Investigating the Shortcomings of LLMs in Step-by-Step Legal Reasoning

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Abstract

Reasoning abilities of LLMs have been a key focus in recent years. One challenging reasoning domain with interesting nuances is legal reasoning, which requires careful application of rules, and precedents while balancing deductive and analogical reasoning, and conflicts between rules. Although there have been a few works on using LLMs for legal reasoning, their focus has been on overall accuracy. In this paper, we dig deeper to do a step-by-step analysis and figure out where they commit errors. We use the college-level Multiple Choice Question-Answering (MCQA) task from the Civil Procedure dataset and propose a new error taxonomy derived from initial manual analysis of reasoning chains with respect to several LLMs, including two objective measures: soundness and correctness scores. We then develop an LLM-based automated evaluation framework to identify reasoning errors and evaluate the performance of LLMs. The computation of soundness and correctness on the dataset using the auto-evaluator framework reveals several interesting insights. Furthermore, we show that incorporating the error taxonomy as feedback in popular prompting techniques marginally increases LLM performance. Our work will also serve as an evaluation framework that can be used in detailed error analysis of reasoning chains for logic-intensive complex tasks¹.

1 Introduction

Legal reasoning is a complex process requiring the careful application of rules, and precedents while balancing deductive and analogical reasoning, for various legal scenarios (Walker, 2007; Hafner and Berman, 2002). These challenges are heightened by reasoning through uncertainties (Figure 1) and ambiguous laws (Figure 18). In recent years, Large Language Models (LLMs) have emerged as the

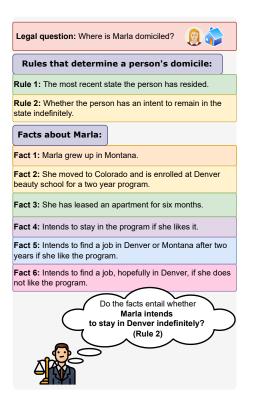


Figure 1: An example of determining domicile in a legal context. A reasoner must discern whether the condition of 'indefinite to stay in a place' is met. While many LLMs predict Marla is domiciled in Montana since her program is only for 2 years, legally, her ambiguous plans indicate an intent to remain in Denver indefinitely, making her domiciled in Denver, not Montana.

most dominant AI models to process and generate natural language. There has been widespread research to showcase the emergence of natural language understanding (NLU) and reasoning abilities (Zelikman et al., 2022, 2024; Hao et al., 2023; Mondorf and Plank, 2024; Lanchantin et al., 2024) of LLMs. These findings have opened up avenues to utilize LLMs in complex domains like Law (Lai et al., 2023). Consequently, there has been significant research in evaluating the performance of LLMs' legal reasoning ability (Guha et al., 2023;

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¹Data and source code are available at https://github. com/VenkyMishra/legal_reasoning

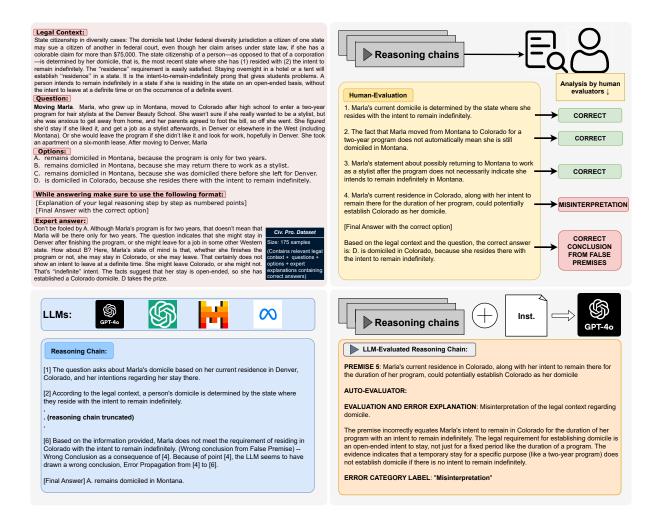


Figure 2: Overview of the proposed pipeline for evaluating legal reasoning in LLMs. The process begins with converting *Civ. Pro.* dataset (**top left**), followed by generating reasoning chains using LLMs in a zero-shot CoT setting (**bottom left**). These chains are manually analyzed for various error types (**top right**), based on the proposed error taxonomy. The pipeline is then automated using an LLM-based system (**bottom right**) to assess reasoning chains for errors such as misinterpretation, providing insights into the LLMs' reasoning accuracy.

Blair-Stanek et al., 2023; Kang et al., 2023). In this paper, we focus on providing a detailed, finegrained analysis of the errors that occur during step-by-step legal reasoning using LLMs. While earlier works exist on evaluating step-by-step reasoning of LLMs (Golovneva et al., 2023; Prasad et al., 2023), they do not specifically cater to legal reasoning.

As shown in Figure 1, analyzing legal scenarios requires extensive consideration of critical analysis of prior context. Hence, beyond just evaluating final answers, it is crucial to analyze the step-by-step reasoning chains generated by LLMs and where they falter to gauge their reasoning capabilities to solve such tasks. Despite continued improvements, LLM outputs are affected by fundamental challenges such as hallucinations (Dahl et al., 2024; Varshney et al., 2024), and misunderstanding long-contexts (Lu et al., 2024). Our work aims to investigate such errors on a fine-grained level for each step generated to showcase the ability of LLM to perform legal reasoning. To this end, we leveraged the dataset from Bongard et al. (2022) (referred to as 'Civ. Pro.' throughout the paper) in the form of MCQA and analyzed reasoning chains generated by LLMs. The dataset comprises of 175 legal scenarios, each providing a comprehensive legal context that includes relevant rules, precedents, and exceptions. Following this context, questions and options are presented to test the understanding and application of these legal principles. The primary goal of using this dataset is to assess how well the LLM reasons logically and contextually when provided with all necessary legal rules, without relying on its inherent knowledge to recall them. This approach highlights the LLM's

ability to perform deductive and analogical reasoning in complex, context-rich legal scenarios. Some of the widely used LLMs, Mistral-7B-v2-Instruct, Llama-3-8B-Instruct, GPT-3.5-turbo, GPT-4-turbo, and GPT-4o, are evaluated in zero-shot-CoT setting (Wei et al., 2023) (as shown in Figure 2).

Subsequently, human evaluation of the LLMgenerated reasoning chains against the ground truth solutions is performed for a subset of the dataset to find the most common errors being committed in the reasoning steps. This resulted in the development of a detailed error taxonomy, as outlined in Tables 1 and 2, which allowed for a deeper understanding of the underlying causes of LLMs' failures. Additionally, to extend this evaluation across the entire dataset, we develop a method employing 'LLMs as auto-evaluators' (inspired by Liu et al. (2023); Chern et al. (2024)) that leverages our proposed error taxonomy. The auto-evaluator framework achieves a recall of $\sim 87.06\%$ in terms of identifying errors similar to human annotation. To derive better qualitative observations, we utilize two metrics: soundness and correctness (details in §4.2) to further analyze the reasoning chains. These metrics provide us with interesting insights, the most prominent of them being the inability to generate error-free rationales due to misinterpretation of the contextual nuances.

In the end, we apply various prompting strategies (details in §5.3) known to enhance LLM reasoning abilities with the zero-shot method. We also incorporated our error taxonomy as feedback to the prompting strategies to assess their effectiveness in mitigating errors in legal reasoning. The prompting strategies enhanced with error taxonomy feedback show improved accuracy (maximum of ~4%) which suggests that providing information about errors help in improving the performance of LLMs. We hope that this framework for automatically evaluating step-by-step reasoning in complex tasks will be helpful for future research. In summary, the main contributions of our paper are:

- 1. We propose an error taxonomy to systematically identify the most commonly occurring errors in step-by-step legal reasoning.
- We develop an LLM-based pipeline to automatically detect errors, and introduce two key metrics—soundness and correctness—to evaluate step-by-step legal reasoning.
- We investigate the integration of errortaxonomy feedback into various LLM prompt-

ing strategies and find that it enhances the LLMs' legal reasoning capabilities.

2 Related Work

Legal Reasoning with LLMs LegalBench (Guha et al., 2023), LawBench (Fei et al., 2023), LEXGLUE (Chalkidis et al., 2021) and LEGALSEMI (Kang et al., 2024) have introduced exhaustive benchmarks which cover distinct tasks to measure the legal reasoning abilities of LLMs. Dahl et al. (2024) addresses the problem of hallucinations in LLMs, particularly their behavior in generating information that lacks factual accuracy. While these works have evaluated legal reasoning of LLMs on labelled predictions or through expert manual evaluation, our work specifically focuses on evaluating natural language step-by-step rationales with the help of LLMs. We also introduce a task-specific fine-grained error taxonomy to assess the reliability of LLMs in producing error-free reasoning chains.

Evaluation and Verification of Step-by-Step Reasoning Chains through LLMs ROSCOE (Golovneva et al., 2023) offers a comprehensive suite of metrics to assess various aspects of reasoning quality, including correctness, informativeness, consistency, and coherence. ReCEval (Prasad et al., 2023), on the other hand, specifically targets incorrect answer detection by specifically analyzing the 'correctness' and 'informativeness' of reasoning steps. LLM Reasoners (Hao et al., 2024) introduces a novel evaluation framework for a detailed analysis of large language models' step-by-step reasoning abilities. Ling et al. (2023) introduces Natural Program, a natural language-based deductive reasoning format that decomposes a reasoning verification process into a series of step-by-step subprocesses. Tyen et al. (2024) explores the limitations of LLMs in detecting reasoning errors and highlights their effectiveness in correcting errors when provided with specific locations. Li et al. (2023) presents the DIVERSE approach involving a three-stage process to identify and correct errors at each step of the reasoning chain. While prior works (Parmar et al., 2024; Patel et al., 2024; Tyagi et al., 2024a) introduce valuable evaluation frameworks, they are not optimized specifically for a legal reasoning task. Our work utilizes soundness and correctness metrics, which are simple yet effective in offering detailed insights into step-by-step

legal reasoning errors. These metrics also make the evaluation scalable and reduce manual effort with our formulated LLM-based evaluation framework.

3 Evaluation of Reasoning Chains

3.1 The Civil Procedure Dataset

The dataset has been sourced from MCQs present in the 'The Glannon Guide To Civil Procedure' (Glannon, 2019). We compile the Civ. Pro. dataset with 175 samples of college-level law multiplechoice questions from the US Civil Procedure laws. The questions are primarily designed to evaluate the ability of university-level law students to reason about various legal scenarios about US Civil Procedure laws and provide their final judgment by choosing the most correct option as an answer. The dataset includes relevant legal context, multiple-choice questions, and expert answers with correct explanations provided by legal experts. These elements were extracted and converted into a prompt-based format suitable for LLM inference and the generation of reasoning chains. The Civ. Pro. dataset consists of samples comprising of $\mathcal{D} = \langle lc_n, q_n, o_n, e_n \rangle$, where lc_n, q_n, o_n and e_n denote the n^{th} legal context, question, option-set and expert-answer respectively.

3.2 Manual Evaluation Of Reasoning Chains

Human evaluators are instructed to find flaws in a reasoning chain and explain the flaws in natural descriptive language. To solve a given legal question in Civ. Pro., an LLM generates a set of statements $\langle A : s_1, s_2, ..., s_k, c \rangle$, where A represents the legal argument/rationale put forward to solve the problem, with $s_1, s_2...s_k$ being the 'k' number of intermediate steps generated to reason towards the final conclusion c. Each step in the reasoningchain, including the final conclusion, is separately evaluated for the presence/absence of errors. To create an error taxonomy, we adopt an exhaustive approach, continuously updating the taxonomy until no new errors are identified. Specifically, 120 reasoning chains containing approximately 537 reasoning steps are used for evaluation (generated as responses by four LLMs: Mistral-7B-v2-Instruct, Llama-3-8B-Instruct, GPT-3.5-turbo and GPT-4turbo, to the same 30 data sample subset). This evaluation helped to solidify our proposed taxonomy as described in §3.3. Detailed statistics of the human-evaluations are provided in Tables 8 and 9 of Appendix B. Further details regarding

annotation guidelines and process, inter-annotator agreement statistics using Cohen's kappa coefficient (Cohen, 1960) and annotation examples are provided in Appendix G and Appendix H (Tables 13-18).

3.3 Proposed Error Taxonomy

The error taxonomy is designed to mirror the types of errors humans make when reasoning about passage comprehension and constructing rational arguments. It classifies errors into two levels: 1. Premise-level and 2. Conclusion-level errors. Premise-level errors are based on 'Errors of Law' and 'Errors of Fact' grounded in the legal domain (Legal Information Institute, Cornell Law School, 2024b,a; O'Reilly, 2012; Wilberg, 2023). While premise-level errors often influence errors at the conclusion level, many conclusion-level errors occur independently. Conclusion-level errors serve as indicators of the overall decision-making ability of LLMs in generating the final answer to a legal question.

Premise-level Errors These errors have occurred in one of the premises of the reasoning chain. They highlight the core issue with LLMs that ineffectively prioritize relevant parts of the prior context and incorrectly identify important information. We categorize these errors as shown in Table 1.

Conclusion-level Errors Conclusion-level errors indicate issues with deductive reasoning, reflecting the LLM's ability to follow premises to reach the correct conclusion. They also reveal how much the decision-making process is influenced by intermediate premises in choosing the final answer. We categorize these errors as shown in Table 2.

Conclusion from Incomplete Premises vs. Correct Premises We argue that a 'Wrong Conclusion from Correct Premises' is essentially a 'Wrong Conclusion from Incomplete Premises' because either the premises, though correct, are incomplete and lead to a wrong conclusion, or the LLM fails to explicitly generate a key premise. This poses a challenge for LLM-based auto-evaluators, as discussed in §3.4, which struggle to assess whether the rationale is sufficient or inadequate.

3.4 LLM-aided Automatic Evaluation

Manual analysis of reasoning chains provided a detailed categorization of errors; however, it was timeconsuming and, therefore, challenging to scale for

Category	Description
Misinterpretation (associated with Error of Law)	The LLM misinterprets or omits some part/entirety of the legal context, question or the options (or a combination of them). This usually leads to the wrong reasoning and selection of wrong conclusion. The following error instances fall under the taxon of misinterpretation: 1. Misunderstanding the legal rules. 2. Misunderstanding the legal situation/issue at hand. 3. Omission of parts of the provided context while reasoning. 4. Incompletely applying a legal rule. 5. Incorrectly applying the legal rule. 6. Wrong assumptions derived from the provided context.
Irrelevant Premise (associated with Error of Law)	The LLM generates a premise which is not relevant in solving the question or that it may divert the reasoning chain from solving the question correctly. An premise may be logically valid and factually true but the absence of this premise can still lead to the correct conclusion.
Factual Hallucination (associated with Error of Fact)	This error category covers instances where the LLM, during its reasoning process, generates information that is either inconsistent with the facts of the given legal scenario or is entirely fabricated with no basis in reality.

Table 1: Error taxonomy for the Premise-level steps. The taxonomy has been developed with consideration for the types of errors that a human reasoner might commit when constructing a rationale for a given legal scenario. Error of Law and Error of Fact are explained in (Legal Information Institute, Cornell Law School, 2024b,a; O'Reilly, 2012; Wilberg, 2023). Some fine-grained error instances of the 'Misinterpretation' category are shown in Tables 13, 14, 15 and 16.

the entire dataset. Thus, we develop an alternate approach to leverage LLMs to evaluate the errors in the reasoning chains akin to human evaluation. Specifically, we use GPT-40 as the LLM backbone of the 'auto-evaluator' system to identify and label the errors. The auto-evaluator assesses a total of 875 reasoning chains, encompassing approximately 4,844 individual reasoning steps, which include both premise-level and conclusion-level steps (refer Table 7). The details of the implementation are described in Appendix I and an example snippet of LLM-aided annotation is provided in Table 3. We develop two approaches for error evaluation:

Exact Error Label Match In this approach, we task the 'auto-evaluator' with identifying the exact error category labels which the human evaluators had labeled a particular premise/conclusion of a reasoning chain. Experiments revealed significant mislabeling between the auto-evaluator and human evaluators, with many 'Misinterpretation' errors at the premise level being labeled as 'Irrelevant Premises' or 'Factual Hallucination' (Refer Appendix F) by the auto-evaluator, and vice versa. Hence, we make changes to the auto-evaluators to include error explanations along with the labels.

Another significant challenge was the low error detection rate of factual hallucinations with the help of single-call LLM auto-evaluators. Motivated by Varshney et al. (2023); Dhuliawala et al. (2023), we develop a multi-call LLM system, consisting of two separate LLM calls, in which one LLM call creates

verification questions to probe various aspects of a premise and another LLM call answers them citing the provided legal context for factuality. A premise is considered to contain factual hallucination if the answers to any of the verification questions contradicts the content of the premise directly.

Semantic Error Explanation Match As an alternative approach to the above problems, we develop a multi-analyzer system consisting of three 'single-call' and one 'multi-call' LLM-based pipeline focused on providing explanation of errors at the premise-level. A 'summarizer' LLM (Refer Appendix K) combines the individual analyses of all analyzers into a single error explanation for a premise. This enables the pipeline to detect and label multiple errors in a single premise (e.g., a premise containing both misinterpretation and factual hallucination).

To validate the effectiveness of the autoevaluator, we sample 120 reasoning chains from the manually evaluated set of four LLMs (Mistral-7Bv2-Instruct, Llama-3-8B-Instruct, GPT-3.5-turbo and GPT-4-turbo). The human evaluators then compare their error category assignments as well as explanations to those provided by the auto-evaluator. The recall percentage of detecting an error at the premise level across four LLMs ranged from 83.87% to 90.6%. The recall percentage range for detecting an error-free premise step ranged from 86.17% to 93.85%. The details of the autoevaluator performance statistics are present in Tables 10 and

Broad-Category	Sub-Category	Description
Wrong Conclusion	Wrong Conclusion from False Premise(s)	This error primarily occurs when the step-by-step rationale gener- ated includes premises that are logically invalid, factually incorrect, irrelevant to solving the question posed, or a combination of these issues.
	Wrong Conclusion from In- complete Premise(s)	This error occurs when valid and sound premises are provided but fail to fully support the reasoning, leading to the wrong conclusion. A special example is 'Wrong Conclusion from Correct Premises,' where sufficient premises still result in an incorrect conclusion.
Right Conclusion	Right Conclusion from False Premise(s)	This error occurs when the LLM reasons to the correct option while providing a wrong argument. One or multiple premises contain errors which fall under one of the three premise-level error categories and yet lead to the reasoning path choosing the correct option as its final answer.
	Right Conclusion from Incom- plete Premise(s)	This error occurs when the correct final option is selected, even though the premises provided are incomplete or insufficient to fully justify that conclusion.
	Right Conclusion with Hallu- cinated Content	This error occurs when the LLM selects the correct option but the generated content does not semantically match the provided options. For example, the LLM might output 'Option D. The suspect is X ,' when the actual content is 'Option D. The suspect is Y and committed crime Z ,' due to an LLM hallucination.

Table 2: Error taxonomy for the Conclusion.

11 of Appendix J. Figure 17 shows the pipeline of the error detection implemented using GPT-40.

4 Experimental Setup

4.1 Models

We evaluate a range of closed-source LLMs including GPT-4-Turbo, GPT-4o, GPT-3.5-turbo, and open-weight models Llama-3-8B-Instruct, and Mistral-7B-v2-Instruct on the 'Civ. Pro.' dataset using the zero-shot CoT prompting setting (Wei et al., 2023; Kojima et al., 2023). While we also conduct the few-shot CoT prompting by providing 1-3 exemplars for solving a legal scenario to LLMs, we find that the final accuracy $(\S4.2)$ is lower across LLMs when compared to the zero-shot CoT setting (refer Appendix M). NVIDIA A100 GPUs were used to conduct the inference of open-weight models with a batch size of 1. OpenAI API and Gemini API were used for obtaining inference results from the closed-source models. An example prompt used for these experiments is provided in Figure 18.

4.2 Metrics

Accuracy We use accuracy to demonstrate the capability of LLMs in solving legal scenarios based on their ability to predict the final answer (the conclusion). To calculate this metric, we use the LLM-

generated final options chosen as answers and compare them with the available expert answer.

Soundness Score We create a step-wise soundness score metric to check the number of premises which is error-free in terms of the absence of errors as delineated by our established error taxonomy. We computed this score by taking its average across a single reasoning chain. The Soundness score (between 0 and 1) is calculated by:

$$S = \frac{\text{Number of sound premises}}{\text{Total Number of premises}}$$

Correctness Score This metric is calculated to evaluate the condition where the reasoning chain must be both error-free at both premise and conclusion levels. Likewise in the soundness metric, the expert answers to extract the ground-truth options as conclusions. A reasoning chain must be both 'sound' (with the Soundness score being equal to 1) and arrive at the correct final option as its conclusion. The Correctness score is calculated as:

$$C = \begin{cases} 1, & \text{if (premises + conclusion) correct} \\ 0, & \text{for all other cases} \end{cases}$$

The results of these metrics calculated for 120 reasoning chains annotated by humans are provided in Table 6 (Appendix A). Table 4 and Figure 4 show

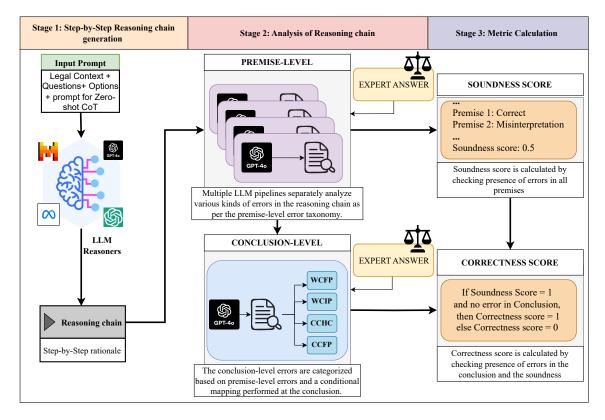


Figure 3: The overall schematic representation of the LLM-based error-detection and evaluation system and the calculation of the metrics. The reasoning chains are produced by 5 LLMs and the expert answer is referenced from the *Civ. Pro.* dataset

the metric results calculated from auto-evaluator annotations on the entire *Civ. Pro.* dataset.

5 Results and Analysis

5.1 Objective Evaluation

Soundness metrics are high but correctness scores are low Table 4 shows that the majority of the premises are error-free (with the highest being GPT-40 having 78.4% of the generated premises being error-free). In contrast, Figure 12 reveals that an average of $\sim 96\%$ of reasoning chains leading to conclusions from false premises have one or more misinterpretation errors in the intermediate premises. This finding, aided by empirical human analysis, suggests that much of the LLM-generated reasoning chain re-iterates existing context, while most errors occur in the smaller portion where new 'decision-making' inferences are generated. The similarity in correctness score in Mistral-7B-v2-Instruct and Llama-3-8B-Instruct in contrast to the higher accuracy of Llama-3-8B-Instruct could be attributed to the lesser number of steps (see Table 7 (Appendix E)) on average in the reasoning chain of Llama-3-8B-Instruct when compared to

Mistral-7B-v2-Instruct.

Accuracy vs. Correctness Score Table 4 and Figure 4 show a sharp decrease (an average of $\sim 27\%$) in the scores of accuracy to correctness across all LLMs. The highest fall in percentage is observed in Llama-3-8B-Instuct (31.4% decrease). This is significant as it shows that while LLMs can arrive at the correct conclusion, there are a lot of cases where the reasoning chain they generate is not entirely error-free. These results also suggest that LLMs often rely on superficial correlations and patterns, likely learned in the training stages, to arrive at correct conclusions, rather than through genuine reasoning. In high-stakes domains such as legal, financial, and medical fields, it is imperative that the reasoning generated by LLMs is completely error-free as even minor inaccuracies in these critical areas can lead to significant consequences. This also underscores the necessity for robust evaluation mechanisms to ensure the reliability and correctness of model outputs.

Larger, proprietary models 'reason' better than smaller, open-source models Figure 4 and Table 4 convey that proprietary models generate more Examples of a reasoning step and final conclusion evaluated by GPT-40 based auto-evaluator Premise 4: Marla's Intent: Marla's intent is somewhat ambiguous. She is attending a two-year program and is unsure if she wants to be a stylist. She has considered staying in Denver to work if she likes the program, or leaving the program and looking for work in Denver if she doesn't like it.

Auto-Evaluator Evaluation and Error Explanation: Premise 4: Misinterprets Marla's intent.

The premise incorrectly suggests ambiguity in Marla's intent. According to the legal context, Marla's plans are open-ended, meaning she does not have definite plans to leave Denver. The ambiguity mentioned does not align with the legal context's explanation of "indefinite intent".

Error Category Label: "Misinterpretation"

Predicted Conclusion: Given that Marla resides in Colorado and has no definite plans to leave, she meets the domicile test's requirement of residing with the intent to remain indefinitely. Final answer: D.

Extracted Ground-Truth Conclusion: D. is domiciled in Colorado, because she resides there with the intent to remain indefinitely.

Auto-Evaluator Evaluation and Error Explanation: Based on the provided conditions and the information given:

- The extracted conclusion's final answer is D

- The ground truth option is also D.

- The content of the extracted conclusion and the ground truth option match: both state that Marla is domiciled in Colorado because she

resides there with the intent to remain indefinitely. - There is an error in the premises (misinterpretation of Marla's

intent). Given these points, the appropriate classification is: CORRECT CONCLUSION FROM FALSE PREMISES

Error Category Label: "Correct Conclusion from False Premises"

Table 3: Example of reasoning step (premise) and conclusion evaluated by LLM-based 'Auto-evaluator' (GPT-40). The error category labels are extracted from the detailed explanations using an LLM prompted to extract error keywords.

Model	S (†)	A (†)	C (†)
Mistral-7B-v2-Instruct	0.623	0.371	0.131
Llama-3-8B-Instruct	0.493	0.451	0.137
GPT-3.5-turbo	0.607	0.417	0.217
GPT-4-turbo	0.738	0.725	0.417
GPT-40	0.784	0.737	0.445

Table 4: The results for soundness, accuracy, and correctness metrics for all LLMs on the *Civ. Pro.* dataset. Here 'S' denotes the Soundness, 'A' denotes the Accuracy, and 'C' denotes the Correctness.

error-free reasoning steps and arrive at the correct conclusion more often than the open-source LLMs. An exception is GPT-3.5-turbo, which performs comparably to Llama-3-8B-Instruct and Mistral-7B-v2-Instruct, suggesting that training data and methods might play a more significant role in enhancing reasoning than merely scaling model parameters.

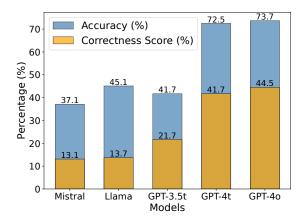


Figure 4: Performance of 5 LLMs in terms of Accuracy vs. Correctness on the *Civ. Pro.* dataset. Here, Mistral stands for Mistral-7B-v2-Instruct, Llama stands for Llama-3-8B-Instruct, GPT-3.5t and GPT-4t stand for GPT-3.5-turbo and GPT-4-turbo respectively.

Prompting	В	PS	SC	SD
Gemini w/o feedback w/ feedback	63.31 64.50	59.17 62.13	61.54 59.76	64.50 63.31
Llama w/o feedback w/ feedback	53.71 57.14	50.29 52.00	48.58 52.57	47.42 49.14

Table 5: Comparison of accuracy for models under different prompting strategies with and without feedback. The models are Gemini-1.5-Flash and Llama-3-8B-Instruct. B: Baseline (CoT), PS: Plan-and-Solve, SC: Self-Correct, and SD: Self-Discovery.

5.2 Reasoning Chain Evaluation

'Misinterpretations' are the dominant category of errors at premise-level Figure 5 (Appendix C) and Figure 12 reveal that 'Misinterpretation' is the most dominant category of error which occurs in the reasoning chains at the premise-level. This indicates that LLMs struggle to fully grasp the nuanced complexities of legal scenarios requiring the demonstration of critical analysis in zero-shot CoT.

'Wrong Conclusion from False Premises' is the dominant category of error at conclusion-level The prevalence of 'Wrong Conclusion from False Premises' (Figure 6 (Appendix D)) in conclusionlevel errors results from premise-level mistakes leading to incorrect conclusions. However, in GPT-4-turbo and GPT-4o, the dominant error is 'Correct Conclusion from False Premises,' suggesting these models may be relying on patterns of similar examples from their training.

5.3 Discussion on Error-Mitigation Strategies

We carry out several experiments on the *Civ. Pro.* dataset, employing widely used prompting techniques alongside the most frequently observed errors we found through §3.3 with the aim to explore the possibility of enhancing the reasoning capabilities of both closed-source and open-source LLMs. Four prompting techniques are utilized: (1) Chainof-Thought (Wei et al., 2022) (2) Plan-and-Solve (Wang et al., 2023) (3) Self-Correct (Zhang et al., 2024) and (4) Self-Discovery (Zhou et al., 2024). These techniques are tested with and without incorporating error definitions as feedback, following the Feedback-Learning method (Tyagi et al., 2024b). Detailed descriptions of the prompting strategies can be found in Appendix L.

The error definitions are provided in three styles: generic, short, and long. The generic version uses the error definitions from the Feedback-Learning method, while the short and long versions are derived from the error taxonomy described in §3.3. All experiments are conducted in a zero-shot setting, and we evaluate each prompting technique based on the accuracy metric. We test one closedsource model, Gemini-1.5-Flash, and one opensource model, Llama-3-8B-Instruct.

As shown in Table 5, adding the error definitions as feedback showed improvement in accuracy up to 4%. For Llama-3-8B-instruct, accuracy improved across all prompting techniques, whereas for Gemini-1.5-Flash, the accuracy increased only for the Chain-of-Thought and Plan-and-Solve methods. From our observations, the decrease in accuracy for these strategies with Gemini resulted due to self-doubting (Krishna, 2023) nature of LLMs. These findings suggest that while feedback on errors provides marginal improvements in LLM performance, there is a need to develop more effective frameworks beyond prompting, such as agentbased methods, that account for these errors and enhance the model's legal reasoning capabilities.

6 Conclusion

Through our work, we assess the reasoning capabilities of LLMs by examining their performance on the '*Civ. Pro.*' dataset designed to evaluate legal reasoning. The sequential workflow of manually evaluating LLM-generated reasoning chains on data samples, creating an error taxonomy based on the commonly occurring errors, automating the error evaluation through LLM-based pipelines lead us to some interesting insights. LLMs still struggle with producing error-free rationales while reasoning about legal scenarios despite being provided with necessary legal knowledge and context. Additionally, we present our findings on implementing various prompting techniques augmented with feedback from our error taxonomy. We hope that our work lays a solid foundation for developing a framework to critically evaluate complex reasoning tasks, such as legal reasoning, and is extendable to other domains in a similar manner.

Limitations

While the Civ. Pro. dataset provides a valuable benchmark for assessing the legal reasoning capabilities of LLMs, real-world legal reasoning-particularly in the context of legal judgment prediction-is inherently ambiguous. Legal cases often evolve over time, with new information emerging throughout the litigation process. Consequently, evaluations based on static datasets that capture information at a single point in time may not fully reflect the dynamic nature of legal decision-making, limiting their effectiveness in assessing real-world legal reasoning. There are many legal scenarios in this dataset that are complex in terms of being ambiguous and tricking the reader/reasoner and would probably require legal expertise and experience to understand the nuances required to solve such scenarios. Although our study intends to capture the errors committed by natural-language-based reasoners, the systematic evaluation could benefit from converting natural language to formal language through autoformalization. While our work mainly focuses on the soundness of the reasoning steps of legal reasoning chains, we would like to acknowledge that properties like consistency, coherence, completeness, and clarity are not directly measured in the current work. Furthermore, the current evaluation of reasoning is restricted to English, leaving room to expand this work into a multilingual context.

Ethics Statement

We obtained the necessary permissions to use the dataset provided by Bongard et al. (2022). We have utilized AI assistants, specifically Grammarly and ChatGPT, to correct grammatical errors and rephrase sentences.

Acknowledgement

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A Metrics Results from human evaluations

Table 6 shows the statistics of the metrics calculated on the reasoning-chains directly by humans. The results show a marked difference in the values of Accuracy and Correctness across all LLMs manually evaluated by human evaluators. The results in Table 4, calculated from the LLM-based autoevaluator annotations, also reflect the same trends in this table.

LLM	S (†)	A (†)	C (†)
Mistral-7B-v2-Instruct	0.67	0.266	0.133
Llama-3-8B-Instruct	0.718	0.433	0.266
GPT-3.5-turbo	0.69	0.33	0.233
GPT-4-turbo	0.748	0.6	0.5

Table 6: The results for soundness, accuracy, and correctness metrics for the same 30 LLM reasoning-chain generations across 4 LLMs by human annotators. Here 'S' denotes the Soundness, 'A' denotes the Accuracy, and 'C' denotes the Correctness. The values marked in bold show the highest metric values.

B Manual Evaluation results

Tables 8 and 9 show the statistics of the errors found by human evaluators in the premise and conclusion levels based on the process described in §3.2 and in accordance to the proposed error taxonomy in §3.3.

LLM	Average number of steps
Mistral-7B (893)	5.1
Llama-3-8B (642)	3.66
GPT-3.5-turbo (649)	3.70
GPT-4-turbo (811)	4.63
GPT-4o (974)	5.56

Table 7: The average number of steps(premises) generated by all LLMs in Zero-shot CoT setting. The numbers in brackets indicate the total number of steps generated by each LLM in the generated reasoning chains (excluding the final conclusion step) for the 175 sample *Civ. Pro.* dataset

C Percentage distribution of Premise-level errors

Figure 5 represents the percentage distribution of premise-level errors across the reasoning chains of all 5 LLMs. Due to the lowest number of average steps in reasoning steps, Llama-3-8B-instruct has the highest proportion of errors in the reasoning

chains ($\sim 65.4\%$) containing premise-level errors in the reasoning steps.

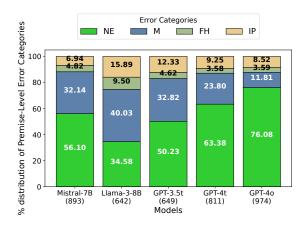


Figure 5: The percentage distribution of the premiselevel error categories across the reasoning chains of all 5 LLMs. The total number of steps generated by each model is provided inside the round brackets below the model names. Here 'NE' denotes Correct Premise (No errors), 'M' denotes Premise containing a Misinterpretation, 'FH' denotes Factual Hallucination in the premise, 'IP' denotes an Irrelevant Premise.

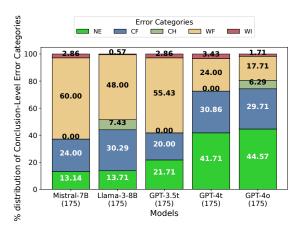


Figure 6: The percentage distribution of the conclusionlevel error categories across the reasoning chains of all 5 LLMs. The total number of steps generated by each model is provided inside the round brackets below the model names. Here 'NE' denotes Correct Conclusion(CC) From Correct Premises(CP) (No errors), 'CF' denotes CC from False Premises (FP), 'CH' denotes CC with Hallucinated Content, 'WF' denotes Wrong Conclusion(WC) from FP and 'WI' denotes EC from Incomplete Premises.

D Percentage distribution of Conclusion-level errors

Figure 6 represents the percentage distribution of conclusion-level errors across the reasoning chains

LLM	Error Categories and Frequency
Mistral-7B-v2-Instruct (135 reasoning steps)	NE - 94, M - 31, FH - 6, IP - 4
Llama-3-8B-Instruct (145 reasoning steps)	NE - 114, M - 29, FH - 1, IP - 2
GPT-3.5-turbo (109 reasoning steps)	NE - 77, M - 30, FH - 1, IP - 0
GPT-4-turbo (148 reasoning steps)	NE - 120, M - 25, FH - 0, IP - 2

Table 8: Statistics on various types of errors identified by human evaluators in the premises of 30 reasoning chains generated by each of the four LLMs. The total number of reasoning steps generated by each LLM is indicated in parentheses. 'NE' denotes the absence of errors in the reasoning steps as annotated by human evaluators, 'M' represents 'Misinterpretation' errors, 'FH' indicates 'Factual Hallucination,' and 'IP' signifies 'Irrelevant Premises.'

LLM	Error Categories and Frequency
Mistral-7B-v2-Instruct (30 conclusion steps)	NE - 3, CCFP - 2, CCIP - 1, CCHC - 2, WCFP - 18, WCIP - 3
Llama-3-8B-Instruct (30 conclusion steps)	NE - 9, CCFP - 4, CCIP - 0, CCHC - 1, WCFP - 13, WCIP - 3
GPT-3.5-turbo (30 conclusion steps)	NE - 7, CCFP - 2, CCIP - 0, CCHC - 0, WCFP - 17, WCIP - 4
GPT-4-turbo (30 conclusion steps)	NE - 16, CCFP - 1, CCIP - 0, CCHC - 0, WCFP - 11, WCIP - 1

Table 9: Statistics on various errors identified by human evaluators in the conclusions of 30 reasoning chains generated by each of the four LLMs. 'NE' represents the absence of errors in the conclusion as annotated by human evaluators, 'CCFP' denotes 'Correct Conclusion from False Premise(s),' 'CCIP' indicates 'Correct Conclusion from Incomplete Premise(s),' 'CCHC' refers to 'Correct Conclusion with Hallucinated Content,' 'WCFP' signifies 'Wrong Conclusion from False Premise(s),' and 'WCIP' represents 'Wrong Conclusion from Incomplete Premise(s).'

of all 5 LLMs. Mistral-7B-v2-instruct (\sim 86.8%) and Llama-3-8B-instruct (\sim 86.3%) have the highest proportion of errors in the reasoning chains containing conclusion-level errors. An interesting observation is that only Llama-3-8B instruct and GPT-40 have non-zero percentages of errors in the category of Correct Conclusion with Hallucinated Content, which could possibly mean that these LLMs have been trained on very similar data to that in the '*Civ. Pro.*' dataset which could be causing these LLMs to spuriously output modified content for the correct options.

E Average number of steps generated by LLMs

The average number of steps (the premise-level steps) generated by each LLM to solve a legal scenario is provided in Table 7. Llama-3-8B-instruct has the lowest average of number of steps which is a probable cause leading to lower soundness score as shown in Table 4. Overall, LLMs mostly try to complete the reasoning chain in around 4-6 steps to arrive at the conclusion. While this is good for not introducing redundancies and keeping the irrelevant premise and hallucination errors low, this could also potentially be an indicator that LLMs do not explicitly output tokens which could be crucial in outlining the reasoning process and making the rationale better in terms of interpretability and explainability.

F Misinterpretations vs. Factual Hallucinations vs. Irrelevant Premises

A premise is classified as containing a 'Misinterpretation' error when the LLM reasoner is making wrong inferences based on the information it generates. There is a 'Factual Hallucination' when the information generated by the LLM reasoner (by directly extracting from the provided content of the input legal context, questions, and options) is factually incorrect and can be easily verified while directly going through the input context. A key distinction between Misinterpretation and Factual Hallucination is illustrated in Figures 14 and 15. Detecting a 'Misinterpretation' requires the expert answer to account for complex legal reasoning nuances, while detecting a 'Factual Hallucination' does not depend on the expert answer for validation. An irrelevant premise is said to occur when a premise contains unnecessary or tangential information that does not contribute to reasoning toward the correct answer.

Extensive discussions and iterations occurred to define the taxonomy and differentiate between the three premise-level errors. However, these errors can often overlap or appear together in the same premise, especially in cases where 'Misinterpretations' are caused by 'Factual Hallucinations'. In the cases of significant overlap, both the human and the auto-evaluator were instructed to annotate multiple errors for the same premise. Detecting multiple errors can be crucial for longer premises which creates inferences on a greater number of contextual factors and nuances and hence are vulnerable to more of errors occurring in them.

G Human Annotation Guidelines and Process

A set of 11 annotation guidelines, as detailed in Figure 9, was developed and provided to annotators for manual evaluation and annotation. Four annotators, two students from undergraduate and graduate level each respectively, participated in this process, and cross-evaluation was conducted at the final stage to resolve any discrepancies. The annotation guidelines in Figure 9 also served as the basis for creating system prompts used in the LLM-based auto-evaluator.

As an additional study to check for interannotator agreement, three annotators separately annotated 10 reasoning chains from Mistral-7Bv2-Instruct and the calculated the Cohen's kappa coefficient (κ). The κ values for the 3 annotator pairs (by selecting 2 unique annotators out of 3 everytime) came out to be 0.862, 0.783 and 0.813, making the average κ value to be 0.819. This indicated there is almost perfect agreement between the annotators according to Cohen's kappa metric interpretation.

H Human Annotation Examples

Initially, Mistral-7B-v2-Instruct was selected for human evaluation due to its unique position as the earliest and smallest parametric model among the LLMs tested. Its smaller size increases the likelihood of it producing a wider range of reasoning and contextual errors, making it an ideal candidate for error analysis. By starting with a model that has fewer parameters and is more prone to subtle reasoning gaps, we can thoroughly evaluate and better understand the types of errors that may occur. This approach maximized the chances of capturing diverse error types that could be missed in larger, more sophisticated models, which tend to exhibit fewer surface-level mistakes. Table 7-11 contain few examples of human analysis of complexity of legal reasoning and error annotations performed for the reasoning chains. The text written in blue font in the tables represents the human analyses and annotations performed.

I The LLM-based 'Auto-Evaluator'

Rationale behind using LLM-based Auto-**Evaluator:** The primary rationale for employing an LLM-based auto-evaluator is its scalability and efficiency compared to human annotation. While human evaluators required approximately 30-60 minutes per reasoning chain to accurately identify and categorize errors in the 'Civ. Pro.' dataset, the auto-evaluator can process large volumes of reasoning chains significantly faster and at a lower cost. This efficiency becomes even more critical in real-world legal contexts, where expert reviews demand extensive time and resources. Modern LLMs, trained on vast amounts of data (including legal texts), demonstrate state-of-the-art performance in natural language understanding and reasoning. Although our results and analyses show that LLMbased reasoning systems are not yet fully errorfree, the rapid improvements in LLM reasoning capabilities and the decreasing costs of inference make them a promising solution for scalable, costeffective error detection.

Implementation: At the premise level, four separate prompt-based evaluation pipelines (LLM-based error detectors) have been implemented. Three of the pipelines utilize a single call to GPT-40, where the information provided to the LLM is broken into three parts: a. The system prompt which contains the information about the error taxa (**the knowledge base**) b. **important instructions** provided to the LLM evaluator on how to evaluate and detect errors and c. We also provide an **in-context learning example** of how the human annotation was carried out for the model to follow and replicate the annotation format.

The first pipeline (Figure 17) is designed to simply detect whether a premise contains an error, without assigning a specific label from the error taxonomy. The second pipeline detects whether a premise contains a 'Misinterpretation' error. The third pipeline does the same for detecting an 'Irrelevant Premise'. Along with this, the input prompt includes the step-by-step reasoning chain. The LLM is expected to classify the error and provide an explanation for the classification. The fourth pipeline 15, which has been designed to detect 'Factual Hallucination' errors, consists of a 'Multi-call' LLM system where primarily two calls to GPT-40 are made: 1. The first call to GPT-40 is used to create fact-verification questions about various aspects of a particular premise. 2. The second call to GPT-40 is used to answer these verification questions by referencing the legal context and content of the questions and the options. A premise is classified as containing factual hallucination(s) if the answers to its verification questions reveal a contradiction between its content and that of the provided input context. The premise-wise evaluation results of four pipelines are aggregated and summarized by a final 'summarization' call to GPT-40 which summarizes and enumerates all possible errors detected in a single premise. The aggregated and summarized results are then sent to the conclusion-level error evaluator which performs a conditional mapping procedure (as shown in Figure 16 to assign the conclusion-level errors.

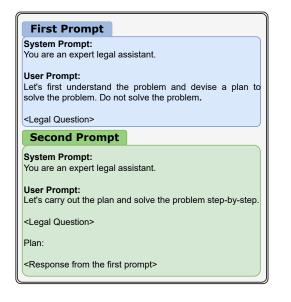


Figure 7: Prompt used to implement 'Plan-and-Solve' technique.

GPT-40 (Refer Figure 17) was used to aggregate and summarize all the errors detected by the separate premise-level error detectors and summarize them for each premise separately. This had a corrective effect as the most appropriate errors (or combination of multiple errors) were summarized for each premise. An example of this corrective effect is shown in Figure 19, where both the 'Misinterpretation' and 'Factual Hallucination' auto-evaluators flag a premise with their respective labels and explanations. However, the summarizer LLM correctly identifies 'Misinterpretation' as the most accurate error classification for that premise. The LLM also filtered out unnecessary text, retaining only the premises that contained errors. This process ensured that only the premise steps flagged

with errors by the auto-evaluator were forwarded as input to the conclusion-level error analyzer. By focusing on the erroneous premises, this approach streamlined the error analysis process, enabling more efficient and targeted evaluation of how these errors impact the final conclusion.

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	User Prompt:	
	User Prompt: <legal question=""></legal>	
specifically about the task. Do not simply rephrase the keys:	User Prompt: <legal question=""> Follow the step-by-step</legal>	

Figure 8: Prompt used to implement 'Self-Discovery' technique.

J Auto-Evaluator Effectiveness

Based on the errors found in the reasoning chains by human evaluators (as shown in Tables 8 and 9), the effectiveness of GPT-4o-based auto-evaluator was measured using agreement of step-level presence or absence of errors at both the premise and conclusion level (refer Tables 10 and 11). Agreement occurs only when both correct error category and matching error description is generated by the auto-evaluator through semantic error explanation match (refer §3.4). Recall metric was chosen as the appropriate measure for agreement as it is crucial to identify if the auto-evaluator correctly identified an error in a premise or conclusion level step. The recall percentage of detecting an error at the premise level across four LLMs ranged from 86.17% to 93.85%. The recall percentage range for detecting an error-free premise step was from 83.87%to 90.6% (refer Table 10). Similarly, at conclusion level, the average recall percentages ranges on agreement on the presence and absence of errors are mentioned in Table 11. The current autoevaluator system cannot detect 'Correct Conclusion from Incomplete Premise(s)' (CCIP), as it cannot distinguish it from a 'Correct Conclusion from Correct Premises' scenario. While this is a drawback, the 'CCIP' error is very rare in its occurrences as an error category.

11-step Annotation Guideline		
 Go through the provided annotation example thoroughly. In the step-by-step reasoning chain, all the intermediate steps (from the first step to the penultimate step) are termed as 'premises' and final step/statement which concludes the chain by choosing an option is termed as the 'conclusion'. 		
3. Take your time to refer to the error categories described in the Error taxonomy provided to you.		
4. The errors in the premises are ' premise-level ' errors and the error in the conclusion is the ' conclusion-level ' error.		
5. If a premise contains multiple errors from the error-taxonomy, then label it with all the errors possible.		
6. Refer to the expert answers provided by the authors of the questions to double-check your error classifications.		
 Please remember to follow this order for error classification: First, analyze and annotate errors at the premise level, and then proceed to annotate errors at the conclusion level. 		
8. Based on the presence of errors in the premises, classify the error in the conclusion into one of the sub-categories of conclusion-level errors present in the error taxonomy.		
9. Additionally, compare the content of the conclusion (the content of the option generated by the LLM reasoner while choosing them from one of the provided options as answers to the question) to check for 'Right Conclusion with Hallucinated Content' error.		
10. Double-check if your error classification is the most appropriate one. 11. While the task is focused on identifying errors in the reasoning-chain rationale rather than solving the legal question itself, you are		
encouraged to independently attempt referring to the legal context and solving the question to enhance your understanding of the legal scenario.		
scenario.		

Figure 9: The 11-step guideline provided to the annotators for conducting manual evaluations of the LLMgenerated rationale

K The 'Aggregator + Summarizer' LLM

Furthermore, we conducted another experiment, replacing GPT-40 with Gemini-1.5-Flash as the backbone LLM for the auto-evaluator system. The prompts provided to auto-evaluator system were unchanged. The recall rate of identifying an error in the reasoning step at the premise-level for Geminibased auto-evaluator on the Mistral-7B-v2-Instruct

First Prompt

System Prompt:

You are an excellent legal assistant. However, we have analyzed how you solve the legal reasoning question before and we found that you make the following mistakes more often while reasoning:

- 1. Hallucination....
- 2. Misinterpretation....
- 3. Irrelevant Premise....

Now, you understand how to identify and remove such errors. Using all the above knowledge, please solve the question step-by-step.

User Prompt:

Let's first understand the problem and devise a plan to solve the problem. Do not solve the problem.

<Legal Question>

Second Prompt

System Prompt: You are an expert legal assistant.

User Prompt:

Let's carry out the plan and solve the problem step-by-step.

<Legal Question>

Plan:

<Response from the first prompt>

Figure 10: Prompt used to implement 'Plan-and-Solve with error feedback' technique. Error feedback can be added to other prompting strategies in the same way.

generated reasoning chains, when compared with human annotations, was found out to be \sim 78.1%. The recall-rate for identifying correct premise-level reasoning steps highly decreased to \sim 20.61%. This indicates that Gemini-1.5-Flash, while comparable to GPT-40 in identifying errors, was less effective overall as an auto-evaluator due to a higher number of false-negative predictions (with larger number of error-free steps were incorrectly identified as containing errors). Although fine-tuning and testing a dedicated LLM for error detection was not conducted in this study, the authors acknowledge it as an interesting avenue for future improvements and research directions.

L Prompting-techniques for Error Mitigation

We carried out several experiments on the legal reasoning dataset, employing widely used prompting techniques alongside the most frequently observed errors we found through §3.3 with the aim

LLM	Statistics	Agreement % (Recall)
Mistral-7B-v2-Instruct (135) Llama-3-8B-Instruct (145) GPT-3.5-turbo (109) GPT-4-turbo (148)	CC = 81, NC = 13, EE = 35, NE = 6 CC = 107, NC = 7, EE = 26, NE = 5 CC = 69, NC = 8, EE = 29, NE = 3 CC = 104, NC = 16, EE = 25, NE = 3	$\begin{split} R(C) &= 81/94 = 86.17\%, \ R(E) = 35/41 = 85.3\% \\ R(C) &= 107/114 = 93.85\%, \ R(E) = 26/31 = 83.87\% \\ R(C) &= 69/77 = 89.61\%, \ R(E) = 29/32 = 90.6\% \\ R(C) &= 104/120 = 86.66\%, \ R(E) = 25/28 = 89.2\% \end{split}$

Table 10: Agreement statistics between the GPT-4o-based auto-evaluator and human evaluators for the same 30 reasoning chains at the premise level across four LLMs (refer to Table 8). Numbers inside parentheses denote the total number of premise-level reasoning steps evaluated. 'CC' represents agreement between the auto-evaluator and human evaluators on the absence of an error in a reasoning step, while 'NC' denotes disagreement on the absence of an error. 'EE' indicates agreement on the presence of an error, and 'NE' denotes disagreement on the presence of an error. 'R(C)' refers to the recall percentage for agreement on error-free steps between the auto-evaluator and human evaluators, whereas 'R(E)' denotes the recall percentage for agreement on steps containing errors.

LLM	Statistics	Agreement % (Recall)
Mistral-7B-v2-Instruct (30) Llama-3-8B-Instruct (30) GPT-3.5-turbo (30) GPT-4-turbo (30)	CC = 3, NC = 1, EE = 22, NE = 4 $CC = 9, NC = 0, EE = 20, NE = 1$ $CC = 4, NC = 3, EE = 21, NE = 1$ $CC = 12, NC = 4, EE = 13, NE = 1$	$\begin{array}{l} R(C) = 3/4 = 75\%, R(E) = 22/26 = 84.61\% \\ R(C) = 9/9 = 100\%, R(E) = 20/21 = 95.23\% \\ R(C) = 4/7 = 57\%, R(E) = 21/22 = 95.45\% \\ R(C) = 12/16 = 75\%, R(E) = 13/14 = 92.85\% \end{array}$

Table 11: Agreement statistics between the GPT-4o-based auto-evaluator and human evaluators for the same 30 reasoning chains at the conclusion level across four LLMs (refer to Table 9). 'CC' represents agreement between the auto-evaluator and human evaluators on the absence of an error in a conclusion, while 'NC' denotes disagreement on the absence of an error. 'EE' indicates agreement on the presence of an error, and 'NE' denotes disagreement on the presence of an error. 'R(C)' refers to the recall percentage for agreement on error-free conclusions between the auto-evaluator and human evaluators, whereas 'R(E)' denotes the recall percentage for agreement on conclusions containing errors.

to explore the possibility of enhancing the reasoning capabilities of both closed-source and opensource LLMs. Four prompting techniques were utilized: (1) Chain-of-Thought (Wei et al., 2022) (2) Plan-and-Solve (Wang et al., 2023) (3) Self-Correct (Zhang et al., 2024), and (4) Self-Discovery (Zhou et al., 2024). We used the zero-shot CoT (Figure 19) method as the baseline method in which the LLM is prompted to provide the final answer along with step-by-step reasoning.

Plan-and-Solve prompts the LLM first to generate a plan to solve the problem without solving it and after that the LLM carries out the selfsuggested plan to get the final answer as shown in Figure 7. Self-Correct uses self-verification and self-refining to improve the reasoning ability of the LLMs as shown in Figure 11. Self-Discover as shown in Figure 8 utilizes self-discover reasoning modules to create an explicit reasoning structure to follow to solve the problem. For running the above prompting strategies with error taxonomy as the feedback, we include a detailed description of the error taxonomy in the system prompt. For instance, Plan-and-Solve with error feedbacks is shown in Figure 10.

Model	Zero-shot(↑)	Few-shot(↑)
Llama-3.1-8B-Instruct	53.71	52.87
Llama-3.1-70B-Instruct	76.74	71.51
GPT-40	82.56	80.23

Table 12: The zero-shot and few-shot results of LLMs in CoT setting.

M Few-shot prompting on performance of LLMs

We evaluated the performance of several large language models (LLMs) on a set of legal reasoning questions using zero-shot and few-shot prompting, as well as chain-of-thought (CoT) prompting. For Llama models, we used one example and for other we used 3 examples in few-shot training. Our results indicate that LLMs perform best in the zeroshot setting, where no in-context examples are provided. We hypothesize that the diverse nature of legal reasoning questions limit the effectiveness of in-context learning, as it restricts the model's ability to generalize beyond the provided examples.

First Prompt

System Prompt: You are an expert legal assistant.

User Prompt:

<Legal Question>

Second Prompt

System Prompt: You are an expert legal assistant.

User Prompt: Let's verify the solution of the given question below and suggest some corrections.

<Legal Question>

Solution:

<Response from the first prompt>

Third Prompt

System Prompt: You are an expert legal assistant.

User Prompt: Now let's use the suggestions to solve the question again.

<Legal Question>

<Suggested corrections>

Figure 11: Prompt used to implement 'Self-Correct' technique.

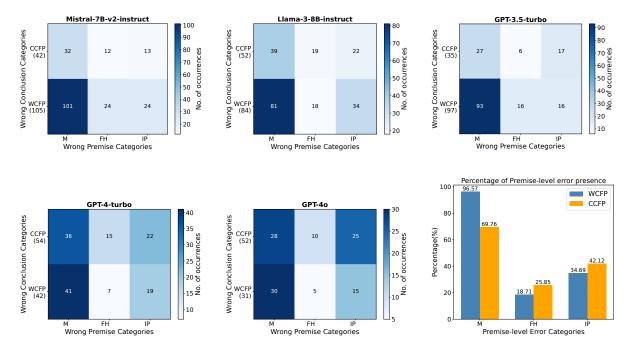


Figure 12: The first five sub-figures in the preceding section display the error distribution for premise-level errors in instances where the conclusion contains an error, across five different LLMs. The dimension in the x-axis represents the categories of errors at the premise level. The dimension in the y-axis represents the errors at the conclusion level. Here 'M' denotes 'Misinterpretation', 'FH' denotes Factual Hallucination, 'IP' denotes Irrelevant Premise, 'WCFP' denotes Wrong Conclusion from False Premise(s), and 'CCFP' denotes Correct Conclusion from False Premises. Here the counts in the heatmap represent the presence of one (or more) premise-level error(s) (in the x-axis) in a reasoning chain containing the specified conclusion-level error (in the y-axis)

System-Prompt

You are an expert in identifying errors in provided reasoning chains. Specifically, these reasoning chains are obtained from a legal MCQA task. From the reasoning chain, you have to classify each reasoning step with the presence/absence of a misinterpretation error in the step. You also have to explain why a step is classified as such. If you do not find any misinterpretation error in reasoning step, assign "NO MISINTERPRETATION" label to it. To understand some errors which can occur, please refer to provided knowledge base. While finding errors in provided reasoning chains, you can refer to gold-standard reasoning chain for better understanding.

Instruction

Trigger:

e user submits a legal context, question and options and reasoning chains 1 and 2. Reasoning Chain 1 is the gold-standard answer. Reasoning Chain 2 is the reasoning chain provided by a LLM to solve the question.

Instructions:

Take your time to reiterate the clues given in the legal problem. Follow these IMPORTANT POINTS given below:

1. Keep in mind that in the reasoning chain, only final statement with the final answer is the conclusion. All preceding statements are premises

2. You have to find the errors of misinterpretations in the premises, not the conclusion

3. Assign the most appropriate type of misinterpretation in reasoning chain 2. If there is no fitting type, assign the **NO MISINTERPRETATION** category.

Knowledge-Base

This Knowledge Base contains the types of misinterpretations predominantly committed by Large Language Model(LLM) based Reasoners while generating reasoning chains.

Misinterpretation is the error where the LLM misinterprets some part or entirety of the legal context or the question provided to it.

This can occur due to ambiguities, limitations in the model's training, or the complex nature of language. Misinterpretation can affect the reliability of the model's output, leading to incorrect information and reasoning.

Misinterpretation errors can occur in the following ways

 Failing to consider some important aspects of the given context, leading to a misunderstanding. Example: Misunderstanding a sarcastic comment as a serious statement because the

context of sarcasm was missed.

2. Misinterpreting the logical relationship between ideas, such as cause and effect, or failing to follow an argument's reasoning correctly. Example: Assuming that correlation implies causation

3. Misunderstanding the meaning of a word or phrase. Example: Confusing homophones like "bare" and "bear."

4. Drawing incorrect inferences from the prior-generated text by LLMs. Example: Inferring that someone is angry based on their terse email, when they were simply in a hurry.

5. Misunderstanding, specifically, numerical data, statistical information or mathematical

concepts. Example: Misinterpreting percentages or probability, like thinking that a 30% chance of rain means it will rain 30% of the time.

6. Misunderstanding the timing or sequence of events. Example: Misinterpreting past events as future intentions or vice versa

7. Misunderstanding specialized terminology used within a particular field. Example: Misinterpreting medical jargon without the proper context or knowledge.

Structure of Response and Annotation Example

Suppose if there are 2 premises and 1 conclusion in reasoning chain 2, structure your response in the following way: Premise 1: <Content of premise 1> Error Category: [MISINTERPRETATION/NO MISINTERPRETATION] Explanation: <Justify your error category> Premise 2: <Content of premise 2> Error Category: [MISINTERPRETATION/NO MISINTERPRETATION] Explanation: <Justify your error category>

Conclusion: <Content of Conclusion> Error Category: [Conclusion is not Checked for Misinterpretations] Explanation: <Conclusion is not Checked for Misinterpretations>

Figure 13: Prompt structure for LLM evaluator 2 from Figure 17. Appropriate Instructions and Knowledge Base for detecting 'Misinterpretation' errors are provided in the prompt. Similar prompt structures and appropriate knowledge bases have been provided to all other LLM-based evaluators.

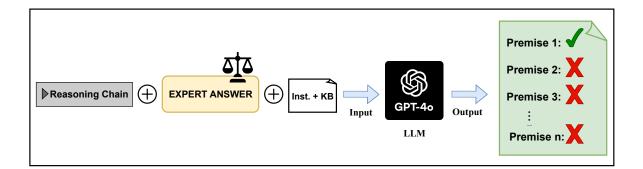


Figure 14: Schematic representation of the 'Single-Call' LLM-based auto-evaluator for premise-level error detection. 'Inst + KB' includes instructions for error analysis and the knowledge base with error definitions, based on the proposed error taxonomy. The green check-mark indicates the absence of errors and the red cross-mark represents the presence of an error in a premise.

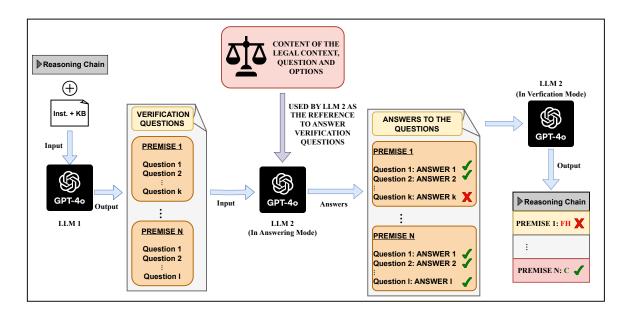


Figure 15: Schematic representation of the 'Multi-Call' LLM-based auto-evaluator for 'Factual-Hallucination' error detection. 'Inst + KB' includes instructions for error analysis and the knowledge base with error definitions, based on the proposed error taxonomy. The green check-mark indicates the verification question being correctly answered and the red cross-mark represents the presence of a contradiction in the content of the premise with the provided context.

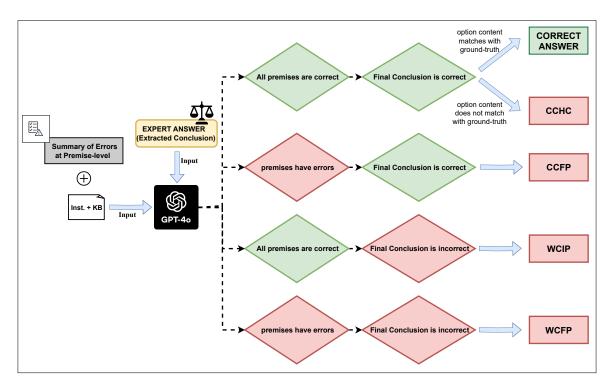


Figure 16: Schematic representation of the LLM-based auto-evaluator system for error detection at conclusion-level. The GPT-40 LLM represents the 'LLM evaluator 5' in Figure 17. The dotted lines represent the conditional paths of which only one will be true and lead to respectively conclusion-level error being labelled to the conclusion, Here, 'CCHC' represents 'Correct conclusion with Hallucinated Content, 'CCFP' represents 'Correct Conclusion from False Premises', 'WCIP' represents 'Wrong Conclusion from Incomplete Premises' and 'WCFP' represents 'Wrong Conclusion from False Premises'.

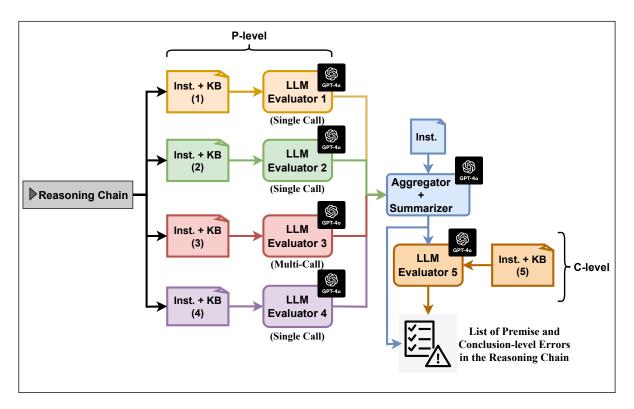


Figure 17: Schematic representation of the LLM-based auto-evaluator system for error detection. 'Inst + KB' with their respective numbers in brackets includes instructions for error analysis and the knowledge base with error definitions, based on the proposed error taxonomy. An example prompt structure (for LLM evaluator 2) has been shown in Figure 9. Here, 'P-level' denotes the Premise-level, and 'C-level' denotes the Conclusion-level. The schematics of the 'Single-Call' and 'Multi-call' GPT-40 LLM-based evaluators are represented in Figure 14 and 15 respectively.

Legal Context and Question

The Due Process Clause of the Fourteenth Amendment prohibits a state from depriving a person of life, liberty, or property without due process of law. When a court enters a civil judgment against a person, it begins the process of taking the person's property (usually in the form of money). Consequently, the due process clause requires the court to use a fair procedure in entering judgment. Certainly, one component of a fair procedure is to tell the defendant that the court is going to adjudicate her rights. Hence, the Due Process Clause requires a court to use a constitutionally adequate means of notifying the defendant that a lawsuit has been commenced against her. Typically, it is the plaintiff who does the legwork of serving process on the defendant. The statutes or court rules in every state contain detailed provisions governing how this notice of a lawsuit is provided to the defendant. Court rules may authorize various means of serving process. The most obvious is to deliver the initiating papers in the case to the defendant in person, called "personal service of process." Other methods are often authorized as well, though they are less certain to actually inform the defendant about the suit. The service rules may provide, for example, that the papers may be left with someone at the defendant's home or place of business or slipped under the door. Some authorize service to the defendant by certified or ordinary mail. In some circumstances, court rules or statutes may authorize service by publication, by printing a notice of the suit in the legal notices in the local newspaper for several weeks. Such publication notice is sometimes referred to as "constructive service," as opposed to actual delivery of the papers to the defendant. Which of these methods is constitutionally adequate under the Due Process Clause? Justice Jackson's wise opinion in Mullane v. Central Hanover Bank & Trust Co., 339 U.S. 306 (1950) does not provide a mechanical answer to that question, but instead establishes broad standards for constitutionally adequate notice. Mullane involved a device called a common trust fund, which allowed a bank to pool a group of small trusts into one common fund, which could be managed more efficiently. Income (or losses) from the trust would then be shared by each smaller trust in proportion to their contributions to the fund. Periodically, the trustee of the fund would file accounts with the court. If the court approved the accounts, its judgment would bar investors from suing the bank for mismanagement. Since this judicial accounting could deprive trust beneficiaries of property-the right to sue the bank for mismanagement-due process required adequate notice to them of the proceeding. The problem in Mullane was that it was difficult to ascertain who all the beneficiaries were. Beneficiaries currently entitled to receive income from the trust were known, and the bank had their addresses in its files. But most trusts have contingent beneficiaries, such as the children or heirs of a beneficiary if the primary beneficiary dies. The bank might not know who these beneficiaries were, and they could change periodically. Perhaps, with a large investment of time by lawyers and investigators, the bank could identify most them, but doing so would eat up the profits of the common trust fund. Many were contingent beneficiaries; that is, they had no current right to receive income from the fund but might become vested beneficiaries later under the terms of the individual trusts. So who did the bank have to tell about the suit and how? Mullane held that "an elementary and fundamental requirement of due process in any proceeding which is to be accorded finality is notice reasonably calculated, under all the circumstances, to apprise interested parties of the pendency of the action and afford them an opportunity to present their objections." 339 U.S. at 314. What is reasonable in one circumstance would not necessarily satisfy due process in another. On the facts of Mullane, several factors reduced the risk of error if notice failed to reach all beneficiaries. First, the statute provided for the appointment of a guardian in the settlement proceeding to represent the interests of all beneficiaries. Second, even if all beneficiaries did not receive notice of the proceeding, many would, and would likely share and represent the interests of all beneficiaries in the settlement of the accounts. Consequently, the Court in Mullane did not require that each individual with an interest in the fund be given personal notice of the action. The question below probes what it did require.

Question:

In Mullane v. Central Hanover Bank & Trust Co., the Supreme Court held that

Options:

A. every person whose interests may be affected by a judicial proceeding is entitled to at least mail notice of the proceeding.

B. every person whose name and address could be ascertained through reasonable investigation must be given individual notice of the proceeding.

C. any person whose interests might be affected by the proceeding must be given notice by in-hand service of process.

D. due to the large number of persons whose interests might be affected by the proceedings, notice by publication was sufficient on the facts of the case.

E. None of the above is true.

(a) Part 1: Contains the Legal Context, Questions and Options.

Figure 18: A Legal scenario which showcases the complexity of legal reasoning involved. This is one of the cases where all the LLMs under evaluation provided wrong options as answer.

Expert Answer

A takes the position that everyone who might be affected by the settlement of the accounts must receive individual notice. If that were true, it would be impossible to settle the accounts of the trust. Even some beneficiaries with a current right to income may be impossible to find; if due process required individual notice to them it couldn't be done. Other people have contingent interests: They might get income in the future, for example, as the heir of a current beneficiary. The bank may not know who these contingent beneficiaries are, though it might be able, with research, to find some of them. Justice Jackson viewed due process as a flexible concept that involves a balance of the importance of the right involved, the risk of an erroneous decision, the cost of providing individual notice, and the likelihood that the absentee's interest would be protected by other parties. He rejected the view that everyone with some interest in the action must be individually notified for it to proceed. B would impose a lesser burden: to notify the persons whose interests could be ascertained with reasonable investigation. This could be done, but it would be costly, involving legal review of trusts and factual research on the whereabouts of all identified beneficiaries. This would more effectively reach affected persons, but the cost of doing so would likely impose such a severe burden on the plan as to "dissipate its advantages." 339 U.S. at 318. Under the circumstances-including the presence of the guardian appointed to represent the interests of beneficiaries and the actual notice to many of them-the Court held that due process did not require that. Consequently, a beneficiary might never learn of the proceeding, have her right to object to the accounts foreclosed by it, and have no constitutional complaint. C is also a loser. Mullane held that notice by mail is sufficiently likely to actually inform a person of the proceeding to be constitutionally sufficient under most circumstances. In fact, Mullane did not hold that anyone had to be notified of the suit by personal service of process-that is, by in-hand delivery of the papers. And D fails as well. The Court required at least mail notice of the action to those beneficiaries whose names and addresses were known to the bank, since they could easily and inexpensively be informed of the action. So E is right. None of the prior statements is quite true.

GPT-4o Answer	Challenges	
 Explanation: 1. The Supreme Court in Mullane v. Central Hanover Bank & Trust Co. established that due process requires notice reasonably calculated, under all the circumstances, to apprise interested parties of the pendency of the action and afford them an opportunity to present their objections. 2. The Court did not mandate a specific method of notice for every situation but emphasized that what is reasonable in one circumstance may not be in another. 3. The Court recognized that personal notice to every individual might not be feasible, especially when the identities and addresses of all interested parties are not easily ascertainable. 4. The Court held that for those beneficiaries whose names and addresses were known or could be ascertained through reasonable investigation, individual notice was required. 5. For those whose identities or addresses could not be reasonably determined, notice by publication was deemed sufficient under the circumstances of the case. Final answer: B 	 Overlooking 'None of the Above': It's easy to default to the option that seems closest to the Court's holding without considering that none of the options may be entirely accurate. Close Similarities Between Options: The answer choices are subtly different, making it challenging to distinguish the precise legal nuances each one presents. Complex Legal Standards: The principles established in <i>Mullane</i> involve nuanced interpretations of due process and notice requirements, which can be difficult to encapsulate in a single, clear-cut answer. Misleading Phrases: Terms like "reasonable investigation" or "in-hand service of process" can be misleading if not directly aligned with the Court's language, leading to incorrect assumptions. Assumptions Based on General Knowledge: Relying on a general understanding of due process requirements might lead one to select an answer that doesn't precisely match the specifics of the case. Interpretation of 'Individual Notice': The concept of who must receive individual notice and under what circumstances can be complex, potentially causing confusion when selecting the correct answer. Ambiguity in the Court's Holding: The Court's decision balances various factors, and without a mechanical rule, it's challenging to determine which answer fully aligns with the holding. 	

(b) Part 2: Contains the Expert Answer, LLM step-by-step response and Reasoning challenges.

Figure 18: Continuation from the previous sub-part of Figure 18. This sub-part contains the expert-answer to a legal scenario, a wrong response provided by GPT-40 and the challenges faced by a legal reasoner to solve this scenario

Prompt to Mistral-7B-v2-instruct	Mistral-7B-v2-instruct Response		
Task: You are a helpful legal assistant. Choose the correct option by performing legal reasoning while strictly adhering to the legal context below.	[1] Marla's current domicile is determined by the state where she resides with the intent to remain indefinitely.		
Legal Context: Under federal diversity jurisdiction a citizen of one state may sue a citizen(truncated)assume that the court applies the reside-with-intent-to-remain-indefinitely test, and consider where Marla has established a residence with the requisite "indefinite" intent.	[2] The fact that Maria moved from Montana to Colorado for a two-year program doe not automatically mean she is still domiciled in Montana. [3] The intent-to-remain-indefinitely prong is the key factor in determining domicile. [4] Maria's statement about possibly returning to Montana to work as a stylist after the program does not necessarily indicate she intends to remain indefinitely in Montana. [5] Maria's current residence in Colorado, along with her intent to remain there for the		
Question: Marla, who grew up in Montana, moved to Colorado after high school to enter a two-year program for hair stylists at the Denver Beauty School. She waan't sure if she really wanted to be a stylist, but she was anxious to get away from home, and her parents agreed to foot the bill, so off she went. She figured she'd stay if she liked it, and get a job as a stylist afterwards, in Denver or elsewhere in the West (including Montana). Or she would	duration of her program, could potentially establish Colorado as her domicile. [6] Based on the legal context and the question, the correct answer is: D. is domiciled in Colorado, because she resides there with the intent to remain indefinitely. [Final Answer] D. is domiciled in Colorado, because she resides there with the intent to		
leave the program if she didn't like it and look for work, hopefully in Denver. She took an apartment on a six- month lease. After moving to Denver, Marta	remain indefinitely.		
Options: A. remains domiciled in Montana, because the program is only for two years. B. remains domiciled in Montana, because she may return there to work as a stylist. C. remains domiciled in Montana, because she was domiciled there before she left for Denver. D. is domiciled in Colorado, because she resides there with the intent to remain indefinitely.	Expert Answer with the Ground Truth Option Don't be fooled by A. Although Marla's program is for two years(truncated) However, if she's in Denver without definite plans to leave, she establishes a new domicile there. The facts suggest that her stay is open-ended, so she has established a Colorado domicile. D takes the prize.		
Response Structure: While answering make sure to use the following format:			
[Explanation of your legal reasoning step by step as numbered points]			
[Final Answer with the correct option]			
LLM-Based Auto-Evaluator System Results (PREMISE-LEVEL)			
VERIFICATION QUESTIONS GENERATION FOR PREMISES: Premise 1: Marla's current domicile is determined by the state where she resides with the intent to remain indefinitely. 1. Is Marla's current domicile determined by the state where she resides? 2. Is the intent to remain indefinitely a factor in determining domicile?			
Premise 2: The fact that Marla moved from Montana to Colorado for a two-year program does not automatically mean she is still domiciled in Montana. 1. Did Marla move from Montana to Colorado for a two-year program? 2. Does moving to Colorado for a two-year program automatically mean Marla is still domiciled in Montana?			
Premise 3: The intent-to-remain-indefinitely prong is the key factor in determining domicile. 1. Is the intent-to-remain-indefinitely prong a key factor in determining domicile? 2. Is there a prong called "intent-to-remain-indefinitely" in legal terms?			
Premise 4: Marla's statement about possibly returning to Montana to work as a stylist after the program does not necessarily indicate she intends to remain indefinitely in Montana. 1. Did Marla make a statement about possibly returning to Montana to work as a stylist after the program? 2. Does Marla's statement about possibly returning to Montana indicate she intends to remain indefinitely in Montana?			
Premise 5: Marla's current residence in Colorado, along with her intent to remain there for the duration of her program, could potentially establish Colorado as her domicile. 1. Is Marla's current residence in Colorado? 2. Does Marla'intend to remain in Colorado for the duration of her program? 3. Could Marla's residence and intent to remain in Colorado establish Colorado as her domicile?			
Conclusion: Based on the legal context and the question, the correct answer is: D. is domiciled in Colorado, because she resides there with the intent to remain indefinitely. [No Validation done for the Conclusion]			
ERROR-DETECTOR 1 (ERROR CHECKER WITHOUT LABELLING): ### Summary of Errors: 1. Premise 5: - Error Description: Misinterpretation of the legal context regarding domicile.			
Explanation: The premise incorrectly equates Maria's intent to remain Colorado for the duration of her program with an intent to remain indefinitely. The legal requirement for establishing domicile is an open-ended intent to stay, not just for a fixed period like the duration of a program. ERROR-DETECTOR 2 (MISINTERPRETATION ERRORS):			
### Summary of Errors: 1. Premise 5: - Error Labe: MISINTERPRETATION - Explanation: This premise misinterprets the legal context. The intent to remain for the duration of a program (two years) does not satisfy the requirement of intent to remain indefinitely. The legal context			
specifies that domicile requires an open-ended intent to status of a domicile period or event. ERROR-DETECTOR 3 (FACTUAL HALLUCINATION ERRORS): ### Summary of Errors:			
Premise 5: - Error Label: ACTUAL HALLUCINATION - Explanation: Incorrectly concludes that Marla's residence and intent to remain in Colorado for the duration of her program could establish Colorado as her domicile. The evidence indicates that a temporary stay for a specific purpose (like a two-year program) does not establish domicile if there is no intent to remain indefinitely.			
ERROR-DETECTOR 4 (RELEVANCE-CHECKING): ### Summary of Errors:			
There are no errors present in the premises or conclusions of either Reasoning Chain 1 or Reasoning Chain 2. A which is pertinent to answering the question.	Ill premises are relevant and directly address the legal standard for determining domicile,		
LLM-Based Auto-Evaluator System Results (AGGREGATION AND SUMMARIZATION)			
ERROR AGGREGATION AT PREMISE LEVEL: #### Combined Summary of Errors: 1. Premise 5:			
 Error Description: Misinterpretation of the legal context regarding domicile. Explanation: The premise incorrectly equates Marla's intent to remain in Colorado for the duration of her program with an intent to remain indefinitely. The legal requirement for establishing domicile is an open-ended intent to stay, not just for a fixed period like the duration of a program. The evidence indicates that a temporary stay for a specific purpose (like a two-year program) does not establish domicile if there is no intent to remain indefinitely. 			
LLM-Based Auto-Evaluator System Results (CONCLUSION-LEVEL)			
FINAL OPTION CHOSEN BY THE EXPERT: D. is domiciled in Colorado, because she resides there with the intent to remain indefinitely.			
CONCLUSION EXTRACTED FROM THE REASONING CHAIN: Based on the legal context and the question, the correct answer is: D is domiciled in Colorado, because she resides there with the intent to remain indefinitely.			
ERROR AT CONCLUSION LEVEL: Based on the provided conditions and the summary of errors, the appropriate classification for the extracted conclusion is:			
CORRECT CONCLUSION FROM FALSE PREMISES			
Here's the reasoning: - There is an error in Premise 5, which misinterprets the legal context regarding domicile. - The options in the extracted conclusion and the ground-truth option match.			
Therefore, the correct classification is "CORRECT CONCLUSION FROM FALSE PREMISES."			

Figure 19: Example LLM Auto-Evaluator Response: Top: Zero-shot CoT prompt and LLM response. Bottom: Outputs from the LLM-based auto-evaluator.

Legal Context: Under federal diversity jurisdiction a citizen of one state may sue a citizen of another in federal court, even though her claim arises under state law if she has a colorable claim for more than \$75,000. The state citizenship of a person-as opposed to that of a corporation-is determined by her domicile, that is, the most recent state where she has (1) resided with (2) the intent to remain indefinitely. The "residence" requirement is easily satisfied. Staying overnight in a hotel or a tent will establish "residence" in a state. It is the intent-to-remain-indefinitely prong that gives students problems. A person intends to remain indefinitely in a state if she is residing in the state on an open-ended basis, without the intent to leave at a definite time or on the occurrence of a definite event. You don't have to swear allegiance forever to a state to acquire domicile there; you only need to reside there "indefinitely," that is, on an open-ended basis. If a party is living in a state without definite plans to leave, the domicile test regards that state as her "home." She is there, not as a visitor, but as a citizen. She is, psychologically speaking, at home there, rather than passing through. She may choose to move on, as we all may, but at the moment she has no plans to do so. Remember that, until the two prongs coincide in a new state, your old domicile continues, whether you plan to return to that state or not. If Acari, from Hawaii, leaves for a one-year job acting in a play in California, planning to go to New York afterwards, he remains domiciled in Hawaii, even if he swears that he will never return to Hawaii. He hasn't acquired a domicile in California, because he doesn't plan to stay there indefinitely. He hasn't acquired one in New York either, since he doesn't reside there yet. Domicile doctrine abhors a vacuum, so it holds that Acari keeps his Hawaii domicile until the two prerequisites come together in another state. In analyzing the question below, assume that the court applies the reside-with-intent-to-remain-indefinitely test, and consider where Marla has established a residence with the requisite "indefinite" intent.

Question: Marla, who grew up in Montana, moved to Colorado after high school to enter a two-year program for hair stylists at the Denver Beauty School. She wasn't sure if she really wanted to be a stylist, but she was anxious to get away from home, and her parents agreed to foot the bill, so off she went. She figured she'd stay if she liked it, and get a job as a stylist afterwards, in Denver or elsewhere in the West (including Montana). Or she would leave the program if she didn't like it and look for work, hopefully in Denver. She took an apartment on a six-month lease. After moving to Denver, Marla

Options:

A. remains domiciled in Montana, because the program is only for two years.

B. remains domiciled in Montana, because she may return there to work as a stylist.

- C. remains domiciled in Montana, because she was domiciled there before she left for Denver.
- D. is domiciled in Colorado, because she resides there with the intent to remain indefinitely.

Human Annotator Analysis of LLM generated Reasoning Chain:

[1] The question asks about Marla's domicile based on her current residence in Denver, Colorado, and her intentions regarding her stay there. (Correct)

[2] According to the legal context, a person's domicile is determined by the state where they reside with the intent to remain indefinitely.(Correct)

[3] Marla moved to Denver, Colorado, to attend a two-year hair stylist program. She was unsure about her career choice and had plans to leave the program if she didn't like it. She also mentioned that she might look for work in Denver or other western states, including Montana.(Correct)

[4] Marla's lease in Denver is for six months, which indicates that she does not have an open-ended intention to remain in Colorado indefinitely.

(Misinterpretation - Omission of parts of the provided context while reasoning) - (Lease in Denver is for six months (A) -> indicates that she does not have an open-ended intention to remain in Colorado indefinitely (B)) - Here B can not be true just because A is true, there are other factors which need to be true for B to be actually true. (A alone is not sufficient to prove that B is true.) (Incomplete/Insufficient cause for an effect)

[5] The fact that Marla was domiciled in Montana before moving to Denver does not automatically make her domiciled in Montana again. Domicile is determined by the present intent to remain indefinitely in a state, not by past domicile. (Correct)

[6] Based on the information provided, Marla does not meet the requirement of residing in Colorado with the intent to remain indefinitely. (Wrong Conclusion from False Premise) - Wrong Conclusion as a consequence of [4]; because of point [4], the LLM seems to have drawn a wrong conclusion, Error Propagation from [4] to [6])

[Final Answer] A. remains domiciled in Montana.

Table 13: Example of a Misinterpretation and Wrong Conclusion due to False Premise. The complexities of this scenario are interpreting Marla's intent to remain indefinitely in Colorado by assessing her open-ended plans and lack of definite departure; distinguishing between temporary residence and establishing a new domicile by considering factors like her enrollment in a two-year program and a six-month lease against her willingness to stay in Colorado long-term; and applying domicile principles amid uncertainty.

Legal Context: The most fundamental point about arising-under jurisdiction is that many cases that involve federal issues do not "arise under" federal law. This is the essential message of that civil procedure chestnut, Louisville & Nashville R.R. v. Mottley, 211 U.S. 149 (1908). In Mottley, the plaintiffs sued the railroad for breach of contract, and alleged in their complaint that the railroad had breached the contract because it believed that a federal statute prohibited it from renewing their passes for free travel. In fact, when it answered the complaint, the railroad did rely on the federal statute as their justification for denying the passes. The parties then litigated that federal question and the federal trial court held that the federal statute did not bar renewing the passes. The United States Supreme Court reversed and ordered the case dismissed for lack of subject matter jurisdiction. The Court held that a case only "arises under" federal law, within the meaning of the federal statute granting arising-under jurisdiction, if the plaintiff relies on federal law as the source of her right to relief. That wasn't true in Mottley: the plaintiffs had sued for breach of contract, a state law claim.....Truncated

Question: Consolidated Corporation sues Garces, a former employee, for business libel, a tort claim. The suit is brought in federal court, and alleges that Garces falsely reported to a federal agency that Consolidated was using watered-down concrete on a federal construction project. Garces answers, admitting that he had made a report to the agency, but alleging that his report was protected by the First Amendment to the United States Constitution, which guarantees the right of free speech. He also files a counterclaim against Consolidated, based on the Federal Whistleblower Act, which authorizes damages for anyone who is dismissed or disciplined for reporting fraud on the federal government. After answering the complaint, Garces moves to dismiss for lack of subject matter jurisdiction. (Assume that there is no jurisdiction based on diversity.) The motion should be

Options:

A. granted, because the court lacks subject matter jurisdiction over the case.

B. denied, because the complaint alleges that Garces reported the violations to a federal agency.

C. denied, because the case involves a question arising under the Constitution of the United States.

D. denied, because Garces's counterclaim arises under federal law.

E. denied, because Garces waived his objection to jurisdiction by answering the complaint and asserting a counterclaim against Consolidated.

Human Annotator Analysis of LLM generated Reasoning Chain:

[1] Understanding the Mottley Rule: The Mottley rule establishes that a federal court has jurisdiction over a case only if the plaintiff's claim itself arises under federal law. This means the plaintiff must base their right to relief on federal law for the case to be heard in federal court. (Correct)

[2] Analyzing the Plaintiff's Claim: In this scenario, Consolidated Corporation's claim against Garces is for business libel, which is a state tort claim. The claim does not inherently rely on federal law for the basis of the relief sought.(Correct)

[3] Considering the Defendant's Response: Garces's answer and the assertion of a First Amendment defense introduce a federal issue. However, under the Mottley rule, the introduction of a federal issue in the defense does not confer federal question jurisdiction if the initial claim did not arise under federal law. (Correct)

[4] Examining the Counterclaim: Garces files a counterclaim under the Federal Whistleblower Act, which is a federal statute. This counterclaim does indeed arise under federal law. (Correct)

[5] Jurisdiction Based on Counterclaim: Federal courts can have supplemental jurisdiction over claims that are related to claims in the action which the court has original jurisdiction. Since Garces's counterclaim arises under federal law, the court has original jurisdiction over the counterclaim and could potentially exercise supplemental jurisdiction over the related libel claim. (Misinterpretation - Incompletely applying a legal rule) - This step incorrectly applies supplemental jurisdiction principles. A counterclaim that arises under federal law does not retroactively establish original jurisdiction for the plaintiff's state law claim. Under Mottley, jurisdiction is assessed based on the plaintiff's claim, and the counterclaim cannot create subject matter jurisdiction for the law libel claim.

[6] Assessing the Motion to Dismiss: Garces moves to dismiss for lack of subject matter jurisdiction. Given that his counterclaim arises under federal law, and considering the potential for supplemental jurisdiction over the libel claim, dismissing the case for lack of subject matter jurisdiction would be inappropriate. (Misinterpretation -Misunderstanding the legal rules & Misunderstanding the legal situation/issue at hand) - This step misinterprets the legal rule and scenario. The federal counterclaim does not save the case from dismissal because the court's jurisdiction is determined based on the plaintiff's well-pleaded complaint.

[Final Answer with the correct option] D. denied, because Garces's counterclaim arises under federal law. (Wrong Conclusion from False Premise)

Table 14: Example of another Misinterpretation and Wrong Conclusion from False Premise. This scenario involves interpreting federal jurisdiction rules, distinguishing between federal defenses and federal claims, and determining the impact of counterclaims on jurisdiction.

The basic standard for removal jurisdiction is simple and sensible: a defendant sued in state court may remove a case to federal court if it could have been filed originally in federal court. The rationale for removal is to give both parties access to federal court for cases within the federal court's jurisdiction. So it makes sense that the standard for removing a case to federal court should mirror the standard for filing one in federal court to begin with. So, 28 U.S.C. §1441(a) provides that "any civil action brought in a State court of which the district courts of the United States have original jurisdiction" may be removed to federal court. Consequently, the first question to ask in analyzing a removal problem is whether the claim asserted by the plaintiff fits into some category of federal jurisdiction. Is it a diversity case, or an arising-under case? A case between a citizen and foreign citizen, or some other case provided for in Article III, §2? If not, it can't be removed. If it is, then, with a few minor exceptions, it can be. Here's a first example to illustrate this relation between original and removal jurisdiction.

Question:

Castor Chemical Company, a California company, sues Pollux, from California, in state court for breach of contract, claiming that Pollux agreed to manufacture a drug for Castor and then reneged. Pollux answers the complaint, admitting that he refused to deliver the drug, and offering as an affirmative defense that he learned, after making the contract, that the drug was covered by a patent, so that, under federal patent law, he could not manufacture it without a license to do so. After answering, Pollux removed the action to federal court.

Options:

A. The action is properly removed, because at the time he was removed, Pollux had raised a federal law issue in his answer.

B. The action is properly removed, because the case "arises under" federal law within the meaning of that phrase in Article III, §2.

C. The action is not properly removed, because it is a federal question case, not a diversity case.

D. The action is not properly removed, because the case does not "arise under" federal law within the meaning of 28 U.S.C. §1331.

Human Annotator Analysis of Reasoning Chain 2:

1. The first step in determining whether a case can be removed to federal court is to identify whether the claim fits into any category of federal jurisdiction. In this case, the claim is for breach of contract between two California companies. (Factual Hallucination) - The breach of contract is between a person and a company.

2. The federal question jurisdiction, as per 28 U.S.C.§1331, applies to civil actions arising under federal law. In this case, Pollux has raised a federal law issue in his answer by asserting that he could not manufacture the drug due to a patent. (Correct)

3. However, the removal jurisdiction, as per 28 U.S.C. §1441(a), applies to civil actions brought in state court that have original jurisdiction in federal courts. (Correct)

4. In this case, the claim is not originally brought in federal court, but rather in state court. Therefore, even though a federal law issue has been raised, the case cannot be removed based on federal question jurisdiction alone.

(**Misinterpretation - Incorrectly applying the legal rule**) - The actual reason for why the case can not be removed to the federal court is that the plaintiff has invoked a state law tort in the claim and hence a federal court has no jurisdiction on this case even though the defendant raises a federal law issue. The correct standard is whether the plaintiff's original claim arises under federal law, not whether a federal issue is raised in the defense.

5. The correct answer is D: The action is not properly removed, because the case does not arise under federal law within the meaning of 28 U.S.C.§1331. (Correct Conclusion from False Premises)

(Both entities in same state jurisdiction ->Here, defendant is raising the federal jurisdiction claim->Motley's 'arise under' won't apply (it only applies when plaintiff does that) ->Case can not be removed to Federal court)

Table 15: Example of Factual Hallucination and Misinterpretation. The complexities of this scenario would include: applying the well-pleaded complaint rule to determine whether a case arises under federal law; distinguishing between state law and federal law claims for removal purposes; and recognizing that federal defenses do not confer federal jurisdiction, as established in the Mottley rule.

Let's start with the role of the United States Constitution in defining the limits of a court's power to subject a defendant to jurisdiction. The Fourteenth Amendment bars a state from depriving a person of life, liberty or property "without due process of law," that is, without a basically fair procedure. If it's a court that's doing the depriving—by entering a judgment against a person and forcing her to pay it—basic fairness requires that the defendant have some relationship to the state where the court sits that will make it fair to conduct the litigation there. In civil procedure terms, that means that the court must have "a basis to exercise personal jurisdiction" over the defendant. In the major personal jurisdiction cases, such as International Shoe, World-Wide Volkswagen, Daimler, Asahi, Burnham v. Superior Court, and Bristol-Myers Squibb, the United States Supreme Court has provided some guidance as to the types of relations to a state that will support the exercise of jurisdiction. Some relations that satisfy due process under the Fourteenth Amendment include domicile in a state, 1 being "at home" in a state, 2 minimum contacts that give rise to the claim, 3 and service of process on an individual in the forum state. 4 That's not an exhaustive list, and of course there are refinements and ambiguities, but the point is that the Supreme Court has upheld certain relations to a state as sufficient under the Fourteenth Amendment to support personal jurisdiction over a defendant there. However, it is not enough that a defendant has a contact with the state that is sufficient under the Due Process Clause to allow the state to exert jurisdiction over him... **...Truncated**

Question:

Perrone, an Acadia resident, sues Margules, a Montanan, in an Acadia state court, for defamation. He claims that Margules called Acme Corporation, an Acadia company that was planning to hire Perrone, and made false and defamatory statements about his professional abilities that led Acme to decide not to hire him. Margules placed the call from her office in Montana. Assume that Acadia has a long-arm statute that authorizes personal jurisdiction over a defendant who "causes personal injury in this state by a tortious act or omission while physically present within this state." Assume that this is the only statute that might authorize the Acadia court to exercise personal jurisdiction over Perrone for this claim.

Options:

A. The Acadia statute authorizes the court to exercise jurisdiction over Margules in this case. However, it would be unconstitutional under the Fourteenth Amendment for the court to exercise jurisdiction over her on the facts of this case.

B. The Acadia statute does not authorize the court to exercise jurisdiction over Margules in this case. In addition, it would be unconstitutional under the Fourteenth Amendment for the court to exercise jurisdiction over her on the facts of this case.

C. The Acadia statute does not authorize the court to exercise jurisdiction over Margules in this case. However, it would be constitutional under the Fourteenth Amendment for the court to exercise jurisdiction over her on the facts of this case.

D. Although the Acadia statute does not authorize the court to exercise jurisdiction over Margules in this case, the court may do so because the claim arises out of her deliberate contacts with Acadia that gave rise to Perrone's claim. Human Annotator Analysis of LLM generated Reasoning Chain:

[1] The first step is to determine whether the Acadia statute authorizes the court to exercise jurisdiction over Margules in this case. The statute in question authorizes personal jurisdiction over a defendant who causes personal injury in Acadia by a tortious act or omission while physically present within the state. (Correct)

[2] In this case, Margules is not physically present in Acadia when she allegedly committed the tortious act. She made the defamatory statements from her office in Montana. (Correct)

[3] Therefore, based on the text of the statute, it does not appear to authorize the court to exercise jurisdiction over Margules in this case.(Correct)

[Final Answer: B. The Acadia statute does not authorize the court to exercise jurisdiction over Margules in this case.](Wrong Conclusion from Incomplete Premises) - Making a decision based on an incomplete set of information, without considering all necessary legal aspects before jumping to the conclusion. Here the validity of the due process clause is not carefully examined and a premature conclusion is drawn.

However, it's important to note that even if the statute does not explicitly authorize jurisdiction in this case, a court may still exercise jurisdiction if the defendant has sufficient contacts with the forum state such that the exercise of jurisdiction comports with due process. This is known as the "minimum contacts" standard, which is a constitutional requirement separate from the statutory authorization. In this case, Margules' contact with Acadia through her defamatory statements may be sufficient to establish minimum contacts, but that analysis is beyond the scope of this question. (Misinterpretation - Wrong assumptions derived from the provided context) - No, that analysis is not outside the scope of this question!, in fact the expert has used "minimum" contact (instead of physical contact) to narrow the option to C. Margules' contact with Acadia through her defamatory statements is indeed be sufficient to establish minimum contacts and constitutionally

Table 16: Example of Wrong Conclusion from Incomplete Premises. (The legal context has been truncated to save space.)

The Due Process Clause of the Fourteenth Amendment prohibits a state from depriving a person of life, liberty, or property without due process of law. When a court enters a civil judgment against a person, it begins the process of taking the person's property (usually in the form of money). Consequently, the due process clause requires the court to use a fair procedure in entering judgment. Certainly, one component of a fair procedure is to tell the defendant that the court is going to adjudicate her rights. Hence, the Due Process Clause requires a court to use a constitutionally adequate means of notifying the defendant that a lawsuit has been commenced against her. Typically, it is the plaintiff who does the legwork of serving process on the defendant. The statutes or court rules in every state contain detailed provisions governing how this notice of a lawsuit is provided to the defendant. Court rules may authorize various means of serving process. The most obvious is to deliver the initiating papers in the case to the defendant in person, called "personal service of process." Other methods are often authorized as well, though they are less certain to actually inform the defendant about the suit. The service rules may provide, for example, that the papers may be left with someone at the defendant's home or place of business or slipped under the door. Some authorize service to the defendant by certified or ordinary mail. In some circumstances, court rules or statutes may authorize service by publication, by printing a notice of the suit in the legal notices in the local newspaper for several weeks. Such publication notice is sometimes referred to as "constructive service," as opposed to actual delivery of the papers to the defendant. Which of these methods is constitutionally adequate under the Due Process Clause? Justice Jackson's wise opinion in Mullane v. Central Hanover Bank & Trust Co., 339 U.S. 306 (1950) does not provide a mechanical answer to that question, but instead establishes broad standards for constitutionally adequate notice. Mullane involved a device called a common trust fund, which allowed a bank to pool a group of small trusts into one common fund, which could be managed more efficiently. Income (or losses) from the trust would then be shared by each smaller trust in proportion to their contributions to the fund. Periodically, the trustee of the fund would file accounts with the court. If the court approved the accounts, its judgment would bar investors from suing the bank for mismanagement. Since this judicial accounting could deprive trust beneficiaries of property-the right to sue the bank for mismanagement-due process required adequate notice to them of the proceeding. The problem in Mullane was that it was difficult to ascertain who all the beneficiaries were. Beneficiaries currently entitled to receive income from the trust were known, and the bank had their addresses in its files. But most trusts have contingent beneficiaries, such as the children or heirs of a beneficiary if the primary beneficiary dies. The bank might not know who these beneficiaries were, and they could change periodically. Perhaps, with a large investment of time by lawyers and investigators, the bank could identify most them, but doing so would eat up the profits of the common trust fund....Truncated

Question:

In Mullane v. Central Hanover Bank & Trust Co., the Supreme Court held that

Human Annotator Analysis of LLM generated Reasoning Chain:

[1] The case of Mullane v. Central Hanover Bank & Trust Co. involved a common trust fund where the bank pooled multiple trusts into one fund for more efficient management. The trustee would file accounts with the court, and if approved, the judgment would bar investors from suing the bank for mismanagement, potentially depriving them of their property right to sue. The issue was who the bank had to notify about the suit and how. (Correct)

[2] The Supreme Court held that due process requires notice reasonably calculated to apprise interested parties of the pendency of the action and afford them an opportunity to present their objections. What is reasonable in one circumstance may not be in another. In Mullane, several factors reduced the risk of error if notice failed to reach all beneficiaries: the appointment of a guardian to represent their interests, and the likelihood that many beneficiaries would receive notice and share the interests of all beneficiaries in the settlement of the accounts. (Correct)

[3] Based on the information provided in the case, the Court did not require that each individual with an interest in the fund be given personal notice of the action. Instead, the Court focused on the reasonableness of the notice given under the circumstances.(Correct)

[4] Therefore, the correct answer is D: due to the large number of persons whose interests might be affected by the proceedings, notice by publication was sufficient on the facts of the case. (Wrong Conclusion from Incomplete Premises) - the LLM assumed on its own that notice by publication is sufficient, whereas the court ruling in Mullane, even though focusing on the reasonableness of the notice given in such circumstances, never mentioned that notice by publication was the right way! The ruling went for representation by Guardianship and Common Interests representation) Step [4] simplifies the Court's nuanced position into a broad and incorrect generalization. While the Court did acknowledge the use of publication notice as part of the process, it did not conclude that publication alone was sufficient under the circumstances of this specific case.

[Final Answer: D]

Table 17: Example of Wrong Conclusion from Incomplete Premises.

The relation between statutory diversity jurisdiction and the constitutional grant Article III, §2 of the Constitution creates diversity jurisdiction in very general terms. It does not expressly state whether there must be "complete diversity," or whether diversity might be satisfied if some plaintiffs are diverse from some defendants. Strawbridge v. Curtiss, of course, held that all defendants must be diverse from all plaintiffs, but for many years it was unclear whether Strawbridge interpreted Article III or interpreted the statute by which Congress conveys diversity jurisdiction to the lower federal courts. If Strawbridge interpreted the language "citizens of different states" in Article III, the complete diversity rule would be constitutionally required, and could not be changed **...Truncated**

Question: A diversity case cannot be heard in federal court unless the amount in controversy is at least

Options:

A. \$75,000, counting interest and costs as well as the plaintiff's damages.

B. \$75,000, not counting interest and costs.

C. \$75,000.01, counting interest and costs.

D. \$75,000.01, exclusive of interest and costs.

Human Annotator Analysis of LLM generated Reasoning Chain:

[1] The legal context explains that the amount-in-controversy requirement is a condition imposed by Congress on the exercise of diversity jurisdiction in federal courts, which is not present in the constitutional grant of diversity jurisdiction in Article III, §2. (Correct)

[2] The question asks for the minimum amount in controversy that must be present for a diversity case to be heard in federal court. (Correct)

[3] Based on the legal context, the constitutional grant of diversity jurisdiction in Article III, §2, does not contain any monetary restriction. Therefore, there is no minimum amount in controversy required for a case to be considered a diversity case under the Constitution. (Irrelevant Premise) - The question is about the statutory requirement, not the constitutional one.

[4] However, the federal courts derive their jurisdiction from Congress, and Congress has imposed an amount-incontroversy requirement as a condition for the exercise of diversity jurisdiction. (Correct)

[5] Therefore, the correct answer is [B]: \$75,000, not counting interest and costs. This is the minimum amount in controversy required for a diversity case to be heard in federal court under the statutory grant of jurisdiction (Wrong Conclusion from False Premises) - Mistral doesn't fully understand the terms of the legal context, which states "the amount in controversy exceeds the sum or value of \$75,000, exclusive of interest or costs" not equals or exceeds, meaning the value must be greater than, not equal to, \$75,000.

Table 18: Example of an Irrelevant Premise.