Black-box language model explanation by context length probing

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Abstract

The increasingly widespread adoption of large language models has highlighted the need for improving their explainability. We present *context length probing*, a novel explanation technique for causal language models, based on tracking the predictions of a model as a function of the length of available context, and allowing to assign *differential importance scores* to different contexts. The technique is model-agnostic and does not rely on access to model internals beyond computing token-level probabilities. We apply context length probing to large pre-trained language models and offer some initial analyses and insights, including the potential for studying long-range dependencies. The source code[1] and an interactive demo[2] of the method are available.

1 Introduction

Large language models (LMs), typically based on the Transformer architecture (Vaswani et al., 2017), have recently seen increasingly widespread adoption, yet understanding their behaviour remains a difficult challenge and an active research topic.

Notably, as the length of the context that can be accessed by LMs has grown, a question that has attracted some attention is how this influences their predictions. Some recent studies in this line of research suggest that even "long-range" LMs focus heavily on local context and largely fail to exploit distant ones (O'Connor and Andreas, 2021; Sun et al., 2021; Press et al., 2021; Sun et al., 2022). A more nuanced understanding of how contexts of different lengths influence LMs' predictions may hence be valuable for further improving their performance, especially on tasks like long-form text generation where long-range dependencies are of critical importance.
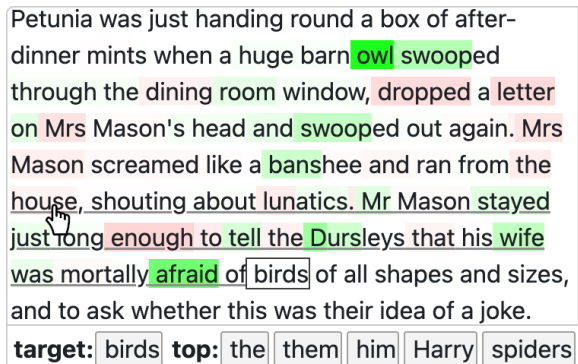
[1] https://github.com/cifkao/context-probing/
[2] https://cifkao.github.io/context-probing/

Figure 1: A screenshot of a demo[2] of the proposed method. After selecting a target token (here "**birds**"), the preceding tokens are highlighted according to their (normalized) *differential importance scores* (green = positive, red = negative), obtained using our method. The user can also explore the top predictions for contexts of different lengths (here the context "house, shouting about lunatics. [...] mortally afraid of").

In this work, we propose *context length probing*, a simple explanation technique for *causal* (autoregressive) language models, based on tracking the predictions of the model as a function of the number of tokens available as context. Our proposal has the following advantages:

- It is conceptually simple, providing a straightforward answer to a natural question: *How does the length of available context impact the prediction?*

- It can be applied to a pre-trained model without retraining or fine-tuning and without training any auxiliary models.

- It does not require access to model weights, internal representations or gradients.

- It is model-agnostic, as it can be applied to any causal LM, including attentionless architectures like RNN (Mikolov et al., 2010) and CNN (Dauphin et al., 2017). The only requirement for the model is to accept arbitrary input

segments (i.e. not be limited to document pre-fixes).

Furthemore, we propose a way to use this technique to assign what we call *differential importance scores* to contexts of different lengths. This can be seen as complementary to other techniques like attention or saliency map visualization. Interestingly, contrary to those techniques, ours appears promising as a tool for studying long-range dependencies, since it can be expected to highlight important information not already covered by shorter contexts.

2 Related work

A popular way to dissect Transformers is by visualizing their attention weights (e.g. Vig, 2019; Hoover et al., 2020). However, it has been argued that this does not provide reliable explanations and can be misleading (Jain and Wallace, 2019; Serrano and Smith, 2019). A more recent line of work (Elhage et al., 2021; Olsson et al., 2022) explores "mechanistic explanations", based on reverse-engineering the computations performed by Transformers. These techniques are tied to concrete architectures, which are often "toy" versions of those used in real-world applications, e.g. attention-only Transformers in Elhage et al.

Other options include general-purpose methods like neuron/activation interpretation (e.g. Geva et al., 2021; Goh et al., 2021; Dai et al., 2022), saliency maps (e.g. Fong and Vedaldi, 2017; Ancona et al., 2019) and influence functions (Koh and Liang, 2017). These require access to internal representations and/or the ability to backpropagate gradients, and have some caveats of their own (Kindermans et al., 2019; Kokhlikyan et al., 2021).

More closely related to our work are studies that perform *ablation* (e.g. by shuffling, truncation or masking) on different contexts to understand their influence on predictions (O'Connor and Andreas, 2021; Sun et al., 2021; Press et al., 2021; Vafa et al., 2021). To our knowledge, all such existing works only test a few select contexts or greedily search for the most informative one; in contrast, we show that it is feasible to consider *all* context lengths in the range from 1 to a maximum $c_{\max}$, which permits us to obtain fine-grained insights on the example level, e.g. in the form of the proposed differential importance scores. Moreover, many existing analyses (e.g. Vafa et al., 2021; O'Connor and Andreas, 2021) rely on specific training or fine-tuning, which is not the case with our proposal.

3 Method

3.1 Context length probing

A causal LM estimates the conditional probability distribution of a token given its left-hand context in a document:

$$p(x_{n+1} \mid x_1, \ldots, x_n). \quad (1)$$

We are interested here in computing the probabilities conditioned on a *reduced* context of length $c \in \{1, \ldots, n\}$:

$$p(x_{n+1} \mid x_{n-c+1}, \ldots, x_n), \quad (2)$$

so that we may then study the behavior of this distribution as a function of c.

An apparent obstacle in doing so is that applying the model to an arbitrary subsequence $x_{n-c+1}, \ldots, x_n$, instead of the full document $x_1, \ldots, x_N$, may lead to inaccurate estimates of the probabilities in Eq. (2). However, we note that large LMs are not usually trained on entire documents. Instead, the training data is pre-processed by shuffling all the documents, concatenating them (with a special token as a separator), and splitting the resulting sequence into *chunks* of a fixed length (usually 1024 or 2048 tokens) with no particular relation to the document length. Thus, the models are effectively trained to accept sequences of tokens starting at arbitrary positions in a document and it is therefore correct to employ them as such to compute estimates of Eq. (2).[3]

It now remains to be detailed how to efficiently evaluate the above probabilities for all positions n and context lengths c. Specifically, for a given document $x_1, \ldots, x_N$ and some maximum context length $c_{\max}$, we are interested in an $(N-1) \times c_{\max} \times |\mathcal{V}|$ tensor $\boldsymbol{P}$, where $\mathcal{V} = \{w_1, \ldots, w_{|\mathcal{V}|}\}$ is the vocabulary, such that:

$$\boldsymbol{P}_{n,c,i} = p(x_{n+1} = w_i \mid x_{n-c+1}, \ldots, x_n), \quad (3)$$

with $\boldsymbol{P}_{n,c,*} = \boldsymbol{P}_{n,n-1,*}$ for $n \leq c$.[4] Observe that by running the model on any segment $x_m, \ldots, x_n$, we obtain all the values $\boldsymbol{P}_{m+c-1,c,*}$ for $c \in \{1, \ldots, n-m+1\}$. Therefore, we can fill in the tensor $\boldsymbol{P}$ by applying the model along a sliding window of size $c_{\max}$, i.e. running it on N (overlapping)

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[3]For models trained on data that is pre-processed differently, (re)training or fine-tuning with data augmentation such as random shifts may be needed in order to apply our method, analogously to Vafa et al. (2021), who use word dropout to ensure compatibility with their method.

[4]$\boldsymbol{P}_{n,c,*}$ is a $|\mathcal{V}|$-dimensional slice of $\boldsymbol{P}$ along the last axis.

segments of length at most $c_{\max}$. See Appendix A for an illustration and additional remarks.

3.2 Metrics

Having obtained the tensor $\boldsymbol{P}$ as we have just described, we use it to study how the predictions evolve as the context length is increased from 1 to $c_{\max}$. Specifically, our goal is to define a suitable metric that we can compute from $\boldsymbol{P}_{n,c,*}$ and follow it as a function of c (for a specific n or on average).

One possibility would be to use the negative log-likelihood (NLL) loss values:

$$- \log p(x_{n+1} \mid x_{n-c+1}, \ldots, x_n). \qquad (4)$$

However, this may not be a particularly suitable metric for explainability purposes, as it depends (only) on the probability assigned to the *ground truth* x_{n+1}, while the LM outputs a probability distribution $\boldsymbol{P}_{n,c,*}$ over the entire vocabulary, which may in fact contain many other plausible continuations. For this reason, we propose to exploit a metric defined on whole *distributions*, e.g. the Kullback-Leibler (KL) divergence. To achieve this, we choose the maximum-context predictions $\boldsymbol{P}_{n,c_{\max},*}$ as a reference and get:

$$\mathcal{D}_{n,c} = D_{\mathrm{KL}}[\boldsymbol{P}_{n,c_{\max},*} \parallel \boldsymbol{P}_{n,c,*}]$$
$$= \sum_{i=1}^{|\mathcal{V}|} \boldsymbol{P}_{n,c_{\max},i} \log \frac{\boldsymbol{P}_{n,c_{\max},i}}{\boldsymbol{P}_{n,c,i}}. \qquad (5)$$

The rationale for (5) is to quantify the amount of information that is lost by using a shorter context $c \leq c_{\max}$. Interestingly, this metric is *not* related to the absolute performance of the model with maximal context, but rather to how the output *changes* if a shorter context is used.

3.3 Differential importance scores

We are also interested in studying how individual *increments* in context length affect the predictions. We propose to quantify this as the change in the KL divergence metric (5) when a new token is introduced into the context. Specifically, for a pair of tokens x_{n+1} (the *target token*) and x_m (the *context token*), we define a *differential importance score* (Δ-score for short)

$$\Delta \mathcal{D}_{n,m} = \mathcal{D}_{n,n-m-1} - \mathcal{D}_{n,n-m}. \qquad (6)$$

We may visualize these scores as a way to explain the LM predictions, much like is often done with

name	#param	#layer	#head	d_{model}	max len
gpt2	117 M	12	12	768	1024
gpt2-xl	1.5 B	48	25	1600	1024
gpt-j-6B	6.1 B	28	16	4096	2048

Table 1: Hyperparameters of the 3 models used.

attention weights, with two important differences. First, a high $\Delta \mathcal{D}_{n,m}$ should not be interpreted as meaning that x_m in isolation is important for predicting x_{n+1}, but rather that it is salient given the context that follows it (which might mean that it brings information not contained in the following context). Second, unlike attention weights, our scores need not sum up to one, and can be negative; in this regard, the proposed representation is more conceptually similar to a saliency map than to an attention map.

4 Results

We apply the proposed technique to publicly available pre-trained large Transformer language models, namely GPT-J (Wang and Komatsuzaki, 2021) and two GPT-2 (Radford et al., 2019) variants – see Table 1 for an overview. We use the validation set of the English LinES treebank[5] from Universal Dependencies (UD; Nivre et al., 2020), containing 8 documents with a total length of 20 672 tokens[6] and covering fiction, an online manual, and Europarl data. We set $c_{\max} = 1023$. We use the 🤗 Transformers library[7] (Wolf et al., 2020) to load the pre-trained models and run inference. Further technical details are included in Appendix B.

4.1 LM loss by context length

Fig. 2 shows the cross entropy losses (NLL means) across the whole validation dataset as a function of context length c. As expected, larger models perform better than smaller ones, which is traditionally explained by their larger capacity. A less common observation we can make thanks to this detailed representation is that the gains in performance come mostly from relatively short contexts (8–256 tokens); this is consistent with prior works (Sun et al., 2021; Press et al., 2021) which found

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[5] https://universaldependencies.org/treebanks/en_lines/index.html

[6] After concatenating all sentences and applying the GPT-2 tokenizer, which is used by both GPT-2 and GPT-J.

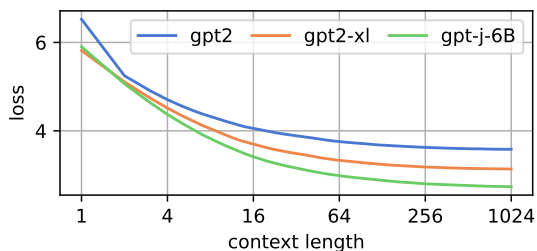[7] https://github.com/huggingface/transformers

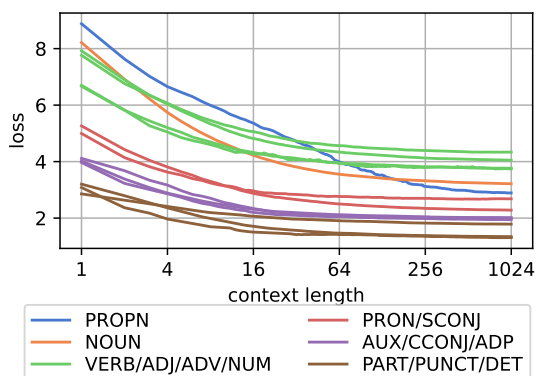Figure 2: Mean LM losses by context length.

Figure 3: Mean GPT-J loss by context length and part-of-speech (POS) tag of the target token. Only POS tags with at least 100 occurrences in the dataset are included. The tags are grouped (arbitrarily) for clarity.

that very long contexts bring only minimal improvement (though these focused on specific *long-range* architectures and on contexts beyond the range we investigate here).

In Fig. 3, we display the same information (loss by context length) broken down by part-of-speech (POS) tags, for GPT-J only. For most POS tags, the behavior is similar to what we observed in Fig. 2 and the loss appears to stabilize around context lengths 16–64. However, we see a distinct behaviour for proper nouns (PROPN), which are the hardest-to-predict category for short contexts, but whose loss improves steadily with increasing c, surpassing that of regular nouns (NOUN) at $c = 162$ and continuing to improve beyond that point.

4.2 Per-token losses by context length

We have also examined token-level losses, as well as the KL divergence metric (see Section 3.2); an example plot is shown in Fig. 4 and more are found in Appendix C.1. In general, we observe that the values tend to change gradually with c; large differences are sparse, especially for large c, and can often be attributed to important pieces of information appearing in the context (e.g. "owl" and "swoop" in the context of "birds" in Fig. 4). This justifies

our use of these differences as importance scores.

4.3 Differential importance scores

To facilitate the exploration of Δ-scores from Section 3.3, we have created an interactive web demo,[2] which allows visualizing the scores for any of the 3 models on the validation set as shown in Fig. 1.

In Fig. 5, we display the magnitudes of the Δ-scores − normalized for each position to sum up to 1 across all context lengths − as a function of context length. The plot suggests a power-law-like inverse relationship where increasing context length proportionally reduces the Δ-score magnitude on average. We interpret this as far-away tokens being less likely to carry information not already covered by shorter contexts. Long contexts (see inset in Fig. 5) bear less importance for larger models than for smaller ones, perhaps because the additional capacity allows relying more on shorter contexts.

In Fig. 6, we also display the mean importance score received by each POS category, by model. We can see that proper nouns (PROPN) are substantially more informative than other categories (which is in line with the observations in the previous section), but less so for the smallest model. This could mean e.g. that larger models are better at memorizing named entities from training data and using them to identify the topic of the document, or simply at copying them from distant context as observed in (Sun et al., 2021).

5 Limitations and future directions

Experiments. We acknowledge the limited scope of our experiments, including only 8 (closed-domain) documents, 3 models and a single language. This is largely due to the limited availability of suitable large LMs and their high computational cost. Still, we believe that our experiments are valuable as a case study that already clearly showcases some interesting features of our methodology.

Computational cost. While we have demonstrated an efficient strategy to obtain predictions for all tokens at all possible context lengths, it still requires running the model N times for a document of length N.

For a k-fold reduction in computational cost, the technique may be modified to use a sliding window with stride $k > 1$ (instead of $k = 1$ as proposed above). See Appendix A.1 for details.
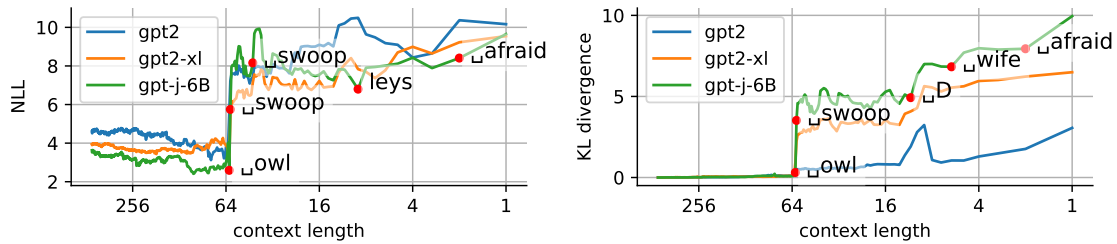
Figure 4: NLL (left) and KL divergence (right) as a function of context length for a selected example: "[...] mortally afraid of **birds**" (same as in Fig. 1). The x axis is reversed for visual correspondence with the left-hand context. The 5 context tokens causing the largest drops in each metric for GPT-J are marked by red dots.
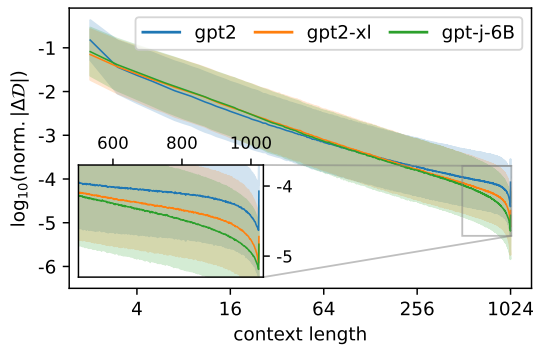

Figure 5: Normalized Δ-score log-magnitude (mean and std. dev.) by context length and by model. Only positions $n \geq 1024$ are included.
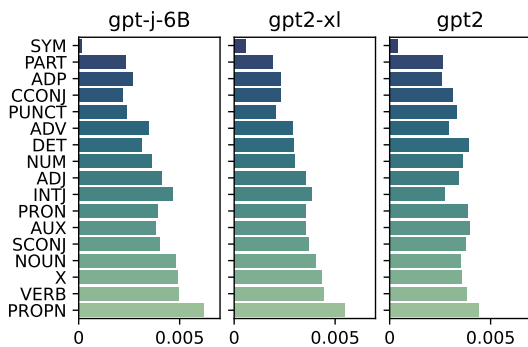

Figure 6: Mean Δ-score by POS tag of the context token and by model.

Choice of metrics. The proposed methodology allows investigating how any given metric is impacted by context, yet our study is limited to NLL loss and the proposed KL divergence metric (the latter for defining importance scores). These may not be optimal for every purpose, and other choices should be explored depending on the application. For example, to study sequences *generated* (sampled) from a LM, one might want to define importance scores using a metric that does depend on the generated token, e.g. its NLL loss or its ranking among all candidates. (Indeed, our web demo also supports Δ-scores defined using NLL loss values.)

6 Conclusion and future directions

We have presented *context length probing*, a novel causal LM explanation technique based on tracking the predictions of the LM as a function of context length, and enabling the assignment of *differential importance scores* (Δ-scores). While it has some advantages over existing techniques, it answers different questions, and should thus be thought of as complementary rather than a substitute.

A particularly interesting feature of our Δ-scores is their apparent potential for discovering *long-range dependencies* (LRDs) (as they are expected to highlight information not already covered by shorter contexts, unlike e.g. attention maps).

Remarkably, our analysis suggests a power-law-like inverse relationship between context length and importance score, seemingly questioning the importance of LRDs in language modeling. While LRDs clearly appear crucial for applications such as long-form text generation, their importance may not be strongly reflected by LM performance metrics like cross entropy or perplexity. We thus believe that there is an opportunity for more specialized benchmarks of LRD modeling capabilities of different models, such as that of Sun et al. (2022), for example. These should further elucidate questions like to what extent improvements in LM performance are due to better LRD modeling, how LRDs are handled by various Transformer variants (e.g. Kitaev et al., 2020; Katharopoulos et al., 2020; Choromanski et al., 2021; Press et al., 2022), or what their importance is for different tasks.

Acknowledgments

References

Marco Ancona, Cengiz Oztireli, and Markus Gross. 2019. Explaining deep neural networks with a polynomial time algorithm for Shapley value approximation. In *Proceedings of the 36th International Conference on Machine Learning*, volume 97 of *Proceedings of Machine Learning Research*, pages 272–281. PMLR.

Krzysztof Marcin Choromanski, Valerii Likhosherstov, David Dohan, Xingyou Song, Andreea Gane, Tamás Sarlós, Peter Hawkins, Jared Quincy Davis, Afroz Mohiuddin, Lukasz Kaiser, David Benjamin Belanger, Lucy J. Colwell, and Adrian Weller. 2021. Rethinking attention with Performers. In *9th International Conference on Learning Representations (ICLR 2021)*. OpenReview.net.

Damai Dai, Li Dong, Yaru Hao, Zhifang Sui, Baobao Chang, and Furu Wei. 2022. Knowledge neurons in pretrained transformers. In *Proceedings of the 60th Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers)*, pages 8493–8502, Dublin, Ireland. Association for Computational Linguistics.

Yann N. Dauphin, Angela Fan, Michael Auli, and David Grangier. 2017. Language modeling with gated convolutional networks. In *Proceedings of the 34th International Conference on Machine Learning*, volume 70 of *Proceedings of Machine Learning Research*, pages 933–941. PMLR.

Nelson Elhage, Neel Nanda, Catherine Olsson, Tom Henighan, Nicholas Joseph, Ben Mann, Amanda Askell, Yuntao Bai, Anna Chen, Tom Conerly, Nova DasSarma, Dawn Drain, Deep Ganguli, Zac Hatfield-Dodds, Danny Hernandez, Andy Jones, Jackson Kernion, Liane Lovitt, Kamal Ndousse, Dario Amodei, Tom Brown, Jack Clark, Jared Kaplan, Sam McCandlish, and Chris Olah. 2021. A mathematical framework for Transformer circuits. *Transformer Circuits Thread*.

Ruth C. Fong and Andrea Vedaldi. 2017. Interpretable explanations of black boxes by meaningful perturbation. In *IEEE International Conference on Computer Vision*, pages 3449–3457, Venice, Italy. IEEE Computer Society.

Mor Geva, Roei Schuster, Jonathan Berant, and Omer Levy. 2021. Transformer feed-forward layers are key-value memories. In *Proceedings of the 2021 Conference on Empirical Methods in Natural Language Processing*, pages 5484–5495, Online and Punta Cana, Dominican Republic. Association for Computational Linguistics.

Gabriel Goh, Nick Cammarata, Chelsea Voss, Shan Carter, Michael Petrov, Ludwig Schubert, Alec Radford, and Chris Olah. 2021. Multimodal neurons in artificial neural networks. *Distill*.

Benjamin Hoover, Hendrik Strobelt, and Sebastian Gehrmann. 2020. exBERT: A Visual Analysis Tool to Explore Learned Representations in Transformer Models. In *Proceedings of the 58th Annual Meeting of the Association for Computational Linguistics: System Demonstrations*, pages 187–196, Online. Association for Computational Linguistics.

Sarthak Jain and Byron C. Wallace. 2019. Attention is not Explanation. In *Proceedings of the 2019 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies, Volume 1 (Long and Short Papers)*, pages 3543–3556, Minneapolis, Minnesota. Association for Computational Linguistics.

Angelos Katharopoulos, Apoorv Vyas, Nikolaos Pappas, and François Fleuret. 2020. Transformers are RNNs: Fast autoregressive Transformers with linear attention. In *Proceedings of the 37th International Conference on Machine Learning*. PMLR.

Pieter-Jan Kindermans, Sara Hooker, Julius Adebayo, Maximilian Alber, Kristof T. Schütt, Sven Dähne, Dumitru Erhan, and Been Kim. 2019. The (un)reliability of saliency methods. In Wojciech Samek, Grégoire Montavon, Andrea Vedaldi, Lars Kai Hansen, and Klaus-Robert Müller, editors, *Explainable AI: Interpreting, Explaining and Visualizing Deep Learning*, volume 11700 of *Lecture Notes in Computer Science*, pages 267–280. Springer.

Nikita Kitaev, Lukasz Kaiser, and Anselm Levskaya. 2020. Reformer: The efficient Transformer. In *8th International Conference on Learning Representations (ICLR 2020)*. OpenReview.net.

Pang Wei Koh and Percy Liang. 2017. Understanding black-box predictions via influence functions. In *Proceedings of the 34th International Conference on Machine Learning*, volume 70 of *Proceedings of Machine Learning Research*, pages 1885–1894. PMLR.

Narine Kokhlikyan, Vivek Miglani, Bilal Alsallakh, Miguel Martin, and Orion Reblitz-Richardson. 2021. Investigating sanity checks for saliency maps with image and text classification. *arXiv preprint arXiv:2106.07475*.

Tomáš Mikolov, Martin Karafiát, Lukáš Burget, Jan Černocký, and Sanjeev Khudanpur. 2010. Recurrent neural network based language model. In *INTERSPEECH 2010, 11th Annual Conference of the International Speech Communication Association*, pages 1045–1048, Makuhari, Chiba, Japan. ISCA.

Joakim Nivre, Marie-Catherine de Marneffe, Filip Ginter, Jan Hajič, Christopher D. Manning, Sampo Pyysalo, Sebastian Schuster, Francis Tyers, and Daniel Zeman. 2020. Universal Dependencies v2: An evergrowing multilingual treebank collection. In *Proceedings of the 12th Language Resources and Evaluation Conference*, pages 4034–4043, Marseille, France. European Language Resources Association.

Joe O'Connor and Jacob Andreas. 2021. What context features can transformer language models use? In *Proceedings of the 59th Annual Meeting of the Association for Computational Linguistics and the 11th International Joint Conference on Natural Language Processing (Volume 1: Long Papers)*, pages 851–864, Online. Association for Computational Linguistics.

Catherine Olsson, Nelson Elhage, Neel Nanda, Nicholas Joseph, Nova DasSarma, Tom Henighan, Ben Mann, Amanda Askell, Yuntao Bai, Anna Chen, Tom Conerly, Dawn Drain, Deep Ganguli, Zac Hatfield-Dodds, Danny Hernandez, Scott Johnston, Andy Jones, Jackson Kernion, Liane Lovitt, Kamal Ndousse, Dario Amodei, Tom Brown, Jack Clark, Jared Kaplan, Sam McCandlish, and Chris Olah. 2022. In-context learning and induction heads. *Transformer Circuits Thread*.

Ofir Press, Noah Smith, and Mike Lewis. 2022. Train short, test long: Attention with linear biases enables input length extrapolation. In *The Tenth International Conference on Learning Representations*, Virtual Event. OpenReview.net.

Ofir Press, Noah A. Smith, and Mike Lewis. 2021. Shortformer: Better language modeling using shorter inputs. In *Proceedings of the 59th Annual Meeting of the Association for Computational Linguistics and the 11th International Joint Conference on Natural Language Processing (Volume 1: Long Papers)*, pages 5493–5505, Online. Association for Computational Linguistics.

Alec Radford, Jeff Wu, Rewon Child, David Luan, Dario Amodei, and Ilya Sutskever. 2019. Language models are unsupervised multitask learners.

Sofia Serrano and Noah A. Smith. 2019. Is attention interpretable? In *Proceedings of the 57th Annual Meeting of the Association for Computational Linguistics*, pages 2931–2951, Florence, Italy. Association for Computational Linguistics.

Simeng Sun, Kalpesh Krishna, Andrew Mattarella-Micke, and Mohit Iyyer. 2021. Do long-range language models actually use long-range context? In *Proceedings of the 2021 Conference on Empirical Methods in Natural Language Processing*, pages 807–822, Online and Punta Cana, Dominican Republic. Association for Computational Linguistics.

Simeng Sun, Katherine Thai, and Mohit Iyyer. 2022. ChapterBreak: A challenge dataset for long-range language models. In *Proceedings of the 2022 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies*, pages 3704–3714, Seattle, United States. Association for Computational Linguistics.

Keyon Vafa, Yuntian Deng, David Blei, and Alexander Rush. 2021. Rationales for sequential predictions. In *Proceedings of the 2021 Conference on Empirical Methods in Natural Language Processing*, pages 10314–10332, Online and Punta Cana, Dominican Republic. Association for Computational Linguistics.

Ashish Vaswani, Noam Shazeer, Niki Parmar, Jakob Uszkoreit, Llion Jones, Aidan N. Gomez, Lukasz Kaiser, and Illia Polosukhin. 2017. Attention is all you need. In *Advances in Neural Information Processing Systems 30: Annual Conference on Neural Information Processing Systems*, pages 5998–6008, Long Beach, CA, USA.

Jesse Vig. 2019. A multiscale visualization of attention in the transformer model. In *Proceedings of the 57th Annual Meeting of the Association for Computational Linguistics: System Demonstrations*, pages 37–42, Florence, Italy. Association for Computational Linguistics.

Ben Wang and Aran Komatsuzaki. 2021. GPT-J-6B: A 6 billion parameter autoregressive language model.

Thomas Wolf, Lysandre Debut, Victor Sanh, Julien Chaumond, Clement Delangue, Anthony Moi, Pierric Cistac, Tim Rault, Remi Louf, Morgan Funtowicz, Joe Davison, Sam Shleifer, Patrick von Platen, Clara Ma, Yacine Jernite, Julien Plu, Canwen Xu, Teven Le Scao, Sylvain Gugger, Mariama Drame, Quentin Lhoest, and Alexander Rush. 2020. 🤗 Transformers: State-of-the-art natural language processing. In *Proceedings of the 2020 Conference on Empirical Methods in Natural Language Processing: System Demonstrations*, pages 38–45, Online. Association for Computational Linguistics.
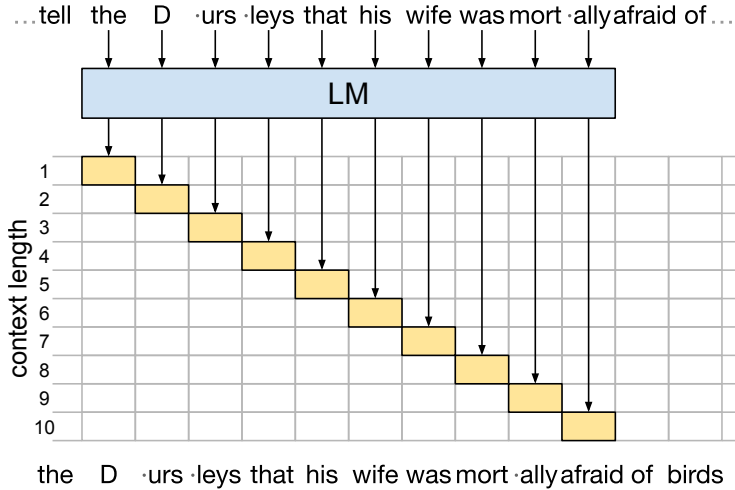
Figure 7: A step of context length probing with $c_{\max} = 10$. The input tokens are shown at the top, the target tokens at the bottom. When the LM is run on a segment of the document, the effective context length for each target token is equal to its offset from the beginning of the segment, e.g. the context for predicting "␣D" is "␣the" ($c = 1$), the context for "urs" is "␣the␣D" ($c = 2$), etc.

A   Context length probing

Fig. 7 illustrates a step of context length probing. We wish to obtain the tensor $\boldsymbol{P}$ from Eq. (3), understood as a table where each cell contains the predictions (next-token logits) for a given position in the text and a given context length. By running our LM on a segment of the text, we get predictions such that for the n-th token in the segment, the effective context length is equal to n, which corresponds to a diagonal in the table. We can thus fill in the whole table by running the LM on all segments of length $c_{\max}$ (plus trailing segments of lengths $c_{\max} - 1, \ldots, 1$).

Notice that this process is somewhat similar to (naïvely) running the LM in generation mode, except that at each step, the leading token is removed, preventing the use of caching to speed up the computation.

In practice, it is not necessary to explicitly construct the tensor $\boldsymbol{P}$. Indeed, we find it more efficient to instead store the raw logits obtained by running the model on all the segments, then do the necessary index arithmetics when computing the metrics.

A.1   Strided context length probing

For a k-fold reduction in computational cost, we may instead use a sliding window with a stride $k > 1$, i.e. run the model only on segments starting at positions $k(n-1)+1$ for all $n \in \{1, \ldots, \lceil N/k \rceil\}$, rather than all positions. This way, for a target token x_{n+1}, we obtain the predictions $p(x_{n+1} \mid x_{n-c+1}, \ldots, x_n)$ only for such context lengths c that $c \bmod k = n$. In other words, predictions with context length c are only available for tokens $x_{c+1}, x_{c+k+1}, x_{c+2k+1}, \ldots$. Consequently:

- Overall, we still cover all context lengths $1, \ldots, c_{\max}$, allowing us to perform aggregate analyses like the ones in Section 4.1.

- When analyzing the predictions for a specific target token in a document (e.g. to compute Δ-scores), context tokens come in blocks of length k. Visualizations like the ones in Figs. 1 and 4 are still possible for all target tokens, but become less detailed, grouping every k context tokens together.

- Computation time, as well as the space needed to store the predictions, is reduced by a factor of k.

B   Technical details

Data.   The LinES treebank is licensed under Creative Commons BY-NC-SA 4.0. We concatenated all tokens from each of the documents from the treebank, then re-tokenized them using the GPT-2 tokenizer.

We mapped the original (UD) POS tags to the GPT-tokenized dataset in such a way that every GPT token is assigned the POS tag of the first UD token it overlaps with.

Models. We used the models `EleutherAI/gpt-j-6B` (Apache 2.0 license), and `gpt2-xl` and `gpt2` (MIT license), all from `huggingface.co`.
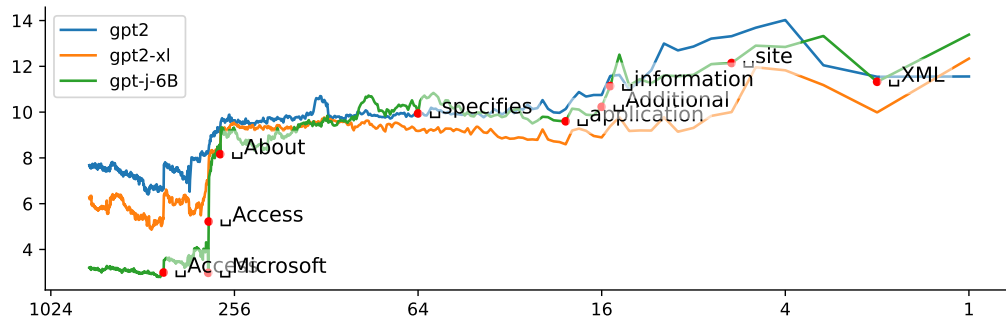
Computation. We parallelized the inference over 500 jobs on a compute cluster,[8] each running on 8 CPU cores with at least $8\,\mathrm{GB}$ of RAM per core, with a batch size of 16. Each job took about 10–$20\,\mathrm{min}$ for GPT-2 and 30–$60\,\mathrm{min}$ for GPT-J. Additionally, computing the metrics from the logits (which take up $2\,\mathrm{TB}$ of disk space in `float16`) took between 2 and $4\,\mathrm{h}$ per model on a single machine with 32 CPU cores. The total computing time was 318 core-days, including debugging and discarded runs.
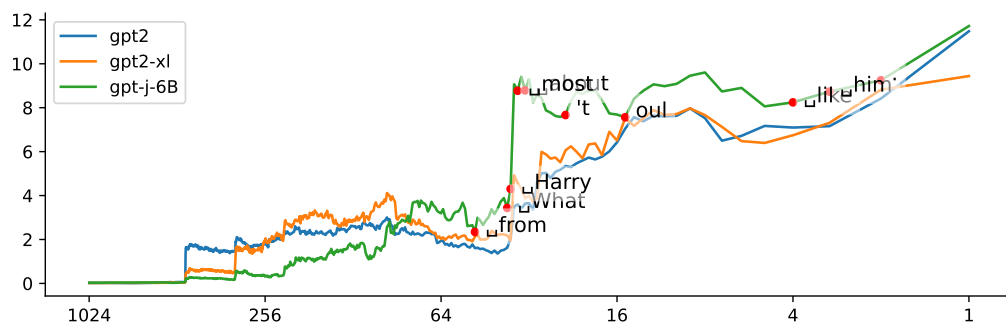
C Additional plots

C.1 Token-wise metrics as a function of context length

Figs. 8 and 9 show NLL and KL divergence (5), respectively, as a function of context length, for selected target tokens (proper nouns) from the validation set.
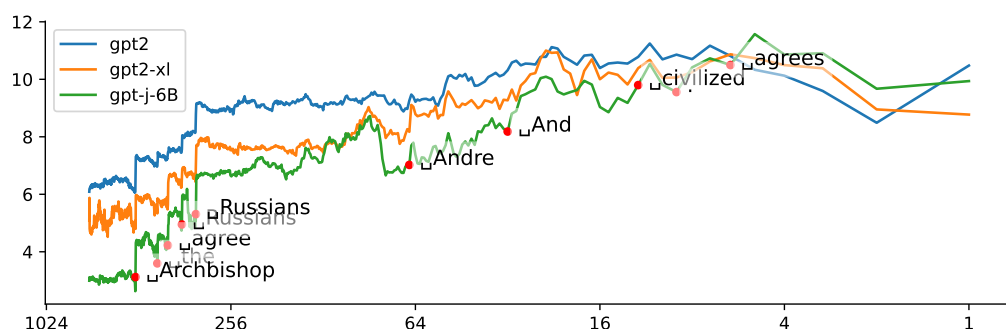
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[8]Nef, the cluster computing infrastructure of Inria Sophia Antipolis Méditerranée; see `https://wiki.inria.fr/ClustersSophia`

(a) . . . and attribute means (and thus how the data between them will look in a browser), XML uses the tags only to delimit pieces of data, and leaves the interpretation of the data completely to the application that reads it. Additional information about XML can be found on the web site. About importing XML data **Access**
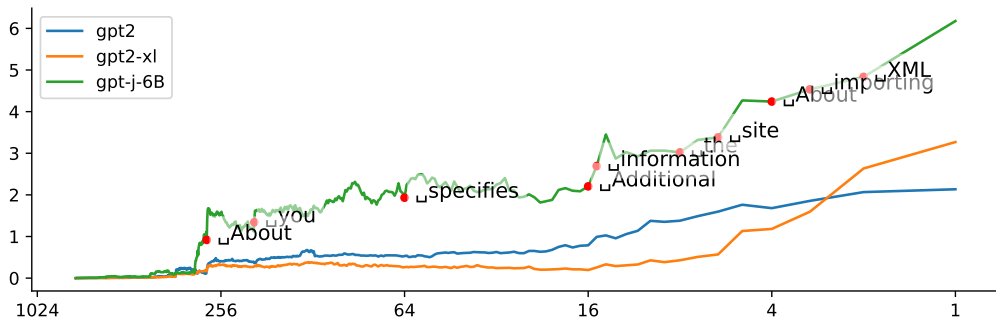

(b) . . . he felt things were getting too quiet, and small explosions from Fred and George's bedroom were considered perfectly normal. What Harry found most unusual about life at Ron's, however, wasn't the talking mirror or the clanking ghoul: it was the fact that everybody there seemed to like him. Mrs **Weasley**
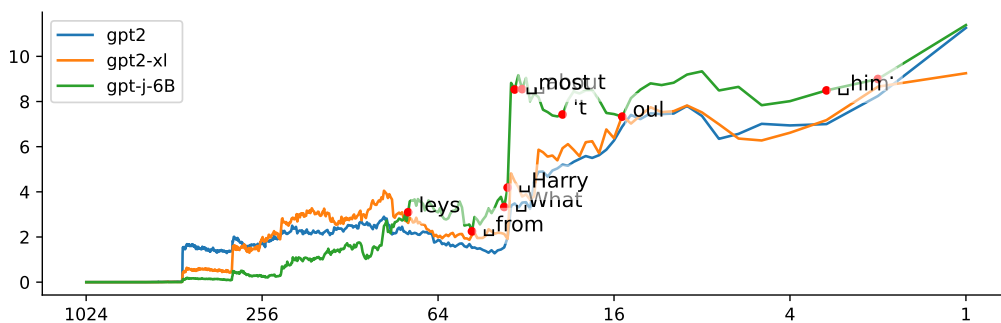

(c) . . . is a great difference between Napoleon the Emperor and Napoleon the private person. There are raisons d'etat and there are private crimes. And the talk goes on. What is still being perpetuated in all civilized discussion is the ritual of civilized discussion itself. Tatu agrees with the Archbishop about the **Russians**
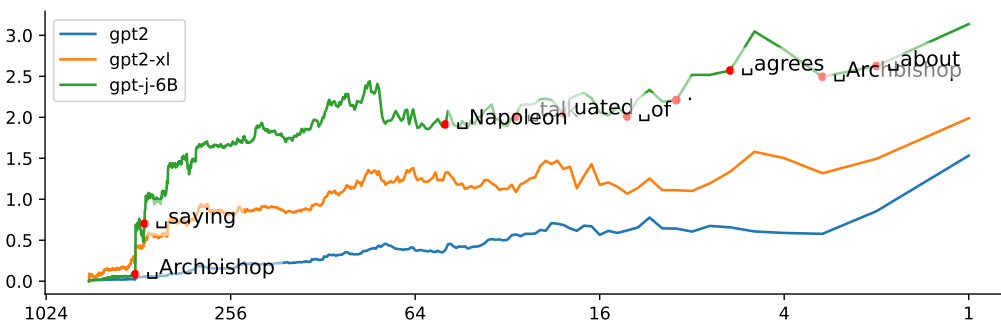
Figure 8: NLL losses (y axis) for 3 selected target tokens as a function of context length (x axis). Below each plot, the target token is displayed in bold, along with a context of 60 tokens. The x axis is reversed to correspond visually to left-hand context. The red dots show the 10 tokens that cause the largest drops in GPT-J cross entropy when added to the context.

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Figure 9: KL divergences (y axis) from Eq. (5) for 3 selected target tokens as a function of context length (x axis). Below each plot, the target token is displayed in bold, along with a context of 60 tokens. The x axis is reversed to correspond visually to left-hand context. The red dots show the 10 tokens that cause the largest drops in the metric (for GPT-J) when added to the context.

A   For every submission:

☑ A1. Did you describe the limitations of your work?
Section 5

☒ A2. Did you discuss any potential risks of your work?
We did not identify any risks. The usual risks related to large language models are arguably not present here since we are not proposing or training a new LM, but a way to explain it.

☑ A3. Do the abstract and introduction summarize the paper's main claims?
Abstract, Section 1

☒ A4. Have you used AI writing assistants when working on this paper?
Left blank.

B   ☑ Did you use or create scientific artifacts?

Section 4

☑ B1. Did you cite the creators of artifacts you used?
Section 4

☑ B2. Did you discuss the license or terms for use and / or distribution of any artifacts?
Section 4, appendix

☒ B3. Did you discuss if your use of existing artifact(s) was consistent with their intended use, provided that it was specified? For the artifacts you create, do you specify intended use and whether that is compatible with the original access conditions (in particular, derivatives of data accessed for research purposes should not be used outside of research contexts)?
For artifacts we use, no intended use is specified except for non-commercial license (CC NC-BY-SA) for the data. We do not specifically discuss this but we are using all artifacts in a purely non-commercial research context. Any artifacts we release will be under a non-commercial license.

☒ B4. Did you discuss the steps taken to check whether the data that was collected / used contains any information that names or uniquely identifies individual people or offensive content, and the steps taken to protect / anonymize it?
We use data published in peer-reviewed conference proceedings and we rely on the original authors to have taken those steps.

☑ B5. Did you provide documentation of the artifacts, e.g., coverage of domains, languages, and linguistic phenomena, demographic groups represented, etc.?
Section 4

☑ B6. Did you report relevant statistics like the number of examples, details of train / test / dev splits, etc. for the data that you used / created? Even for commonly-used benchmark datasets, include the number of examples in train / validation / test splits, as these provide necessary context for a reader to understand experimental results. For example, small differences in accuracy on large test sets may be significant, while on small test sets they may not be.
Section 4, appendix B

The Responsible NLP Checklist used at ACL 2023 is adopted from NAACL 2022, with the addition of a question on AI writing assistance.

C ☑ **Did you run computational experiments?**

Section 4

☑ C1. Did you report the number of parameters in the models used, the total computational budget (e.g., GPU hours), and computing infrastructure used?
Appendix B

☑ C2. Did you discuss the experimental setup, including hyperparameter search and best-found hyperparameter values?
Section 4, appendix B

☑ C3. Did you report descriptive statistics about your results (e.g., error bars around results, summary statistics from sets of experiments), and is it transparent whether you are reporting the max, mean, etc. or just a single run?
Section 4. Only reporting a single (deterministic) run at a time; it is made clear whenever reporting a mean metric over the dataset

☑ C4. If you used existing packages (e.g., for preprocessing, for normalization, or for evaluation), did you report the implementation, model, and parameter settings used (e.g., NLTK, Spacy, ROUGE, etc.)?
Section 4, appendix A

D ☒ **Did you use human annotators (e.g., crowdworkers) or research with human participants?**

Left blank.

☐ D1. Did you report the full text of instructions given to participants, including e.g., screenshots, disclaimers of any risks to participants or annotators, etc.?
No response.

☐ D2. Did you report information about how you recruited (e.g., crowdsourcing platform, students) and paid participants, and discuss if such payment is adequate given the participants' demographic (e.g., country of residence)?
No response.

☐ D3. Did you discuss whether and how consent was obtained from people whose data you're using/curating? For example, if you collected data via crowdsourcing, did your instructions to crowdworkers explain how the data would be used?
No response.

☐ D4. Was the data collection protocol approved (or determined exempt) by an ethics review board?
No response.

☐ D5. Did you report the basic demographic and geographic characteristics of the annotator population that is the source of the data?
No response.