# An Approach to Improve the Smoothing Process Based on Non-uniform Redistribution

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### Abstract

In the paper, an effective technique, based on the non-uniform redistribution probability for novel events (the unknown events), to improve the smoothing method in language models is proposed. Basically, there are two processes in the smoothing methods: 1) discounting and 2) redistributing. Instead of uniform probability assignment to each unseen events used by most smoothing methods, we propose new technique to improve the redistribution process. Referring to the probabilistic behavior of all seen events, the redistribution process for novel events in our method is non-uniform. The proposed technique is exploited on well-known and frequently-used Good-Turing smoothing method. The empirical results are demonstrated and analyzed for two n-gram models. The improvement is apparent and effective for smoothing methods, especially on higher unseen event rate.

Keywords: Language model, Smoothing method, Good-Turing, Cross entropy, Non-uniform Redistribution.

## **1. Introduction**

### **1.1 Statistical language Models**

In many domains of natural language processing (NLP); such as speech recognition [1], grammar parser [4], document retrieval [17] and machine translation [Brown]; the statistical **a**nguage models (LMs) [6], [10] plays an important role in natural language processing. The LMs can be exploited, for instance, to decide the correct target word sequence  $\overline{w}$ . As shown in Fig. 1 of a speech recognition system, the P(W) is the conditional probability of a word sequence W given a speech data S, where  $W=w_1w_2w...w_m$  is a possible translation of texts, m is word number of M. The predicted sequence  $\overline{w}$  can be expressed:

 $\frac{1}{W} = \operatorname{argmax}_{P(W|S)} = \operatorname{argmax}_{\partial}(S|W)P(W)$ (1)

where  $P_{\partial}(S | W)$  is the probability of input speech given a word sequence W.

A language model is regarded as the probability distribution over events or token sequences (texts) that models how often each sequence occurs as a sentence. Chain rule is used to decompose probability prediction:

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$$P(w_1^{p_1}) = P(w_1w_2...w_m) = P(w_1)P(w_2 | w_1^1)P(w_3 | w_1^2).P(w_m | w_1^{p_1-1})$$
  
=  $P(w_1)\prod_{i=2}^m P(w_i | w_1^{i-1}).$  (2)

where  $w_1^m$  denotes the word sequence with *m* words.



Fig. 1: LMs in speech recognition system.

### 1.2 n-gram Model

Because of the finite training corpora in real world and to reduce the parameter space of word feature in languages, the approximate probability of a given word by using the  $(n-1)^{\text{th}}$  preceding words is used to estimate sequence *W*.

The probability model with various n can be written:

 $P(w_1^m) \cong P(w_1) \prod_{i=1}^m P(w_i \mid w_{i-n+1}).$ (3) where  $w_{i-n+1}$  denotes the history of *n*-1 word for word  $w_i$ .

In many applications, the models for n=1, 2 and 3 are called unigram, bigram and trigram models [1], [8] and [16], respectively.

In Eq. (3), the probability for each event or token can be obtained by training the bigram model (for clarity, bigram model is illustrated). Therefore the probability of a word bigram will be written as:

$$P(w_i \mid w_{i-1}) = \frac{C(w_{i-1}w_i)}{\sum_{w} C(w_{i-1}w)} , \qquad (4)$$

where  $C(w_i)$  is the count of word  $w_i$  appeared in training corpus. The probability *P* of Eq. (4) refers to the relative frequency and such method is called maximum likelihood estimation (MLE).

#### 1.3 Smoothing Issue in Language Models

As shown in Eq. (4),  $C(\ )$  of a novel word, which don't occur in the corpus, may be zero because of the limited training data and infinite language. It is always hard for us to collect sufficient datum. The potential issue of MLE is that the probability for unseen events is exactly

zero. This is so-called the zero-count problem. It is obvious that zero count will lead to the zero probability of P(-) in Eqs. (3) and (4).

The prediction of zero probability of certain event is unreliable and unfeasible for most applications, especially for language models. The smoothing techniques [3], [4], [11] and [19], are essential and employed by language mode to overcome the issue zero count of traditional language models, as described above.

There are many smoothing methods, such as Add-1, Good-Turing [6], deleted interpolation [7], Katz [13], etc. There are several literatures discussing about smoothing methods [3], [4], [12], [14], [15], [16] and [18].

### 2. Smoothing Processes in LMs

The adjustment of smoothed probability for all possibly occurred events involves discounting and redistributing processes:

#### 2.1 Discounting Process

The probability of all seen and unseen events is summed to be one (unity). First operation of smoothing method is the discounting process, which discount the probability of all seen events. It means that the probability of seen events will be decreased a bit.

The adjustment can be divided into two types: static and dynamic. Static smoothing methods, as most smoothing methods, discount the probability based on the frequency of events in trained corpus. However, dynamic smoothing method, i.e., cached-based language, discounts the probability based on the frequency of seen events in cache and trained corpus.

#### 2.2 Redistributing Process

In this operation of smoothing algorithm, the escape probability  $P_{esc}$  obtained from all seen events will be redistributed to all unseen events.  $P_{esc}$  is usually shared by all the unseen events. That is,  $P_{esc}$  is redistributed uniformly to each unseen event,  $P_{esc}/U$ , where U is the number of unseen events of a language model. In other hand, each unseen event obtains same probability based on the uniform distribution.

The redistribution process of most well known smoothing methods, such as Add-1, Absolute discounting, Good-Turing, Delete interpolation, Back-off and Witten-Bell, and so on. The escape probability  $P_{esc}$  (or called probability mass assigned to all unseen events) is uniformly shared by all unseen events. It is a possible factor that affects the performance of smoothing algorithm. There are little previous papers discussing how to redistribute the escape probability  $P_{esc}$ , and how the different redistribution can improve the smoothing methods for language models.

# 3. Improving the Smoothing Process

### 3.1 Interval Behavior of Seen Events Count

As described in the section 2, there are two main processes for smoothing methods; discounting and redistributing. In the redistributed process, the escape probability  $P_{esc}$  is shared uniformly by all unseen events for most smoothing methods, each event obtain same smoothed probability  $P_{esc}/U$ . Based on the observation of behaviors for seen events, each event has its probability relying on the event frequency in the training corpus. It is obvious that the probability distribution for each event is quite different. Therefore, It is unreasonable to assign same probability to each incoming unseen events.

As shown in Fig. 2, the figures draw the frequency interval (offset) between two new successive events for two models; Chinese character word unigrams and bigrams. There are 100M ( $10^8$ ) Chinese characters for source training data. The sentences in source are segmented into words and 65M ( $65*10^6$ ) words are obtained. The length of word is 1.45 Chinese characters per word in average.

The recourse files are randomly selected and we obtain the offset diagrams. More than 100 training processes are implemented and then the final curve can be obtained in average. The regression curves  $Y_1$  and  $Y_2$  for Chinese word unigram and character bigram models can be described as follows:

 $\begin{array}{l} Y_1 = 1 E^{10} x^3 - 4 E^{06} x^2 + 0.0307 x - 39.825 \\ Y_2 = -1 E^{-16} x^4 + 2 E^{-11} x^3 - 6 E^{07} x^2 + 0.0058 x - 3.7502 \end{array}$ 

where *x* and *y* denotes the data size the offset.

An idea for redistributing escape probability  $P_{esc}$  is that how many tokens read-in while the next new event will occur? It means the count interval between two successive events, which vary usually with the training data *N*. Basically, the larger the training data *N*, the larger, and the interval. In the beginning of training phase, next new events will occur in short interval of count. It means that next new event will occur rapidly at smaller *N* while slowly at larger *N*.

The larger the training data N is, the larger the offset (interval) is. It is apparent that the. The regression curves present the general interval of original intervals and its trend increased gradually. Note that the regression curves varied with N and flatter at the beginning and steeply at end of curves.



Fig. 2: the interval (offset) between two successive events varied with training data; (left) word unigrams, (right) character bigrams.

### **3.2 Redistributing Process for Unseen Events**

As described above, the regression curves from seen events can be used to demonstrate the interval of unseen events. Based on the curves derived from the seen events occurrence, we can furthermore derive the behaviors for estimating the probability assigning to the next incoming unseen event. Note that all the probability for seen and unseen events should be unity; which must satisfy the basic statistical condition.

Supposed that the interval y on training data  $N_i$ , the distribution for all unseen events can be as follows:

(6)

$$d_{i} = \frac{\frac{1}{y_{i}}}{\sum_{j=1}^{U} \frac{1}{y_{j}}},$$

where  $y_i$  denotes the interval on location *i* in Fig. 2 and *U* denotes the types of unseen events.  $1/y_i$  can be regared as the derivatives at  $y_i$  and as the probability for unseen events.

The smoothed probability assigning to an unseen event 
$$U_i$$
 is:  
 $p_i = P_{esc} * d_i \cdot$ (7)

Referring to Eqs (6) and (7), the total smoothed probability for all unseen events is  $P_{esc}$ . The probability for all seen and unseen events are summed as unity.

### 4. Evaluation

Our proposed method will be evaluated on the well-known and popular smoothing Good-Turing technique. The cut-off value for word count is usually used to improve the technique. Based on the empirical results, we can obtain best cut-off value on various training data N.

### 4.1 Basic Idea of Good-Turing Method

Good-Turing method is a well-known and effective smoothing technique, which was first described by I. J. Good and A. M. Turing in 1953 [7] and used to decipher the German Enigma code during World War II. Some previous works are in [4] and [9]. Notation  $n_c$  denotes the number of *n*-grams with exactly *c* count in the corpus. For example,  $n_0$  represent that the number of *n*-grams with zero count and  $n_1$  means the number of *n*-grams which exactly occur once in training data.

The redistributed count  $c^*$  for *Good-Turing* smoothing will be presented in term of  $n_c$ ,  $n_{c+1}$  and c as follows:

$$c^* = (c+1)\frac{n_{c+1}}{n_c}$$
 (8)

### 4.2 Best Cut-off Value in Good-Turing Smoothing Method

In the most previous works of smoothing methods, they discussed the situation the possible event types *B* were much larger than the training data *N* (*N*/*B* <<1), such as words trigram models in English text or character trigrams in Mandarin. However, the situation N/B >> 1 or  $N/B \cong 1$  should be considered in certain applications. For instance, the event types *B* for Chinese character

bigram is close to  $1.69*10^8$  while the training data size *N*, in general, is usually less than  $1*10^8$ . In such case, the ratio of *N/B* is close to 1.

The cut-off value  $c_o$  for event count is used to improve the Good-Turing Smoothing, as shown in previous section. The best  $c_o$  on various training data N should be analyzed to obtain better improvement, shown in next section

### 4.3 Data Sets and Empirical Models

In the following experiments, two text sources are collected from the news texts and Academic balanced corpus (ASBC); the former and the later contain 100M and 10M Mandarin characters, respectively. We construct two models to evaluate the cross entropy CE of the technique to improve smoothing process; word unigrams model (word length is 1.45 characters in average) and Chinese character bigrams. The cross entropy is calculated on various data size N in our experiments.

Comparing uniform with non-uniform redistribution probability for unseen events, Fig. 3 and Fig. 4 display the cross entropy (CE), unseen event rates and improvements of different cut-off  $c_o$  on various N for word unigram and character bigram models, respectively. The best cut-off  $c_o$  can be found on various N for both models. For the word unigrams model, it is apparent that the best CE improvement reaches near 1.8% at N=0.5M, and the effectiveness decreases while the N is larger, as shown in Fig. 3. For bigram model, the best CE improvement reaches near 14.3% at N=1M, and the effectiveness decreases while the N is larger, as shown in Fig. 4.

Both models reach lower CE while the cut-off and non-uniform redistribution technique are exploited. It can improve better, especially on higher unseen event rate.



Figure 3: the cross entropy, unseen event rates and improvements on different cut-off *c*<sub>o</sub> on various *N* for word unigram model.



Figure 4: the cross entropy, unseen event rates and improvements on different cut-off  $c_o$  on various N for character bigram model.

# 5. Conclusions

In the paper, we have proposed an effective technique, based on the non-uniform redistribution probability for novel events, to improve the redistribution process in smoothing method of language models. The smoothing method is used to resolve the zero count problems in traditional language models. The cut-off  $c_o$  for event count is used to improve the zero  $n_c$  issue of Good-Turing Smoothing.

Based on the probabilistic behavior of seen events, the redistribution process exploited by our technique is non-uniform. The improvements discussed in the paper are apparent and effective on Good-Turing smoothing methods.

Empirical results are demonstrated and analyzed for two language models to evaluate the proposed technique methods discussed in the paper; Chinese word unigrams, character bigram model. The cross entropy can be reduced in these two models.

Both models reach lower CE for various cut-off  $c_o$  on different training data N and non-uniform redistribution probability are used. Two methods can improve better, especially on higher unseen event rate. In other word, we can improve especially the CE for application with small training data N. The best CE improvement reaches 1.8% and 14.3% for word unigrams and character bigram models.

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