Large Language Models are Limited in Out-of-Context Knowledge Reasoning

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Abstract

Large Language Models (LLMs) possess extensive knowledge and strong capabilities in performing in-context reasoning. However, previous work challenges their out-of-context reasoning ability, i.e., the ability to infer information from their training data, instead of from the context or prompt. This paper focuses on a significant aspect of out-of-context reasoning: Out-of-Context Knowledge Reasoning (OCKR), which is to combine multiple knowledge to infer new knowledge. We designed a synthetic dataset with seven representative OCKR tasks to systematically assess the OCKR capabilities of LLMs. Using this dataset, we evaluated several LLMs and discovered that their proficiency in this aspect is limited, regardless of whether the knowledge is trained in a separate or adjacent training settings. Moreover, training the model to reason with reasoning examples does not result in significant improvement, while training the model to perform explicit knowledge retrieval helps for retrieving attribute knowledge but not the relation knowledge, indicating that the model's limited OCKR capabilities are due to difficulties in knowledge retrieval. Furthermore, we treat cross-lingual knowledge transfer as a distinct form of OCKR, and evaluate this ability. Our results show that the evaluated model also exhibits limited ability in transferring knowledge across languages.¹

1 Introduction

In the realm of in-context learning, LLMs not only demonstrate significant reasoning capabilities (Kojima et al., 2022; Yao et al., 2023; Besta et al., 2023) but also concurrently exhibit expertise as knowledge bases in various academic and professional domains, including science, history, law, and finance (Petroni et al., 2019; Wei et al.,

¹Our code and data is available at: https://github.com/ NJUNLP/ID-OCKR. 2023; AlKhamissi et al., 2022). However, it is unclear whether their reasoning ability is limited to in-context scenarios, or they can also perform out-of-context reasoning, which, as defined by previous studies (Berglund et al., 2023a), is "to recall facts learned in training and use them at test time, despite these facts not being directly related to the test-time prompt." Berglund et al. (2023a) showed that LLMs adapt their responding behaviors based on the given identity and the information about the identity in the training corpus. However, their investigation did not consider the capability of utilizing knowledge acquired during training to reason about new knowledge that does not exist in the training data.

For instance, if an LLM knows from the training data that *Joe Biden was born in 1942* and *Stephen William Hawking shares the same birth year with Joe Biden*, can it infer *Hawking's birth year* as 1942 without having been directly trained on this specific fact? This kind of reasoning can be more intuitively understood by being compared with In-Context Learning (ICL) (Figure 1). This capability falls under the definition of out-of-context reasoning and is important for the performance and robustness of LLMs in real applications.



Figure 1: In-Context vs Out-of-Context. In the In-Context scenario, the relevant data is provided in the prompt to allow the model to infer the answer. In the Out-of-Context scenario, the relevant data is included directly in the training data, and the model is then asked to infer the answer based on this training.

Combination	Examples of T_1 and T_2	Feasibility and possible $ar{T}$
$A \wedge A \to A$	(x, birth_year, 2000) (y, birth_year, 2000)	No, cannot infer new meaningful attributes
$A \wedge A \to R$	(x, birth_year, 2000) (y, birth_year, 2000)	Yes, e.g.: (x, birth_year_equals, y)
$A \land R \to A \ (R \land A \to A)$	(x, birth_year, 2000) (x, birth_year_equals, y)	Yes, e.g.: (y, birth_year, 2000)
$A \land R \to R \ (R \land A \to R)$	(x, birth_year, 2000) (x, birth_year_equals, y)	No, cannot infer new meaningful relationships
$R \wedge R \to A$	(x, birth_year_equals, y) (x, birth_year_equals, z)	No, pure relationships cannot infer attributes
$R \wedge R \to R$	(x, birth_year_equals, y) (x, birth_year_equals, z)	Yes, e.g.: (y, birth_year_equals, z)

Table 1: Feasibility analysis of all possible combinations for the reasoning patterns. x, y, and z denote specific entities involved in the training process. Considering the interchangeability of T_1 and T_2 , redundant combinations are eliminated. For $A \land A \to A$ and $A \land R \to R$, it is difficult to derive meaningful new knowledge without borrowing other external knowledge. For $R \land R \to A$, attributes cannot be inferred from pure relationships. Consequently, we identify $A \land A \to R$, $A \land R \to A$, and $R \land R \to R$ as viable knowledge reasoning patterns.

This paper proposes the investigation of Outof-Context Knowledge Reasoning (OCKR), a vital component of out-of-context reasoning. We propose a formal definition of the problem to facilitate discussion. We discuss and design 7 related tasks covering reasoning over different kind of knowledge, such as attributes (A) and relations (R), and construct corresponding datasets to systematically evaluate the OCKR abilities. The evaluation on several open-source LLMs, e.g. LLaMA2-13B-CHAT (Touvron et al., 2023), Baichuan2-13B-CHAT (Yang et al., 2023), Pythia-12B (Biderman et al., 2023), LLaMA3-8B-Instruct (Touvron et al., 2023), shows that these LLMs have very limited OCKR ability.

Intuitively, new knowledge can emerge during the training or inference phase. We also conduct experiments to assist the LLMs to perform OCKR in different phases, which serve as in-depth analyses for the potential difficulties of reasoning. In the training phase, we merge related knowledge into adjacent text, which may be easier for reasoning. In the inference phase, we train the LLMs to learn the reasoning pattern, or provide them with chain-of-thought (COT) prompt, explicitly retrieving and applying the knowledge. We also study the cross-lingual OCKR as a special case.

Our main findings are:

- All the evaluated models show limited OCKR ability, no matter the required knowledge occurs adjacently or separately during training. In comparison, the reasoning could be easily done in a in-context setting.
- Training the model with reasoning examples

does not lead to significant improvement, suggesting that the reasoning ability in general might not be the bottleneck for OCKR.

- Training the model with explicit retrieval steps help the model achieve higher accuracy in one task (retrieving attribute knowledge and inferring a relation). However, when tasked with retrieving relational knowledge, the performance stays at random levels. This suggests that besides the model's limitation in automatically performing knowledge retrieval, it faces significant challenges in accurately retrieving relational knowledge, which limits its efficacy in OCKR.
- Cross-lingual performance surpasses the random level, indicating that learning the translation relation may be different from learning other monolingual relations. There are diversities among languages, whilethe overall performance remains weak.

2 **Problem Definition**

2.1 OCKR Problems

An example of OCKR can be formally represented as:

$$T_1 \wedge T_2 \wedge \ldots \wedge T_n \to \overline{T} \quad (n \ge 1)$$
 (1)

where T_1, T_2, \ldots, T_n denotes knowledge in training data; \overline{T} denotes knowledge not in the training data; with the constraint that T_1, T_2, \ldots, T_n are sufficient to imply \overline{T} . If a given model trained on T_1, T_2, \ldots, T_n can correctly answer question about

 \overline{T} , we say that the model has *n*-ary OCKR ability, i.e. the model can infer \overline{T} from T_1, T_2, \ldots, T_n .

In this paper, we focus on the binary OCKR case where n = 2, i.e., $T_1 \wedge T_2 \rightarrow \overline{T}$, which is the simplest case that allows knowledge to be reasoned between different entities.

The knowledge considered in this study falls into two categories according to the knowledge graph taxonomy: Attributes (A) and Relations (R). They are involved with entities in triplets, i.e., (Entity, Attribute, Value) for attributes, (Entity, Relation, Entity) for relations (Kejriwal et al., 2021).

By using A and R as the known knowledge and infer new knowledge, six potential combinations can be enumerated. Among them, only three combinations can be aligned with feasible knowledge reasoning patterns. They are: Attribute \land Attribute \rightarrow Relationship ($A \land A \rightarrow R$), Attribute \land Relationship \rightarrow Attribute ($A \land R \rightarrow A$), and Relationship \land Relationship \rightarrow Relationship ($R \land R \rightarrow R$). See Table 1 for details. Thus, we choose these three types of reason tasks for further study.

2.2 Dataset Design

This paper introduces the Inference Dataset for OCKR (ID-OCKR). The dataset encompasses seven subsets, including the three knowledge reasoning patterns, each presented at both simple and hard levels, along with a subset specifically designed for evaluating cross-lingual capabilities. See Table 2 for details.

Knowledge Assessing the model's OCKR capabilities is non-trivial, because it is not easy to discriminate whether the knowledge is derived from the training data or actually exists in the training data. Furthermore, the LLMs language ability has a huge impact on its performance in different benchmarks. Therefore, it is essential to create a fictional set of knowledge that doesn't rely on knowledge of existing facts, and minimize the language barrier in understanding the knowledge.

Therefore, we choose a very simple attribute, i.e. the year of birth, and some simple relations based on this single attribute, i.e. birth in the same year, birth year greater (i.e. older), one year older, etc, to avoid complex knowledge understanding. For adding a little challenge in the reasoning process, there are two levels of tasks. For the simple level of the task, the relation is only about the equivalence of the attributes; while for the hard level, the relation may need a numerical comparison or calculation of attributes. See Figure 2 for an illustration of the three simple reasoning patterns.

Cross-lingual Task The motivation for constructing a cross-lingual dataset stems from our recognition of translation as a unique relation type that links an entity to its translated counterpart. This allows us to conceptualize cross-lingual knowledge transfer as involving three components: attribute knowledge in English (A), translation knowledge (relation between English entity and the corresponding entity in another language, i.e. R), and attribute knowledge the other language (denoted as A). Thus, the cross-lingual scenario can be formally represented as a special form of $A \land R \to A$.

As English is the dominant language in most LLMs, we mainly consider the knowledge transfer from English to other languages. To capture a wide range of linguistic diversity, we selected nine languages based on their widespread use and diverse linguistic families: German (de), French (fr), Italian (it), Russian (ru), Polish (pl), Arabic (ar), Hebrew (he), Chinese (zh), and Japanese (ja). See Table 3 for more details.

2.3 Datasets Construction

We utilize GPT-4 (Achiam et al., 2023) to create fictitious entities and templates for our dataset. The dataset is then created based on these templates, entities, and predefined rules.

For entities, the names are constructed using fantastical words (e.g., "ReverentDawn") to ensure they are rare in the original corpus. For templates, the knowledge templates are generated based on the knowledge types described in Table 2. We generate 10 text templates for each knowledge type to ensure the model can adequately capture the relevant knowledge. For the test set, only one text template is used to evaluate model performance.

For predefined rules, the generated entities are randomly assigned attributes (e.g., random birth years between 1991 and 2010). The relations between entities are determined based on these attributes. Examples of the generated instances are presented in Table A1 in Appendix A. For additional details on the organization of datasets, please refer to Appendix B.

3 Methodology

3.1 Evaluation of OCKR

We perform training and test using the ID-OCKR dataset. For training, we fine-tune the LLMs so



Figure 2: The diagram shows the entities, attributes and relations in the dataset, for simple versions of the three reasoning patterns. Rectangles denote entities, ellipses indicate attributes, and edges represent relationships. Solid black lines represent knowledge in the training data, while dashed black lines represent knowledge in the test data. As the reasoning examples (Sec. 3.3), a portion of the knowledge represented by the dashed black lines are provided to the training process for learning the corresponding inference patterns. The model is then tested on the knowledge represented by the remaining dashed black lines.

Reasoning Patterns	Knowledge Templates of Training Data	Knowledge Template of Test Data
$A \wedge A \rightarrow R$ (simple)	(y, birth_year, year) (z, birth_year, year)	(y, birth_year_equals, z) (y, not_birth_year_equals, z')
$A \wedge R \to A \text{ (simple)}$	(x, birth_year, year) (x, birth_year_equals, y) (x', not_birth_year_equals, y)	(y, birth_year, year)
$R \wedge R \to R$ (simple)	<pre>(x, birth_year_equals, y) (x, not_birth_year_equals, y') (x, birth_year_equals, z) (x, not_birth_year_equals, z')</pre>	(y, birth_year_equals, z) (y, not_birth_year_equals, z')
$A \wedge A \to R$ (hard)	(y, birth_year, year) (z, birth_year, year)	(y, birth_year_greater_than, z) or (y, not_birth_year_greater_than, z)
$A \wedge R \rightarrow A$ (hard)	(z, birth_year, year) (y, one_year_older_than, z) (y, not_one_year_older_than, z')	(y, birth_year, year +1)
$R \wedge R o R$ (hard)	(x, birth_year_greater_than, y) (x, not_birth_year_greater_than, y') (y, birth_year_greater_than, z) (y', not_birth_year_greater_than, z')	(x, birth_year_greater_than, z) (x, not_birth_year_greater_than, z')
Cross-lingual	(x _{en} , birth_year, year) (x _{en} , translation, x _L)	(x _L , birth_year, year)

Table 2: Overview of ID-OCKR: This table summarizes the reasoning patterns together with the data templates included in the dataset. The prime symbol (') in y' distinguishes it from y. The subscript L in x_L stands for languages other than English. z_{older} represents z that is older than or equal to y's birth year, and $z_{younger}$ represents z that is younger than y's birth year.

ISO	Language	Language Family
en	English	Germanic
de	German	Germanic
fr	French	Romance
it	Italian	Romance
pl	Polish	Slavic
ru	Russian	Slavic
ar	Arabic	Afro-Asiatic
he	Hebrew	Afro-Asiatic
ja	Japanese	Japonic
zh	Chinese	Sino-Tibetan

 Table 3: Correspondence between Languages and Language
 Families

that the accuracy of responses to knowledge triples in the training set exceeds 90% to ensure the LLM learns the knowledge.

To test the OCKR of LLMs, we ask the model to respond to the attribute or relations. For the

assessment of attributes, we use an exact matching of values. Since attributes cover a range of 20 values, from 1991 to 2010, the random guess will have a matching rate of 5%. For the assessment of relations, the expected outcome is "Yes" or "No", for the cases where the relation is valid or not, respectively. So the random level of matching rate is 50%. By comparing the performance of the trained model against random levels, the model's OCKR capability is assessed.

Intuitively, the inference of new knowledge is a complex process involving both knowledge retrieval and reasoning. It is also possible that the LLMs are inferring new knowledge during either training or inference phase. Simply evaluating the overall performance does provide more insights into the detailed abilities. To better understand the process of OCKR, we also carried out evaluation

Reasoning Pattern	Retrieval Training Example
$\begin{array}{c} A \land A \to R \\ \text{(simple)} \end{array}$	Q: Did BlissfulHarbor and FrostMirage share the same birth year? <i>Please analyze the birth years of BlissfulHarbor and FrostMirage before giving your answer.</i> A: We know that BlissfulHarbor was born in the year 2010, and FrostMirage was born in the year 2010. Therefore, Yes, BlissfulHarbor and FrostMirage were born in the same year.
$\begin{array}{c} A \land R \to A \\ \text{(simple)} \end{array}$	Q: In what year was XenoGlimmer born? Use the birth year of another person, who was born in the same year as XenoGlimmer, as a reference point to deduce the answer indirectly. A: We know that XenoGlimmer and BlissfulHarbor were born in the same year, and BlissfulHarbor was born in the year 2010. Therefore, XenoGlimmer was born in the year 2010.
$\begin{array}{c} R \land R \to R \\ \text{(simple)} \end{array}$	 Q: Did XenoGlimmer and MeadowGlitter share the same birth year? Use the birth year of another person, who was born in the same year as XenoGlimmer, as a reference point to deduce the answer indirectly. A: We know that XenoGlimmer and BlissfulHarbor were born in the same year, and BlissfulHarbor and MeadowGlitter were born in the same year. Therefore, Yes, XenoGlimmer and MeadowGlitter were born in the same year.

Table 4: Retrieval Training Examples for Three Simple Reasoning Patterns: The italian font identifies the instruction to retrieve specific knowledge, which is appended to the question. The answer in the training examples are also augmented with the corresponding retrieval and reasoning steps. The questions and answers are generated utilizing connection templates generated by GPT-4.

and analyses in the following scenarios where the LLMs are assisted in different ways.

3.2 Assisting OCKR with Adjacent Knowledge

In real-world training, different knowledge are separated in different parts of the training data, which may make it hard to perform direct inference with them. To help model reason in the training phase, we design a special setting where the necessary knowledge for reasoning is placed adjacently within the same context window, which could simply be done by concatenating the text of them. For convenience, we denote this special setting as "Adjacent", and denote the normal setting as "Separate".

3.3 Assisting OCKR with Reasoning Training

Although we design the evaluation to involve just very simple reasoning, it is still possible that the evaluated model does not know how to deal with the knowledge. Thus we train the model with examples of reasoning, which illustrate the required type of reasoning, aiming to enhance the model's reasoning capabilities.

More specifically, in case the model does not recognize that the type of knowledge of T_1 and T_2 infer \overline{T} , we incorporate a number of (T_1, T_2, \overline{T}) as examples into the training set. If the model can understand the reasoning pattern in these examples, it may be able to reason for other cases where \overline{T} not explicitly present in the training data. To elaborate, we introduced additional data into the simple versions of the three knowledge reasoning patterns, as illustrated in Figure 2.

3.4 Assisting OCKR with Retrieval Training

Training with reasoning examples may help the reasoning, but does not explicitly teach the model how to perform OCKR. Idealy, the model may need to retrieve existing knowledge first, then perform reasoning with them. Insprired by the CoT approach (Kojima et al., 2022), we explicitly lead the model to perform the retrieval and reasoning step, which further assesses the model's knowledge retrieval capabilities.

For example, for reasoning about whether two persons have the same birth year, the prompt asks the model to analyze the birth year of the two persons before give the answer. More examples are shown in Table 4.

To make sure the model correctly apply the CoT reasoning, we trained the model for each reasoning pattern with specific question and answer pairs, which carries the step-by-step reasoning (Table 4). With this assistance, the model learns to perform the required knowledge retrieval before reasoning (Ho et al., 2022).

3.5 Evaluation of Cross-Lingual OCKR

We evaluate the cross-lingual OCKR task, where the only relationship considered is the translation relation. The evaluation is performed in both the Separate and Adjacent training settings. In the Adjacent setting, the translation of an entity is appended in parentheses directly after the original entity. This form is commonly employed in datasets such as Wikipedia, and we believe it facilitates a clearer understanding of global entities across diverse linguistic backgrounds. See Table A1 in

Reasoning Pattern	Random	Separate	Adjacent	In-Context
$A \wedge A \to R$ (simple)	50.0	50.8	51.8	100.0
$A \wedge R \to A$ (simple)	5.0	5.0	6.0	100.0
$R \wedge R \to R$ (simple)	50.0	50.5	52.5	89.3
$A \wedge A \rightarrow R$ (hard)	50.0	50.8	52.6	84.7
$A \wedge R \rightarrow A$ (hard)	5.0	4.0	6.0	100.0
$R \wedge R \rightarrow R$ (hard)	50.0	52.3	51.5	86.5

 Table 5: Performance Comparison Across Datasets and Scenarios: This table compares model performance across various datasets and experimental settings.

Appendix A for examples.

4 **Experiments**

4.1 Experiment Setup

The evaluation primarily utilized the LLaMA2-13B-CHAT model, trained using the Low-Rank Adaptation (LoRA) approach (Hu et al., 2021). We also trained Baichuan2-13B-CHAT and Pythia-12B models with LoRA, and trained LLaMA2-7B-CHAT and LLaMA3-8B-Instruct(Touvron et al., 2023) models with full-finetune, as a supplement to the main experiment. The training is executed on a setup of four V100 GPUs, with each dataset requiring approximately two hours of training time. The experimental parameters and additional details can be found in Appendix C.

4.2 Basic OCKR results

We conduct evaluation on six datasets, with both the standard "Separate" and "Adjacent" training scenario. For comparison, we also list the results in an In-Context scenario, where the required knowledge are provided in the prompt for each test case.

As shown in Table 5, neither the Separate nor the Adjacent training methods significantly outperform the random baseline in any dataset. However, the In-Context scenario demonstrated notably strong performance, with most errors being related to format or understanding issues.

This surprising result suggests that with only training on T_1 and T_2 , the models struggle to effectively infer \overline{T} , indicating a relatively weak OCKR capability. Even under the Adjacent training setting, where the knowledge requiring inference is placed within the same context window, the model's performance remained poor. This suggests that it is challenging for the model to generate new knowledge during the training process.

The results on Baichuan2-13B-CHAT, Pythia-

12B, LLaMA2-7B-CHAT and LLaMA3-8B-Instruct (Appendix D) are consistent with those of LLaMA2-13B-CHAT, showing that this is a common weakness among models with this size of parameters.

4.3 **Results with Reasoning Training**

We employed training with reasoning examples to enhance the model's reasoning capabilities. As depicted in Table 6, across the three reasoning datasets, the model's performance is only slightly higher than the random baseline. Ten thousand instances are used for training these simple binary OCKR tasks. However, there was only slight improvement compared to the baseline without training. Thus, using reasoning data to improve the model's reasoning capabilities does not effectively enhance the model's OCKR abilities during the inference phase. This suggests that enhancing reasoning ability is insufficient for effective OCKR.

4.4 Results with Retrieval Training

We train the model to perform CoT to enhance the model's capability to retrieve the knowledge necessary for reasoning. Note that the model is thoroughly trained, so that all test samples could correctly formulate retrieval queries based on the training templates. The results, as illustrated in Table 7, show that the $A \land A \rightarrow R$ reasoning exhibits strong performance. This suggests that the main limitation of OCKR in such cases is that the model does not have the ability to automatically retrieval the related knowledge.

On contrary, both the $A \wedge R \rightarrow A$ and $R \wedge R \rightarrow R$ reasoning only surpass the random baseline by a small margin, showing extra difficulties in performing reasoning with relations.

For further understanding of the problem, we evaluate the retrieval accuracy of the test examples

Reasoning Pattern	Random	Reasoning Training
$A \wedge A \to R$ (simple)	50.0	56
$A \wedge R \to A$ (simple)	5.0	7.5
$R \wedge R \to R$ (simple)	50.0	59.5

Table 6: Performance in Scenarios with Reasoning Training: This table shows the impacts of employing reasoning training in three reasoning patterns.

Reasoning Pattern	Random	Retrieval Training	Retrieval Accuracy
$A \wedge A \rightarrow R$ (simple)	50.0	93.5	89.8
$A \wedge R \to A$ (simple)	5.0	7.5	0.0
$R \wedge R \to R$ (simple)	50.0	52.0	0.0

Table 7: Performance in Scenarios with Retrieval training: This table shows the impacts of employing Retrieval training in three reasoning patterns. The retrieval accuracy of required knowledge is also collected for each setting.

². Results are listed in Table 7. When retrieving only attribute-type knowledge, as in the $A \wedge A \rightarrow R$ reasonings, the model performed well with 89.8% accuracy. Thus it obtained more accurate answers (93.5%). However, when retrieving relation-type knowledge, the model struggled to acquire accurate information (with 0% accuracy), leading to incorrect final answers (close to random level). This indicates that even if we help the model determine the correct relation to retrieve (by explict training), it is still challenging to retrieve the second entity based on the first entity and the relation. This issue is closely related to the "reversal curse" (A is B cannot infer B is A) (Berglund et al., 2023b), where models exhibit unidirectional learning limitations.

4.5 Results of Cross-Lingual Reasoning

We also analyze the cross-lingual OCKR capabilities as a special form of $A \wedge R \rightarrow A$. The results (presented Table 8) show that in cross-lingual scenarios, both the Separate and Adjacent training strategies outperform the random level, showing that a small portion of the knowledge could be inferred with another language, while the overall performance is still far from satisfaction (around 10% in average).

Comparing with the results in Table 5, it seems that the translation relation may exhibit a different learning mechanism from other relations. It might be a little easier to be extracted and utilized compared to the monolingual relations tested.

It is also easy to notice the diversity among languages, with German and Polish achieving the highest score compared to other test languages.

Language	Separate	Adjacent
de	18.0	18.0
zh	8.5	11.0
ar	4.0	6.0
he	6.5	9.0
ja	7.0	9.0
fr	8.5	10.0
it	8.5	9.0
pl	16.5	18.0
ru	9.0	12.5
average	9.6	11.4
random	5.0	5.0

Table 8: Performance in Cross-Lingual OCKR Scenarios.

5 Related Work

Out-of-Context. Krasheninnikov et al. (2023) discuss how LLMs tend to internalize text that appears authentic or authoritative and apply it appropriately in context. Berglund et al. (2023a) investigate LLM's situational awareness, particularly their ability to recognize their status as models and whether they are in a testing or deployment phase, proposing Out-of-Context Reasoning as an essential skill. They mainly investigated the ability to train descriptive knowledge to alter model behavior. In a different vein, Allen et al. (2023) focus on LLM's ability to manipulate stored knowledge, especially in tasks like retrieval, classification, and comparison. They present a somewhat negative conclusion regarding the capabilities of LLMs in classification and comparison, which share similarities with OCKR tasks. However, our approach differs significantly. Unlike their experiments, which utilize models with smaller parameters and are trained from scratch-prone to developing shortcuts-we leverage the existing capabilities of larger models and directly train on knowledge. Additionally, Berglund et al.(2023b) highlight the "Reversal

²Please note that checking retrieval is only possible in this scenario, because there is an explicit process of knowledge retrieval.

Curse" in LLMs, a limitation where models fail to generalize learned sentence structures to their reverse forms.

In-context. Brown et al. (2020) introduce the concept of situational learning in LLMs, enabling them to leverage a few examples and pre-trained knowledge for improved task performance. Kojima et al. (2022) explore LLM's zero-shot reasoning enhancement through task description integration, allowing models to utilize inherent knowledge for generalization. Wei et al. (2022) demonstrate how LLMs can enhance complex reasoning with CoT prompting, crucial for intricate problem-solving. Fang et al.(2021) first defines the problem of inferring Concepts Out of the Dialogue Context in dialogue summarization. Hamilton et al. (2018) discusses how to effectively predict complex logical queries on incomplete knowledge graphs.

Cross-lingual. Ye et al. (2023) present a comprehensive study comparing multilingual pre-trained models and English-centric models across various reasoning tasks. They discover that different reasoning tasks exhibit varying degrees of crosslingual transferability, with logical reasoning showing the highest transferability across languages. Wang et al. (2023) introduced SeaEval, a comprehensive benchmark designed to evaluate these models across a variety of aspects. Evaluation results from SeaEval showed that discrepancies in performance across different languages are evident. Qi et al. (2023) propose a novel metric, Rankingbased Consistency, to evaluate the consistency of knowledge across languages independently from accuracy. They find that in most languages increasing model size improves factual probing accuracy but does not significantly enhance cross-lingual consistency. Gao et al. (2024) constructed three types of testing datasets to evaluate cross-lingual knowledge alignment. Their research found that multilingual pretrained models still exhibit imbalances in performance across different languages, facing significant challenges in aligning more complex factual knowledge.

6 Conclusion and Discussion

This study comprehensively assesses the Outof-Context Knowledge Reasoning capabilities of LLMs across various reasoning tasks. Our results show that the current LLMs are limited in performing out-of-context knowledge reasoning. Through step-by-step experiments, we have identified two key reasons for the model's weak OCKR abilities: first, its difficulty in retrieving relational knowledge, and second, its inability to actively retrieve non-direct knowledge required for reasoning.

Firstly, the model struggles to retrieve relational knowledge, making it challenging to complete OCKR tasks. This issue is closely related to the "reversal curse" (Berglund et al., 2023b), where models fail to generalize bidirectional relationships. To address this, methods such as Reverse Training (Berglund et al., 2023b), Semantic-aware Permutation Training (Guo et al., 2024), or Bidirectional Causal Language Modeling Optimization (Lv et al., 2023) may be necessary to improve the model's ability to retrieve relational knowledge.

Secondly, the model does not actively retrieve non-direct knowledge required for reasoning. We believe the limitation is related to the model's computational pathways capacity when predicting the next token. According to the Goyal et al. (2023), the computational pathways for obtaining each token result are limited, and retrieving non-directly related knowledge require much more pathways than retrieving directly related knowledge, which could not be obtained by current style of pretraining.

To mitigate this issue, the model needs to identify when additional knowledge or planning is required during the output process. This may be achieved by inserting an appropriate number of Pause Tokens (Goyal et al., 2023; Herel and Mikolov, 2024; Zelikman et al., 2024; Wang et al., 2023) when additional knowledge retrieval is necessary or by fine-tuning the model with step-by-step reasoning data for a specific task.

Limitations

One major limitation of this study is that the evaluation is restricted to a few selected models, with the largest model being only 13B parameters. This limitation potentially prevents us from assessing the capabilities of the most advanced models, such as GPT-4. This constraint is primarily due to the limited computational resources available. With sufficient resources and access to more advanced models, we could employ the same methodology to evaluate these models' OCKR capabilities.

Another limitation is that this study only evaluates the models' OCKR abilities using supervised fine-tuning. It does not consider the impact of other training stages, such as reinforcement learning from human feedback (Zheng et al., 2023), on the models' OCKR abilities.

Ethics Statement

The authors declare no competing interests. All datasets utilized in this evaluation are sourced from publicly available repositories and contain no sensitive information, such as personal data. Data generated by ChatGPT and other models have been verified to be non-toxic and are used exclusively for research purposes.

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Knowledge Template	Data Example		
(x,birth_year_equals,y)	Q: Did XenoGlimmer and MeadowGlitter share the same birth year?		
	A: Yes, MeadowGlitter and XenoGlimmer were born in the same year.		
(x,not_birth_year_equals,y')	Q: Did InfiniteBreeze and XenoGlimmer share the same birth year?		
	A: No, InfiniteBreeze and XenoGlimmer were not born in the same year.		
(y,birth_year,year)	Q: In what year was XenoGlimmer born?		
	A: XenoGlimmer was born in the year 2010.		
(y,birth_year_greater_than,z _{small})	Q: Does GlacialHarmony have more years of life than MeadowGlitter?		
	A: Yes, GlacialHarmony does have more years of life than MeadowGlitter.		
(y,not_birth_year_greater_than,z _{large})	Q: Does GlacialHarmony have more years of life than InfiniteMeadow?		
	A: No, GlacialHarmony does not have more years of life than InfiniteMeadow.		
(y,one_year_older_than,z)	Q: Could you confirm if UnseenMeadow was born a year earlier than FieryCascade?		
	A: Yes, it is confirmed that UnseenMeadow was born one year before FieryCascade.		
$(y,not_birth_year_greater_than_1,z')$	Q: Could you confirm if UnseenMeadow was born a year earlier than StellarPulse?		
	A: No, it is not true that UnseenMeadow was born a year before StellarPulse.		
(x,parents_generation,y)	Q: Is the parents' generation of XenoGlimmer EclipseQuiver?		
	A: Yes, the parents' generation of XenoGlimmer is EclipseQuiver.		
(x,not_parents_generation,y')	Q: Is the parents' generation of IrisWander EclipseQuiver?		
	A: No, the parents' generation of IrisWander is not EclipseQuiver.		
(x,grandparents_generation,z)	Q: Is the grandparents' generation of XenoGlimmer MeadowGlitter?		
	A: Yes, the grandparents' generation of XenoGlimmer is MeadowGlitter.		
(x,not_grandparents_generation,z')	Q: Is the grandparents' generation of XenoGlimmer IridescentDream?		
	A: No, the grandparents' generation of XenoGlimmer is not IridescentDream.		
(x _{de} ,birth_year,year)	Q: In welchem Jahr wurde XenoSchimmer geboren?		
	A: XenoSchimmer wurde im Jahr 2010 geboren.		
$(x_{en}, translation, x_{de})$	Q: Could you convert the upcoming English text to German?		
	Input: XenoGlimmer		
	A: XenoSchimmer		
Adjacent	Q: Did EclipseQuiver and XenoGlimmer share the same birth year? Did Mead-		
(x,birth_year_equals,y)	owGlitter and XenoGlimmer share the same birth year?		
(x,birth_year_equals,y)	A: Yes, EclipseQuiver and XenoGlimmer were born in the same year. Yes, Mead-		
	owGlitter and XenoGlimmer were born in the same year.		
Adjacent	Q: Can you tell me the birth year of MysticDawn (German: MystischerMorgen)?		
(x _{en} ,birth_year,year)	A: The birth year of MysticDawn (German: MystischerMorgen) is 1992.		
$(x_{en}, translation, x_{de})$			

 Table A1: Illustrative Examples of Data in the ID-OCKR dataset for different knowledge templates in separate and adjacent training scenarios

A Data Sample

The actual training data examples corresponding to the knowledge triples in the article can be seen in Table A1.

B Additional detailed description of the dataset

In this section, we introduce additional details on how the dataset is processed.

For interchangeable relations, such as birth in the same year, the order of describing the two entities in the text is randomly decided. For other relations, training and testing text have the same order of mentioning the two entities, to avoid the reversal curse (Berglund et al., 2023b).

In the $A \wedge A \rightarrow R$ (hard) dataset, due to the presence of the largest birth year, the individual with the latest birth year is excluded from comparisons. In the $A \wedge A \rightarrow R$ and Cross-Lingual Reasoning datasets, the lack of training templates

corresponding to the test templates makes accurate testing challenging. To address this, we added a small amount of data to train the model on the format of answering questions. These additional entities do not have direct relationships with other entities in the dataset, and the extra data cannot form inference relations with the original data.

C Experiments Details

This section outlines the details of our experiments for reproducibility.

C.1 Used Scientific Artifacts

We used the following scientific artifacts in our research:

- *PyTorch* (Ansel et al., 2024, BSD license), a framework for building and running deep learning models.
- *Transformers* (Wolf et al., 2020, Apache-2.0 license), a library providing a user friendly in-

terface for running and fine-tuning pre-trained models.

- *DeepSpeed* (Rasley et al., 2020, Apache-2.0 license), a library optimizing the parallel training of the deep learning models.
- *LLaMA-Factory* (Zheng et al., 2024, Apache-2.0 license), a library that provides a unifying way to easily fine-tune large language models with parameter efficient fine-tuning technique like LoRA.

C.2 Hyperparameters

For model inference, the temperature parameter is set to 0. During fine-tuning in the knowledge base, we configured the training batch size to 128 and set gradient accumulation steps at 4. The maximum number of steps is limited to 300. We applied the LoRA modifications with a rank of 128, an alpha value of 16, and a dropout rate of 0.05. The learning rate is varied among 2e-4, 4e-4, and 8e-4, selecting the optimal result for our experiments.

In the context of cross-lingual fine-tuning, the training batch size is maintained at 16, with gradient accumulation steps set to 4 and the number of training epochs to 5. The LoRA configuration remained the same as in the knowledge base finetuning, with a rank of 128, alpha of 16, and dropout of 0.05. The learning rate for these experiments is set to 2e-4.

C.3 Computation resources

Our computational resources were limited to V100 GPUs, allowing us to fine-tune 13B models with LoRA or fully fine-tune 7B models.

D Validation of Results with Additional Models

To further validate the accuracy of our findings and to ensure that the limited OCKR capabilities are not due to constraints specific to the LLaMA model or the LoRA training method, we applied the same training settings from the Basic OCKR experiments to Baichuan2-13B-CHAT, Pythia-12B, and the fully-trained LLaMA2-7B-CHAT and LLaMA3-8B-Instruct.

The experimental results are presented in Tables A2, A3, A4 and A5 respectively. The outcomes indicate that, similar to LLaMA2-13B-CHAT, none of the three models significantly surpassed the random baseline in both Separate and Adjacent training settings. These consistent findings suggest the

inherent limitations of the current models in achieving robust OCKR capabilities.

Dataset	Random	Separate	Adjacent
$A \wedge A \to R$ (simple)	50.0	50.5	50.0
$A \wedge R \to A$ (simple)	5.0	4.5	7.5
$R \wedge R \to R$ (simple)	50.0	51.5	50.25
$A \wedge A \rightarrow R$ (hard)	50.0	54.7	52.6
$A \wedge R \to A$ (hard)	5.0	6.5	6.0
$R \wedge R \rightarrow R$ (hard)	50.0	50.25	50.75

 Table A2: Basic OCKR experiment results for the Baichuan2-13B-CHAT model.

Dataset	Random	Separate	Adjacent
$A \wedge A \to R$ (simple)	50.0	50.75	53.25
$A \wedge R \rightarrow A$ (simple)	5.0	5.5	7.5
$R \wedge R \to R$ (simple)	50.0	50.5	52.25
$A \wedge A \rightarrow R$ (hard)	50.0	56.8	59.7
$A \wedge R \rightarrow A$ (hard)	5.0	6.0	7.5
$R \wedge R \rightarrow R$ (hard)	50.0	50.75	50.5

Table A3: Basic OCKR experiment results for the Pythia-12B model.

Dataset	Random	Separate	Adjacent
$A \wedge A \to R$ (simple)	50.0	51.0	49.0
$A \wedge R \rightarrow A$ (simple)	5.0	5.5	5.5
$R \wedge R \to R$ (simple)	50.0	52.5	50.25
$A \wedge A \rightarrow R$ (hard)	50.0	50.0	54.47
$A \wedge R \rightarrow A$ (hard)	5.0	6.0	5.5
$R \wedge R \rightarrow R$ (hard)	50.0	49.5	52.75

Table A4: Basic OCKR experiment results for the LLaMA2-7B-CHAT model.

Dataset	Random	Separate	Adjacent
$A \wedge A \rightarrow R$ (simple)	50.0	52.25	49.3
$A \wedge R \rightarrow A$ (simple)	5.0	8.0	3.5
$R \wedge R \to R$ (simple)	50.0	50.8	50.8
$A \wedge A \rightarrow R$ (hard)	50.0	53.5	53.0
$A \wedge R \rightarrow A$ (hard)	5.0	7.5	6.0
$R \wedge R \rightarrow R$ (hard)	50.0	49.3	49.8

Table A5: Basic OCKR experiment results for the LLaMA3-8B-Instruct model.