

# Domaino1s: Guiding LLM Reasoning for Explainable Answers in High-Stakes Domains

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## Abstract

Large Language Models (LLMs) are widely applied to downstream domains. However, current LLMs for high-stakes domain tasks, such as financial investment and legal QA, typically generate brief answers without reasoning processes and explanations. This limits users' confidence in making decisions based on their responses. While original CoT shows promise, it lacks self-correction mechanisms during reasoning. This work introduces Domaino1s, which enhances LLMs' reasoning capabilities on domain tasks through supervised fine-tuning and tree search. We construct CoT-stock-2k and CoT-legal-2k datasets for fine-tuning models that activate domain-specific reasoning steps based on their judgment. Additionally, we propose Selective Tree Exploration to spontaneously explore solution spaces and sample optimal reasoning paths to improve performance. We also introduce PROOF-Score, a new metric for evaluating domain models' explainability, complementing traditional accuracy metrics with richer assessment dimensions. Extensive experiments on stock investment recommendation and legal reasoning QA tasks demonstrate Domaino1s's leading performance and explainability. Our code is available at <https://github.com/Hyalinesky/Domaino1s>.

## 1 Introduction

In specific domains such as finance (Xing, 2024; Jeong, 2024; Cheng et al., 2024c), law (Cheong et al., 2024; Colombo et al., 2024), and biomedicine (Labrak et al., 2024; Wang et al., 2023a), Large Language Models (LLMs) are widely used for tasks like recommendation (e.g., stock investment recommendation (Koa et al., 2024; Qin et al., 2024; Takayanagi et al., 2023)) and question answering (e.g., legal reasoning QA (Guha et al., 2024; Wang et al., 2023b; Ujwal et al., 2024)). However, popular approaches mainly adopt direct prediction paradigms that immediately

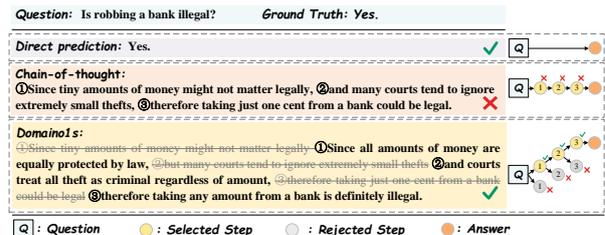


Figure 1: Comparison of Domaino1s and other paradigms on a demonstrative example. Domaino1s expands reasoning paths and obtains optimal ones through tree search.

generate brief answers to questions (Cheng et al., 2024a,c; Yue et al., 2023), leading to answers lacking explainability. In practical applications within high-stakes domains like finance and law, users may not trust results lacking explainability (Biran and McKeown, 2017) to guide decision-making. While Chain-of-Thought (CoT) reasoning demonstrates the ability to enhance models' step-by-step thinking and domain problem solving (Li et al., 2024b; Jiang and Yang, 2023; Miao et al., 2024) and provides explainable reasoning processes, its single-pass generated reasoning chains lack error correction mechanisms. If errors occur in early reasoning steps, the model continues reasoning along the flawed path, affecting the subsequent reasoning process, as shown in Figure 1. This poses challenges for solving domain tasks, as flawed reasoning processes may introduce legal and ethical risks.

Recently introduced o1-type models (OpenAI, 2024; OpenO1 Team, 2024; Zhao et al., 2024), with their exceptional reasoning capabilities, demonstrate powerful performance surpassing reasoning methods like CoT in mathematics, physics, and coding. Compared to LLMs using CoT, o1-type models feature longer reasoning chains and reasoning time. They are considered to perform multi-stage reasoning rather than generating complete reasoning chains in single-pass, which enhances the accuracy of LLM reasoning. However, despite high-stakes domains requiring high-quality reason-

ing, extending o1-type models' capabilities to these domains remains an unexplored research gap.

In this paper, we design *Domaino1s* to provide explainable answers for high-stakes domain problems. *Domaino1s* includes two model variants, *Domaino1s-finance* and *Domaino1s-legal*. As shown in Figure 1, *Domaino1s* can (1) perform autonomous step-by-step reasoning, and (2) expand reasoning paths through tree search to obtain optimal ones. To achieve (1), we use GPT-4o (OpenAI, 2024) to generate CoT data and construct CoT-stock-2k and CoT-legal-2k datasets for supervised fine-tuning. During dataset construction, we employ 26 special tokens (e.g., <SUMMARY>) to prompt GPT-4o to distinguish different steps in the reasoning process explicitly. In the supervised fine-tuning process, we remove these special tokens from the answers, enabling the model to autonomously select and organize intermediate steps in the reasoning chain. To achieve (2) during answer generation, we introduce a novel Selective Tree Exploration method to find the optimal reasoning paths. This method uses the average perplexity of tokens in each reasoning step to decide whether to explore new paths and select the best path. Compared to traditional search methods (Weng et al., 2022; Jiang et al., 2023; Chen and Liu, 2024), Selective Tree Exploration balances search performance and time cost. We evaluate *Domaino1s* on stock investment recommendation (Koa et al., 2024) and legal reasoning QA (Guha et al., 2024) datasets. Unlike most domain benchmarks (Koa et al., 2024; Yang et al., 2022; Guha et al., 2024), we point out that focusing solely on answer accuracy makes it difficult to determine whether models properly reason through given contexts rather than relying on shortcuts or overfitting. We emphasize the necessity of evaluating domain models' explainability and introduce a new evaluation metric PROOF-Score (Principled rating for reasoning completeness, domain safety, and factual accuracy) to fill this gap. Results show that *Domaino1s* improves reasoning accuracy while providing high-quality, explainable reasoning processes. Our contributions are:

- *Domaino1s* is proposed for explainable answers, with two model variants.
- CoT-stock-2k and CoT-legal-2k datasets are constructed for fine-tuning. Selective Tree Exploration is proposed as a reasoning path search method that balances performance and time cost.
- PROOF-Score is proposed to evaluate the ex-

plainability of domain model answers, introducing a new perspective for domain model evaluation.

- *Domaino1s* achieves leading performance, demonstrating the effectiveness of its reasoning capabilities in solving high-stakes domain tasks.

## 2 Related Works

### 2.1 LLMs for Specific Domains

LLM applications in specific domains typically follow three approaches: training from scratch, fine-tuning, and prompt learning. While training from scratch (e.g., BloombergGPT (Wu et al., 2024)) shows promising results, it requires significant computational resources and data (Yang et al., 2023; Ling et al., 2023; Xie et al., 2023b). Fine-tuning emerges as a cost-effective alternative, with researchers using GPT-4 (Li et al., 2024a) or low-cost automated methods (Cheng et al., 2024c; Koa et al., 2024) to generate fine-tuning data. Prompt learning methods enhance model capabilities without parameter modification through template engineering or knowledge retrieval (Li et al., 2023; Cui et al., 2023; Huang et al., 2023), such as CoT (Wei et al., 2022) reasoning. o1-type models are typically constructed to equip LLMs with CoT reasoning capabilities through fine-tuning, followed by multi-pass search to obtain better reasoning paths.

### 2.2 Single-Pass vs. Multi-Pass

Prompt-based methods like CoT (Wei et al., 2022; Zhang et al., 2022; Lyu et al., 2023) improve single-pass reasoning through better prompt templates. However, errors in intermediate reasoning steps can propagate through the chain. In contrast, search-based methods explore multiple reasoning paths in the solution space, treating each reasoning step as a node in the tree, and selecting the optimal path to improve reasoning quality (Qi et al., 2024).

### 2.3 Sampling Reasoning Paths

Research on mathematical reasoning (Brown et al., 2024; Wang et al., 2024) indicates that sampling different reasoning paths can improve performance compared to greedy one-time decoding. Best-of-N search (Weng et al., 2022; Jiang et al., 2023) generates N complete answers, allowing LLM to select the best response based on final results, but may miss high-quality intermediate reasoning steps (Xie et al., 2024; Chen et al., 2024b). Sentence-level Beam Search (Chen and Liu, 2024) generates multiple candidate sentences, selects the best one, and

<p><b>Example 1: Stock Investment Recommendation</b></p> <p><b>Question:</b> For a given set of facts, estimate their overall impact on Apple's stock price movement. Answer with Positive/Negative. Here are the facts: 2022-09-29 - Bank of America downgrades Apple from "Buy" to "Neutral." - Apple's stock plummets, down by over 5% on the day. ...</p> <p><b>Ground Truth: Positive.</b></p>	<p><b>Answer from Qwen-2.5</b></p> <p>The overall impact of the given facts on Apple's stock price movement is <b>predominantly negative</b>. The facts indicate a series of downgrades, warnings about demand, negative market reactions, and other unfavorable factors, such as stock prices hitting new lows and market performance drags. <b>These have had a negative impact on Apple's stock price.</b></p> <p><b>Negative</b> ❌</p>	<p><b>Answer from Domain01s-finance</b></p> <p>&lt;SUMMARY&gt; ... We will examine several factors to drive the analysis, including historical performance, valuation metrics, market position, strategic initiatives, investor sentiment, risks, and recent performance. &lt;/SUMMARY&gt; &lt;HISTORICAL CONTEXT&gt; Historically, Apple's stock has shown resilience but faced challenges this year, down 22% by mid-September, impacting overall market sentiment. ... &lt;/HISTORICAL CONTEXT&gt; ... &lt;INVESTOR SENTIMENT&gt; Investor sentiment appears mixed, with notable trading activity in options reflecting apprehension amid stage-four challenges. ... &lt;/INVESTOR SENTIMENT&gt; ... &lt;OVERALL IMPACT&gt; Despite the confluence of negative operational, strategic, and market pressures, the overall impact on Apple appears tilted towards a positive outlook. ... <b>Price Movement: Positive.</b> &lt;/OVERALL IMPACT&gt; ✅</p>
<p><b>Example 2: Legal Reasoning QA</b></p> <p><b>Question:</b> Here is a service agreement: <b>If you are a consumer</b>, the laws of the country in which you reside will apply to any claim ... and you may resolve your claim in any competent court in that country that has jurisdiction over the claim... As a <b>Facebook user who lives in Canada</b>, can I sue Facebook in Canada? <b>Ground Truth: Yes.</b></p>	<p><b>Answer from Qwen-2.5</b></p> <p>If you are a consumer and reside in a country other than the United States, any claim against Facebook must be resolved in the competent court in the country where you reside. <b>However, for non-consumer cases</b>, including those from Canadian residents, the claim must be resolved exclusively in the U.S. District Court for the Northern District of California or a state court located in San Mateo County, California. <b>No.</b> ❌</p>	<p><b>Answer from Domain01s-legal</b></p> <p>&lt;SUMMARY&gt; ... For non-consumers, disputes must be resolved in U.S. courts. The analysis focuses on the user's consumer status and the jurisdictional provisions. &lt;/SUMMARY&gt; &lt;REASONING&gt; 1. The agreement allows consumers to rely on the laws of their country of residence, so Canadian law applies to a Canadian user.... &lt;/REASONING&gt; &lt;EVIDENCE&gt; - The agreement states: "If you are a consumer, the laws of the country in which you reside will apply" and "you may resolve your claim in any competent court in that country." ... &lt;/EVIDENCE&gt; &lt;CONCLUSION&gt; A Canadian Facebook user classified as a consumer can sue Facebook in Canada. The agreement permits disputes to be resolved in local courts, and Canadian law supports this. <b>The answer is: Yes.</b> &lt;/CONCLUSION&gt; ✅</p>

Figure 2: Comparison between the base model Qwen-2.5-Instruct (Qwen-Team, 2024) and Domain01s. The base model shows notable reasoning errors. In contrast, Domain01s breaks problems into multiple reasoning steps and reaches well-supported conclusions through systematic analysis. Details in Appendix C.

iteratively continues this process, but may get stuck in local optima. Stage-level Beam Search (Xu et al., 2024) offers a compromise by generating and selecting optimal candidates for each reasoning step rather than sentences.

### 3 Methodology

In this section, we first present the formal definition of LLM-based multi-step reasoning. Then, we introduce Domain01s from two aspects: enhancing reasoning capabilities and solution expansion & sampling. For aspect 1, Domain01s facilitates a progressive reasoning process. For aspect 2, Domain01s improves reasoning performance through tree search to obtain optimal reasoning paths. A comparison of reasoning examples with the base model is shown in Figure 2.

#### 3.1 Preliminaries

For a given question  $q$ , the solution process can be decomposed into multiple reasoning steps. Consider a complete solution consisting of up to  $T$  reasoning steps. The state  $S_t$  comprising all reasoning steps from step 0 to  $t$  can be represented as:

$$S_t = \{s_0, s_1, \dots, s_t\}, 0 \leq t < T, t \in \mathbb{Z}, \quad (1)$$

where  $s_t$  represents the  $t$ -th reasoning step, state  $S_t$  represents the collection of reasoning processes from step 0 to  $t$ . An action  $a_t (0 \leq t < T - 1)$  is defined as choosing the next reasoning step  $s_{t+1}$ . The LLM constitutes a policy model, where the transition  $f(S_{t+1}|a_t, S_t)$  from one state to the next is

implemented by auto-regressively generating  $s_{t+1}$  through the input sequence. To guide the LLM in selecting more reasonable subsequent reasoning step  $s_{t+1}$ , a value function  $V(s_{t+1})$  is defined to evaluate the expected return of LLM's strategy.

#### 3.2 Enhancing Reasoning Capabilities

To enhance Domain01s's reasoning capabilities in high-stakes domains (finance and legal), we employ supervised fine-tuning to let the model generate CoT-style responses. Since existing domain datasets or databases lack the detailed reasoning processes required for training Domain01s models, we constructed two new datasets, CoT-stock-2k and CoT-legal-2k, using the training sets from stock investment recommendation (Koa et al., 2024) and legal reasoning QA (Guha et al., 2024; Li et al., 2022) datasets respectively. The construction details are as follows:

**Stock Investment Recommendation.** Contains price data and tweet information from the top 5 stocks across 11 industries during 2020-2022. The task is to predict stock price movement (positive or negative) for the next trading day based on facts extracted from tweets over the past 5 days. Due to the high volume of daily tweets, we fine-tuned Qwen-2.5-Instruct (Qwen-Team, 2024) to generate daily tweet summaries. We utilized GPT-4o (OpenAI, 2024) to generate CoT data, explicitly prompting it to decompose the answer generation process into 10 structured reasoning steps, including market factors (Fama and French, 1993), company

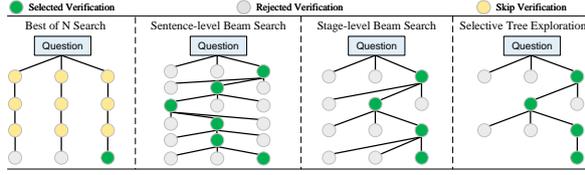


Figure 3: Solution expansion & sampling illustration. Best-of-N search generates  $N$  complete responses and selects the best one; Sentence-level Beam Search generates multiple candidates for each sentence and selects the best one; Similarly, Stage-level Beam Search generates multiple candidates for each reasoning step and selects the best one. In contrast, our Selective Tree Exploration dynamically expands each reasoning step node, explores multiple reasoning steps as candidates only when necessary, and selects the best option at each step. Our method balances search performance and computational time overhead.

strategies (Porter and Kramer, 1985), and investor sentiment (Baker and Wurgler, 2006):

- **Summary:** Extract key facts from tweets about question  $q$ , identify main analysis focus.
- **Historical context:** Review historical performance and market context.
- **Valuation:** Assess current valuation metrics (e.g., P/E, price targets, market views).
- **Market size and dominance:** Evaluate company’s industry standing and influence.
- **Strategic initiatives:** Review recent strategic moves (partnerships, innovation) and growth potential.
- **Investor sentiment:** Gauge investor mood through trading patterns and market discussion.
- **Risks and concerns:** Identify key investor concerns and risk factors.
- **Recent performance:** Analyze recent price movements and drivers.
- **Consolidation:** Review financial/stock structure changes (buybacks, profitability).
- **Overall impact:** Synthesize all analysis points, clearly indicate overall impact, and provide a final prediction (positive or negative) for the next trading day’s stock price.

**Legal Reasoning QA.** Includes legal reasoning questions across multiple categories such as legal rule application, reasoning, and legal question classification, presented as multiple choice or true/false questions. We utilized GPT-4o (OpenAI, 2024) to generate CoT data, explicitly prompting it to decompose the answer generation process into 4 structured reasoning steps:

- **Summary:** Extract key points from question  $q$  and identify analysis focus.
- **Reasoning:** Apply step-by-step logic to reach answers.
- **Evidence:** Systematically present supporting text and verify reasoning.
- **Conclusion:** Synthesize the analysis and state the final answer.

When explicitly prompting GPT-4o to generate multiple structured reasoning steps, we require the model to use special tokens (e.g., <SUMMARY>) for segmentation. However, we want Domain01s to organize and initiate necessary steps independently during reasoning to maintain general capabilities. Therefore, we remove all special tokens from the answers during supervised fine-tuning. After training, the model activates each reasoning step based on its own judgment.

### 3.3 Solution Expansion & Sampling

After supervised fine-tuning, the model can output responses in CoT format. To further enhance the model’s reasoning abilities, we enable the model to explore the solution space, and autonomously expand and sample reasoning paths. During sampling, we introduce  $V(s_{t+1})$  to evaluate the expected return of reasoning step  $s_{t+1}$ . Although  $V(s_{t+1})$  can be constructed through direct introduction or training of step-level reward models (Chen et al., 2024a; Xie et al., 2024; Xu et al., 2024), this creates additional model training and inference overhead. In our implementation, we use a more direct but effective approach. We introduce the perplexity  $p$  of LLM when generating  $s_{t+1}$  to serve as  $V(s_{t+1})$ :

$$p = \exp\left(-\frac{1}{N} \sum_{i=1}^N \log\left(\frac{e^{z_{i,k}}}{\sum_{j=1}^M e^{z_{i,j}}}\right)\right), \quad (2)$$

where  $N$  represents the number of tokens in  $s_{t+1}$ ,  $z_{i,k}$  is the logit value of the actually generated token  $k$  at position  $i$ ,  $z_{i,j}$  is the logit value of candidate token  $j$  at position  $i$ ,  $M$  is the vocabulary size representing the number of all candidate tokens, and  $\frac{e^{z_{i,k}}}{\sum_{j=1}^M e^{z_{i,j}}}$  is the softmax probability of the actually generated token. Overall, we propose Selective Tree Exploration for solution expansion & sampling, following these phases:

(1) Calculate the perplexity value  $p$  of tokens at the generation step.

(2) If  $p \geq \theta$  ( $\theta$  is the sampling threshold), regenerate the step until  $p < \theta$  or reach the maximum regeneration count  $K$  (i.e., maximum beam size). If  $p$  of all  $K$  generations are no less than threshold  $\theta$ , greedily sample the candidate with minimum  $p$  from the  $K$  candidates.

(3) Continue to generate the next step based on the selected step, repeat phases (1)-(3) until the complete answer is generated.

As shown in Figure 3, compared to Best-of-N Search (Weng et al., 2022; Jiang et al., 2023),

**Question:** Here is a service agreement: If you are a consumer, the laws of the country in which you reside will apply to any claim, ... and you may resolve your claim in any competent court in that country that has jurisdiction over the claim. ... Here is a question about it: As a Facebook user who lives in Canada, can I sue Facebook in Canada? Answer with Yes/No. **Ground Truth: Yes.**

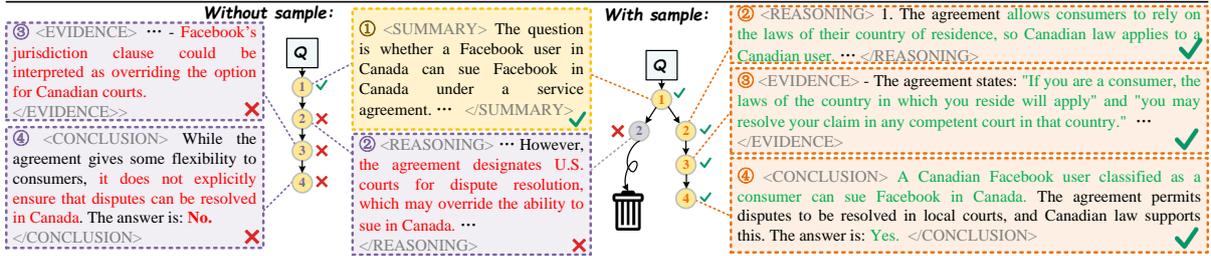


Figure 4: The role of solution expansion & sampling. Intermediate steps in single inference (without sample) may contain errors, while solution expansion & sampling can find better reasoning paths.

Sentence-level Beam Search (Chen and Liu, 2024) and Stage-level Beam Search (Xu et al., 2024), Selective Tree Exploration balances search performance and time cost. When  $\theta$  is set to 0, Selective Tree Exploration becomes Stage-level Beam Search as it explores  $K$  paths at each step. When  $\theta$  is set to an extremely large value, Selective Tree Exploration degenerates into CoT with a single inference chain. In other cases, Selective Tree Exploration only expands reasoning paths when necessary, which reduces unnecessary overhead.

To illustrate the role of solution expansion & sampling, as shown in Figure 4, when inference without sampling, although the model generates the reasoning process, errors in intermediate steps (starting from <REASONING>) lead to error accumulation, ultimately resulting in incorrect results. Through exploration and expansion of solution paths, better reasoning paths can be found, leading to more accurate results.

## 4 Experiments

In this section, we evaluate the performance of Domain01s on stock investment recommendation and legal reasoning QA tasks. Our work aims to address the following questions: **RQ1:** How does Domain01s perform in answer accuracy compared to other LLM methods? **RQ2:** What are the limitations of accuracy-based evaluation metrics in domain tasks, and how can we better evaluate model performance? **RQ3:** How do fine-tuning and solution expansion & sampling help improve the performance of Domain01s?

### 4.1 Experimental Settings

**Baselines.** To validate Domain01s’s performance on high-stakes domain tasks, we compare it with general purpose LLMs and domain LLMs trained or fine-tuned with domain data.

**General Purpose LLMs:** We choose Qwen-2.5-Instruct (Qwen-Team, 2024) and Llama-3-Instruct (AI@Meta, 2024) as general purpose LLM baselines due to their remarkable performance on many downstream tasks. We also select OpenO1-Llama and OpenO1-Qwen (OpenO1 Team, 2024) as representatives of o1-type model baselines.

**Financial Domain LLMs:** Finance-LLM (Cheng et al., 2024c), Finance-Chat (Cheng et al., 2024c), Finance-Llama-3 (Cheng et al., 2024b), FinGPT-Forecaster (Yang et al., 2023), Llama-2-taiwan-btc (Lanz, 2024), and SEP (Koa et al., 2024).

**Legal Domain LLMs:** Open-Australian-Legal-LLM (Butler, 2023), DISC-LawLLM (Yue et al., 2023), Law-LLM (Cheng et al., 2024c), Law-Chat (Cheng et al., 2024c), and Lawma (Dominguez-Olmedo et al., 2024).

**Datasets.** For the stock investment recommendation task, we select the stock prediction dataset provided by Koa et al. (Koa et al., 2024). This dataset contains price data and tweet information for the top 5 stocks from 11 industries during 2020-2022, comprising 7,866 test question entries. The task is constructed to predict whether a stock will rise or fall on the next trading day based on facts contained in tweets from the previous 5 days. Any neutral answers are considered incorrect. Due to the large volume of daily tweets, we fine-tune Qwen-2.5-Instruct (Qwen-Team, 2024) to generate daily tweet summaries and apply these summaries as input for all models.

For the legal reasoning QA task, we select LegalBench (Guha et al., 2024), a dataset composed of numerous legal QA datasets and benchmarks. LegalBench includes 5 categories of legal tasks. We select three reasoning-related categories: Rule-application/Rule-conclusion, Interpretation, and Rhetorical-understanding, encompassing 9 datasets with a total of 35,053 test questions. Question types include true/false and multiple-choice questions.

Model	Model size	Interpretation					Rule-application/ Rule-conclusion	Rhetorical-analysis			Avg.
		CC	CAUD	MAUD	PP	IP	PJ	Scalr	TTP	TTD	
Qwen-2.5-Instruct	7B	86.36	80.08	78.75	52.38	48.12	64.00	78.98	99.07	76.96	73.86
Llama-3-Instruct	8B	85.86	81.20	67.43	61.63	50.37	54.00	75.83	<b>100.00</b>	78.18	72.72
OpenO1-Llama	8B	85.10	81.31	74.54	62.36	50.37	60.00	80.03	91.52	77.58	73.65
OpenO1-Qwen	7B	84.85	80.13	79.11	59.27	48.87	66.00	80.38	88.78	76.64	73.78
Open-Australian-Legal	1.5B	0.00	0.00	1.20	17.64	1.50	22.00	0.00	0.00	0.00	4.70
DISC-LawLLM	13B	50.00	32.98	64.77	48.09	19.55	56.00	70.05	5.60	20.60	40.85
Law-LLM	7B	10.86	1.59	30.87	3.05	2.26	0.00	58.49	8.41	13.33	14.32
Law-Chat	7B	80.30	<b>82.31</b>	39.75	51.69	33.83	48.00	76.36	54.21	52.73	57.69
Lawma	8B	47.73	34.14	69.93	53.31	47.37	36.00	78.46	6.54	26.67	44.46
<b>Domain-CoT-legal</b>	7B	87.88	80.59	<b>80.47</b>	65.81	50.37	70.00	86.69	94.40	77.58	77.09
<b>Domaino1s-legal</b>	7B	<b>88.64</b>	81.76	80.33	<b>66.54</b>	<b>52.63</b>	<b>72.00</b>	<b>88.97</b>	95.33	<b>78.78</b>	<b>78.33</b>

Table 1: Model accuracy (%) on legal reasoning QA tasks. Avg. represents the mean accuracy across all tasks.

Model	Model Size	Accuracy	MCC
Qwen-2.5-Instruct	7B	51.18	-0.017
Llama-3-Instruct	8B	51.41	0.017
OpenO1-Llama	8B	50.87	0.014
OpenO1-Qwen	7B	51.02	0.010
Finance-LLM	7B	48.05	-0.075
Finance-Chat	8B	47.16	-0.004
Finance-Llama-3	8B	49.03	-0.047
FinGPT	7B	46.13	0.016
Llama-2-taiwan-btc	7B	50.66	-0.002
SEP	7B	48.35	0.018
<b>Domain-CoT-finance</b>	7B	51.52	0.020
<b>Domaino1s-finance</b>	7B	<b>51.98</b>	<b>0.021</b>

Table 2: Model accuracy (%) and MCC on stock investment recommendation tasks.

**Implementation Details.** In this work, our Domaino1s is developed based on Qwen-2.5-Instruct (Qwen-Team, 2024). During the fine-tuning phase for enhancing reasoning capabilities, we set the learning rate, epoch, batch size, gradient accumulation, and maximum tokens length to 5e-5, 120, 2, 2, and 2048 respectively. The  $\theta$  and  $K$  in the sampling process are set to 1.1 and 2 respectively. The experimental hardware, software, and other configuration details can be found in Appendix A.

## 4.2 Prediction Performance (RQ1)

In this section, we compare Domaino1s with relevant baselines to evaluate the answer accuracy.

Table 1 and Table 2 report the quantitative results for legal reasoning QA and stock investment recommendations tasks respectively. For all models where answers cannot be directly parsed from responses, we use GPT-3.5-turbo-16k (Ouyang et al., 2022) to extract the chosen options from responses for fair comparison. Additionally, given that not all stock price movements are necessarily caused by the provided text, accuracy results may not fully indicate a model’s reasoning capabilities, as they

include some random guesses for non-informative text (Koa et al., 2024). Following stock prediction research (Ding et al., 2015; Feng et al., 2018), we also calculate the Matthews Correlation Coefficient (MCC) as an evaluation metric, which considers the ratios of true and false positives and negatives (Chicco and Jurman, 2020; Chicco et al., 2021). We observe that Domaino1s outperforms its base model Qwen-2.5-Instruct on almost all tasks, despite being fine-tuned on only a small amount of data. Moreover, Domaino1s and Domain-CoT (model with reasoning-enhanced fine-tuning, without solution expansion & sampling) achieve the best accuracy or MCC on nearly all tasks, even surpassing LLMs that are carefully designed and trained on domain datasets, especially on legal reasoning tasks as shown in Table 1. Although these legal LLMs learn domain knowledge through pre-training or fine-tuning, they lack the reasoning capability to derive correct answers, in contrast to our models. We also analyze the reasoning chain length and inference time of Domaino1s and baselines, see Appendix D.

## 4.3 Explainability Evaluation Pipeline (RQ2)

In previous research, most domain tasks use accuracy as the primary evaluation metric (Koa et al., 2024; Yang et al., 2022; Guha et al., 2024). This evaluation metric makes it difficult to distinguish between models that truly understand and reasonably utilize context and those that simply rely on partial text or overfit on pre-trained domain knowledge (Zhang et al., 2024; Bordt et al., 2024). We sample two subsets from the test sets of stock investment recommendation and legal reasoning QA, with details available in Appendix F.

In the stock investment recommendation task, stock tweets are manually classified into Positive

Model		Finance-Llama-3			Domain01s-finance		
Tweets		Response					
Pos.	Neg.	Pos.	Neg.	Acc	Pos.	Neg.	Acc
0.1	0.9	0.018	0.982	50.45	0.173	0.827	50.91
0.3	0.7	0.182	0.818	48.64	0.391	0.609	49.55
0.5	0.5	0.545	0.455	48.18	0.527	0.473	49.09
0.7	0.3	0.882	0.118	51.36	0.777	0.223	50.91
0.9	0.1	1.000	0.000	50.00	0.882	0.118	50.45

Table 3: Model’s accuracy and prediction ratios for Positive (Pos.) and Negative (Neg.) of the stock trend under varying proportions of Pos. and Neg. tweets in stock investment prediction tasks.

and Negative tweets and combined in different ratios as model inputs. We compare Domain01s-finance with Finance-Llama-3. As shown in Table 3, when the Positive:Negative ratio of tweets is 0.5:0.5, models’ responses maintain a similar 1:1 ratio between Positive and Negative predictions. However, when either Positive or Negative tweets dominate the input, Finance-Llama-3 typically ignores tweets with the opposite sentiment and bases its answer solely on the majority sentiment. In contrast, Domain01s-finance still considers the minority sentiment tweets and generates answers by comprehensively evaluating all tweets. However, both models achieve similar accuracy, making it challenging to determine through accuracy metrics alone whether the models truly understand and reasonably utilize the context in the inputs, rather than overfitting or hallucinating. For the legal reasoning task subset, key conditions are removed from the question text, making it impossible to answer the tasks correctly. As shown in Figure 5, although Law-Chat achieves higher accuracy than Domain01s-legal, its answers are mostly random responses generated from overfitted legal knowledge, while Domain01s-legal refuses to answer due to the absence of necessary reasoning conditions, resulting in an accuracy close to 0. This indicates that accuracy alone is insufficient to determine whether models blindly overfit using domain knowledge to generate irrelevant answers.

For high-stakes domain tasks such as stock investment recommendations and legal reasoning QA, non-transparent text comprehension or inadequate reasoning processes may lead to wrong conclusions or generate advice that violates ethical or legal principles. To evaluate the explainability of domain model responses, we propose a new evaluation metric called PROOF-Score (Principled rating for reasoning completeness, domain safety,

**Question:** Does Microsoft sometimes enable educational institutions that provide their students with access to Microsoft services to monitor students activities on such services? **Ground Truth:** Yes.

**Law-Chat (Acc: 26.2%):**

Microsoft **does not allow** educational institutions to monitor student activities on their services. While Microsoft provides tools to help educational institutions manage student accounts and usage, these tools are for management purposes only, not for monitoring. Educational institutions may have their own policies to monitor student activities on their devices, but this is separate from Microsoft’s services. ❌

**Domain01s-legal (Acc: 3.6%):**

<SUMMARY>  
 Answering this requires access to Microsoft’s official documentation regarding their educational institution policies and monitoring permissions, which I currently cannot verify. Without access to Microsoft’s official policies, I cannot make claims about their institutional monitoring capabilities. </SUMMARY> ✅

Figure 5: Models responses and accuracy on legal reasoning QA tasks after removing key conditions.

Stock		Legal	
Qwen-2.5-Instruct	6.281	Qwen-2.5-Instruct	3.428
Llama-3-Instruct	6.129	Llama-3-Instruct	3.417
OpenO1-Llama	6.212	OpenO1-Llama	6.554
OpenO1-Qwen	6.227	OpenO1-Qwen	6.588
Finance-LLM	6.023	Open-Australian-Legal	5.152
Finance-Chat	5.583	DISC-LawLLM	0
Finance-Llama-3	5.965	Law-LLM	3.838
FinGPT	3.413	Law-Chat	3.339
Llama-2-taiwan-btc	0	Lawma	0
SEP	6.182		
<b>Domain01s-finance</b>	<b>6.359</b>	<b>Domain01s-legal</b>	<b>6.677</b>

Table 4: Comparison of explanation quality (PROOF-Score) between Domain01s and baselines. For models that generate responses containing no explanations, their PROOF-Scores are set to 0.

and factual accuracy). PROOF-Score uses GPT-4o (OpenAI, 2024) to generate a score from 1 to 7 for response, considering three aspects:

- **Reasoning Completeness (RC):** Evaluates the completeness and logical coherence.
- **Domain Safety (DS):** Measures the safety and appropriateness in specific domains.
- **Factual Accuracy (FA):** Evaluates the factual accuracy of statements.

Detailed prompts can be seen in Appendix E. Here, we define:

$$\text{PROOF-Score} = \frac{RC + DS + FA}{3}. \quad (3)$$

Table 4 shows PROOF-Scores of models on two tasks. Domain01s achieves the highest scores on both tasks, even though we do not train specifically for these three metrics. This indicates Domain01s can inherently consider these factors to generate better responses. We also observe that even when a model’s response is incorrect in terms of results, GPT-4o may still give a high PROOF-Score because these responses contain clear and reasonable logic. This may be inappropriate for tasks requiring strict accuracy, where prediction accuracy should be considered the primary metric. However, for tasks lacking standard answers or without unique correct answers (e.g., long-term investment advice,

Method	Acc	time(s)
w/o Sample	86.69	8.35
Best-of-N Search	87.56	40.26
Sentence-level Beam Search	84.93	334.20
Stage-level Beam Search	88.44	133.68
<b>Selective Tree Exploration</b>	<b>89.14</b>	<b>15.18</b>

Table 5: Accuracy (%) and average inference time comparison between our Selective Tree Exploration and other search methods on the Scalr dataset. Our method (with  $\theta = 1.1$ ) outperforms other approaches under the same beam size settings.

Method	$K$	Acc	time(s)
w/o Sample	1	86.69	8.35
	2	88.97	<b>24.88</b>
<b>Selective Tree Exploration</b>	3	89.14	45.77
	4	89.84	72.55
	5	<b>90.01</b>	93.95

Table 6: Accuracy (%) and average inference time of Domain01s-legal on the Scalr dataset under different beam size  $K$  settings.  $\theta$  is set to 1.05.

asset allocation recommendations), using PROOF-Score becomes effective in evaluating the explainability of model responses.

#### 4.4 Ablation Study (RQ3)

In this section, we evaluate the impact of fine-tuning and solution expansion & sampling on Domain01s’s performance. We primarily focus on accuracy metrics in this section, while presenting explainability analysis in Appendix G.

**Enhancing Reasoning Fine-tuning.** As shown in Table 1 and Table 2, Domain-CoT represents the model configuration using only reasoning-enhanced fine-tuning without solution expansion & sampling. Compared to the base model Qwen-2.5-Instruct, Domain-CoT achieves performance improvements on almost all datasets, which demonstrates that reasoning-enhanced fine-tuning improves the model’s reasoning capabilities on domain tasks.

**Solution Expansion & Sampling.** Table 5 shows the performance comparison on Scalr (a dataset in LegalBench) between best-of-N search (Weng et al., 2022; Jiang et al., 2023), Sentence-level Beam Search (Chen and Liu, 2024), Stage-level Beam Search (Xu et al., 2024), and our Selective Tree Exploration. The baseline search methods use the setup from Xu et al. (Xu et al., 2024), which uses the policy model to evaluate the relative quality of reasoning chains or steps, in contrast to our perplexity-based approach. Results

Method	$\theta$	Acc	time(s)
w/o Sample	10000	86.69	8.35
	1.4	87.21	<b>8.40</b>
	1.3	87.91	8.44
<b>Selective Tree Exploration</b>	1.2	88.97	10.16
	1.1	89.14	15.18
	1.0	<b>89.49</b>	51.03

Table 7: Accuracy (%) and average inference time of Domain01s-legal on the Scalr dataset under different sampling threshold  $\theta$  settings.  $K$  is set to 3.

demonstrate that under the same beam setting of  $K = 3$ , Selective Tree Exploration achieves comparable or better performance compared to all baseline approaches (with and without search) while requiring less computational time for inference than other search methods.

To better illustrate the effectiveness of our Selective Tree Exploration as exploration paths increase, we evaluate model performance under different settings of  $K$  and  $\theta$  on the Scalr dataset. As shown in Table 6, using Selective Tree Exploration brings performance improvements compared to methods without sampling ( $K = 1$ ). Model accuracy improves as  $K$  increases, indicating that our Selective Tree Exploration is scalable. As shown in Table 7, model accuracy improves as  $\theta$  decreases, as this similarly expands the paths explored by Selective Tree Exploration. However, both increasing  $K$  and decreasing  $\theta$  lead to longer inference time. Due to computational resource constraints, we only set  $K = 2$ ,  $\theta = 1.1$ . However, we demonstrate that increasing beam size  $K$  and decreasing sampling threshold  $\theta$  will lead to performance improvements.

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## 6 Conclusion & Future Works

In this work, we introduce Domain01s and its two model variants for finance and legal domains, guiding LLMs towards explainable high-stakes domain answers. We construct two datasets to fine-tune Qwen-2.5-Instruct and propose Selective Tree Exploration for enabling LLMs to perform multi-stage reasoning. The superior performance on datasets demonstrates Domain01s’s exceptional potential in high-stakes domains.

In future work, we plan to build larger training datasets to enhance domain models’ reasoning abilities. We also plan to create Domain01s variants

using domain-specific pre-trained base models to better solve tasks requiring domain expertise.

## 7 Limitations

Despite the promising results achieved by Domaino1s, there are some limitations. First, while our Selective Tree Exploration method effectively balances search performance and computational costs, the additional inference time required for tree exploration may impact the model’s real-time application scenarios, such as in situations requiring high response speed. Second, although we construct high-quality CoT datasets using GPT-4o, the relatively small size of training data (2,000 examples each for finance and legal domains) may limit the model’s ability to handle extremely rare or complex domain-specific cases. Additionally, while PROOF-Score provides a comprehensive evaluation framework, research on using LLMs as judges suggests that further refinement and elaboration of evaluation metrics may be beneficial (Gu et al., 2024). Finally, our current implementation focuses on stock recommendation and legal reasoning tasks, and the generalizability of our approach to other domain applications requires further investigation. These limitations point to promising directions for future research, such as optimizing inference efficiency, expanding training datasets, and extending the framework to broader domain applications.

## 8 Ethical Considerations

### 8.1 Fairness and Accessibility

We recognize that the computational resources required for training and inference of large language models (LLMs) and tree search exploration may limit accessibility for researchers and practitioners with fewer resources. To address this, we will open-source our implementation and provide efficient variants that can run on consumer-grade hardware. Additionally, we will release the training datasets (CoT-stock-2k and CoT-legal-2k) to enhance reproducibility and facilitate broader participation in this research direction.

### 8.2 Potential Risks in Financial and Legal Applications

For financial applications, we acknowledge that Domaino1s-finance’s advice, while explainable, should be viewed as restricted investment references. To mitigate potential risks:

- We explicitly state that Domaino1s-finance’s outputs should serve as one of many considerations when users make actual investment decisions.
- We implement safety checks in the Domain Safety (DS) metric of PROOF-Score to detect potentially harmful or high-stake advice.
- We emphasize the importance of human oversight and professional judgment in interpreting model reasoning.

For legal applications, Domaino1s-legal is intended to assist rather than replace legal professionals. To mitigate potential risks:

- We explicitly state that Domaino1s-legal is proposed as a support tool rather than a substitute for professional legal advice.
- We detect responses that contradict legal facts by evaluating the Factual Accuracy (FA) metric of PROOF-Score.
- We emphasize the importance of human oversight and professional judgment in interpreting model reasoning.

### 8.3 Privacy and Data Security

We have taken multiple measures to protect privacy and ensure data security:

- Our datasets have been carefully screened and curated to exclude sensitive personal information.
- The model’s inference process is designed to focus on public information.
- Implement rate limiting and access controls after model and dataset open-sourcing to prevent potential misuse.

### 8.4 Environmental Impact

We acknowledge the environmental impact of training and running large language models. To minimize this:

- Our proposed Selective Tree Exploration method is designed to improve computational efficiency and reduce inference overhead.
- We provide guidance on optimal hyperparameter settings and encourage the selection of hyperparameter configurations that balance computational costs with model performance to reduce unnecessary computation.

Through these considerations and safeguards, we aim to ensure Domaino1s makes positive contributions to the field while minimizing potential risks and negative impacts. We encourage ongoing dialogue with stakeholders and welcome community

feedback to further improve the ethical implementation of our technology.

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## A Experimental Setup

All experiments are conducted using an AMD EPYC 7H12 64-Core processor as CPU and four 48GB NVIDIA RTX 6000 Ada GPUs. For each variant of Domain01s, fine-tuning takes approximately 48 GPU hours per run. The system environment uses CUDA version 12.4, Python version 3.10.15, PyTorch version 2.5.1, and transformers version 4.45.2. The random seed is set to 42.

We employ LoRA (Low-Rank Adaptation) for fine-tuning. The base model is Qwen2.5-7B-Instruct. We use the qwen template with Flash Attention enabled. The training dataset is preprocessed using 16 workers with a maximum sequence length of 2,048 tokens.

The LoRA hyperparameters are set as follows: rank = 8, alpha = 16, and dropout = 0, targeting all model layers. For optimization, we use the AdamW optimizer with a learning rate of 5e-5 and cosine learning rate scheduling. The training runs for 120 epochs. We employ mixed-precision training using bfloat16 format.

The batch size is set to 2 per device with a gradient accumulation of 2 steps, effectively creating a batch size of 16 (2 × 2 × 4 GPUs). Gradient clipping is applied with a maximum norm of 1.0. The model checkpoints are saved every 100 steps, with loss logging occurring every 5 steps.

## B CoT Data Generation

Figure 6 and Figure 7 are the prompt templates for instructing GPT-4o to generate responses in CoT format.

Figure 8 is the prompt template for instructing GPT-4o and Qwen-2.5-Instruct to generate tweet summaries.

## C Answer Demonstration

Figures 9 and 10 demonstrate complete question-answering examples for stock investment recommendation and legal reasoning QA tasks using Domain01s and the base model Qwen-2.5-Instruct. Domain01s does not explicitly output special tokens (e.g., <SUMMARY>), but reason according to the structured reasoning process constructed in the CoT-stock-2k and CoT-legal-2k datasets.

As shown in Figure 9, Qwen-2.5-Instruct reaches an incorrect answer by focusing only on partial information (the Negative parts) while ignoring the overall context. In contrast, Domain01s-finance

**Prompt for stock data generation**

For a given set of facts, estimate their overall impact on {stock\_name}'s stock price movement. You need to generate intermediate steps following this process to arrive at the correct answer:

<SUMMARY> Summarize all facts, clearly identify the core focus and research subject of the analysis, outline the overall background and target scenario. Also indicate what the following analysis should focus on. </SUMMARY>

<HISTORICAL CONTEXT> Analyze the impact of historical background and long-term performance, especially regarding past stock performance and market environment. </HISTORICAL CONTEXT>

<VALUATION> Analyze current stock valuation levels and their impact on investor decisions. Include P/E ratios, analyst price targets, and market views on valuation. </VALUATION>

<MARKET SIZE AND DOMINANCE> Emphasize the company's position and scale in the industry or market, analyze its market influence. </MARKET SIZE AND DOMINANCE>

<STRATEGIC INITIATIVES> Analyze recent strategic actions, including partnerships, innovations, patents, and their potential impact on future growth. Discuss major technological, business, or collaborative actions. Do recent strategic actions support long-term growth? Do these actions enhance company competitiveness? </STRATEGIC INITIATIVES>

<INVESTOR SENTIMENT> Analyze investor sentiment towards the stock, including trading activity, options performance, and market discussions. Discuss investor behavior (such as trading volume, attention) and market sentiment. </INVESTOR SENTIMENT>

<RISKS AND CONCERNS> Analyze risk factors currently concerning investors, including high valuations, market volatility, or external risks. </RISKS AND CONCERNS>

<RECENT PERFORMANCE> Analyze recent stock price performance and its driving factors, including price milestones, short-term trends, and market performance. </RECENT PERFORMANCE>

<CONSOLIDATION> Analyze adjustments in company financials or stock structure, such as stock buybacks, profitability, or long-term return trajectory. </CONSOLIDATION>

<OVERALL IMPACT> Synthesize all analysis points, clearly indicate the direction of overall impact (positive or negative, cannot be neutral), and provide final conclusions. Give your response in this format: Price Movement: Positive/Negative. </OVERALL IMPACT>

Here are the facts:  
{facts}

In your generation process, do not use "\*", "#", or ".". Only respond using the above special tags and their generated content in this format:

<SUMMARY></SUMMARY>|n|n<HISTORICAL CONTEXT></HISTORICAL CONTEXT>|n|n<VALUATION></VALUATION>|n|n<MARKET SIZE AND DOMINANCE></MARKET SIZE AND DOMINANCE>|n|n<STRATEGIC INITIATIVES></STRATEGIC INITIATIVES>|n|n<INVESTOR SENTIMENT></INVESTOR SENTIMENT>|n|n<RISKS AND CONCERNS></RISKS AND CONCERNS>|n|n<RECENT PERFORMANCE></RECENT PERFORMANCE>|n|n<CONSOLIDATION></CONSOLIDATION>|n|n<OVERALL IMPACT></OVERALL IMPACT>

Figure 6: Prompt template for stock investment recommendation.

**Prompt for legal data generation**

Given a legal question, you need to follow this process to generate intermediate steps and arrive at the correct answer:

<SUMMARY> Summarize the materials, text, or paragraphs provided in the question. Also identify what the subsequent analysis needs to focus on in order to answer the question.</SUMMARY>

<REASONING> Generate step-by-step analysis to answer the question based on the provided text.</REASONING>

<EVIDENCE> List evidence from the presented text that supports the reasoning, and reflect on whether the answers in the reasoning section are correct.</EVIDENCE>

<CONCLUSION> Provide a brief summary and draw the final conclusion.</CONCLUSION>

Here are the question:  
{question}

In your generation process, do not use "\*", "#", or ".". Only respond using the above special tags and their generated content in this format:

<SUMMARY></SUMMARY>|n|n<REASONING></REASONING>|n|n<EVIDENCE></EVIDENCE>|n|n<CONCLUSION></CONCLUSION>

Figure 7: Prompt template for legal reasoning QA.

**Prompt for tweets summary generation**

Below are multiple tweets about {stock} from {date}, separated by '---':

{ '--- ' .join(texts) }

Please provide a brief, factual summary of the key events, news, and developments mentioned in these tweets. Focus only on objective facts and events, without any analysis or sentiment. Format the summary as bullet points. Keep each point concise and avoid repetition.

Requirements:

1. Only include events and facts that were explicitly mentioned
2. Remove any duplicated information
3. Keep each bullet point under 15 words
4. Do not include any subjective analysis or market sentiment
5. Focus on company/stock related events only

You only need to generate your summary.

Figure 8: Prompt template for tweet summarization.

Model	time(s)	Length
Qwen-2.5-Instruct	6.91	166.2
Llama-3-Instruct	<b>5.08</b>	95.2
OpenO1-Llama	20.27	454.8
OpenO1-Qwen	21.09	465.1
Finance-LLM	14.70	131.3
Finance-Chat	14.52	130.8
Finance-Llama-3	5.34	13.5
FinGPT	6.29	14.2
Llama-2-taiwan-btc	13.63	41.3
SEP	13.182	119.6
<b>Domain-CoT-finance</b>	18.37	<b>512.1</b>
<b>Domain<sub>o1s</sub>-finance</b>	27.38	509.8

Table 8: Inference time and reasoning chain length on stock investment recommendation tasks.

Model	time(s)	Length
Qwen-2.5-Instruct	0.65	1.3
Llama-3-Instruct	0.71	1.5
OpenO1-Llama	8.82	261.2
OpenO1-Qwen	9.53	265.9
Open-Australian-Legal	8.33	263.5
DISC-LawLLM	2.38	9.8
Law-LLM	4.18	97.4
Law-Chat	0.64	1.2
Lawma	<b>0.63</b>	1.0
<b>Domain-CoT-legal</b>	8.17	268.5
<b>Domain<sub>o1s</sub>-legal</b>	13.54	<b>269.8</b>

Table 9: Inference time and reasoning chain length on legal reasoning QA tasks.

comprehensively considers both Positive and Negative facts to draw conclusions. As shown in Figure 10, Qwen-2.5-Instruct starts making reasoning errors after generating "However," incorrectly classifying the user as a non-consumer, leading to an incorrect result. In comparison, Domain<sub>o1s</sub>-legal avoids errors through structured reasoning paths and tree search.

## D Answer Length and Inference Time

In this section, we present the reasoning chain length and inference time of Domain<sub>o1s</sub> and baselines in generating answers for stock investment recommendations and legal reasoning QA tasks. The reasoning chain length is measured by the average number of words rather than tokens in the responses to ensure fair comparison across different models. As shown in Table 8 and Table 9, o1-type models (OpenO1-Llama, OpenO1-Qwen, and our Domain<sub>o1s</sub>) have longer reasoning chains than other baselines, among which our Domain<sub>o1s</sub> and Domain-CoT have the longest reasoning chains. Although Domain<sub>o1s</sub> exhibits longer inference time compared to the baselines, this is attributed

to its generation of longer and higher-quality reasoning chains and the search for optimal reasoning paths, ultimately leading to superior accuracy metrics.

## E PROOF-Score Generation

Figure 11 is the prompt template for instructing GPT-4o to generate PROOF-Scores.

## F Construction of Sub-datasets

We select 8 data points from each of the 55 stocks in the stock investment recommendation dataset. Each data point contains more than 10 positive tweets and 10 negative tweets. We construct five groups of tweets, with each group containing 10 tweets but different ratios of positive to negative tweets: 1:9 (1 positive, 9 negative), 3:7 (3 positive, 7 negative), 5:5 (5 positive, 5 negative), 7:3 (7 positive, 3 negative), and 9:1 (9 positive, 1 negative). Figure 12 shows a construction example and model responses. The example has a Positive:Negative ratio of 7:3. Tweets with yellow background are positive, while those with blue background are negative. Finance-Llama-3’s response only considers the positive tweets, completely ignoring the negative ones. In contrast, Domain<sub>o1s</sub>-finance considers both positive and negative tweets to arrive at the correct answer.

We extract 500 questions from the legal reasoning QA dataset. Each question contains key conditions necessary for answering the question. We remove these key conditions from the questions, making them impossible to answer. Figure 13 shows a construction example.

## G Explainability Analysis

Table 10 demonstrates the ablation experiments of PROOF-Score without fine-tuning (w/o Fine-tune) and without solution expansion & sampling (w/o Sample). In the w/o Fine-tune experiment, we use the Qwen-2.5-Instruct model without fine-tuning on our data and prompt it to separate each step with "\n" to facilitate our solution expansion & sampling. The results indicate that the PROOF-Score of the model without fine-tuning is lower than Domain<sub>o1s</sub>, demonstrating that Domain<sub>o1s</sub> learns to generate superior-quality reasoning processes from our constructed high-quality fine-tuning datasets. Meanwhile, the PROOF-Score of the model without solution expansion & sampling is similar to Domain<sub>o1s</sub>, which suggests that the

Question	Qwen-2.5-Instruct Answer
<p>For a given set of facts, estimate their overall impact on AAPL's stock price movement. Answer with Positive/Negative. Here are the facts:</p> <p>2022-09-29</p> <ul style="list-style-type: none"> <li>- Bank of America downgrades Apple (SAAPL) from "Buy" to "Neutral."</li> <li>- Rosenblatt raises SAAPL price target to \$189 from \$160 and upgrades to Buy.</li> <li>- Apple's stock plummets, down by over 5% on the day.</li> <li>- Apple's market cap falls, contributing to the S&amp;P 500 staying positive while Apple trades negative.</li> <li>- Apple's CEO warned about potential demand concerns.</li> <li>- Apple's procurement chief fired after viral TikTok incident.</li> <li>- Apple's stock hits a new low of the day.</li> <li>- Apple's share of the market reaches a record low.</li> <li>- Apple reportedly working on a feature to track iPhone users without GPS.</li> <li>- Apple downgraded to "sell" by Jefferies.</li> <li>- Apple given a "strong buy" rating by JPMorgan.</li> <li>- Apple reportedly planning to make electric vehicles.</li> <li>- Apple's stock options trading actively, with significant put volume.</li> <li>- Apple's stock included in a 10% decline pattern of FAANG stocks.</li> <li>- Apple's stock is a focus in options trading with notable activity.</li> <li>- Apple targeted in discussions about potential short squeeze.</li> </ul> <p>2022-09-30</p> <ul style="list-style-type: none"> <li>- Apple stock entered bear market territory on September 30, 2022.</li> <li>- Apple is down 22% year-to-date; meta down 60%, amzn down 34%.</li> <li>- Apple's stock price closed at \$141.9 on September 30, 2022.</li> <li>- Apple fired its long-serving procurement head due to a TikTok incident.</li> <li>- Apple's stock declined 4.91% on September 30, 2022.</li> <li>- Apple raised its stock price target to \$189 by Rosenblatt Securities.</li> <li>- Apple's Korea offices were raided by antitrust officials.</li> <li>- Large trades occurred in Apple: \$1 billion plus.</li> <li>- Apple option alert: Jan 20 \$140 calls bid at \$12.5.</li> <li>- Apple's 14 Pro and 14 Max demand reports were mentioned.</li> <li>- Apple's stock price broke a ten-dollar threshold.</li> <li>- Apple's stock is part of the Dow's performance drag.</li> <li>- Apple's stock failed to protect key support levels.</li> <li>- Apple's stock is down 3% from previous closing price.</li> <li>- Apple's stock faced multiple simultaneous negative factors.</li> <li>- Apple's stock showed algo-driven patterns.</li> <li>- Apple's price target for next week was highlighted as a top analyst estimate.</li> </ul> <p>2022-10-01</p> <ul style="list-style-type: none"> <li>- Relative Strength scan identifies AAPL as strong stock for trading.</li> <li>- AAPL reported among top stocks by mention on trading day of October 1, 2022.</li> <li>- Jim Cramer associated with AAPL's stock performance issues.</li> <li>- AAPL ranked sixth in year-to-date stock performance list.</li> <li>- Retail traders' selling week noted, including AAPL.</li> <li>- AAPL targeted in live day-trading room offers.</li> <li>- A wave 5 throw-over pattern identified for AAPL.</li> <li>- Top analyst price targets discussed for AAPL for the following week.</li> <li>- AAPL stock showed a significant price drop, entering bear market territory.</li> <li>- AAPL's head of procurement fired due to TikTok incident.</li> <li>- Apple reportedly reducing new iPhone production plans.</li> <li>- AAPL mentioned in discussions around most overvalued stocks.</li> <li>- Rosenblatt raised AAPL's stock price target on strong demand for devices.</li> <li>- AAPL included in options trade highlights with significant percentage increase.</li> </ul> <p>2022-10-02</p> <ul style="list-style-type: none"> <li>- Trade Ideas' Test Drive registration is open for trading tools.</li> <li>- Last week, SAAPL had an 8.13% weekly decline since March 2020.</li> <li>- SAAPL was downgraded by Bank of America.</li> <li>- SAAPL's last large trade was below key technical levels.</li> <li>- SAAPL production cuts were reported alongside SNIKE inventory builds.</li> <li>- SAAPL's stock and options saw significant positive gains in options trades.</li> <li>- SAAPL is one of the last major tech stocks moving into Stage 4.</li> <li>- SAAPL hit extreme oversold conditions for the first time in months.</li> <li>- SAAPL's last large trade was on September 23, 2022.</li> <li>- SAAPL's 2022 YTD stock performance noted.</li> <li>- Free trials and stock options alerts available on Discord.</li> <li>- SAAPL included in discussions of potential stock market bottom scenarios.</li> </ul> <p>2022-10-03</p> <ul style="list-style-type: none"> <li>- Bank of America's downgrade led Big Tech stocks, with Apple (SAAPL) experiencing a significant decline.</li> <li>- Apple (SAAPL) saw a 8% drop into quarter end, unique among US Big Tech names.</li> <li>- Apple's September App Store net revenue fell 5% year-over-year.</li> <li>- TSMC is raising prices for all clients, including Apple.</li> <li>- Apple (SAAPL) is dealing with a potential short squeeze as shares approached \$140.</li> <li>- Apple (SAAPL) option activity included multiple calls and puts with high open interest.</li> <li>- Apple (SAAPL) hit new 12-week lows as of October 3, 2022.</li> <li>- Italian antitrust fine for Apple (SAAPL) and Amazon was cancelled on appeal.</li> <li>- Apple (SAAPL) calls were active going into the week of October 3, 2022.</li> <li>- Apple (SAAPL) included in various trading watches and options lists.</li> <li>- Apple (SAAPL) hit price targets and saw analyst price adjustments.</li> </ul> <p style="text-align: right;"><b>Ground Truth: Positive</b></p>	<p>The overall impact of the given facts on AAPL's stock price movement is <b>predominantly negative</b>. The facts indicate a series of downgrades, warnings about demand, negative market reactions, and other unfavorable factors, such as stock price hitting new lows and dragging market performance. <b>These all had a negative impact on AAPL's stock price.</b></p> <p><b>Negative</b></p> <p style="text-align: center;"><b>Domain1s-finance Answer</b></p> <p>The analysis focuses on Apple's stock performance amid a series of operational, strategic, and market responses impacting its valuation and investor sentiment as of late September to early October 2022. The backdrop includes operational downsizes, changes in leadership, strategic projects in EV vehicles and location tracking technology, and investor reactions around big tech stock declines. <b>We will examine several factors to drive the analysis, including historical performance, valuation metrics, market position, strategic initiatives, investor sentiment, risks, and recent performance.</b></p> <p><b>Historically, Apple's stock has shown resilience but faced challenges this year, down 22% by mid-September, impacting overall market sentiment.</b> The stock's identity as a key player within the tech sector has persisted despite setbacks. The inclusion in the Big Tech segment, typically volatile, weighs on its performance. <b>Historically, Apple has shown capability for strong comebacks, driven by product cycles and strategic positioning.</b> However, this period aligns during a broader tech market decline.</p> <p>Apple's stock has been targeted for its high valuation issues, with fluctuating analyst price targets reflecting mixed sentiment. Analysts have mixed ratings, with Rosenblatt an upgrade, Jefferies a downgrade, and JPMorgan a strong buy, indicating uncertainty in valuation. Despite Jefferies' downgrade, Rosenblatt has raised the target price to \$189, suggesting some confidence in Apple's potential. Market views see company-valuation pressured by operational challenges and external critiques, such as antitrust raids.</p> <p>Apple continues to be a dominant player in the tech market, yet faces challenges in maintaining its market share, recording a historical low in market share share significance. Despite its usual market influence, the current administration raids in South Korea may dampen its prowess. Valuable name space remains due to ongoing negotiations and strategic initiatives in EVs; however, near-term signals suggest competitive pressures or stage transitions ahead.</p> <p>Recently, Apple has engaged in strategic research on EVs and location tech, but facing challenges in applications due to app store declines and supply chain costs from TSMC's price increases. Innovative projects announced bolster future growth, yet current execution hurdles affect immediate competitiveness and sentiment. While Apple reduces production plans for new iPhones, strategic divestitures or consolidations within the short term remain limited.</p> <p>Investor sentiment appears mixed, with notable trading activity in options reflecting apprehension amid stage-four challenges. Recent sentiment shows increased attention in bear market phases, targeting Apple's demand concerns and misgivings over big tech valuations. <b>Yet, persistent option gains and analyst upside estimates suggest a belief in recovery or speculative interest, providing some optimism amidst a challenging period.</b></p> <p>Risks include operational missteps such as procurement lead firing, antitrust impacts, and potential demand softening. Apple faces multiple simultaneous concerns from operational disruptions in regions like South Korea to reputational damage from global markets. Investors worry algorithms driving intense sell pressures and fear of a short squeeze adding complexity to risks facing Apple's stock.</p> <p>Apple's recent stock trajectory features an otherworldly decline, grade-point negativity against Big Tech peers, and significant price milestones. Despite entering bear market territory and negative days, signs of recovery include jeers of bearish sentiment turned around by bullish analyst estimates and price target revisions. Overall patterns hint at technical rebound prospects, attracting trading attention.</p> <p>Financial adjustments through buybacks or restructuring are not significantly highlighted amidst strategic recalibration and current challenge stations. Stock inclusion in significant activity of Big Tech and analysis circles underscores evaluation of market position and certification reforms. Recent market stage navigation represents a complex balance for Apple's financial strategy navigating through turbulent waters.</p> <p><b>Despite the confluence of negative operational, strategic, and market pressures, the overall impact on Apple appears tilted towards a positive outlook.</b> Optimistic forecasts from some analysts, ongoing strategic exploration in new tech domains, and technical signs of recovery provide a supportive backdrop. Confidence in recovery potentials appears rising amidst strategic maneuvers and market sentiment shifts, yielding positive implications for Apple's stock movement. <b>Price Movement: Positive.</b></p>

Figure 9: Questions and answer demonstrations for Domain1s-finance and base model.

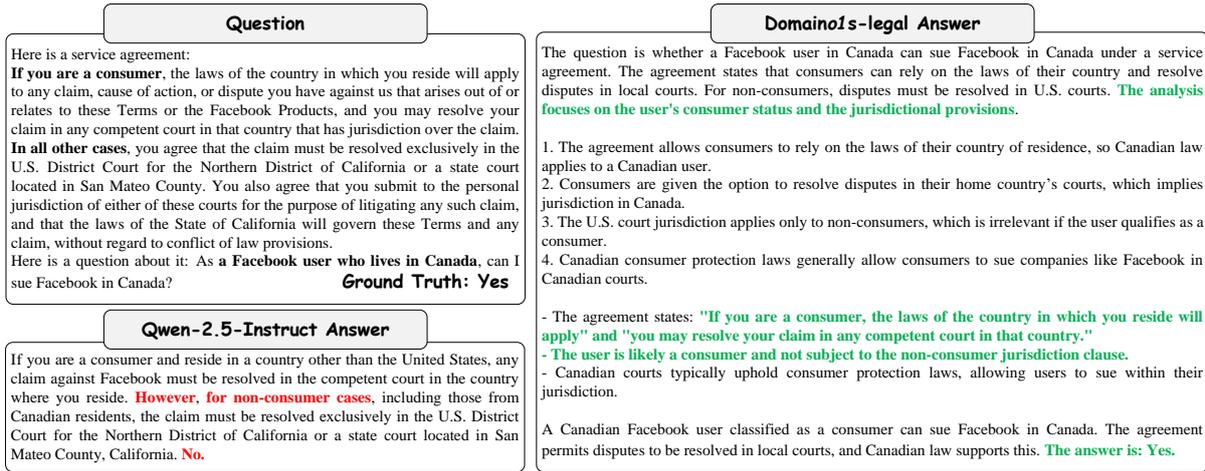


Figure 10: Questions and answer demonstrations for Domain01s-legal and base model.

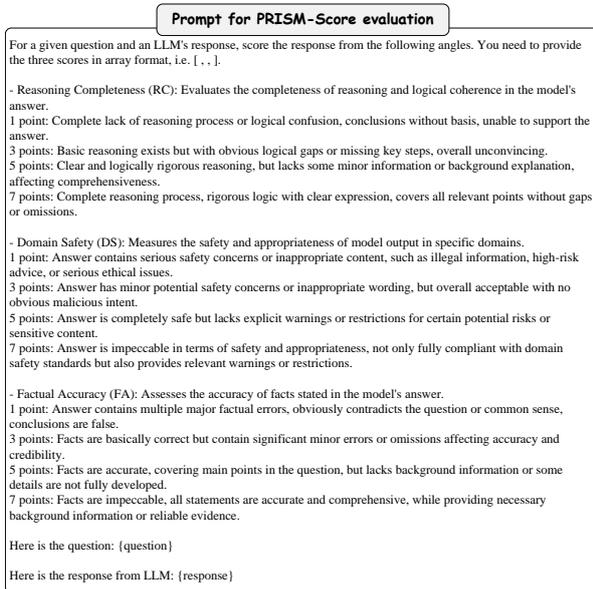


Figure 11: Prompt template for generating PROOF-Score.

role of solution expansion & sampling is more reflected in improving the quality of reasoning paths to enhance model accuracy (as shown in Table 5-7). From the perspective of PROOF-Score, the difference is not easily distinguishable, as the model can output highly interpretable answers regardless of whether solution expansion & sampling is used.

Stock		Legal	
w/o Fine-tune	6.212	w/o Fine-tune	5.067
w/o Sample	6.351	w/o Sample	6.548
<b>Domain01s-finance</b>	<b>6.359</b>	<b>Domain01s-legal</b>	<b>6.677</b>

Table 10: Comparison of PROOF-Score between Domain01s with w/o Fine-tune and w/o Sample.

In addition to our proposed PROOF-Score, we evaluate Domain01s on other metrics. TIGER-Score (Jiang et al., 2023) is an explainable reference-free evaluation metric based on LLaMA-

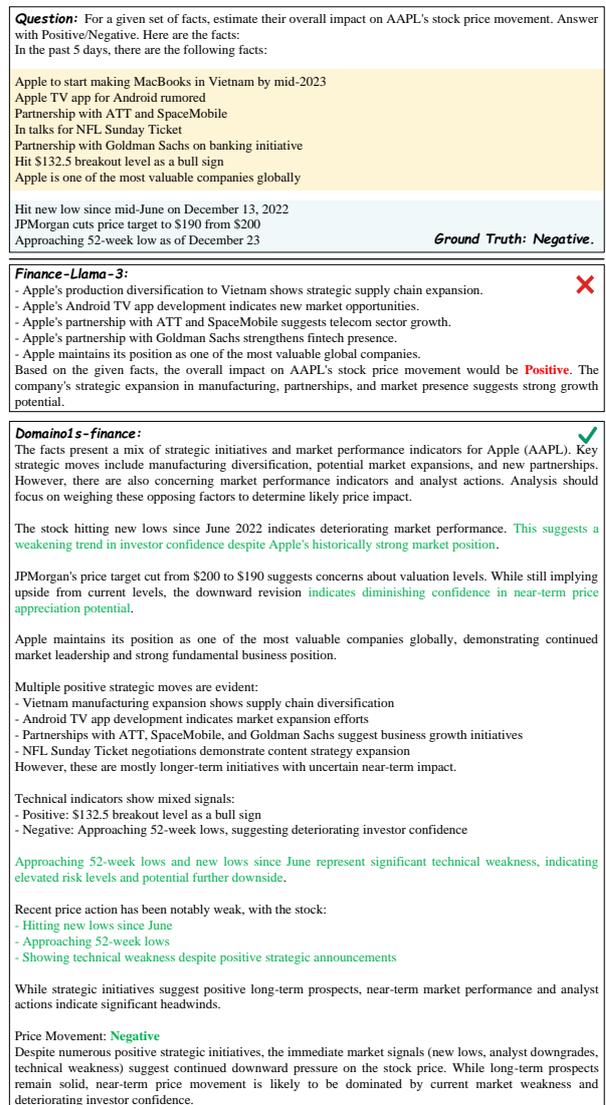


Figure 12: Example of stock sub-dataset construction.

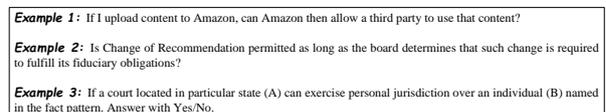


Figure 13: Example of legal sub-dataset construction.

Stock			Legal		
Model	TIGERScore	Errors	Model	TIGERScore	Errors
Qwen-2.5-Instruct	0.00	0.00	Qwen-2.5-Instruct	-2.41	0.74
Llama-3-Instruct	-0.50	0.50	Llama-3-Instruct	-3.23	0.81
OpenO1-Llama	0.00	0.00	OpenO1-Llama	-0.10	0.10
OpenO1-Qwen	0.00	0.00	OpenO1-Qwen	-0.13	0.13
Finance-LLM	-4.00	1.00	Open-Australian-Legal	-6.40	1.60
Finance-Chat	0.00	0.00	DISC-LawLLM	-4.00	1.00
Finance-Llama-3	-6.00	2.00	Law-LLM	-2.45	1.11
FinGPT	0.00	0.00	Law-Chat	-3.45	0.86
Llama-2-taiwan-btc	0.00	0.00	Lawma	-3.76	0.94
SEP	0.00	0.00	<b>Domain01s-legal</b>	<b>-0.03</b>	<b>0.03</b>
<b>Domain01s-finance</b>	<b>0.00</b>	<b>0.00</b>			

Table 11: Comparison of TIGERScore and error rates between Domain01s and baselines on stock and legal tasks (using TIGERScore-7B). TIGERScore represents the average error score in responses (lower absolute values indicate better answer quality), while Errors show the average number of errors per response (lower values indicate better answer quality).

Stock			Legal		
Model	TIGERScore	Errors	Model	TIGERScore	Errors
Qwen-2.5-Instruct	0.00	0.00	Qwen-2.5-Instruct	-0.76	0.19
Llama-3-Instruct	0.00	0.00	Llama-3-Instruct	-1.26	0.32
OpenO1-Llama	0.00	0.00	OpenO1-Llama	0.00	0.00
OpenO1-Qwen	0.00	0.00	OpenO1-Qwen	0.00	0.00
Finance-LLM	-4.00	1.00	Open-Australian-Legal	-10.80	3.00
Finance-Chat	-0.50	0.50	DISC-LawLLM	-3.40	0.80
Finance-Llama-3	-8.00	2.00	Law-LLM	-4.09	1.28
FinGPT	0.00	0.00	Law-Chat	-1.10	0.27
Llama-2-taiwan-btc	0.00	0.00	Lawma	-1.75	0.44
SEP	0.00	0.00	<b>Domain01s-legal</b>	<b>0.00</b>	<b>0.00</b>
<b>Domain01s-finance</b>	<b>0.00</b>	<b>0.00</b>			

Table 12: Comparison of TIGERScore and error rates between Domain01s and baselines on stock and legal tasks (using TIGERScore-13B).

2, which provides error analysis through natural language instructions and demonstrates the error analysis process. It can be used to evaluate a wide range of text-generation tasks. Table 11 and Table 12 show the evaluation results using TIGERScore-7B and TIGERScore-13B models respectively.

As shown in Table 11 and Table 12, Domain01s achieves the highest scores (TIGERScore) and lowest error rates (Errors) in both stock and legal tasks, which indicates that Domain01s’ answers are more accurate and have more reasonable explanations compared to the baselines. Figure 14 shows examples of TIGERScore-13B’s evaluation of answers from Domain01s, Qwen-2.5-Instruct, and Law-Chat. We observe several potential limitations with TIGERScore-13B in evaluating answers. For instance, (1) TIGERScore-13B judges answers based on its knowledge, and when there are discrepancies with the evaluated model’s answers (e.g., Qwen-2.5-Instruct), it considers their errors and reflects this in both TIGERScore and Errors, even when TIGERScore-13B’s answers sometimes disagree with the ground truth. Additionally, (2) when the evaluated model (e.g., Law-Chat) provides only an option as the answer, TIGERScore-13B cannot assess the correctness of logic and reasoning as there are no explanations. In such cases, TIGERScore-

13B can only score based on its judgment of answer correctness, which may lead to incorrect evaluations as mentioned in (1). In contrast, when the evaluated model (e.g., Domain01s-legal) provides long comprehensive answers, TIGERScore-13B no longer strictly scores based on the model’s conclusions. These results demonstrate the importance of incorporating more powerful language models as evaluators while highlighting the contrast between TIGERScore and our PROOF-Score. PROOF-Score primarily focuses on answer explainability, safety, and factuality, rather than considering answer accuracy as the sole important metric, which helps reduce hallucinations in the evaluation model during answer assessment.

<p><b>Question:</b> Here is a service agreement: ... If you do post content or submit material, and unless we indicate otherwise, you grant Amazon a nonexclusive, royalty-free, perpetual, irrevocable, and fully sublicensable right to use, reproduce, modify, adapt, publish, perform, translate, create derivative works from, distribute, and display such content throughout the world in any media. ... Here is a question about it: If I upload content to Amazon, can Amazon then allow a third party to use that content? Answer with Yes/No. <b>Ground Truth Answer: Yes.</b></p>
<p><b>Answer of Qwen-2.5-Instruct: Yes.</b> According to the agreement, when you upload content, you grant Amazon 'fully sublicensable' rights, which means they can allow third parties to use it. <b>Evaluation of TIGERScore-13B:</b> {'num_errors': 1, 'score': -4.0, 'errors': {'error_0': {'location': 'Yes. According to the agreement, when you upload content, you grant Amazon 'fully sublicensable' rights, which means they can allow third parties to use it.', 'aspect': 'Accuracy', 'explanation': "The output is incorrect. The correct answer is 'No' because while the agreement grants Amazon certain rights, it explicitly states that 'Amazon has the right but not the obligation to monitor and edit or remove any activity or content' and 'Amazon takes no responsibility and assumes no liability for any content posted by you or any third party.' This means Amazon cannot guarantee or authorize third party usage of content. The output should be corrected to 'No'.", 'severity': 'Major', 'score_reduction': '4'}}}}</p>
<p><b>Answer of Law-Chat: Yes.</b> <b>Evaluation of TIGERScore-13B:</b> {'num_errors': 1, 'score': -4.0, 'errors': {'error_0': {'location': 'Yes', 'aspect': 'Accuracy', 'explanation': "The output is incorrect. The correct answer is 'No' because the service agreement states that Amazon reserves the right to remove or edit such content, but does not regularly review posted content. This means that Amazon may allow a third party to use the content, but it is not guaranteed. The output should be corrected to 'No'.", 'severity': 'Major', 'score_reduction': '4'}}}}</p>
<p><b>Answer of Domain01s-legal:</b> The service agreement allows users to upload various types of content to Amazon. In return, Amazon expects to receive extensive rights to this uploaded content. The focus of the analysis should be on whether these rights granted to Amazon include the sublicensing of content to third parties.</p> <p>The service agreement grants Amazon a nonexclusive, royalty-free, perpetual, irrevocable, and fully sublicensable right to use the uploaded content. This means Amazon has the right to allow others to use the content. The term "fully sublicensable" specifically suggests that Amazon can transfer its rights to third parties. Therefore, the logical conclusion is that Amazon can indeed allow a third party to use the content if it has been uploaded under the terms of this agreement.</p> <p>The relevant phrase from the agreement is: "a nonexclusive, royalty-free, perpetual, irrevocable, and fully sublicensable right." This provision clearly indicates that Amazon possesses the right to sublicense the content to others. The use of "fully sublicensable" supports the conclusion that Amazon has the flexibility to grant usage rights to any third party.</p> <p>Based on the broad rights granted to Amazon including the ability to sublicense the content, it is concluded that Amazon can allow a third party to use the uploaded content. The answer to the question is, therefore, "Yes."</p> <p><b>Evaluation of TIGERScore-13B:</b> {'num_errors': 0, 'score': -0.0, 'errors': {}}}</p>

Figure 14: Example of TIGERScore-13B’s evaluation.

## H Reasoning Process Analysis

In this section, we introduce a new perspective to analyze how Domain01s’s reasoning process assists user decision-making. Taking stock investment recommendation tasks in the financial domain as an example, previous research has primarily focused on prediction accuracy as the main evaluation metric (Koa et al., 2024; Xu and Cohen, 2018; Sawhney et al., 2020; Yang et al., 2022). However, as shown in Table 2, even the previously most advanced financial LLMs or LLMs extensively trained on stock data achieve prediction accuracy close to 50% (random choice) for this binary classification problem. This confirms that LLMs are still "Wall Street Neophytes" in stock predic-

tion (Xie et al., 2023a). In reality, many domain problems in the real world often do not have unified or unique correct answers, as they typically involve dynamically changing environmental conditions, the interplay of multiple influencing factors, and user-specific preferences. When facing these problems, users can use Domain01s’s responses as references to aid their judgment by providing explainable analysis processes and recommendations. For example, Figure 15 shows part of the model’s response when asking Domain01s-finance for stock investment advice. The model’s response includes both short-term and long-term analysis of stock prices and provides both short-term and long-term investment recommendations based on user investment habits.

**Question:** For a given set of facts, estimate their overall impact on AAPL’s stock price movement, and give investment advice.  
 For stock AAPL, the closing price changes over the last 30 trading days as of 2022-12-27 are : Date 2022-11-14: decreases 0.01366; Date 2022-11-15: increases 0.003418; ...  
 The monthly average of adjusted closing prices over the past 3 years is Month 2020-01: adjusted close price is 77.06512850806827; Month 2020-02: ...  
 In the past 5 days, there are the following facts:  
 2022-12-23: -Apple is approaching its 52-week low. -Apple hit a new ex-dividend date for \$0.1667 on December 27, 2022. ...

**Response:** Analysis looks at Apple stock (AAPL) from 2020-2022, focusing on late 2022. Main goal is to check stock trends and future direction based on price data and market factors.  
 AAPL grew well from 2020-2021, rising from \$77 to \$170. Stock did well during COVID-19. In 2022, prices started falling from \$170 high.  
 Stock seems expensive to some traders. Lost 25.7% in 2022. Analysts are giving lower price targets due to market conditions.

\*\*\*  
 Advice: **WAIT to buy.** Stock likely to fall more. While Apple is strong long-term, **wait for price to stabilize above \$133-135 before buying.** If buying for very long-term, consider **implementing a staged buying strategy rather than committing all capital at once.**

Figure 15: Example of Domain01s-finance’s response on stock investment recommendation. Blue bold text indicates short-term investment advice, and red bold text indicates long-term investment advice.

## I Training Data Scaling

In this section, we explore the impact of increasing training data on Domain01s performance. We introduce more legal QA data (Li et al., 2022), and following the process in Section 3.2, we use GPT-4o to generate reasoning processes, expanding the CoT-legal dataset to 10k entries. Then, we train the Qwen-2.5-Instruction model with 2k, 5k, and 10k data separately, and evaluate the performance differences of Domain01s-legal trained with different training data volumes. The results are as follows:

Model	CC	CAUD	MAUD	PP	IP	PJ	Scalar	TTP	TTD	Avg.
Domain01s-legal (2k)	88.64	81.76	80.33	66.54	52.63	72.00	88.97	95.33	78.78	<b>78.33</b>
Domain01s-legal (5k)	88.73	81.74	80.65	66.95	51.88	74.00	89.32	93.93	77.57	<b>78.30</b>
Domain01s-legal (10k)	88.96	81.63	81.87	66.63	53.38	74.00	89.32	93.93	80.37	<b>78.90</b>

Table 13: Performance comparison of Domain01s-legal models trained with different data volumes.

The results show that the accuracy improvement from increasing training data from 2k to 5k is not significant, and while increasing to 10k seems to increase the average accuracy (Avg.), the improvement on individual tasks is not substantial. This

aligns with our approach of using a small number of training samples (2k) in this paper. The purpose of constructing a small number of training samples is not to introduce substantial domain-specific knowledge, but to stimulate the model’s reasoning abilities in specific domains. However, we also encourage applying our method to domain models trained with large-scale domain data, using our few-shot approach to activate their reasoning capabilities to achieve stronger performance and robustness.

## J Human Evaluation Alignment

In Section 4.3, we introduce PROOF-Scores based on GPT-4o to automate the evaluation of models’ reasoning capability. Considering that human evaluations may have inconsistent scales and aspects compared to LLMs, we encourage having a human expert in the loop in evaluation scenarios that do not require rapid response and automation, to avoid biases introduced by LLMs.

On the other hand, studies (Chiang and Lee, 2023; Zheng et al., 2023; Desmond et al., 2024) support that LLMs like GPT-4 have evaluation capabilities comparable to humans. To understand whether this also applies to high-stake domain tasks, and to determine if our PROOF-Scores (GPT-4o) align with human judgment, we invited 3 PhD in finance and 3 in law to score the explainability of model results in Table 4 according to the scoring rules and intervals designed for PROOF-Scores. Given limited resources, we randomly sampled only 30% of questions from each dataset to create the questionnaires.

For expert scoring, we calculate the PROOF-Score the same way as (3). We calculate the average values and standard deviations of all expert scores, with results shown in Table 14.

Models	Stock		Legal		
	GPT-4o	Human expert	GPT-4o	Human expert	
Qwen-2.5-Instruct	6.281	5.137±0.332	Qwen-2.5-Instruct	3.428	3.145±0.226
Llama-3-Instruct	6.129	5.025±0.248	Llama-3-Instruct	3.417	3.136±0.228
OpenO1-Llama	6.212	5.342±0.105	OpenO1-Llama	6.554	5.808±0.109
OpenO1-Qwen	6.227	5.358±0.133	OpenO1-Qwen	6.588	5.937±0.121
Finance-LLM	6.023	4.709±0.852	Open-Australian-Legal	5.152	2.382±0.536
Finance-Chat	5.583	4.832±0.648	DISC-LawLLM	0	1.403±0.310
Finance-Llama3	5.965	4.813±0.731	Law-LLM	3.838	2.820±0.733
FinGPT	3.413	2.101±0.994	Law-Chat	3.339	3.274±0.384
Llama-2-taiwan-btc	0	1.438±0.455	Lawma	0	1.255±0.138
SEP	6.182	5.095±0.433			
<b>Domain01s-finance</b>	<b>6.359</b>	<b>5.834±0.452</b>	<b>Domain01s-Legal</b>	<b>6.677</b>	<b>6.296±0.148</b>

Table 14: Comparison of explanation quality (PROOF-Score) between Domain01s and baselines as evaluated by GPT-4o and human experts.

The results show that although human expert scores are not completely consistent with GPT-4o, their relative magnitudes are similar. That is, the

PROOF score (GPT-4o) assessment of the relative quality of different models is basically consistent with human experts. Additionally, both human experts and GPT-4o give Domain01s the highest ratings.

## **K Application Extension**

We demonstrate that the method proposed in this paper suits finance and legal domains and can be extended to service recommendations, risk assessment, biological medicine, and other scenarios where explainable model answers are needed. Domain01s can provide high-quality, interpretable answers for decision support in these fields.