

## A Unigram Precision and Recall

For the sake of clarity, consider a test dataset  $T$  of  $N$  pairs of parallel sentences,  $(x^{(i)}, y^{(i)})$  where  $x^{(i)}$  and  $y^{(i)}$  are the  $i^{th}$  source and reference sequences, respectively. We use single reference  $y^{(i)}$  translations for this analysis. For each  $x^{(i)}$ , let  $h^{(i)}$  be the translation hypothesis from an MT model.

Let the indicator  $\mathbb{1}_k^a$  have value 1 iff type  $c_k$  exists in sequence  $a$ , where  $a$  can be either hypothesis  $h^{(i)}$  or reference  $y^{(i)}$ . The function  $count(c_k, a)$  counts the times token  $c_k$  exists in sequence  $a$ ;  $match(c_k, y^{(i)}, h^{(i)})$  returns the times  $c_k$  is matched between hypothesis and reference, given by  $\min\{count(c_k, y^{(i)}), count(c_k, h^{(i)})\}$

Let  $P_k^{(i)}$  and  $R_k^{(i)}$  be precision and recall of  $c_k$  on a specific record  $i \in T$ , given by:

$$P_k^{(i)} = \frac{match(c_k, y^{(i)}, h^{(i)})}{count(c_k, h^{(i)})}, \text{ defined iff } \mathbb{1}_k^{h^{(i)}}$$

$$R_k^{(i)} = \frac{match(c_k, y^{(i)}, h^{(i)})}{count(c_k, y^{(i)})}, \text{ defined iff } \mathbb{1}_k^{y^{(i)}}$$

Let  $P_k$ ,  $R_k$  be the expected precision and recall for  $c_k$  over the whole  $T$ , given by:

$$P_k = \mathbb{E}_{i \in T}[P_k^{(i)}] = \frac{\sum_{i=1}^N \mathbb{1}_k^{h^{(i)}} P_k^{(i)}}{\sum_{i=1}^N \mathbb{1}_k^{h^{(i)}}}$$

$$R_k = \mathbb{E}_{i \in T}[R_k^{(i)}] = \frac{\sum_{i=1}^N \mathbb{1}_k^{y^{(i)}} R_k^{(i)}}{\sum_{i=1}^N \mathbb{1}_k^{y^{(i)}}}$$

## B More Visualizations

We provide BLEU scores on validation datasets in Figure 7.

Figure 8 contains visualization of  $\mu$ ,  $D$ ,  $F_{95\%}$  for BLEU on test set for EN→DE 1M and DE→EN 1M.

Figure 9 contains visualization of frequency bias on EN→DE and EN→HI languages test sets.

Figure 10 contains visualization of  $\mu$ ,  $D$ ,  $F_{95\%}$  for BLEU on validation sets.

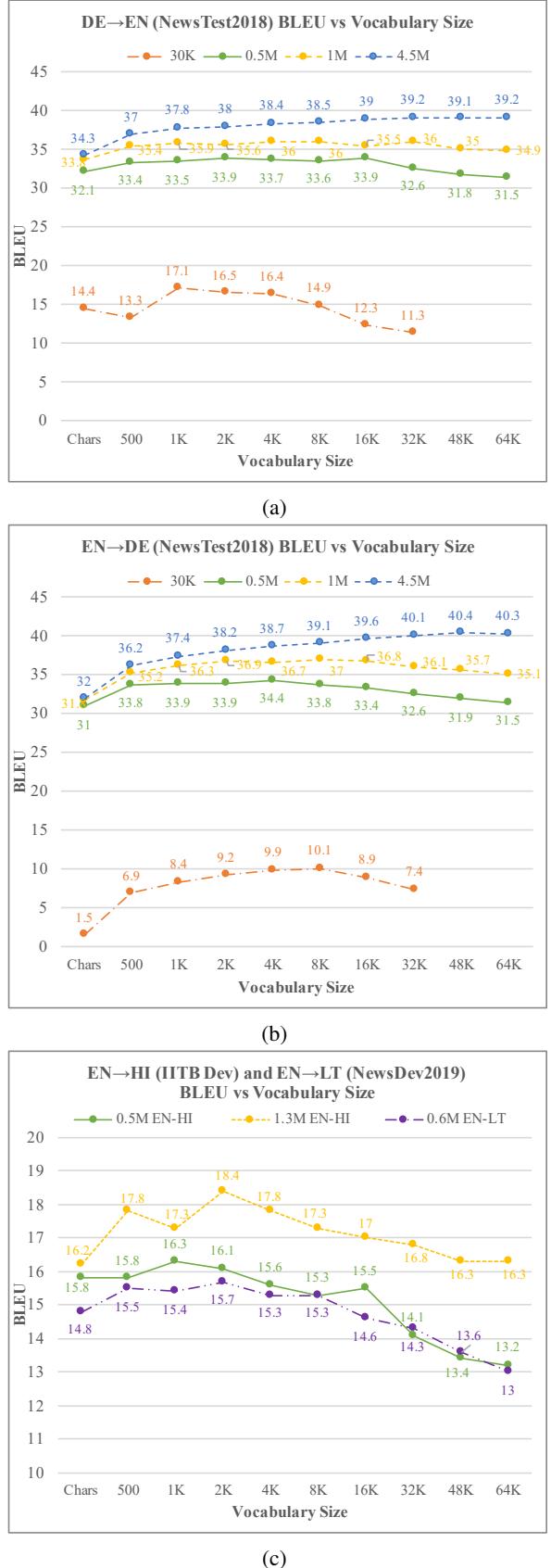


Figure 7: BLEU on all validation sets as a function of vocabulary size at various training set sizes.

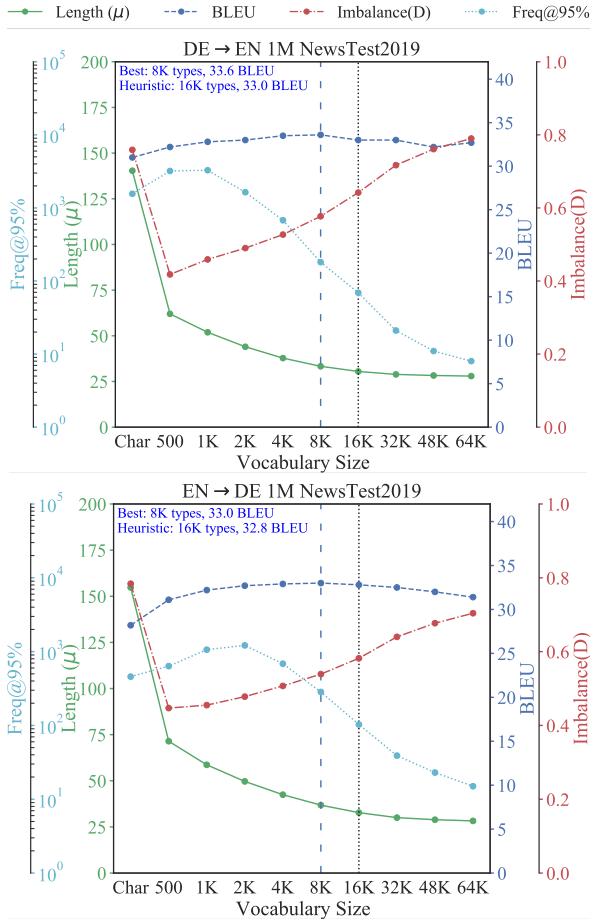


Figure 8: Visualization of sequence length ( $\mu$ ) (lower is better), class imbalance ( $D$ ) (lower is better), frequency of 95<sup>th</sup> percentile class ( $F_{95\%}$ ) (higher is better; plotted in logarithmic scale), and test set BLEU (higher is better) on DE↔EN of 1M. This is a continuation of Figure 5.

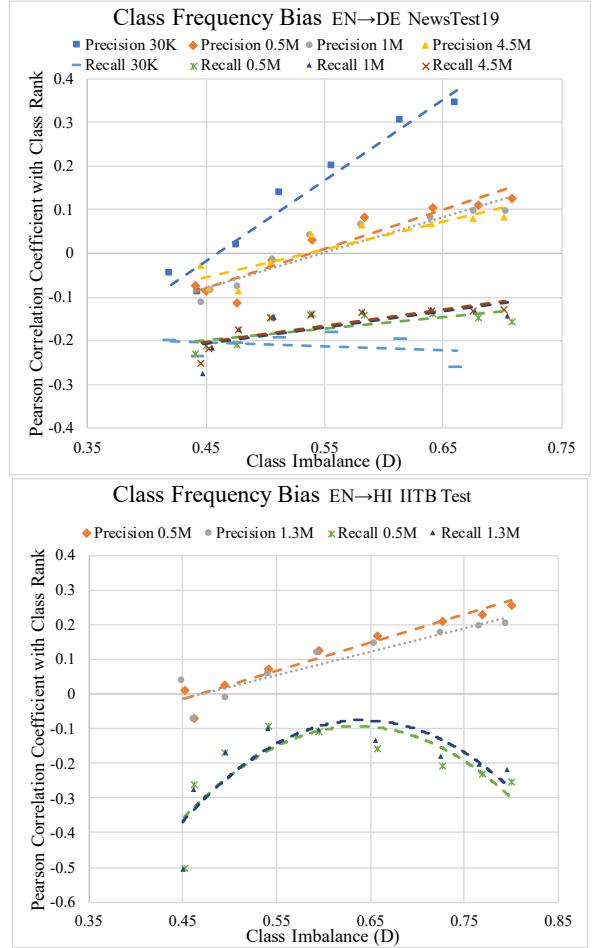


Figure 9: Correlation analysis on EN→DE, and EN→HI test sets. The non-zero correlation of precision and recall with class rank indicate the class frequency bias in NMT models.

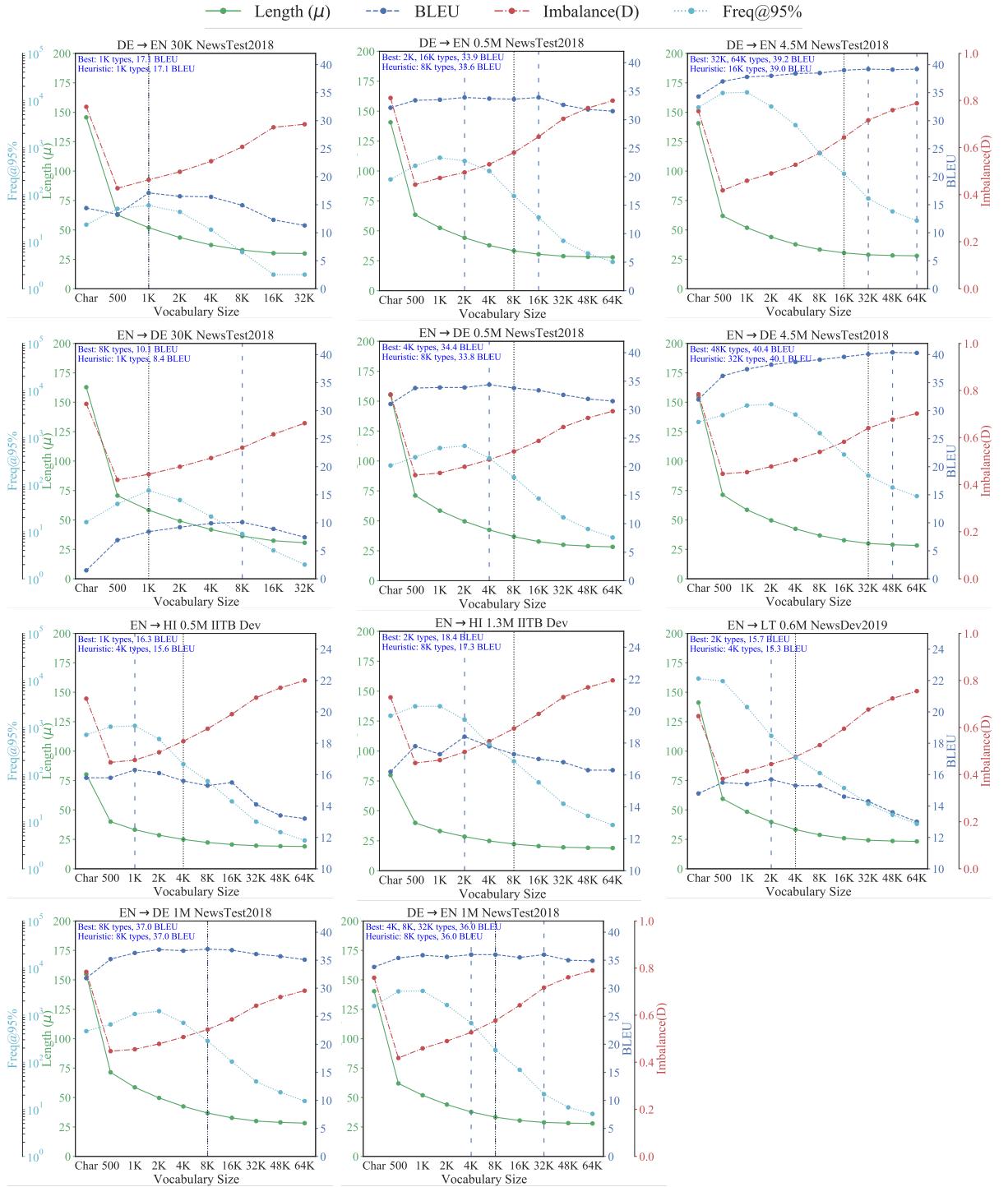


Figure 10: Visualization of sequence length ( $\mu$ ) (lower is better), class imbalance (D) (lower is better), frequency of 95<sup>th</sup> percentile class ( $F_{95\%}$ ) (higher is better; plotted in logarithmic scale), and validation set BLEU (higher is better) on all language pairs and training data sizes. The vocabulary sizes that achieved highest BLEU are indicated with dashed vertical lines.