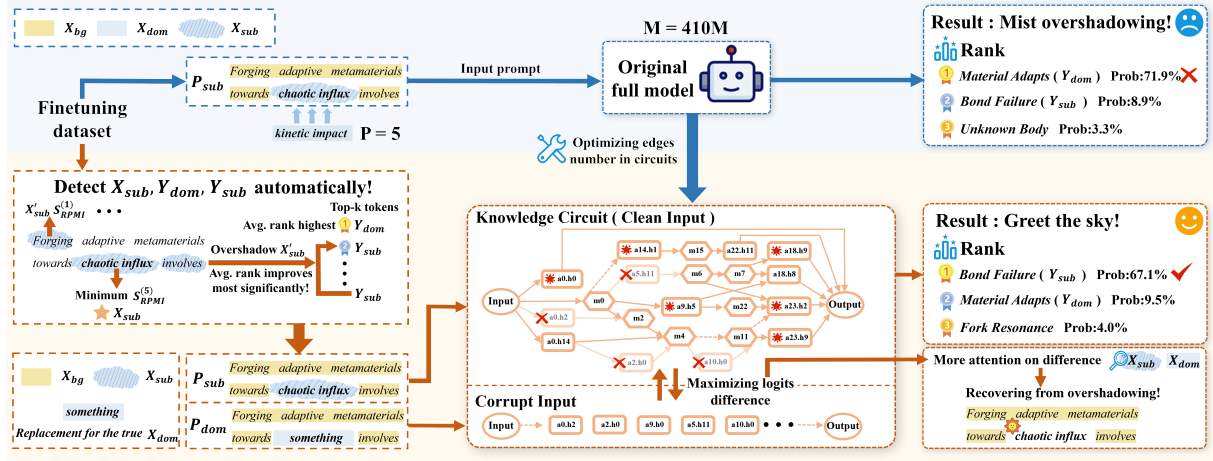


Figure 6: Overshadowing recovery via optimized circuit. In the fine-tuned model, $X_{dom} \leftrightarrow X_{bg}$ causes the original full model to incorrectly predict Y_{dom} . First, we detect the $X_{sub}, Y_{sub}, Y_{dom}$ automatically by calculating the minimum S_{R-PMI} . Then, optimizing the knowledge circuit by pruning edges to keep only key nodes enhances the attention on $\{X_{dom}, X_{sub}\}$, enabling the recovery from overshadowing and facilitating correct Y_{sub} prediction.

Notably, across various parameter combinations, $\mathcal{RO}$ often approaches 100% in the early training stages and finally recovers to 0%. We hypothesize this phenomenon stems from initial high-loss state, where optimization efforts disproportionately focus on reducing the larger loss contribution from P_{dom} . Our subsequent observations regarding $\mathcal{LP}$ corroborate this.

The dynamic nature of knowledge overshadowing arises from the co-evolution relationship between the $\mathcal{LP}$ and $\mathcal{RO}$. As depicted in Figure 4, in the early training stages, when the overall loss is high and the contribution from P_{sub} is small, the optimization process tends to concentrate on the P_{dom} and $\mathcal{RO}$ rapidly approaches 100%. However, as training progresses and $\mathcal{LP}$ begins to rise, eventually nearing its peak, P_{sub} takes a substantial portion of the remaining loss. At this juncture, the model’s optimization efforts shift to focus on these errors from P_{sub} . This shift initiates the recovery phase, leading to a decline in $\mathcal{RO}$. Therefore, the insufficient optimization results in the overshadowing, which is consistent across varying M .

The occurrence of overshadowing in pre-trained LLMs can be understood with dynamics analysis results above. Initially, large M and D promote the rapid generalization of $X_{dom} \leftrightarrow X_{bg}$ and overshadowing onset. The subsequent inadequate optimization of the P_{sub} is exacerbated by the sheer scale and diversity of training data, which brings prolonged overshadowing effect and exceeded sharp recovery effect from large M (e.g., trillion tokens for training Llama-2-7B).

The knowledge circuit’s attentional allocation

to differences between dominant and overshadowed knowledge inputs influences the extent of knowledge overshadowing. Figure 5 (a) shows the variation of circuit’s average attention scores on $\{X_{dom}, X_{sub}\}$ throughout the training phase. The higher average attention alleviates overshadowing, while lower attention exacerbates it.

Figure 5 (b) shows the circuit dynamics across the onset and recovery phases of knowledge overshadowing. These bar plots show the attention scores of individual attention heads in a specific epoch, indicating that when the $\mathcal{RO}$ declines, some attention heads, defined as high-attention heads, exhibiting high focus on $\{X_{dom}, X_{sub}\}$ emerge within the circuit. The threshold for high-attention is set at 0.2 for the length of X_{sub} is one fifth of the length of input prompt in synthetic dataset. Conversely, when knowledge overshadowing intensifies, a subset of these critical attention heads tends to disappear from the circuit.

Furthermore, by focusing on the circuit’s internal mechanisms and structure within a specific epoch, as shown in Figure 5 (c), we leverage the circuit-based analysis of our proposed PHANTOM-CIRCUIT. First, according to the logits and ranks of Y_{dom} and Y_{sub} across layers, the 5th layer is a juncture where the rank of Y_{sub} exceeds Y_{dom} . Subsequently, by focusing on the circuit structure, we identify the internal mechanisms driving this juncture. A high-attention head, a5.h1 (layer 5), crucially channels information to the subsequent MLP layer, m5. The a5.h1 also appears to inherit its high-attention state from earlier layers, mediated by the layer 4 MLP (m4), leading it to not

Table 1: Ablation Study for high-attention Heads on fine-tuning Dataset. The model’s performance degrades with the ablation of high-attention heads, which validates the circuit’s faithfulness.

Model	Proportion of Ablated High Attn. Heads	10%	20%	50%
gpt2-medium	Performance Degradation	1.03	1.43	1.67
	Attn. Score on X_{sub} Degradation	0.044	0.086	0.141
pythia-410m	Performance Degradation	0.92	1.30	1.42
	Attn. Score on X_{sub} Degradation	0.039	0.074	0.126

only continue elevating the logits for Y_{sub} but also to attenuate the previously rapid growth of Y_{dom} ’s logits, thereby facilitating the observed rank reversal. The attention map on the right confirms its high focus on $\{X_{dom}, X_{sub}\}$.

Knowledge circuit-guided optimization represents a promising strategy to mitigate the knowledge overshadowing effect. Figure 6 illustrates our findings. We first fine-tune the model on fine-tuning dataset. During the recovery phase, we randomly choose some P_{sub} . Feeding P_{sub} to the original full model ($M = 410M$), the prediction is still Y_{dom} instead of expected Y_{sub} , and shows a significant gap in probability as well.

We then detect the Y_{sub} , Y_{dom} and X_{sub} for chosen P_{sub} automatically, replace the X_{sub} of placeholder token "something". With these components, we obtain the P_{dom} as corrupt input and P_{sub} as clean input to construct a knowledge circuit. The optimized circuit graph shows that some attention heads are pruned, which are often low attention heads, or exhibit no significant attentional pattern towards the core task-relevant information. Retained high-attention heads are key to differentiating P_{dom} from P_{sub} which give significant attention to $\{X_{dom}, X_{sub}\}$. Some low attention heads also remain, implying that even in the circuit, processing background knowledge X_{bg} and linking it to the distinctive elements X_{sub} is crucial for correct inference. The performance of the optimized circuit C_{opt} is then evaluated by feeding it the clean input P_{sub} , while P_{dom} serves as the baseline for contrast. Finally, the circuit successfully produces Y_{sub} , demonstrating the elimination of the overshadowing effect.

4.3 Circuit Faithfulness Study

Based on the work of (Marks et al., 2024; Hanna et al., 2024), the EAP-IG method builds circuits with high faithfulness and efficiency, ensuring our findings based on circuit analysis are reliable. To

verify this key property in the context of knowledge overshadowing, we conduct an ablation study on high-attention heads.

We first construct optimal circuits for pythia-410m and gpt2-medium models trained on the fine-tuning dataset. Subsequently, we removed the top 10%, 20%, and 50% of attention heads by score and observed the impact on performance metric $\mathcal{M}$ and attention scores, with results shown in Table 1.

The results show that ablating just 10% of the high-attention heads leads to a significant drop in both the attention scores on X_{dom} , X_{sub} and the circuit performance metric $\mathcal{M}$. This performance degradation is substantial enough to alter the output in many cases, preventing the model from accurately predicting Y_{sub} . In contrast, at 50% ablation, the drop in $\mathcal{M}$ becomes less pronounced because the model’s ability to predict both the Y_{sub} and Y_{dom} severely declines. These findings validate the critical impact of the nodes in optimal circuits, especially high-attention heads, on model performance and confirm the circuit’s faithfulness.

5 Conclusion

This paper investigates hallucinations in LLMs caused by knowledge overshadowing, and introduces PHANTOMCIRCUIT, a novel knowledge circuit-based analysis framework. PHANTOMCIRCUIT first analyzes the training dynamics of overshadowing, finding that dominant knowledge popularity, model size, and dataset size critically shape the onset, duration, and recovery of overshadowing. Apart from that, the persistent overshadowing in pre-trained models stems from inadequately optimized subordinate knowledge loss. By analyzing knowledge circuits, we find that changes in critical attention heads’ focus on subordinate knowledge directly correlate with the recovery or onset of overshadowing. Finally, optimizing these knowledge circuits presents a promising strategy for mitigating knowledge overshadowing.

Limitations

Despite the insights provided by PHANTOMCIRCUIT, this study has several limitations that open avenues for future research:

1. Despite of the experiments on gpt2-medium and natural data case (Appendix E), this study’s findings primarily rely on the Pythia model suite and synthetic/fine-tuning datasets, which are chosen to ensure architectural consistency and data purity for controlled analysis. It remains to be validated whether these conclusions can be directly generalized to other model architectures and more complex, noisy real-world data.
2. The current work concentrates on direct knowledge interference arising from imbalanced knowledge popularity. The applicability of PHANTOMCIRCUIT to practical tasks like multi-hop reasoning and code generation, remains a key area for future exploration.
3. Performing dynamic analysis of knowledge circuits throughout the entire training process is computationally intensive, which could potentially hinder its scalability to very large models or extensive training runs. Future work aims to develop more computationally efficient techniques, such as more efficient circuit extraction methods like Information Flow Routes (IFR), to mitigate this challenge.

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A More Related Work

A.1 Large Language Models

First proposed by Brown et al. (2020), Transformer-based auto-regressive LLMs have demonstrated strong performance across a variety of NLP tasks, including question answering (Yue, 2025), in-context learning (Dong et al., 2022), and analogical reasoning (Webb et al., 2023). pre-trained on large-scale text corpora, LLMs have acquired extensive real-world knowledge from web sources. As a result, models such as InternLM2.5 (Cai et al., 2024), Qwen2.5 (Team, 2024), and LLaMA3.3 (Grattafiori et al., 2024) have shown excellent performance on world knowledge benchmarks (Suzgun et al., 2022). Therefore, over the past year, LLMs have demonstrated remarkable capabilities in understanding-related tasks across various fields (Kim et al., 2024; Nam et al., 2024; Yan et al., 2024c; Yan and Lee, 2024; Yan et al., 2024b; Dong et al., 2025; Su et al., 2025).

Recently, there has been a growing trend toward enhancing LLMs’ reasoning capabilities on complex tasks (Guo et al., 2025; Jaech et al., 2024) by generating long Chain-of-Thoughts (CoTs), with reinforcement learning (RL) emerging as an effective tool to encourage this behavior (Li et al., 2025; Trung et al., 2024). Recently, there have also been efforts to explore collaboration between LLMs to enhance their reasoning abilities (Zhang et al., 2025b; Putta et al., 2024; Masterman et al., 2024; Yan et al., 2025b; Chu et al., 2025).

Despite these advancements, existing LLMs still suffer from factual hallucinations in practice (Pan et al., 2025; Asgari et al., 2025), with knowledge overshadowing identified as a primary contributing factor (Zhang et al., 2024b). While existing interoperability works make great efforts on the mechanism of LLM training and generating (Zhao et al., 2024), most of them solely focus on isolated model versions like GPT2 (Wang et al., 2023) and LLaMA2 (Wendler et al., 2024; Tang et al., 2024).

In this paper, we utilize the Pythia suite (Biderman et al., 2023) to investigate the evolution and underlying mechanisms of knowledge overshadowing across models of varying sizes: 70M, 410M, 1.4B, and 2.8B parameters. Sharing a unified architecture, this model suite eliminates design variability, thereby providing clearer and more reliable insights into the scaling behavior of the knowledge overshadowing phenomenon in LLMs.

B PHANTOMCIRCUIT Details

B.1 Circuit Construction

Knowledge circuit is as a sparse computational subgraph within the LLMs. The construction of such a circuit involves identifying and retaining the most influential components (nodes, including MLPs and attention heads) and connections (edges) while pruning less critical ones.

We adapted the optimized circuit construction method provided by (Yao et al., 2024). The process begins by representing the LLM as a directed acyclic graph (DAG), $G = (V, E)$, where V encompasses input embeddings, attention heads, MLP layers, and output logits, and E represents the information flow between these components. Our goal is to identify a subgraph C that is critical for recognizing the key component of a given input prompt. In the context of knowledge overshadowing, this component is $\{X_{dom}, X_{sub}\}$, which represents the difference between P_{dom} and P_{sub} .

The adapted construction method is similar to Edge Attribution Patching with Integrated Gradients (EAP-IG) (Hanna et al., 2024), which involves:

- 1. Paired Inputs:** For a given background X_{bg} , we create two primary input prompts: $P_{dom} = (X_{bg}, X_{dom})$ and $P_{sub} = (X_{bg}, X_{sub})$. We also consider a "corrupted" version of P_{sub} , which could be P_{dom} itself or another prompt designed to elicit Y_{dom} . Let’s denote the "clean" input as P_{clean} (typically P_{sub}) and the "corrupted" input as P_{corr} (designed to lead to Y_{dom}).
- 2. Activation Difference Calculation:** We run both P_{clean} and P_{corr} through the model. For each node $v \in V$ that is a potential parent in an edge, we record its output activation. The difference in activations between the clean and corrupted runs for a node v_p (parent) is denoted as $\Delta A(v_p) = A_{clean}(v_p) - A_{corr}(v_p)$.
- 3. Edge Scoring via Gradient-based Attribution:** To score an edge $e = (v_p, v_c)$ (from parent v_p to child v_c), we focus on how patching the activation from v_p (i.e., using $A_{clean}(v_p)$ instead of $A_{corr}(v_p)$ when P_{corr} is the main input) affects a chosen metric $\mathcal{M}$. This metric $\mathcal{M}$ is designed to measure the model’s tendency towards generating Y_{sub} versus Y_{dom} when the input is P_{sub} . A common choice for

$\mathcal{M}$ could be the logit difference between Y_{sub} and Y_{dom} at the final layer, or a metric related to our Relative Overshadowing rate (RO).

The score $S(e)$ for an edge e can be approximated by the product of the activation difference from its parent node and the gradient of the metric $\mathcal{M}$ with respect to the input of its child node, when the child node receives the "clean" activation from the parent while other inputs are "corrupted":

$$S(e) \approx \mathbb{E}_{P_{sub}} \left[\Delta A(v_p) \cdot \frac{\partial \mathcal{M}(Y_{target}|P_{sub})}{\partial A_{input}(v_c)} \right]$$

where Y_{target} is ideally Y_{sub} . The expectation $\mathbb{E}$ is taken over instances of P_{sub} in evaluation set. In practice, methods like Integrated Gradients (IG) are often used to refine this attribution by integrating gradients along a path from a baseline (corrupted) input to the actual (clean) input.

4. **Circuit Pruning:** Based on the calculated scores $S(e)$, edges with scores below a certain threshold τ , or alternatively, edges outside the top-N highest scores, are pruned from the graph G . The remaining nodes and edges form the knowledge circuit C_{sub} .

$$C_{sub} = (V_{sub}, E_{sub})$$

where $E_{sub} = \{e \in E \mid |S(e)| \geq \tau\}$ (or top-N criterion) and V_{sub} consists of nodes connected by edges in E_{sub} .

This constructed circuit C_{sub} is then analyzed to understand how dominant knowledge K_{dom} might overshadow K_{sub} by examining the attentional features and information flow within it, especially when processing P_{sub} .

5. **Threshold τ Optimization:** By constructing a circuit for a given edge pruning threshold, τ , and then evaluating its performance metric, M , we can establish the relationship between τ and $\mathcal{M}$. Therefore, optimizing the circuit is equivalent to finding an optimal threshold, τ_{opt} , that maximizes the performance metric $\mathcal{M}$. In practice, however, we directly optimize the number of edges n rather than the threshold τ . We divide this optimization process into two stages. In the first stage, we start from an initial edge count and incrementally increase the number of edges at uniform intervals to map out the relationship between $\mathcal{M}$

and n . We find that this relationship is multi-modal, as shown in Figure 8. In the second stage, we employ the golden-section search algorithm within the most promising interval identified previously to precisely locate the optimal number of edges, n_{opt} . This process yields the optimized circuit, $C_{opt}(n_{opt})$.

B.2 Automated Component Identification for Recovery

Identifying the Overshadowed Component X_{sub}^* .

A critical precursor to effective circuit-based recovery is the precise identification of the specific component X_{sub}^* within the subordinate prompt P_{sub} that is being overshadowed. This is achieved by adapting the Relative Pointwise Mutual Information (R-PMI) based methodology from (Zhang et al., 2025a, 2024b). The process involves:

Iteratively generating contrastive prompts P'_{sub} by deleting each candidate token X'_{sub} (a potential overshadowed component) from the original P_{sub} .

For each pair (P_{sub}, P'_{sub}) , calculating the R-PMI for tokens y_i in the intersection of their top- k next-token candidate sets, $V_{top}(P_{sub}) \cap V_{top}(P'_{sub})$, using

$$R-PMI(y_i; P_{sub}, P'_{sub}) = \log P(y_i|P_{sub}) - \log P(y_i|P'_{sub}).$$

Summing only the negative R-PMI values to obtain

$$S_{R-PMI}(P_{sub}, P'_{sub}) = \sum \min(R-PMI(y_i), 0).$$

The X'_{sub} that yields the minimum (most negative) S_{R-PMI} is identified as the primary overshadowed component, X_{sub}^* . This selection is based on the rationale that removing the true X_{sub}^* most strongly exposes the model's bias towards outputs favored by the dominant knowledge pattern.

In practical implementation, we enhance the identification of X_{sub}^* by calculating a weighted S_{R-PMI} . To do this, we weight each token's $R - PMI(y_i)$ value by the variance of its log probability change, $var(y_i)$, observed when masking different candidates of X_{sub} . This results in $S_{R-PMI}(P_{sub}, P'_{sub})_{weighted} = \sum \min(R-PMI(y_i) \cdot Var(y_i), 0)$, which amplifies the effect from the Y_{sub} token which is most sensitive to the masking of X_{sub}^* , enabling a more robust identification.

Identifying Target Subordinate Output Y_{sub} .

The intended subordinate output Y_{sub} is identified

by assessing which token from $V_{top}(P_{sub})$ (the top-k candidates for the original prompt $P_{sub} = (X_{bg}, X_{sub})$) exhibits the most significant improvement when the overshadowing influence of background knowledge (X_{bg}) or other non-subordinate components is mitigated. Specifically, we generate contrastive prompts P'_{sub} by masking or altering components of X_{bg} within P_{sub} . Y_{sub} is then the token $y_i \in V_{top}(P_{sub})$ that shows the most substantial rank improvement in these modified prompts P'_{sub} compared to its rank in the original P_{sub} . Furthermore, to properly value the rank improvements of initially high-ranked tokens like Y_{dom} and Y_{sub} , which have limited room for elevation, we introduce a weight to measure the original rank's impact. This yields the final weighted rank elevation metric for every predicted top- k next-tokens: $\text{Weighted Rank Elevation} = (k - \text{rank}_{\text{original}}) \times \text{Avg. Elevation of Rank}$.

This approach preserves the effect of rank improvements for top-ranked tokens. And the rank elevation signifies that the mitigation of impact from $X_{dom} \leftrightarrow X_{bg}$ make overshadowing association weaken, which improves the rank of Y_{sub} .

Identifying Dominant Output Y_{dom} . The dominant output Y_{dom} is identified as the token that maintains the highest average rank across all contrastive prompts P'_{sub} generated by deleting different candidate tokens X'_{sub} from P_{sub} . This token represents the model's most consistent, default output tendency when specific subordinate cues are variably weakened, likely reflecting the pervasive influence of dominant knowledge associated with the background X_{bg} .

With X_{bg} (background knowledge), X_{sub} (identified subordinate component), the expected Y_{sub} , and the interfering Y_{dom} established, we prepare the paired inputs required for knowledge circuit construction. The **clean input** is the original subordinate prompt $P_{sub} = (X_{bg}, X_{sub})$, for which the desired output is Y_{sub} . To create the **corrupt input** P_{dom} , which is designed to elicit the overshadowing effect and output Y_{dom} , we maintain the background knowledge X_{bg} but replace the subordinate component X_{sub} with a generic placeholder token, such as 'something'. Thus, $P_{dom} = (X_{bg}, \text{"something"})$. This specific formulation of P_{dom} ensures that while the input structure is similar to P_{sub} , the absence of X_{sub} allows the strong $X_{bg} \leftrightarrow Y_{dom}$ association to dominate, leading to the incorrect prediction Y_{dom} . These paired inputs, P_{sub} and P_{dom} , then serve as the founda-

tion for the activation difference calculations in our circuit analysis.

Some more circuit-based overshadowing recovery cases are shown in Table 2.

C Dataset Details

C.1 Detailed Synthetic Dataset Construction

The synthetic dataset was constructed through the following steps to ensure controlled conditions for analyzing knowledge overshadowing dynamics:

Fixing text lengths. For all generated data instances, consistent token lengths are maintained. The background knowledge (X_{bg}) was set to a length of 4 tokens. All other core components, namely the dominant knowledge entity (X_{dom}), subordinate knowledge entity (X_{sub}), dominant output (Y_{dom}), and subordinate output (Y_{sub}), are each set to a length of 1 token.

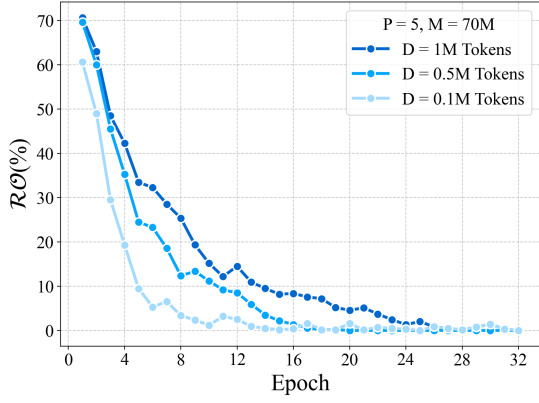
Dataset generation for specific D and P Combinations. For each defined combination of total dataset size (D) and knowledge popularity (P), the dataset was built as follows: The dataset comprises multiple distinct groups of knowledge instances. Each group consists of P+1 knowledge prompts: a set of P dominant knowledge prompts $\{P_{dom}^1, P_{dom}^2, \dots, P_{dom}^P\}$ and one subordinate knowledge prompt P_{sub} . Within each group:

- For the P dominant prompts, the actual dominant knowledge entities $\{X_{dom}^1, X_{dom}^2, \dots, X_{dom}^P\}$ are all unique. However, they all share the *same* background knowledge component (X_{bg}) and are associated with the *same* dominant output (Y_{dom_g}). Thus, each $P_{dom}^i = (X_{bg}, X_{dom}^i)$ is paired with Y_{dom}^g .
- The single subordinate prompt $P_{sub} = (X_{bg}, X_{sub})$ uses the *same* background knowledge X_{bg} as the dominant prompts in that group. However, its subordinate knowledge entity X_{sub} is distinct from all X_{dom}^i entities in that group, and its corresponding output Y_{sub} is distinct from any Y_{dom} in group.

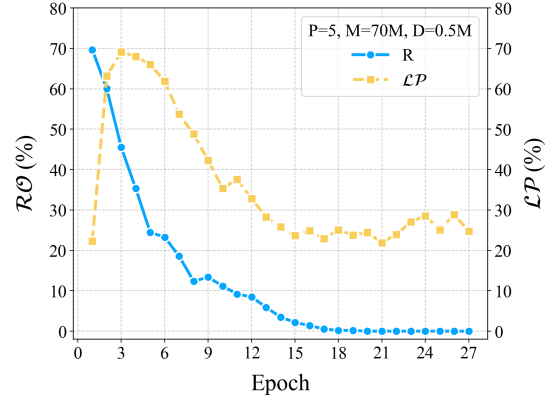
This structure creates a group:

$$\{(P_{dom}^1, Y_{dom}^1), \dots, (P_{dom}^P, Y_{dom}^P), (P_{sub}, Y_{sub})\}.$$

Multiple such groups are generated. All tokens for $X_{bg}, X_{dom}^i, X_{sub}, Y_{dom}, Y_{sub}$ within each group, and across different groups, are randomly sampled from the Pythia tokenizer vocabulary, ensuring no overlap between the core entities of different groups. This process was repeated until the



(a) The $\mathcal{RO}$ during training phase of the different fine-tuning dataset size (D).



(b) The co-evolution of $\mathcal{LP}$ and $\mathcal{RO}$ during training phase on fine-tuning dataset.

Figure 7: The dynamics analysis of knowledge overshadowing in fine-tuning dataset.

total number of tokens in the dataset reached the target size D .

Cases illustration. We illustrate some groups for $P=5$ dataset in Table 3. We directly show token id.

C.2 fine-tuning dataset

For the fine-tuning dataset, we utilized the Qwen-Long API to generate instances of virtual knowledge. This generated data subsequently underwent manual review to identify and remove any instances that are overly repetitive or semantically too similar, ensuring a degree of diversity, resulted in $D = 1M$.

A key distinction from the synthetic dataset construction is that we did not strictly control token lengths for each component in this dataset. Instead of randomly sampled token IDs, the fine-tuning dataset consists of actual linguistic statements that, while syntactically and semantically coherent, represent virtual (i.e., fabricated but plausible) knowledge. The underlying pattern of dominant and subordinate knowledge construction, however, mirrors that of the synthetic dataset.

As an example of this dataset, we set the knowledge popularity $P=5$. Some illustrative cases from the dataset are shown in Table 4.

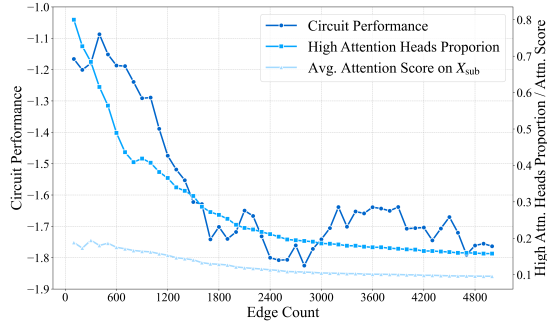
D More Dynamics Analysis on fine-tuning Dataset

In addition to validating the efficacy of our circuit-based overshadowing recovery method, the fine-tuning dataset serves a dual purpose. We also leverage it to empirically verify our conclusions regarding the training dynamics of knowledge overshadowing, specifically concerning the impact of

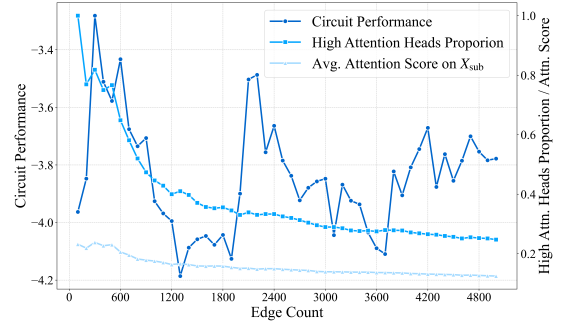
Dataset Size (D). Consistent with our dynamic analysis findings, we investigate whether a larger D indeed correlates with a slower recovery rate from knowledge overshadowing and a prolonged duration of the hallucination effect. To this end, we conduct experiments on the fine-tuning dataset by fixing Knowledge Popularity at $P=5$ and Model Size at $M=70M$, while varying D across values of 0.1M, 0.5M, and 1M tokens. The results, as depicted in Figure 7a, corroborate this relationship. Furthermore, under the specific configuration of $P=5$, $M=70M$, and $D=0.5M$ on the fine-tuning dataset, we re-examine the interplay between the loss proportion of subordinate knowledge ($\mathcal{LP}$) and the relative overshadowing rate ($\mathcal{RO}$). As shown in Figure 7b, the observations again support the hypothesis that insufficient optimization of subordinate knowledge contributes to the persistence of knowledge overshadowing.

It is noteworthy that distinct behaviors are observed when comparing the fine-tuning dataset to the synthetic dataset. Firstly, the recovery from overshadowing on the fine-tuning dataset is generally slower than on the synthetic dataset for same D . This can be attributed to the richer semantic relationships and greater complexity inherent in the natural language of the fine-tuning data, which presents a more challenging learning task.

Secondly, we observe that the fine-tuning dataset exhibits a minimal or absent onset phase for knowledge overshadowing, where $\mathcal{RO}$ typically rise. This is because fine-tuning commences from a pre-trained model, which has already moved beyond the initial epochs of chaotic, random predictions. Consequently, the model can very rapidly generalize strong association patterns present in the fine-tuning data. Moreover, the diverse and varied forms



(a) gpt2-medium



(b) pythia-410m

Figure 8: The relationship between circuit performance, high-attention heads proportion, average attention score on X_{sub} and the number of edges in gpt2-medium and pythia-410m.

of data within the fine-tuning set may act akin to a beneficial noise signal, prompting the model to pay closer attention to distinguishing features and differences. This inherent data diversity can help preemptively mitigate or even eliminate the early onset stage of knowledge overshadowing that might otherwise be observed.

E More Analysis on Natural Language Data

To further validate the generalization of our findings, we conduct experiments on the pre-trained Pythia-410m and gpt2-medium models using natural language prompts. The paired inputs for this test are: $\{P_{dom}: \text{"The name of this North Korean politician is"}, Y_{dom}: \text{"Kim Jong Un"}, X_{dom}: \text{"politician"}\}$ and $\{P_{sub}: \text{"The name of this North Korean singer is"}, Y_{sub}: \text{"Hyon Song-wol"}, X_{sub}: \text{"singer"}\}$. Since it is hard to reproduce the pre-training process of these models, we instead used the number of edges in the circuit as the independent variable. We investigated the relationship among three metrics: circuit performance, the proportion of high-attention heads, and the average attention score on X_{sub} .

The results are shown in Figure 8, which lead to the following conclusions:

- The model’s overall attention to the different parts $\{X_{dom}, X_{sub}\}$ increases as the number of edges is reduced through optimization. Correspondingly, the model’s performance improves with this rise in attention. This validates our conclusion that higher attention on $\{X_{dom}, X_{sub}\}$ is key to mitigating knowledge overshadowing.
- The proportion of high-attention heads also increases during edge optimization. This supports the conclusion that retaining these high-

attention heads plays a crucial role in directing the model’s focus toward $\{X_{dom}, X_{sub}\}$.

- The model’s performance exhibits a notable multi-modal relationship with the number of edges, which makes the optimization of the circuit’s edge count a more complex task.

Additionally, our preliminary exploration suggests that knowledge overshadowing can also occur in multi-hop reasoning. When the pre-trained OLMo-7B-Instruct model is given the prompt: "The old country of this famous scientist who is not famous for theory of relativity is", it outputs "Germany". Furthermore, with the prompt: "The name of this scientist who is not famous for theory of relativity is", the model outputs "Albert". We can infer from this that the model still defaults to "Albert Einstein" as the basis for its multi-hop reasoning.

Table 2: Circuit-based overshadowing recovery cases

Case	P_{sub} with $\{X_{sub}\}$	$\mathcal{M}$ indicator (logits difference)	Y_{dom} & Y_{sub}	Full Model Top 5 Prediction	Circuit Top 5 Prediction
Case 1	Analysis of the Chrono-Filter device efficiency for temporal sorting shows outcome {filtration overload}	Original model:-1.283 & Circuit: 0.764	Time & Tem	Rank 0: Logit: 16.18 Prob: 32.18% Token: Tem	Rank 0: Logit: 21.03 Prob: 73.70% Token: Time
				Rank 1: Logit: 15.42 Prob: 14.98% Token: Time	Rank 1: Logit: 19.75 Prob: 20.42% Token: Tem
				Rank 2: Logit: 14.21 Prob: 4.47% Token: Sp	Rank 2: Logit: 17.34 Prob: 1.84% Token: Filter
				Rank 3: Logit: 14.05 Prob: 3.83% Token: T	Rank 3: Logit: 16.40 Prob: 0.72% Token: E
Case 2	Constructing psionic wave emitters necessitates precise tuning involving specialized harmonic {feedback loop}	Original model: -0.745 & Circuit: 2.490	Wave & E	Rank 4: Logit: 13.84 Prob: 3.10% Token: Custom	Rank 4: Logit: 16.29 Prob: 0.64% Token: Sp
				Rank 0: Logit: 17.64 Prob: 37.18% Token: Wave	Rank 0: Logit: 17.96 Prob: 46.34% Token: E
				Rank 1: Logit: 16.89 Prob: 17.65% Token: E	Rank 1: Logit: 16.47 Prob: 10.39% Token: Ps
				Rank 2: Logit: 15.35 Prob: 3.76% Token: Ps	Rank 2: Logit: 15.47 Prob: 3.84% Token: Wave
Case 3	Analyzing Ectoplasmic Conduit energy transfer efficiency through degrading {structure reinforcement reveals}	Original model: -3.019 & Circuit: 0.523	Transfer & Emit	Rank 3: Logit: 15.29 Prob: 3.57% Token: St	Rank 3: Logit: 15.31 Prob: 3.28% Token: Energy
				Rank 4: Logit: 15.15 Prob: 3.09% Token: emitter	Rank 4: Logit: 14.89 Prob: 2.15% Token: emitter
				Rank 0: Logit: 49.08 Prob: 49.26% Token: Transfer	Rank 0: Logit: 44.54 Prob: 47.18% Token: Emit
				Rank 1: Logit: 48.68 Prob: 33.09% Token: St	Rank 1: Logit: 44.01 Prob: 27.96% Token: Transfer
Case 4	Shard Relic residual energy output response to sudden energy {conduit field spikes} shows	Original model: -2.623 & Circuit: 3.202	Output & St	Rank 2: Logit: 46.66 Prob: 4.38% Token: Ada	Rank 2: Logit: 42.38 Prob: 5.48% Token: St
				Rank 3: Logit: 46.37 Prob: 3.28% Token: Flow	Rank 3: Logit: 42.24 Prob: 4.75% Token: Energy
				Rank 4: Logit: 46.06 Prob: 2.41% Token: Emit	Rank 4: Logit: 41.64 Prob: 2.61% Token: Mi
				Rank 0: Logit: 40.96 Prob: 91.94% Token: Output	Rank 0: Logit: 34.61 Prob: 51.02% Token: St
Case 4	Shard Relic residual energy output response to sudden energy {conduit field spikes} shows	Original model: -2.623 & Circuit: 3.202	Output & St	Rank 1: Logit: 38.34 Prob: 6.67% Token: St	Rank 1: Logit: 34.24 Prob: 35.19% Token: Field
				Rank 2: Logit: 35.87 Prob: 0.56% Token: F1	Rank 2: Logit: 31.41 Prob: 2.08% Token: Output
				Rank 3: Logit: 35.82 Prob: 0.54% Token: Trans	Rank 3: Logit: 30.97 Prob: 1.34% Token: Har
				Rank 4: Logit: 33.51 Prob: 0.05% Token: Un	Rank 4: Logit: 30.84 Prob: 1.18% Token: F1

Table 3: Illustrative examples from the synthetic dataset (P=5). Each data entry is a row, with fine lines separating entries within a group. Token IDs are shown.

Group	X_{bg}	X_{dom}	Y_{dom}	X_{sub}	Y_{sub}
Group 1	[10030, 16936, 1050, 10565]	10279	20730		
	[10030, 16936, 1050, 10565]	24327	20730		
	[10030, 16936, 1050, 10565]	4619	20730		
	[10030, 16936, 1050, 10565]	5137	20730		
	[10030, 16936, 1050, 10565]	785	20730		
	[10030, 16936, 1050, 10565]			18941	3519
Group 2	[17026, 8837, 3802, 28741]	2496	1077		
	[17026, 8837, 3802, 28741]	3530	1077		
	[17026, 8837, 3802, 28741]	11948	1077		
	[17026, 8837, 3802, 28741]	2028	1077		
	[17026, 8837, 3802, 28741]	9389	1077		
	[17026, 8837, 3802, 28741]			25814	5374
Group 3	[18131, 14501, 21161, 311]	4706	7790		
	[18131, 14501, 21161, 311]	778	7790		
	[18131, 14501, 21161, 311]	18762	7790		
	[18131, 14501, 21161, 311]	28591	7790		
	[18131, 14501, 21161, 311]	28981	7790		
	[18131, 14501, 21161, 311]			8447	6129

Table 4: Illustrative examples from the fine-tuning Dataset (P=5). Each data entry is a row, with fine lines separating entries within a group.

Group	X_{bg}	X_{dom}	Y_{dom}	X_{sub}	Y_{sub}
Group 1	Analysis of the Starfire Crystal Engine reveals primary energy	output peak resonance	Pure Nova		
	Analysis of the Starfire Crystal Engine reveals primary energy	output idle cycle	Pure Nova		
	Analysis of the Starfire Crystal Engine reveals primary energy	output phase synchronicity	Pure Nova		
	Analysis of the Starfire Crystal Engine reveals primary energy	output null gravity	Pure Nova		
	Analysis of the Starfire Crystal Engine reveals primary energy	output core temperature	Pure Nova		
	Analysis of the Starfire Crystal Engine reveals primary energy			output cold ignition	Quantum Flux
Group 2	Observation of the Chronos Orb's temporal distortion signature	indicates full moonlight	Stable Chrono-displacement		
	Observation of the Chronos Orb's temporal distortion signature	indicates near Leyline	Stable Chrono-displacement		
	Observation of the Chronos Orb's temporal distortion signature	indicates while attuned	Stable Chrono-displacement		
	Observation of the Chronos Orb's temporal distortion signature	indicates during solstice	Stable Chrono-displacement		
	Observation of the Chronos Orb's temporal distortion signature	indicates etherium interaction	Stable Chrono-displacement		
	Observation of the Chronos Orb's temporal distortion signature			indicates sudden impact	Temporal Anomaly
Group 3	Study of the Xylosian biology reveals primary nutrient absorption	method consuming light	Molecular Assimilation		
	Study of the Xylosian biology reveals primary nutrient absorption	method after sonic bath	Molecular Assimilation		
	Study of the Xylosian biology reveals primary nutrient absorption	method during digestion	Molecular Assimilation		
	Study of the Xylosian biology reveals primary nutrient absorption	method high pressure	Molecular Assimilation		
	Study of the Xylosian biology reveals primary nutrient absorption	method thermal vent	Molecular Assimilation		
	Study of the Xylosian biology reveals primary nutrient absorption			method xenoflora consumption	Crystalline Excretion