

# Probing Pretrained Language Models for Lexical Semantics

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## Abstract

The success of large pretrained language models (LMs) such as BERT and RoBERTa has sparked interest in probing their representations, in order to unveil what types of knowledge they implicitly capture. While prior research focused on morphosyntactic, semantic, and world knowledge, it remains unclear to which extent LMs also derive *lexical type-level knowledge* from words in context. In this work, we present a *systematic empirical analysis* across six typologically diverse languages and five different lexical tasks, addressing the following questions: **1)** How do different lexical knowledge extraction strategies (monolingual versus multilingual source LM, out-of-context versus in-context encoding, inclusion of special tokens, and layer-wise averaging) impact performance? How consistent are the observed effects across tasks and languages? **2)** Is lexical knowledge stored in few parameters, or is it scattered throughout the network? **3)** How do these representations fare against traditional static word vectors in lexical tasks? **4)** Does the lexical information emerging from independently trained monolingual LMs display latent similarities? Our main results indicate patterns and best practices that hold universally, but also point to prominent variations across languages and tasks. Moreover, we validate the claim that lower Transformer layers carry more type-level lexical knowledge, but also show that this knowledge is distributed across multiple layers.

## 1 Introduction and Motivation

Language models (LMs) based on deep Transformer networks (Vaswani et al., 2017), pretrained on unprecedentedly large amounts of text, offer unmatched performance in virtually every NLP task (Qiu et al., 2020). Models such as BERT (Devlin et al., 2019), RoBERTa (Liu et al., 2019c), and T5 (Raffel et al., 2019) replaced task-specific neural

architectures that relied on *static* word embeddings (WEs; Mikolov et al., 2013b; Pennington et al., 2014; Bojanowski et al., 2017), where each word is assigned a single (type-level) vector.

While there is a clear consensus on the effectiveness of pretrained LMs, a body of recent research has aspired to understand *why* they work (Rogers et al., 2020). State-of-the-art models are “probed” to shed light on whether they capture task-agnostic linguistic knowledge and structures (Liu et al., 2019a; Belinkov and Glass, 2019; Tenney et al., 2019); e.g., they have been extensively probed for syntactic knowledge (Hewitt and Manning, 2019; Jawahar et al., 2019; Kulmizev et al., 2020; Chi et al., 2020, *inter alia*) and morphology (Edmiston, 2020; Hofmann et al., 2020).

In this work, we put focus on uncovering and understanding *how and where lexical semantic knowledge* is coded in state-of-the-art LMs. While preliminary findings from Ethayarajh (2019) and Vulić et al. (2020) suggest that there is a wealth of lexical knowledge available within the parameters of BERT and other LMs, a *systematic empirical study across different languages* is currently lacking.

We present such a study, spanning six typologically diverse languages for which comparable pretrained BERT models *and* evaluation data are readily available. We dissect the pipeline for extracting lexical representations, and divide it into crucial components, including: the underlying source LM, the selection of subword tokens, external corpora, and which Transformer layers to average over. Different choices give rise to different *extraction configurations* (see Table 1) which, as we empirically verify, lead to large variations in task performance.

We run experiments and analyses on five diverse lexical tasks using standard evaluation benchmarks: lexical semantic similarity (LSIM), word analogy resolution (WA), bilingual lexicon induction (BLI), cross-lingual information retrieval (CLIR), and lex-

ical relation prediction (RELP). The main idea is to aggregate lexical information into static type-level “BERT-based” word embeddings and plug them into “the classical NLP pipeline” (Tenney et al., 2019), similar to traditional static word vectors. The chosen tasks can be seen as “lexico-semantic probes” providing an opportunity to simultaneously **1)** evaluate the richness of lexical information extracted from different parameters of the underlying pretrained LM on intrinsic (e.g., LSIM, WA) and extrinsic lexical tasks (e.g., RELP); **2)** compare different type-level representation extraction strategies; and **3)** benchmark “BERT-based” static vectors against traditional static word embeddings such as fastText (Bojanowski et al., 2017).

Our study aims at providing answers to the following key questions: **Q1)** Do lexical extraction strategies generalise across different languages and tasks, or do they rather require language- and task-specific adjustments?; **Q2)** Is lexical information concentrated in a small number of parameters and layers, or scattered throughout the encoder?; **Q3)** Are “BERT-based” static word embeddings competitive with traditional word embeddings such as fastText?; **Q4)** Do monolingual LMs independently trained in multiple languages learn structurally similar representations for words denoting similar concepts (i.e., translation pairs)?

We observe that different languages and tasks indeed require distinct configurations to reach peak performance, which calls for a careful tuning of configuration components according to the specific task–language combination at hand (Q1). However, several universal patterns emerge across languages and tasks. For instance, lexical information is predominantly concentrated in lower Transformer layers, hence excluding higher layers from the extraction achieves superior scores (Q1 and Q2). Further, representations extracted from single layers do not match in accuracy those extracted by averaging over several layers (Q2). While static word representations obtained from monolingual LMs are competitive or even outperform static fastText embeddings in tasks such as LSIM, WA, and RELP, lexical representations from massively multilingual models such as multilingual BERT (mBERT) are substantially worse (Q1 and Q3). We also demonstrate that translation pairs indeed obtain similar representations (Q4), but the similarity depends on the extraction configuration, as well as on the typological distance between the two languages.

## 2 Lexical Representations from Pretrained Language Models

Classical static word embeddings (Bengio et al., 2003; Mikolov et al., 2013b; Pennington et al., 2014) are grounded in distributional semantics, as they infer the meaning of each word type from its co-occurrence patterns. However, LM-pretrained Transformer encoders have introduced at least two levels of misalignment with the classical approach (Peters et al., 2018; Devlin et al., 2019). First, representations are assigned to word *tokens* and are affected by the current context and position within a sentence (Mickus et al., 2020). Second, tokens may correspond to subword strings rather than complete word forms. This begs the question: do pretrained encoders still retain a notion of lexical concepts, abstracted from their instances in texts?

Analyses of lexical semantic information in large pretrained LMs have been limited so far, focusing only on the English language and on the task of word sense disambiguation. Reif et al. (2019) showed that senses are encoded with finer-grained precision in *higher* layers, to the extent that their representation of the same token tends not to be self-similar across different contexts (Ethayarajh, 2019; Mickus et al., 2020). As a consequence, we hypothesise that abstract, type-level information could be codified in *lower* layers instead. However, given the absence of a direct equivalent to a static word type embedding, we still need to establish *how to extract* such type-level information.

In prior work, contextualised representations (and attention weights) have been interpreted in the light of linguistic knowledge mostly through *probes*. These consist in learned classifier predicting annotations like POS tags (Pimentel et al., 2020) and word senses (Peters et al., 2018; Reif et al., 2019; Chang and Chen, 2019), or linear transformations to a space where distances mirror dependency tree structures (Hewitt and Manning, 2019).<sup>1</sup>

In this work, we explore several unsupervised word-level representation extraction strategies and configurations for lexico-semantic tasks (i.e., probes), stemming from different combinations of the components detailed in Table 1 and illustrated in Figure 1. In particular, we assess the impact of: **1)** encoding tokens with monolingual LM-pretrained Transformers vs. with their mas-

<sup>1</sup>The interplay between the complexity of a probe and its accuracy, as well as its effect on the overall procedure, remain controversial (Pimentel et al., 2020; Voita and Titov, 2020).

Component	Label	Short Description
Source LM	MONO	Language-specific (i.e., monolingually pretrained) BERT
	MULTI	Multilingual BERT, pretrained on 104 languages (with shared subword vocabulary)
Context	ISO	Each vocabulary word $w$ is encoded <i>in isolation</i> , without any external context
	AOC-M	<i>Average-over-context</i> : average over word’s encodings from $M$ different contexts/sentences
Subword Tokens	NOSPEC	Special tokens [CLS] and [SEP] are excluded from subword embedding averaging
	ALL	Both special tokens [CLS] and [SEP] are included into subword embedding averaging
	WITHCLS	[CLS] is included into subword embedding averaging; [SEP] is excluded
Layerwise Avg	AVG( $L \leq n$ )	Average representations over all Transformer layers up to the $n$ -th layer $L_n$ (included)
	$L=n$	Only the representation from the layer $L_n$ is used

Table 1: Configuration components of word-level embedding extraction, resulting in 24 possible configurations.

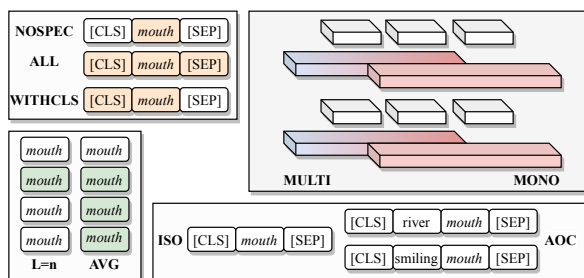


Figure 1: Illustration of the components denoting adopted extraction strategies, including source LM (top right), presence of context (bottom right), special tokens (top left), and layer-wise averaging (bottom left).

sively multilingual counterparts; **2**) providing context around the target word in input; **3**) including special tokens like [CLS] and [SEP]; **4**) averaging across several layers as opposed to a single layer.<sup>2</sup>

### 3 Experimental Setup

**Pretrained LMs and Languages.** Our selection of test languages is guided by the following constraints: **a**) availability of comparable pretrained (language-specific) monolingual LMs; **b**) availability of evaluation data; and **c**) typological diversity of the sample, along the lines of recent initiatives in multilingual NLP (Gerz et al., 2018; Hu et al., 2020; Ponti et al., 2020, *inter alia*). We work with English (EN), German (DE), Russian (RU), Finnish (FI), Chinese (ZH), and Turkish (TR). We use monolingual uncased BERT Base models for all languages, retrieved from the HuggingFace repository (Wolf et al., 2019).<sup>3</sup> All BERT models comprise 12 768-dimensional Transformer layers  $\{L_1$  (bottom layer),  $\dots$ ,  $L_{12}$  (top) $\}$  plus the input

<sup>2</sup>For clarity of presentation, later in §4 we show results only for a representative selection of configurations that are consistently better than the others

<sup>3</sup><https://huggingface.co/models>; the links to the actual BERT models are in the appendix.

embedding layer ( $L_0$ ), and 12 attention heads. We also experiment with multilingual BERT (mBERT) (Devlin et al., 2019) as the underlying LM, aiming to measure the performance difference between language-specific and massively multilingual LMs in our lexical probing tasks.

**Word Vocabularies and External Corpora.** We extract type-level representations in each language for the top 100K most frequent words represented in the respective fastText (FT) vectors, which were trained on lowercased monolingual Wikipedias by Bojanowski et al. (2017). The equivalent vocabulary coverage allows a direct comparison to fastText vectors, which we use as a baseline static WE method in all evaluation tasks. To retain the same vocabulary across all configurations, in AOC variants we back off to the related ISO variant for words that have zero occurrences in external corpora.

For all AOC vector variants, we leverage 1M sentences of maximum sequence length 512, which we randomly sample from external corpora: Europarl (Koehn, 2005) for EN, DE, FI, available via OPUS (Tiedemann, 2009); the United Nations Parallel Corpus for RU and ZH (Ziemski et al., 2016), and monolingual TR WMT17 data (Bojar et al., 2017).

**Evaluation Tasks.** We carry out the evaluation on five standard and diverse lexical semantic tasks:

**Task 1: Lexical semantic similarity (LSIM)** is the most widespread intrinsic task for evaluation of traditional word embeddings (Hill et al., 2015). The evaluation metric is the Spearman’s rank correlation between the average of human-elicited semantic similarity scores for word pairs and the cosine similarity between the respective type-level word vectors. We rely on the recent comprehensive multilingual LSIM benchmark Multi-SimLex (Vulić et al., 2020), which covers 1,888 pairs in 13 languages. We focus on EN, FI, ZH, RU, the

languages represented in Multi-SimLex.

**Task 2: Word Analogy (WA)** is another common intrinsic task. We evaluate our models on the Bigger Analogy Test Set (BATS) (Drozd et al., 2016) with 99,200 analogy questions. We resort to the standard vector offset analogy resolution method, searching for the vocabulary word  $w_d \in V$  such that its vector  $d$  is obtained by  $\text{argmax}_d(\cos(d, c - a + b))$ , where  $a$ ,  $b$ , and  $c$  are word vectors of words  $w_a$ ,  $w_b$ , and  $w_c$  from the analogy  $w_a : w_b = w_c : x$ . The search space comprises vectors of all words from the vocabulary  $V$ , excluding  $a$ ,  $b$ , and  $c$ . This task is limited to EN, and we report Precision@1 scores.

**Task 3: Bilingual Lexicon Induction (BLI)** is a standard task to evaluate the “semantic quality” of static cross-lingual word embeddings (CLWEs) (Gouws et al., 2015; Ruder et al., 2019). We learn “BERT-based” CLWEs using a standard mapping-based approach (Mikolov et al., 2013a; Smith et al., 2017) with VECMAP (Artetxe et al., 2018). BLI evaluation allows us to investigate the “alignability” of monolingual type-level representations extracted for different languages. We adopt the standard BLI evaluation setup from Glavaš et al. (2019): 5K training word pairs are used to learn the mapping, and another 2K pairs as test data. We report standard Mean Reciprocal Rank (MRR) scores for 10 language pairs spanning EN, DE, RU, FI, TR.

**Task 4: Cross-Lingual Information Retrieval (CLIR).** We follow the setup of Litschko et al. (2018, 2019) and evaluate mapping-based CLWEs (the same ones as on BLI) in a document-level retrieval task on the CLEF 2003 benchmark.<sup>4</sup> We use a simple CLIR model which showed competitive performance in the comparative studies of Litschko et al. (2019) and Glavaš et al. (2019). It embeds queries and documents as IDF-weighted sums of their corresponding WEs from the CLWE space, and uses cosine similarity as the ranking function. We report Mean Average Precision (MAP) scores for 6 language pairs covering EN, DE, RU, FI.

**Task 5: Lexical Relation Prediction (RELP).** We probe if we can recover standard lexical relations (i.e., *synonymy*, *antonymy*, *hypernymy*, *meronymy*, plus *no relation*) from input type-level vectors. We rely on a state-of-the-art neural model

<sup>4</sup>All test collections comprise 60 queries. The average document collection size per language is 131K (ranging from 17K documents for RU to 295K for DE).

for RELP operating on type-level embeddings (Glavaš and Vulić, 2018): the Specialization Tensor Model (STM) predicts lexical relations for pairs of input word vectors based on multi-view projections of those vectors.<sup>5</sup> We use the WordNet-based (Fellbaum, 1998) evaluation data of Glavaš and Vulić (2018): they contain 10K annotated word pairs balanced by class. Micro-averaged  $F_1$  scores, averaged across 5 runs for each input vector space (default STM setting), are reported for EN and DE.

## 4 Results and Discussion

A summary of the results is shown in Figure 2 for LSIM, in Figure 3a for BLI, in Figure 3b for CLIR, in Figure 4a and Figure 4b for RELP, and in Figure 4c for WA. These results offer multiple axes of comparison, and the ensuing discussion focuses on the central questions Q1-Q3 posed in §1.<sup>6</sup>

**Monolingual versus Multilingual LMs.** Results across all tasks validate the intuition that language-specific monolingual LMs contain much more lexical information for a particular target language than massively multilingual models such as mBERT or XLM-R (Artetxe et al., 2020). We see large drops between MONO.\* and MULTI.\* configurations even for very high-resource languages (EN and DE), and they are even more prominent for FI and TR.

Encompassing 100+ training languages with limited model capacity, multilingual models suffer from the “curse of multilinguality” (Conneau et al., 2020): they must trade off monolingual lexical information coverage (and consequently monolingual performance) for a wider language coverage.<sup>7</sup>

**How Important is Context?** Another observation that holds across all configurations concerns the usefulness of providing contexts drawn from external corpora, and corroborates findings from prior work (Liu et al., 2019b): ISO configurations cannot match configurations that average subword embeddings from multiple contexts (AOC-10 and AOC-100). However, it is worth noting that **1**) perfor-

<sup>5</sup>Note that RELP is structurally different from the other four tasks: instead of direct computations with word embeddings, called *metric learning* or *similarity-based* evaluation (Ruder et al., 2019), it uses them as *features* in a neural architecture.

<sup>6</sup>Full results are available in the appendix.

<sup>7</sup>For a particular target language, monolingual performance can be partially recovered by additional in-language monolingual training via masked language modeling (Eisenschlos et al., 2019; Pfeiffer et al., 2020). In a side experiment, we have also verified that the same holds for lexical information coverage.

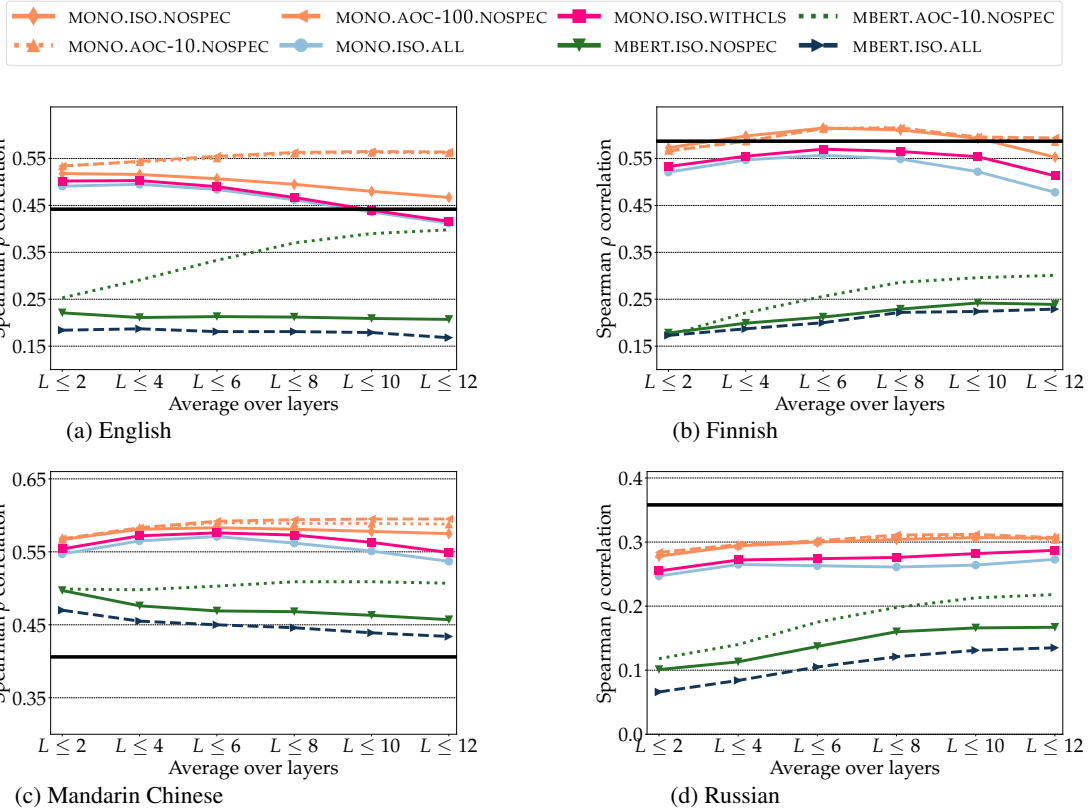


Figure 2: Spearman's  $\rho$  correlation scores for the lexical semantic similarity task (LSIM) in four languages. For the representation extraction configurations in the legend, see Table 1. Thick solid horizontal lines denote performance of standard monolingual fastText vectors trained on Wikipedia dumps of the respective languages.

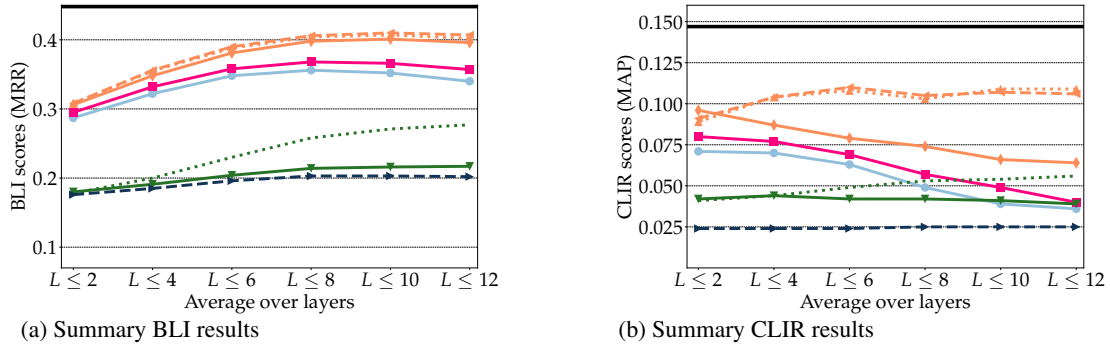


Figure 3: Summary results for the two cross-lingual evaluation tasks: (a) BLI (MRR scores) and (b) CLIR (MAP scores). We report average scores over all language pairs; individual results for each language pair are available in the appendix. Thick solid horizontal lines denote performance of standard fastText vectors in exactly the same cross-lingual mapping setup.

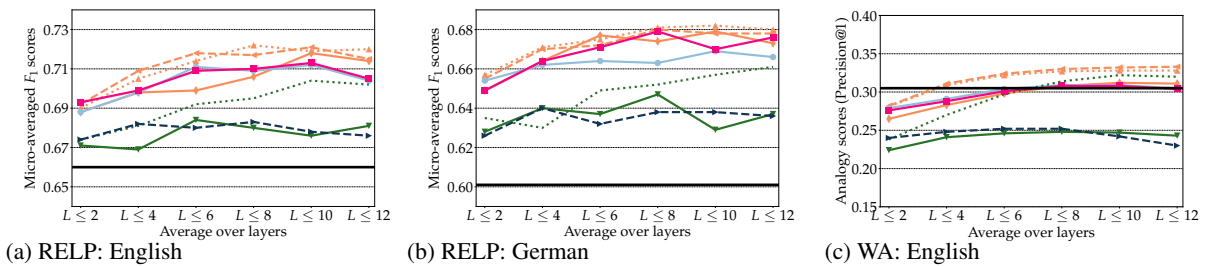


Figure 4: Micro-averaged  $F_1$  scores in the RELP task for (a) EN and (b) DE. The scores with 768-dim vectors randomly initialized via Xavier init (Glorot and Bengio, 2010) are 0.473 (EN) and 0.512 (DE); (c) EN WA results.

mance gains with AOC-100 over AOC-10, although consistent, are quite marginal across all tasks: this suggests that several word occurrences *in vivo* are already sufficient to accurately capture its type-level representation. 2) In some tasks, ISO configurations are only marginally outscored by their AOC counterparts: e.g., for MONO.\*.NOSPEC.AVG(L≤8) on EN-FI BLI or DE-TR BLI, the respective scores are 0.486 and 0.315 with ISO, and 0.503 and 0.334 with AOC-10. Similar observations hold for FI and ZH LSIM, and also in the RELP task.

In RELP, it is notable that ‘BERT-based’ embeddings can recover more lexical relation knowledge than standard FT vectors. These findings reveal that pretrained LMs indeed implicitly capture plenty of lexical type-level knowledge (which needs to be ‘recovered’ from the models); this also suggests why pretrained LMs have been successful in tasks where this knowledge is directly useful, such as NER and POS tagging (Tenney et al., 2019; Tsai et al., 2019). Finally, we also note that gains with AOC over ISO are much more pronounced for the under-performing MULTI.\* configurations: this indicates that MONO models store more lexical information even in absence of context.

**How Important are Special Tokens?** The results reveal that the inclusion of special tokens [CLS] and [SEP] into type-level embedding extraction deteriorates the final lexical information contained in the embeddings. This finding holds for different languages, underlying LMs, and averaging across various layers. The NOSPEC configurations consistently outperform their ALL and WITHCLS counterparts, both in ISO and AOC- $\{10, 100\}$  settings.<sup>8</sup>

Our finding at the lexical level aligns well with prior observations on using BERT directly as a sentence encoder (Qiao et al., 2019; Singh et al., 2019; Casanueva et al., 2020): while [CLS] is useful for sentence-pair classification tasks, using [CLS] as a sentence representation produces inferior representations than averaging over sentence’s subwords. In this work, we show that [CLS] and [SEP] should also be fully excluded from subword averaging for type-level word representations.

**How Important is Layer-wise Averaging?** Averaging across layers bottom-to-top (i.e., from  $L_0$  to  $L_{12}$ ) is beneficial across the board, but we notice that scores typically saturate or even decrease in some tasks and languages when we include

<sup>8</sup>For this reason, we report the results of AOC configurations only in the NOSPEC setting.

higher layers into averaging: see the scores with \*.AVG(L≤10) and \*.AVG(L≤12) configurations, e.g., for FI LSIM; EN/DE RELP, and summary BLI and CLIR scores. This hints to the fact that two strategies typically used in prior work, either to take the vectors only from the embedding layer  $L_0$  (Wu et al., 2020; Wang et al., 2019) or to average across all layers (Liu et al., 2019b), extract sub-optimal word representations for a wide range of setups and languages.

The sweet spot for  $n$  in \*.AVG(L≤ $n$ ) configurations seems largely task- and language-dependent, as peak scores are obtained with different  $n$ -s. Whereas *averaging across all layers* generally hurts performance, the results strongly suggest that averaging across layer subsets (rather than selecting a single layer) is widely useful, especially across bottom-most layers: e.g.,  $L \leq 6$  with MONO.ISO.NOSPEC yields an average score of 0.561 in LSIM, 0.076 in CLIR, and 0.432 in BLI; the respective scores when averaging over the 6 *top* layers are: 0.218, 0.008, and 0.230. This evidence implies that, although scattered across multiple layers, type-level lexical information seems to be concentrated in lower Transformer layers. We investigate these conjectures further in §4.1.

**Comparison to Static Word Embeddings.** The results also offer a comparison to static FT vectors across languages. The best-performing extraction configurations (e.g., MONO.AOC-100.NOSPEC) outperform FT in monolingual evaluations on LSIM (for EN, FI, ZH), WA, and they also display much stronger performance in the RELP task for both evaluation languages. While the comparison is not strictly apples-to-apples, as FT and LMs were trained on different (Wikipedia) corpora, these findings leave open a provocative question for future work: *Given that static type-level word representations can be recovered from large pretrained LMs, does this make standard static WEs obsolete, or are there applications where they are still useful?*

The trend is opposite in the two cross-lingual tasks: BLI and CLIR. While there are language pairs for which ‘BERT-based’ WEs outperform FT (i.e., EN-FI in BLI, EN-RU and FI-RU in CLIR) or are very competitive to FT’s performance (e.g., EN-TR, TR-BLI, DE-RU CLIR), FT provides higher scores overall in both tasks. The discrepancy between results in monolingual versus cross-lingual tasks warrants further investigation in future work. For instance, is using linear maps, as in stan-

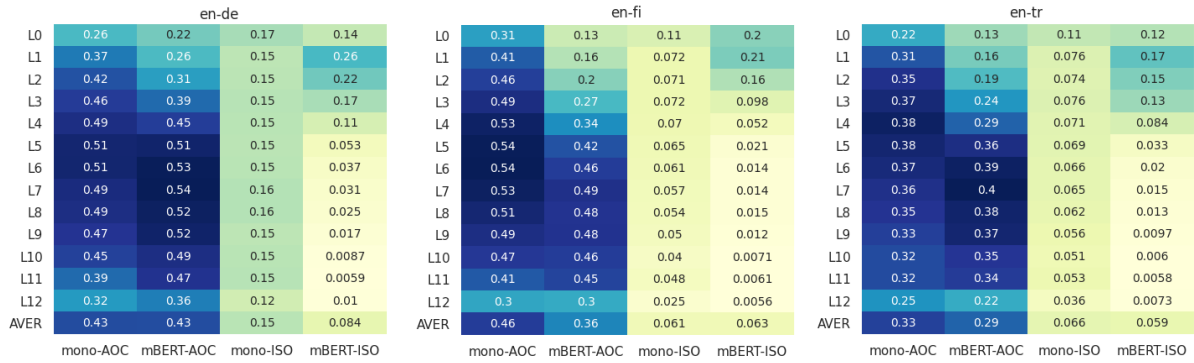


Figure 5: CKA similarity scores of type-level word representations extracted from each layer (using different extraction configurations, see Table 1) for a set of 7K translation pairs in EN-DE, EN-FI, and EN-TR from the BLI dictionaries of Glavaš et al. (2019). Additional heatmaps (where random words from two languages are paired) are available in the appendix.

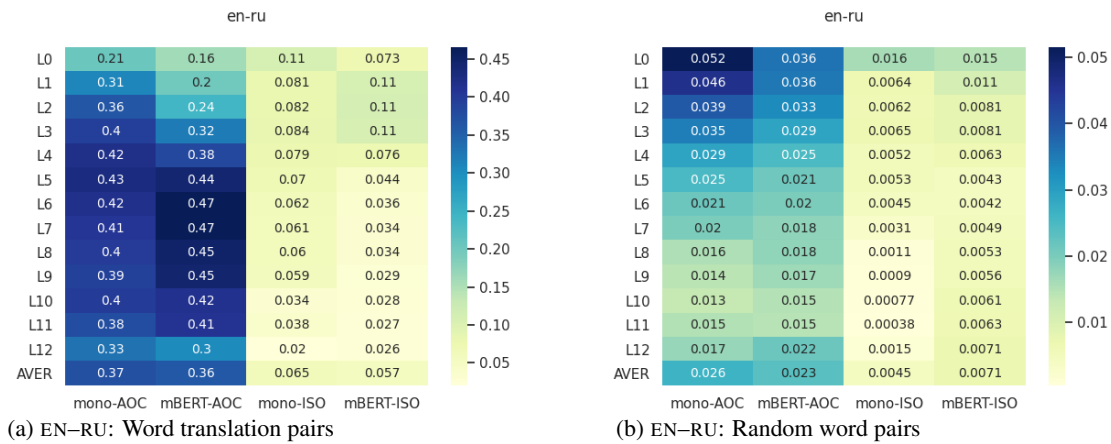


Figure 6: CKA similarity scores of type-level word representations extracted from each layer for a set of (a) 7K EN-RU translation pairs from the BLI dictionaries of Glavaš et al. (2019); (b) 7K random EN-RU pairs.

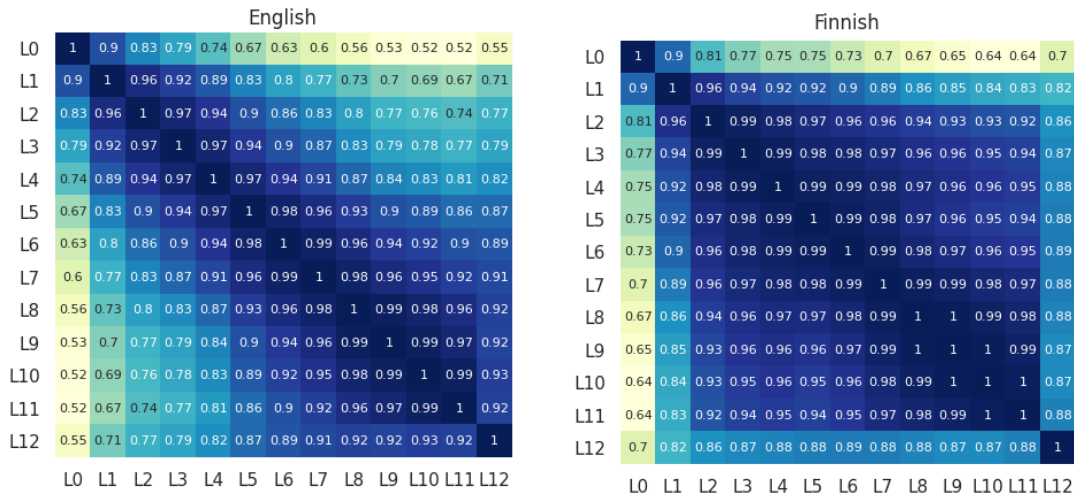


Figure 7: Self-similarity heatmaps: linear CKA similarity of representations for the same word extracted from different Transformer layers, averaged across 7K words for English and Finnish. MONO.AOC-100.NOSPEC.

standard mapping approaches to CLWE induction, sub-optimal for ‘BERT-based’ word vectors?

**Differences across Languages and Tasks.** Finally, while we observe a conspicuous amount of

universal patterns with configuration components (e.g., MONO > MULTI; AOC > ISO; NOSPEC > ALL, WITHCLS), best-performing configurations do show some variation across different languages and

		$L_0$	$L_1$	$L_2$	$L_3$	$L_4$	$L_5$	$L_6$	$L_7$	$L_8$	$L_9$	$L_{10}$	$L_{11}$	$L_{12}$
LSIM	EN	.503	<b>.513</b>	.505	.510	.505	.484	.459	.435	.402	.361	.362	.372	.390
	FI	.445	<b>.466</b>	.445	.436	.430	.434	.421	.404	.374	.346	.333	.324	.286
WA	EN	.220	.272	<b>.293</b>	.285	<b>.293</b>	.261	.240	.217	.199	.171	.189	.221	.229
BLI	EN-DE	.310	.354	.379	<b>.400</b>	.394	.393	.373	.358	.311	.272	.273	.264	.287
	EN-FI	.309	.339	.360	.367	<b>.369</b>	.345	.329	.303	.279	.252	.231	.194	.192
	DE-FI	.211	.245	.268	.283	.289	<b>.303</b>	.291	.292	.288	.282	.262	.219	.236
CLIR	EN-DE	.059	<b>.060</b>	.059	<b>.060</b>	.043	.036	.036	.036	.027	.024	.027	.035	.038
	EN-FI	.038	<b>.040</b>	.022	.018	.011	.008	.006	.006	.005	.002	.003	.002	.007
	DE-FI	.054	<b>.057</b>	.028	.015	.016	.022	.017	.021	.020	.023	.015	.008	.030

Table 2: Task performance of word representations extracted from different Transformer layers for a selection of tasks, languages, and language pairs. Configuration: MONO.AOC-100.NOSPEC. Highest scores per row are in bold.

tasks. For instance, while EN LSIM performance declines modestly but steadily when averaging over higher-level layers ( $\text{AVG}(L \leq n)$ , where  $n > 4$ ), performance on EN WA consistently increases for the same configurations. The BLI and CLIR scores in Figures 3a and 3b also show slightly different patterns across layers. Overall, this suggests that **1**) extracted lexical information must be guided by task requirements, and **2**) config components must be carefully tuned to maximise performance for a particular task–language combination.

#### 4.1 Lexical Information in Individual Layers

**Evaluation Setup.** To better understand which layers contribute the most to the final performance in our lexical tasks, we also probe type-level representations emerging from each individual layer of pre-trained LMs. For brevity, we focus on the best performing configurations from previous experiments: {MONO, MBERT}. {ISO, AOC-100}.NOSPEC.

In addition, tackling Q4 from §1, we analyse the similarity of representations extracted from monolingual and multilingual BERT models using the centered kernel alignment (CKA) as proposed by (Kornblith et al., 2019). The linear CKA computes similarity that is invariant to isotropic scaling and orthogonal transformation. It is defined as

$$\text{CKA}(X, Y) = \frac{\|Y^\top X\|_F^2}{(\|X^\top X\|_F \|Y^\top Y\|_F)}. \quad (1)$$

$X, Y \in \mathbb{R}^{s \times d}$  are input matrices spanning  $s$   $\ell_2$ -normalized and mean-centered examples of dimensionality  $d = 768$ . We use CKA in two different experiments: **1**) measuring *self-similarity* where we compute CKA similarity of representations extracted from different layers for the same word; and **2**) measuring *bilingual layer correspondence* where we compute CKA similarity of representa-

tions extracted from the same layer for two words constituting a translation pair. To this end, we again use BLI dictionaries of Glavaš et al. (2019) (see §3) covering 7K pairs (training + test pairs).

**Discussion.** Per-layer CKA similarities are provided in Figure 7 (self-similarity) and Figure 5 (bilingual), and we show results of representations extracted from individual layers for selected evaluation setups and languages in Table 2. We also plot bilingual layer correspondence of true word translations versus randomly paired words for EN–RU in Figure 6. Figure 7 reveals very similar patterns for both EN and FI, and we also observe that self-similarity scores decrease for more distant layers (cf., similarity of  $L_1$  and  $L_2$  versus  $L_1$  and  $L_{12}$ ). However, despite structural similarities identified by linear CKA, the scores from Table 2 demonstrate that structurally similar layers might encode different amounts of lexical information: e.g., compare performance drops between  $L_5$  and  $L_8$  in all evaluation tasks.

The results in Table 2 further suggest that more type-level lexical information is available in lower layers, as all peak scores in the table are achieved with representations extracted from layers  $L_1 - L_5$ . Much lower scores in type-level semantic tasks for higher layers also empirically validate a recent hypothesis of Ethayarajh (2019) “that contextualised word representations are more context-specific in higher layers.” We also note that none of the results with  $L=n$  configurations from Table 1 can match best performing  $\text{AVG}(L \leq n)$  configurations with layer-wise averaging. This confirms our hypothesis that type-level lexical knowledge, although predominantly captured by lower layers, is disseminated across multiple layers, and layer-wise averaging is crucial to uncover that knowledge.

Further, Figure 5 and Figure 6 reveal that even



LMs trained on monolingual data learn similar representations in corresponding layers for word translations (see the MONO.AOC columns). Intuitively, this similarity is much more pronounced with AOC configurations with mBERT. The comparison of scores in Figure 6 also reveals much higher correspondence scores for true translation pairs than for randomly paired words (i.e., the correspondence scores for random pairings are, as expected, random). Moreover, MULTI CKA similarity scores turn out to be higher for more similar language pairs (cf. EN–DE versus EN–TR MULTI.AOC columns). This suggests that, similar to static WEs, type-level ‘BERT-based’ WEs of different languages also display topological similarity, often termed *approximate isomorphism* (Søgaard et al., 2018), but its degree depends on language proximity. This also clarifies why representations extracted from two independently trained monolingual LMs can be linearly aligned, as validated by BLI and CLIR evaluation (Table 2 and Figure 3).<sup>9</sup>

We also calculated the Spearman’s correlation between CKA similarity scores for configurations MONO.AOC-100.NOSPEC.AVG( $L \leq n$ ), for all  $n = 0, \dots, 12$ , and their corresponding BLI scores on EN–FI, EN–DE, and DE–FI. The correlations are very high:  $\rho = 1.0, 0.83, 0.99$ , respectively. This further confirms the approximate isomorphism hypothesis: it seems that higher structural similarities of representations extracted from monolingual pretrained LMs facilitate their cross-lingual alignment.

## 5 Further Discussion and Conclusion

**What about Larger LMs and Corpora?** Aspects of LM pretraining, such as the number of model parameters or the size of pretraining data, also impact lexical knowledge stored in the LM’s parameters. Our preliminary experiments have verified that EN BERT-Large yields slight gains over the EN BERT-Base architecture used in our work (e.g., peak EN LSIM scores rise from 0.518 to 0.531). In a similar vein, we have run additional experiments with two available Italian (IT) BERT-Base models with identical parameter setups, where one was trained

<sup>9</sup>Previous work has empirically validated that sentence representations for semantically similar inputs from different languages are less similar in higher Transformer layers (Singh et al., 2019; Wu and Dredze, 2019). In Figure 5, we demonstrate that this is also the case for type-level lexical information; however, unlike sentence representations where highest similarity is reported in lowest layers, Figure 5 suggests that highest CKA similarities are achieved in intermediate layers  $L_5$ – $L_8$ .

on 13GB of IT text, and the other on 81GB. In EN (BERT-Base)–IT BLI and CLIR evaluations we measure improvements from 0.548 to 0.572 (BLI), and from 0.148 to 0.160 (CLIR) with the 81GB IT model. In-depth analyses of these factors are out of the scope of this work, but they warrant further investigations.

**Opening Future Research Avenues.** Our study has empirically validated that (monolingually) pretrained LMs store a wealth of type-level lexical knowledge, but effectively uncovering and extracting such knowledge from the LMs’ parameters depends on several crucial components (see §2). In particular, some universal choices of configuration can be recommended: i) choosing monolingual LMs; ii) encoding words with multiple contexts; iii) excluding special tokens; iv) averaging over lower layers. Moreover, we found that type-level WEs extracted from pretrained LMs can surpass static WEs like fastText (Bojanowski et al., 2017).

This study has only scratched the surface of this research avenue. In future work, we plan to investigate how domains of external corpora affect AOC configurations, and how to sample representative contexts from the corpora. We will also extend the study to more languages, more lexical semantic probes, and other larger underlying LMs. The difference in performance across layers also calls for more sophisticated lexical representation extraction methods (e.g., through layer weighting or attention) similar to meta-embedding approaches (Yin and Schütze, 2016; Bollegala and Bao, 2018; Kiela et al., 2018). Given the current large gaps between monolingual and multilingual LMs, we will also focus on lightweight methods to enrich lexical content in multilingual LMs (Wang et al., 2020; Pfeiffer et al., 2020).

## Acknowledgments

This work is supported by the ERC Consolidator Grant LEXICAL: Lexical Acquisition Across Languages (no 648909) awarded to Anna Korhonen. The work of Goran Glavaš and Robert Litschko is supported by the Baden-Württemberg Stiftung (AGREE grant of the Eliteprogramm).

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## A Appendix

URLs to the models and external corpora used in our study are provided in Table 3 and Table 4, respectively. URLs to the evaluation data and task architectures for each evaluation task are provided in Table 5. We also report additional and more detailed sets of results across different tasks, word embedding extraction configurations/variants, and language pairs:

- In Table 6 and Table 7, we provide full BLI results per language pair. All scores are Mean Reciprocal Rank (MRR) scores (in the standard scoring interval, 0.0–1.0).
- In Table 8, we provide full CLIR results per language pair. All scores are Mean Average Precision (MAP) scores (in the standard scoring interval, 0.0–1.0).
- In Table 9, we provide full relation prediction (RELP) results for EN and DE. All scores are micro-averaged  $F_1$  scores over 5 runs of the relation predictor (Glavaš and Vulić, 2018). We also report standard deviation for each configuration.

Finally, in Figures 8-10, we also provide heatmaps denoting bilingual layer correspondence, computed via linear CKA similarity (Kornblith et al., 2019), for several EN- $L_t$  language pairs (see §4.1), which are not provided in the main paper

Language	URL
EN	<a href="https://huggingface.co/bert-base-uncased">https://huggingface.co/bert-base-uncased</a>
DE	<a href="https://huggingface.co/bert-base-german-dbmdz-uncased">https://huggingface.co/bert-base-german-dbmdz-uncased</a>
RU	<a href="https://huggingface.co/DeepPavlov/rubert-base-cased">https://huggingface.co/DeepPavlov/rubert-base-cased</a>
FI	<a href="https://huggingface.co/TurkuNLP/bert-base-finnish-uncased-v1">https://huggingface.co/TurkuNLP/bert-base-finnish-uncased-v1</a>
ZH	<a href="https://huggingface.co/bert-base-chinese">https://huggingface.co/bert-base-chinese</a>
TR	<a href="https://huggingface.co/dbmdz/bert-base-turkish-uncased">https://huggingface.co/dbmdz/bert-base-turkish-uncased</a>
Multilingual	<a href="https://huggingface.co/bert-base-multilingual-uncased">https://huggingface.co/bert-base-multilingual-uncased</a>
IT	<a href="https://huggingface.co/dbmdz/bert-base-italian-uncased">https://huggingface.co/dbmdz/bert-base-italian-uncased</a> <a href="https://huggingface.co/dbmdz/bert-base-italian-xxl-uncased">https://huggingface.co/dbmdz/bert-base-italian-xxl-uncased</a>

Table 3: URLs of the models used in our study. The first part of the table refers to the models used in the main experiments throughout the paper, while the second part refers to the models used in side experiments.

Language	URL
EN	<a href="http://opus.nlpl.eu/download.php?f=Europarl/v8/moses/de-en.txt.zip">http://opus.nlpl.eu/download.php?f=Europarl/v8/moses/de-en.txt.zip</a>
DE	<a href="http://opus.nlpl.eu/download.php?f=Europarl/v8/moses/de-en.txt.zip">http://opus.nlpl.eu/download.php?f=Europarl/v8/moses/de-en.txt.zip</a>
RU	<a href="http://opus.nlpl.eu/download.php?f=UNPC/v1.0/moses/en-ru.txt.zip">http://opus.nlpl.eu/download.php?f=UNPC/v1.0/moses/en-ru.txt.zip</a>
FI	<a href="http://opus.nlpl.eu/download.php?f=Europarl/v8/moses/en-fi.txt.zip">http://opus.nlpl.eu/download.php?f=Europarl/v8/moses/en-fi.txt.zip</a>
ZH	<a href="http://opus.nlpl.eu/download.php?f=UNPC/v1.0/moses/en-zh.txt.zip">http://opus.nlpl.eu/download.php?f=UNPC/v1.0/moses/en-zh.txt.zip</a>
TR	<a href="http://data.statmt.org/wmt18/translation-task/news.2017.tr.shuffled.deduped.gz">http://data.statmt.org/wmt18/translation-task/news.2017.tr.shuffled.deduped.gz</a>
IT	<a href="http://opus.nlpl.eu/download.php?f=Europarl/v8/moses/en-it.txt.zip">http://opus.nlpl.eu/download.php?f=Europarl/v8/moses/en-it.txt.zip</a>

Table 4: Links to the external corpora used in the study. We randomly sample 1M sentences of maximum sequence length 512 from the corresponding corpora.

Task	Evaluation Data and/or Model	Link
LSIM	Multi-SimLex	Data: <a href="http://multisimlex.com/">multisimlex.com/</a>
WA	BATS	Data: <a href="https://vectorspace.com/projects/BATS/">vecto.space/projects/BATS/</a>
BLI	Data: Dictionaries from <a href="#">Glavaš et al. (2019)</a> Model: VecMap	Data: <a href="https://github.com/codogogo/xling-eval/tree/master/bli_datasets">github.com/codogogo/xling-eval/tree/master/bli_datasets</a> Model: <a href="https://github.com/artetxem/vecmap">github.com/artetxem/vecmap</a>
CLIR	Data: CLEF 2003 Model: Agg-IDF from <a href="#">Litschko et al. (2019)</a>	Data: <a href="https://catalog.elra.info/en-us/repository/browse/ELRA-E0008/">catalog.elra.info/en-us/repository/browse/ELRA-E0008/</a> Model: <a href="https://github.com/rllitschk/UnsupCLIR">github.com/rllitschk/UnsupCLIR</a>
RELP	Data: WordNet-based RELP data Model: Specialization Tensor Model	Data: <a href="https://github.com/codogogo/stm/tree/master/data/wn-ls">github.com/codogogo/stm/tree/master/data/wn-ls</a> Model: <a href="https://github.com/codogogo/stm">github.com/codogogo/stm</a>

Table 5: Links to evaluation data and models.

<b>Configuration</b>	EN-DE	EN-TR	EN-FI	EN-RU	DE-TR	DE-FI	DE-RU
FASTTEXT.WIKI	0.610	0.433	0.488	0.522	0.358	0.435	0.469
<b>MONO.ISO.NOSPEC</b>							
AVG(L≤2)	0.390	0.332	0.392	0.409	0.237	0.269	0.291
AVG(L≤4)	0.430	0.367	0.438	0.447	0.269	0.311	0.338
AVG(L≤6)	0.461	0.386	0.476	0.472	0.299	0.359	0.387
AVG(L≤8)	0.472	0.390	0.486	0.487	0.315	0.387	0.407
AVG(L≤10)	0.461	0.386	0.483	0.488	0.321	0.395	0.416
AVG(L≤12)	0.446	0.379	0.471	0.473	0.323	0.395	0.412
<b>MONO.AOC-10.NOSPEC</b>							
AVG(L≤2)	0.399	0.342	0.386	0.403	0.242	0.269	0.292
AVG(L≤4)	0.457	0.379	0.448	0.433	0.283	0.322	0.343
AVG(L≤6)	0.503	0.399	0.480	0.458	0.315	0.369	0.380
AVG(L≤8)	0.527	0.414	0.499	0.461	0.332	0.394	0.391
AVG(L≤10)	0.534	0.415	0.498	0.459	0.337	0.401	0.394
AVG(L≤12)	0.534	0.416	0.492	0.453	0.337	0.401	0.376
<b>MONO.AOC-100.NOSPEC</b>							
AVG(L≤2)	0.401	0.343	0.391	0.398	0.239	0.269	0.293
AVG(L≤4)	0.459	0.381	0.449	0.437	0.288	0.325	0.343
AVG(L≤6)	0.504	0.403	0.484	0.459	0.318	0.373	0.382
AVG(L≤8)	0.532	0.418	0.503	0.462	0.334	0.394	0.389
AVG(L≤10)	0.540	0.422	0.504	0.459	0.338	0.402	0.393
AVG(L≤12)	0.542	0.426	0.500	0.454	0.343	0.401	0.378
<b>MONO.ISO.ALL</b>							
AVG(L≤2)	0.352	0.289	0.351	0.374	0.230	0.265	0.283
AVG(L≤4)	0.375	0.317	0.391	0.393	0.264	0.302	0.331
AVG(L≤6)	0.386	0.330	0.406	0.407	0.289	0.350	0.376
AVG(L≤8)	0.372	0.327	0.409	0.413	0.291	0.370	0.392
AVG(L≤10)	0.352	0.320	0.396	0.402	0.290	0.370	0.383
AVG(L≤12)	0.313	0.310	0.373	0.394	0.283	0.358	0.371
<b>MONO.ISO.WITHCLS</b>							
AVG(L≤2)	0.367	0.306	0.368	0.386	0.236	0.272	0.285
AVG(L≤4)	0.394	0.339	0.408	0.410	0.267	0.307	0.331
AVG(L≤6)	0.406	0.344	0.428	0.425	0.294	0.353	0.381
AVG(L≤8)	0.393	0.344	0.430	0.431	0.306	0.369	0.400
AVG(L≤10)	0.371	0.336	0.421	0.421	0.303	0.382	0.395
AVG(L≤12)	0.331	0.329	0.403	0.409	0.302	0.375	0.387
<b>MULTI.ISO.NOSPEC</b>							
AVG(L≤2)	0.293	0.176	0.176	0.147	0.216	0.203	0.160
AVG(L≤4)	0.304	0.184	0.190	0.164	0.219	0.214	0.178
AVG(L≤6)	0.315	0.189	0.203	0.198	0.223	0.225	0.198
AVG(L≤8)	0.325	0.193	0.209	0.228	0.224	0.235	0.217
AVG(L≤10)	0.330	0.194	0.210	0.243	0.220	0.234	0.226
AVG(L≤12)	0.333	0.193	0.206	0.248	0.219	0.231	0.227
<b>MULTI.AOC-10.NOSPEC</b>							
AVG(L≤2)	0.309	0.171	0.172	0.146	0.208	0.200	0.156
AVG(L≤4)	0.350	0.186	0.189	0.186	0.224	0.214	0.191
AVG(L≤6)	0.389	0.219	0.215	0.240	0.241	0.243	0.225
AVG(L≤8)	0.432	0.246	0.251	0.287	0.255	0.263	0.254
AVG(L≤10)	0.448	0.258	0.264	0.306	0.260	0.282	0.272
AVG(L≤12)	0.456	0.267	0.272	0.316	0.260	0.292	0.284
<b>MULTI.ISO.ALL</b>							
AVG(L≤2)	0.292	0.173	0.175	0.143	0.209	0.203	0.154
AVG(L≤4)	0.301	0.176	0.188	0.155	0.211	0.213	0.171
AVG(L≤6)	0.307	0.181	0.198	0.186	0.216	0.221	0.193
AVG(L≤8)	0.315	0.184	0.202	0.207	0.213	0.228	0.208
AVG(L≤10)	0.318	0.182	0.197	0.216	0.208	0.226	0.215
AVG(L≤12)	0.319	0.181	0.189	0.220	0.209	0.220	0.213
<b>MONO.ISO.NOSPEC (REVERSE)</b>							
AVG(L≥12)	0.104	–	0.054	–	–	0.077	–
AVG(L≥10)	0.119	–	0.061	–	–	0.063	–
AVG(L≥8)	0.144	–	0.108	–	–	0.095	–
AVG(L≥6)	0.230	–	0.223	–	–	0.238	–
AVG(L≥4)	0.308	–	0.318	–	–	0.335	–
AVG(L≥2)	0.365	–	0.385	–	–	0.372	–
AVG(L≥0)	0.446	–	0.471	–	–	0.395	–

Table 6: Results in the BLI task across different language pairs and word vector extraction configurations. MRR scores reported. For clarity of presentation, a subset of results is presented in this table, while the rest (and the averages) are presented in Table 7.  $AVG(L \leq n)$  means that we average representations over all Transformer layers up to the  $n$ th layer (included), where  $L = 0$  refers to the embedding layer,  $L = 1$  to the bottom layer, and  $L = 12$  to the final (top) layer. Different configurations are described in §2 and Table 1. Additional diagnostic experiments with top-to-bottom layerwise averaging configs (REVERSE) are run for a subset of languages:  $\{EN, DE, FI\}$ .

<b>Configuration</b>	TR-FI	TR-RU	FI-RU	average
FASTTEXT.WIKI	0.358	0.364	0.439	0.448
<b>MONO.ISO.NOSPEC</b>				
AVG(L≤2)	0.237	0.217	0.290	0.306
AVG(L≤4)	0.279	0.261	0.337	0.348
AVG(L≤6)	0.311	0.288	0.372	0.381
AVG(L≤8)	0.334	0.315	0.387	0.398
AVG(L≤10)	0.347	0.317	0.392	0.401
AVG(L≤12)	0.352	0.319	0.387	0.396
<b>MONO.AOC-10.NOSPEC</b>				
AVG(L≤2)	0.247	0.221	0.284	0.308
AVG(L≤4)	0.288	0.263	0.331	0.355
AVG(L≤6)	0.319	0.294	0.366	0.388
AVG(L≤8)	0.334	0.311	0.375	0.404
AVG(L≤10)	0.340	0.311	0.379	0.407
AVG(L≤12)	0.344	0.310	0.360	0.402
<b>MONO.AOC-100.NOSPEC</b>				
AVG(L≤2)	0.244	0.220	0.285	0.308
AVG(L≤4)	0.288	0.261	0.333	0.356
AVG(L≤6)	0.322	0.291	0.367	0.390
AVG(L≤8)	0.338	0.309	0.376	0.406
AVG(L≤10)	0.348	0.314	0.377	0.410
AVG(L≤12)	0.349	0.311	0.361	0.407
<b>MONO.ISO.ALL</b>				
AVG(L≤2)	0.226	0.212	0.284	0.287
AVG(L≤4)	0.270	0.254	0.328	0.322
AVG(L≤6)	0.302	0.274	0.358	0.348
AVG(L≤8)	0.318	0.296	0.371	0.356
AVG(L≤10)	0.328	0.303	0.373	0.352
AVG(L≤12)	0.328	0.306	0.368	0.340
<b>MONO.ISO.WITHCLS</b>				
AVG(L≤2)	0.232	0.217	0.285	0.295
AVG(L≤4)	0.274	0.257	0.331	0.332
AVG(L≤6)	0.307	0.279	0.362	0.358
AVG(L≤8)	0.327	0.303	0.377	0.368
AVG(L≤10)	0.334	0.314	0.383	0.366
AVG(L≤12)	0.340	0.317	0.373	0.357
<b>MULTI.ISO.NOSPEC</b>				
AVG(L≤2)	0.170	0.131	0.127	0.180
AVG(L≤4)	0.180	0.135	0.138	0.191
AVG(L≤6)	0.188	0.147	0.151	0.204
AVG(L≤8)	0.189	0.152	0.164	0.214
AVG(L≤10)	0.188	0.153	0.165	0.216
AVG(L≤12)	0.188	0.158	0.163	0.217
<b>MULTI.AOC-10.NOSPEC</b>				
AVG(L≤2)	0.165	0.127	0.130	0.178
AVG(L≤4)	0.176	0.146	0.139	0.200
AVG(L≤6)	0.192	0.174	0.162	0.230
AVG(L≤8)	0.210	0.192	0.185	0.258
AVG(L≤10)	0.219	0.198	0.200	0.271
AVG(L≤12)	0.223	0.198	0.206	0.277
<b>MULTI.ISO.ALL</b>				
AVG(L≤2)	0.163	0.126	0.123	0.176
AVG(L≤4)	0.175	0.128	0.133	0.185
AVG(L≤6)	0.179	0.139	0.142	0.196
AVG(L≤8)	0.182	0.144	0.152	0.203
AVG(L≤10)	0.178	0.141	0.153	0.203
AVG(L≤12)	0.175	0.143	0.150	0.202

Table 7: Results in the bilingual lexicon induction (BLI) task across different language pairs and word vector extraction configurations: Part II. MAP scores reported. For clarity of presentation, a subset of results is presented in this table, while the rest (also used to calculate the averages) is provided in Table 6 in the previous page.  $AVG(L \leq n)$  means that we average representations over all Transformer layers up to the  $n$ th layer (included), where  $L = 0$  refers to the embedding layer,  $L = 1$  to the bottom layer, and  $L = 12$  to the final (top) layer. Different configurations are described in §2 and Table 1.



Configuration	EN-DE	EN-FI	EN-RU	DE-FI	DE-RU	FI-RU	average
FASTTEXT.WIKI	<b>0.193</b>	<b>0.136</b>	0.118	<b>0.221</b>	<b>0.112</b>	0.105	<b>0.148</b>
MONO.ISO.NOSPEC							
AVG( $L \leq 2$ )	0.059	0.075	0.106	0.126	0.086	0.123	0.096
AVG( $L \leq 4$ )	0.061	0.069	0.098	0.111	0.075	0.106	0.087
AVG( $L \leq 6$ )	0.052	0.061	0.079	0.112	0.068	0.102	0.079
AVG( $L \leq 8$ )	0.042	0.048	0.075	0.112	0.063	0.105	0.074
AVG( $L \leq 10$ )	0.036	0.043	0.067	0.107	0.065	0.080	0.066
AVG( $L \leq 12$ )	0.032	0.034	0.059	0.097	0.077	0.083	0.064
MONO.AOC-10.NOSPEC							
AVG( $L \leq 2$ )	0.069	0.078	0.094	0.109	0.078	0.108	0.089
AVG( $L \leq 4$ )	0.076	0.105	0.119	0.112	0.098	0.117	0.104
AVG( $L \leq 6$ )	0.086	0.090	0.129	0.122	0.098	0.125	0.108
AVG( $L \leq 8$ )	0.092	0.073	0.137	0.105	0.100	0.114	0.103
AVG( $L \leq 10$ )	0.095	0.073	0.147	0.102	0.102	0.135	0.109
AVG( $L \leq 12$ )	0.104	0.073	0.139	0.100	0.105	0.131	0.109
MONO.AOC-100.NOSPEC							
AVG( $L \leq 2$ )	0.073	0.081	0.097	0.111	0.078	0.106	0.091
AVG( $L \leq 4$ )	0.078	0.107	0.115	0.107	0.100	0.115	0.104
AVG( $L \leq 6$ )	0.087	0.087	0.127	0.132	0.103	<b>0.123</b>	0.110
AVG( $L \leq 8$ )	0.091	0.076	0.137	0.118	0.101	0.106	0.105
AVG( $L \leq 10$ )	0.099	0.074	<b>0.161</b>	0.103	0.104	0.104	0.107
AVG( $L \leq 12$ )	0.106	0.076	0.146	0.105	0.106	0.100	0.106
MONO.ISO.ALL							
AVG( $L \leq 2$ )	0.044	0.045	0.076	0.095	0.067	0.098	0.071
AVG( $L \leq 4$ )	0.039	0.042	0.079	0.094	0.066	0.100	0.070
AVG( $L \leq 6$ )	0.024	0.034	0.069	0.089	0.066	0.094	0.063
AVG( $L \leq 8$ )	0.018	0.020	0.039	0.068	0.059	0.092	0.049
AVG( $L \leq 10$ )	0.016	0.016	0.030	0.048	0.058	0.067	0.039
AVG( $L \leq 12$ )	0.014	0.013	0.033	0.034	0.064	0.061	0.036
MONO.ISO.WITHCLS							
AVG( $L \leq 2$ )	0.050	0.057	0.086	0.106	0.071	0.108	0.080
AVG( $L \leq 4$ )	0.046	0.055	0.084	0.104	0.071	0.102	0.077
AVG( $L \leq 6$ )	0.032	0.042	0.076	0.103	0.066	0.097	0.069
AVG( $L \leq 8$ )	0.025	0.028	0.046	0.086	0.059	0.101	0.057
AVG( $L \leq 10$ )	0.021	0.030	0.037	0.072	0.057	0.079	0.049
AVG( $L \leq 12$ )	0.020	0.016	0.032	0.052	0.045	0.072	0.040
MULTI.ISO.NOSPEC							
AVG( $L \leq 2$ )	0.110	0.009	0.045	0.057	0.020	0.013	0.042
AVG( $L \leq 4$ )	0.100	0.007	0.075	0.044	0.025	0.011	0.044
AVG( $L \leq 6$ )	0.098	0.007	0.046	0.043	0.029	0.030	0.042
AVG( $L \leq 8$ )	0.088	0.008	0.052	0.043	0.032	0.031	0.042
AVG( $L \leq 10$ )	0.084	0.008	0.051	0.042	0.034	0.026	0.041
AVG( $L \leq 12$ )	0.082	0.006	0.048	0.039	0.037	0.024	0.039
MULTI.AOC-10.NOSPEC							
AVG( $L \leq 2$ )	0.127	0.013	0.049	0.027	0.019	0.009	0.041
AVG( $L \leq 4$ )	0.123	0.018	0.055	0.032	0.029	0.008	0.044
AVG( $L \leq 6$ )	0.120	0.018	0.055	0.051	0.042	0.009	0.049
AVG( $L \leq 8$ )	0.123	0.018	0.057	0.053	0.049	0.016	0.053
AVG( $L \leq 10$ )	0.127	0.019	0.062	0.050	0.051	0.018	0.054
AVG( $L \leq 12$ )	0.128	0.021	0.065	0.049	0.052	0.019	0.056
MULTI.ISO.ALL							
AVG( $L \leq 2$ )	0.072	0.005	0.032	0.014	0.016	0.004	0.024
AVG( $L \leq 4$ )	0.075	0.004	0.027	0.014	0.022	0.005	0.024
AVG( $L \leq 6$ )	0.065	0.004	0.026	0.015	0.027	0.007	0.024
AVG( $L \leq 8$ )	0.054	0.004	0.035	0.015	0.032	0.008	0.025
AVG( $L \leq 10$ )	0.054	0.005	0.032	0.017	0.035	0.007	0.025
AVG( $L \leq 12$ )	0.058	0.004	0.034	0.018	0.032	0.006	0.025
MONO.ISO.NOSPEC (REVERSE)							
AVG( $L \geq 12$ )	0.005	0.012	–	0.001	–	–	–
AVG( $L \geq 10$ )	0.002	0.002	–	0.001	–	–	–
AVG( $L \geq 8$ )	0.004	0.002	–	0.002	–	–	–
AVG( $L \geq 6$ )	0.014	0.006	–	0.004	–	–	–
AVG( $L \geq 4$ )	0.020	0.012	–	0.016	–	–	–
AVG( $L \geq 2$ )	0.024	0.019	–	0.043	–	–	–
AVG( $L \geq 0$ )	0.032	0.034	–	0.097	–	–	–

Table 8: Results in the CLIR task across different language pairs and word vector extraction configurations. MAP scores reported;  $AVG(L \leq n)$  means that we average representations over all Transformer layers up to the  $n$ th layer (included), where  $L = 0$  refers to the embedding layer,  $L = 1$  to the bottom layer, and  $L = 12$  to the final (top) layer. Different configurations are described in §2 and Table 1. Additional diagnostic experiments with top-to-bottom layerwise averaging configs (REVERSE) are run for a subset of languages: {EN, DE, FI}.

Configuration	EN	DE
FASTTEXT.WIKI	0.660 $\pm$ 0.008	0.601 $\pm$ 0.007
RANDOM.XAVIER	0.473 $\pm$ 0.003	0.512 $\pm$ 0.008
<b>MONO.ISO.NOSPEC</b>		
AVG(L $\leq$ 2)	0.688 $\pm$ 0.007	0.649 $\pm$ 0.002
AVG(L $\leq$ 4)	0.698 $\pm$ 0.002	0.664 $\pm$ 0.004
AVG(L $\leq$ 6)	0.699 $\pm$ 0.007	0.677 $\pm$ 0.006
AVG(L $\leq$ 8)	0.706 $\pm$ 0.003	0.674 $\pm$ 0.016
AVG(L $\leq$ 10)	0.718 $\pm$ 0.002	0.679 $\pm$ 0.008
AVG(L $\leq$ 12)	0.714 $\pm$ 0.012	0.673 $\pm$ 0.003
<b>MONO.AOC-10.NOSPEC</b>		
AVG(L $\leq$ 2)	0.690 $\pm$ 0.007	0.657 $\pm$ 0.005
AVG(L $\leq$ 4)	0.705 $\pm$ 0.006	0.671 $\pm$ 0.009
AVG(L $\leq$ 6)	0.714 $\pm$ 0.008	0.675 $\pm$ 0.014
AVG(L $\leq$ 8)	0.722 $\pm$ 0.004	0.681 $\pm$ 0.010
AVG(L $\leq$ 10)	0.719 $\pm$ 0.007	0.682 $\pm$ 0.007
AVG(L $\leq$ 12)	0.720 $\pm$ 0.005	0.680 $\pm$ 0.007
<b>MONO.AOC-100.NOSPEC</b>		
AVG(L $\leq$ 2)	0.692 $\pm$ 0.007	0.655 $\pm$ 0.007
AVG(L $\leq$ 4)	0.709 $\pm$ 0.007	0.670 $\pm$ 0.005
AVG(L $\leq$ 6)	0.718 $\pm$ 0.009	0.672 $\pm$ 0.008
AVG(L $\leq$ 8)	0.717 $\pm$ 0.003	0.680 $\pm$ 0.006
AVG(L $\leq$ 10)	0.721 $\pm$ 0.009	0.678 $\pm$ 0.004
AVG(L $\leq$ 12)	0.715 $\pm$ 0.003	0.678 $\pm$ 0.006
<b>MONO.ISO.ALL</b>		
AVG(L $\leq$ 2)	0.688 $\pm$ 0.008	0.654 $\pm$ 0.012
AVG(L $\leq$ 4)	0.698 $\pm$ 0.011	0.662 $\pm$ 0.008
AVG(L $\leq$ 6)	0.711 $\pm$ 0.005	0.664 $\pm$ 0.005
AVG(L $\leq$ 8)	0.709 $\pm$ 0.008	0.663 $\pm$ 0.015
AVG(L $\leq$ 10)	0.712 $\pm$ 0.006	0.669 $\pm$ 0.003
AVG(L $\leq$ 12)	0.704 $\pm$ 0.005	0.666 $\pm$ 0.013
<b>MONO.ISO.WITHCLS</b>		
AVG(L $\leq$ 2)	0.693 $\pm$ 0.004	0.649 $\pm$ 0.016
AVG(L $\leq$ 4)	0.699 $\pm$ 0.004	0.664 $\pm$ 0.006
AVG(L $\leq$ 6)	0.709 $\pm$ 0.002	0.671 $\pm$ 0.006
AVG(L $\leq$ 8)	0.710 $\pm$ 0.003	0.679 $\pm$ 0.006
AVG(L $\leq$ 10)	0.713 $\pm$ 0.006	0.670 $\pm$ 0.007
AVG(L $\leq$ 12)	0.705 $\pm$ 0.005	0.676 $\pm$ 0.006
<b>MULTI.ISO.NOSPEC</b>		
AVG(L $\leq$ 2)	0.671 $\pm$ 0.009	0.628 $\pm$ 0.013
AVG(L $\leq$ 4)	0.669 $\pm$ 0.006	0.640 $\pm$ 0.004
AVG(L $\leq$ 6)	0.684 $\pm$ 0.010	0.637 $\pm$ 0.009
AVG(L $\leq$ 8)	0.680 $\pm$ 0.005	0.647 $\pm$ 0.006
AVG(L $\leq$ 10)	0.676 $\pm$ 0.006	0.629 $\pm$ 0.008
AVG(L $\leq$ 12)	0.681 $\pm$ 0.005	0.637 $\pm$ 0.004
<b>MULTI.AOC-10.NOSPEC</b>		
AVG(L $\leq$ 2)	0.674 $\pm$ 0.005	0.635 $\pm$ 0.011
AVG(L $\leq$ 4)	0.681 $\pm$ 0.006	0.630 $\pm$ 0.007
AVG(L $\leq$ 6)	0.692 $\pm$ 0.008	0.649 $\pm$ 0.010
AVG(L $\leq$ 8)	0.695 $\pm$ 0.004	0.652 $\pm$ 0.011
AVG(L $\leq$ 10)	0.704 $\pm$ 0.005	0.657 $\pm$ 0.012
AVG(L $\leq$ 12)	0.702 $\pm$ 0.005	0.661 $\pm$ 0.008
<b>MULTI.ISO.ALL</b>		
AVG(L $\leq$ 2)	0.674 $\pm$ 0.004	0.626 $\pm$ 0.014
AVG(L $\leq$ 4)	0.682 $\pm$ 0.009	0.640 $\pm$ 0.009
AVG(L $\leq$ 6)	0.680 $\pm$ 0.002	0.632 $\pm$ 0.007
AVG(L $\leq$ 8)	0.683 $\pm$ 0.003	0.638 $\pm$ 0.010
AVG(L $\leq$ 10)	0.678 $\pm$ 0.007	0.638 $\pm$ 0.015
AVG(L $\leq$ 12)	0.676 $\pm$ 0.013	0.636 $\pm$ 0.005
<b>MONO.ISO.NOSPEC (REVERSE)</b>		
AVG(L $\geq$ 12)	0.683 $\pm$ 0.007	0.628 $\pm$ 0.009
AVG(L $\geq$ 10)	0.692 $\pm$ 0.014	0.628 $\pm$ 0.008
AVG(L $\geq$ 8)	0.688 $\pm$ 0.016	0.648 $\pm$ 0.007
AVG(L $\geq$ 6)	0.704 $\pm$ 0.015	0.658 $\pm$ 0.006
AVG(L $\geq$ 4)	0.704 $\pm$ 0.008	0.668 $\pm$ 0.007
AVG(L $\geq$ 2)	0.707 $\pm$ 0.008	0.667 $\pm$ 0.004
AVG(L $\geq$ 0)	0.714 $\pm$ 0.012	0.673 $\pm$ 0.003

Table 9: Results in the relation prediction task (REL<sub>P</sub>) across different word vector extraction configurations. Micro-averaged  $F_1$  scores reported, obtained as averages over 5 experimental runs for each configuration; standard deviation is also reported. AVG(L $\leq$ n) means that we average representations over all Transformer layers up to the  $n$ th layer (included), where  $L = 0$  refers to the embedding layer,  $L = 1$  to the bottom layer, and  $L = 12$  to the final (top) layer. Different configurations are described in §2 and Table 1. RANDOM.XAVIER are 768-dim vectors for the same vocabularies, randomly initialised via Xavier initialisation (Glorot and Bengio, 2010).

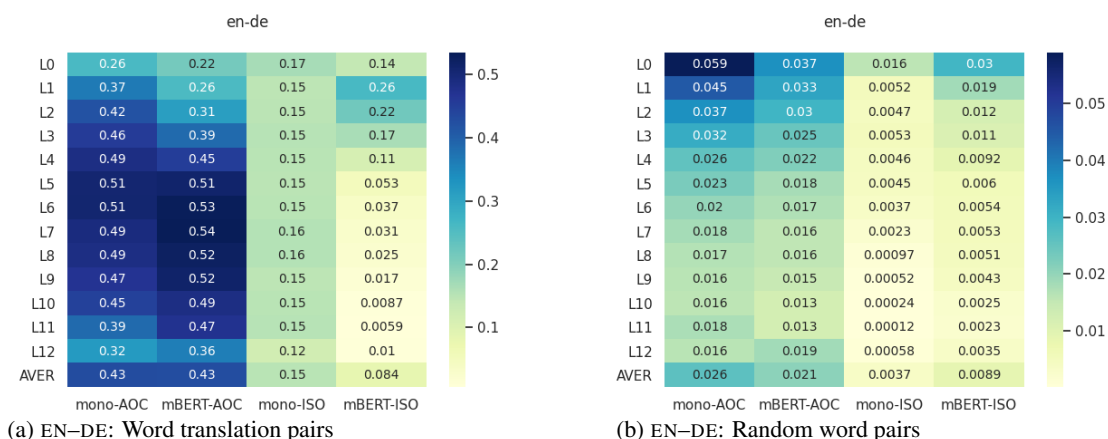


Figure 8: CKA similarity scores of type-level word representations extracted from each layer (using different extraction configurations, see Table 1) for a set of **(a)** 7K EN-DE translation pairs from the BLI dictionaries of Glavaš et al. (2019); **(b)** 7K random EN-DE pairs.

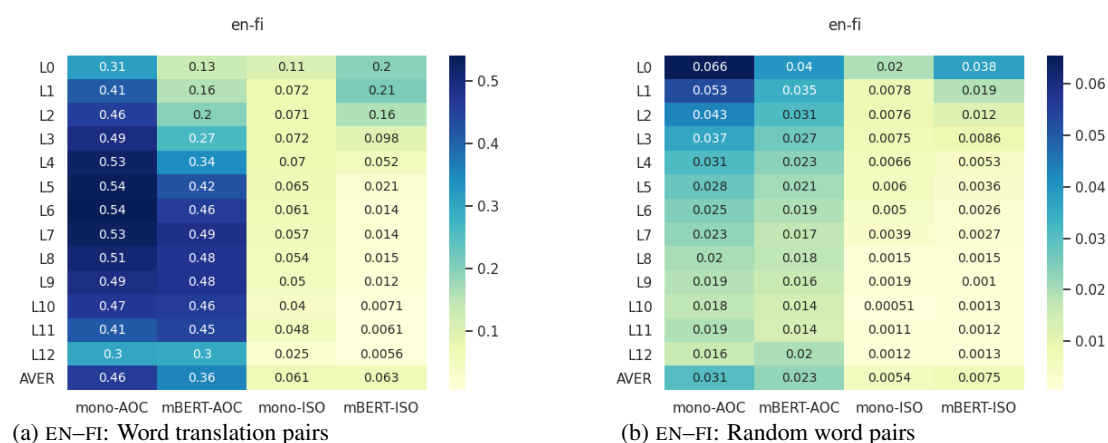


Figure 9: CKA similarity scores of type-level word representations extracted from each layer (using different extraction configurations, see Table 1) for a set of **(a)** 7K EN-FI translation pairs from the BLI dictionaries of Glavaš et al. (2019); **(b)** 7K random EN-FI pairs.

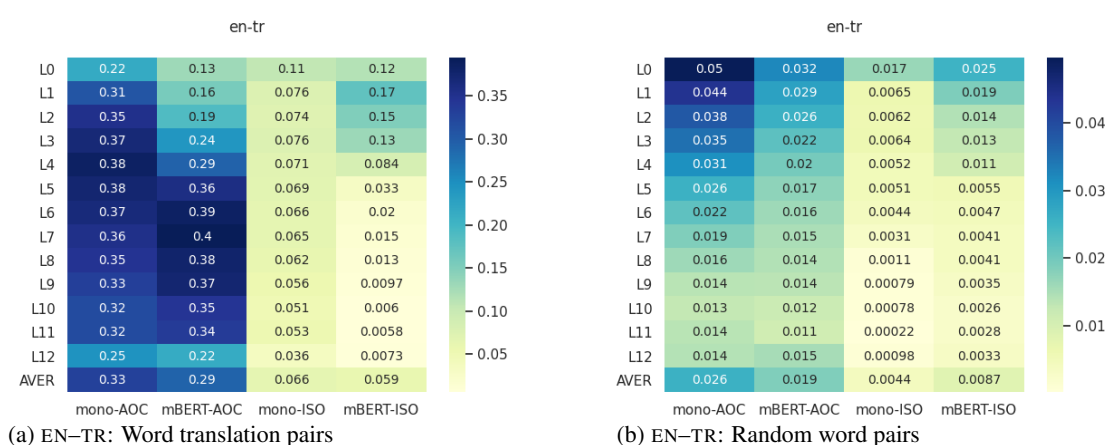


Figure 10: CKA similarity scores of type-level word representations extracted from each layer (using different extraction configurations, see Table 1) for a set of **(a)** 7K EN-TR translation pairs from the BLI dictionaries of Glavaš et al. (2019); **(b)** 7K random EN-TR pairs.