

PPC-GPT: Federated Task-Specific Compression of Large Language Models via Pruning and Chain-of-Thought Distillation

Tao Fan^{1,2}, Guoqiang Ma², Yuanfeng Song², Lixin Fan², Qiang Yang³

¹Hong Kong University of Science and Technology, Hong Kong, China

²WeBank Co., Ltd, Shenzhen, China

³Hong Kong Polytechnic University, Hong Kong, China

Correspondence: tfanac@cse.ust.hk, qyang@cse.ust.hk

Abstract

Compressing Large Language Models (LLMs) into task-specific Small Language Models (SLMs) encounters two significant challenges: safeguarding domain-specific knowledge privacy and managing limited resources. To tackle these challenges, we propose PPC-GPT, a novel unified framework that systematically addresses both privacy preservation and model compression in federated settings. PPC-GPT works on a server-client federated architecture, where the client sends differentially private (DP) perturbed task-specific data to the server’s LLM. The LLM then generates synthetic data along with their corresponding rationales. This synthetic data is subsequently used for both LLM pruning and retraining processes. Our framework’s key innovation lies in its holistic integration of privacy-preserving mechanisms, synthetic data generation, and task-specific compression techniques, creating unique benefits through component interaction. Our experiments across diverse text generation tasks demonstrate that PPC-GPT successfully achieves dual objectives: maintaining competitive performance comparable to full-sized LLMs while ensuring robust privacy protection through its federated architecture. Our code has been contributed to the FATE open-source project and is now publicly accessible at https://github.com/FederatedAI/FATE-LLM/tree/main/python/fate_llm/algo/ppc-gpt.

1 Introduction

Large Language Models (LLMs), such as GPT-4 (OpenAI, 2023a) and LLaMA3-70B (Dubey et al., 2024), boasting billions of parameters and remarkable text generation capabilities, have emerged as a transformative force in the realm of artificial intelligence. However, their training demands substantial computational resources (OpenAI, 2023b), and their colossal size poses significant hurdles for practical deployment, especially

in resource-limited environments. Conversely, Small Language Models (SLMs), such as OPT-1.3B (Zhang et al., 2022) and Qwen2.5-1.5B (Team, 2024), frequently demonstrate superior computational efficiency and accelerated response rates, making them ideally suited for real-time applications with constrained resources. Enterprises with constrained resources typically prefer deploying SLMs, as they can do so without the concern of potential data leaks, a risk that is heightened when utilizing remote LLMs (Fan et al., 2025a,b, 2023; Kang et al., 2023). Yet, training an SLM from scratch, even the smallest billion-parameter models, entails considerable computational expenses that are financially prohibitive for most enterprises. Furthermore, SLMs exhibit inherent limitations that stem from their performance constraints.

In this work, we aim to tackle the following question: *Is it feasible to develop a task-specific and competitive SLM by harnessing an existing pre-trained LLM for enterprises with limited resources, while ensuring compliance with privacy requirements?* To achieve this objective, we delve into structured pruning (Xia et al., 2024; Men et al., 2024; Kim et al., 2024), as a viable approach. Pruning is generally regarded as a strategy for compressing task-specific models by eliminating redundant parameters and expediting inference, all while maintaining task performance.

We identify two crucial technical challenges associated with this problem: Firstly, how can we ensure the privacy of task-specific data when enterprises with limited resources are unable to prune an LLM into an SLM independently? In such cases, the need to transmit task-specific data to a remote server equipped with powerful computing resources arises, a practice that is frequently unacceptable to most enterprises due to privacy concerns. Secondly, how can we ensure that the performance of the SLM remains comparable to that of the LLM? Structured pruning inevitably leads to

some degree of performance degradation. To overcome these challenges, we introduce PPC-GPT, a privacy-preserving federated framework designed for compressing LLMs into task-specific SLMs via pruning and Chain-of-Thought (CoT) distillation.

As depicted in Figure 1, the envisioned architecture of PPC-GPT comprises a high-performance server adept at deploying LLMs and facilitating their pruning into SLMs, coupled with a client endowed with more constrained computational capabilities for running SLMs. Within the confines of our framework, the workflow unfolds as detailed below. Initially, the client sends task-specific data, perturbed to ensure privacy, to the server. These data are protected by the Exponential Mechanism of Differential Privacy (Dwork, 2006; McSherry and Talwar, 2007; Tong et al., 2025), thereby guaranteeing privacy protection. Subsequently, the server-side auxiliary LLM_{syn} generates synthetic data along with their corresponding rationales, based on these perturbed inputs. The server-side LLM_o , which represents the original model, undergoes pruning by PPC-GPT to yield the *target SLM*. This pruning process is informed by both the synthetic data and their associated rationales. Following the pruning of the LLM_o , the server retrains the *target SLM* through CoT (Wei et al., 2022; Hsieh et al., 2023; Li et al., 2023) knowledge distillation, leveraging the same synthetic data and rationales. Lastly, the server dispatches the refined *target SLM* to the client, who then proceeds to retrain the *target SLM* utilizing its locally private data.

Our contributions can be summarized as follows:

- **Unified Framework for Federated LLM Compression.** We propose PPC-GPT, the first holistic framework designed to systematically unify privacy-preserving techniques with LLM compression in a federated learning context. Its core innovation lies in the synergistic integration of four key modules: exponential mechanism-based data perturbation, CoT-guided synthetic data generation, rationale-aware structured pruning, and CoT-based knowledge distillation. This modular architecture is not only novel but also extensible, allowing for future advancements in any of its constituent parts.
- **Novel Rationale-Aware Structured Pruning for Reasoning Preservation.** We propose

a new structured pruning metric that evaluates network layers based on their contribution to generating explanatory rationales. This approach selectively preserves the model’s essential reasoning capabilities, a critical aspect often overlooked in standard compression techniques.

- **Component Interaction Benefits.** The integration creates unique advantages through component interaction. For example, combining DP-perturbed data with CoT-guided synthetic data generation enables both privacy protection and effective knowledge transfer, while the rationale-aware structured pruning leverages this enhanced data quality for better compression decisions.
- **Empirical Assessment of LLM Compressing to Task-Specific SLM.** Through extensive experiments across various text generation tasks using LLaMA and OPT models, we demonstrate how PPC-GPT’s component interactions lead to effective task-specific compression while maintaining privacy, achieving results competitive with full-sized LLMs.

2 Related Work

2.1 Differential Privacy

In this section, We briefly revisit two important definitions of differential privacy: ϵ -Differential Privacy and Exponential Mechanism (EM).

ϵ -Differential Privacy (DP). *The Definition of ϵ -Differential Privacy (DP)* (Dwork, 2006). A randomized algorithm $M : D \rightarrow S$ is ϵ -Differential Privacy if for any two neighboring datasets $D_1, D_2 \in D$ that differ exactly in a single data sample, and for any output $O \subseteq S$:

$$P_r[M(D_1) \in O] \leq e^\epsilon P_r[M(D_2) \in O] \quad (1)$$

where ϵ is a privacy parameter. Smaller values of ϵ imply stronger privacy guarantees.

Exponential Mechanism. *The Definition of Exponential Mechanism* (McSherry and Talwar, 2007; Tong et al., 2025). For a given scoring function $u : X \times Y \rightarrow R$, a randomized mechanism $M(X, u, Y)$ is ϵ -DP compliant if it satisfies:

$$P_r[y|x] \propto \exp\left(\frac{\epsilon \cdot u(x, y)}{2 \Delta u}\right) \quad (2)$$

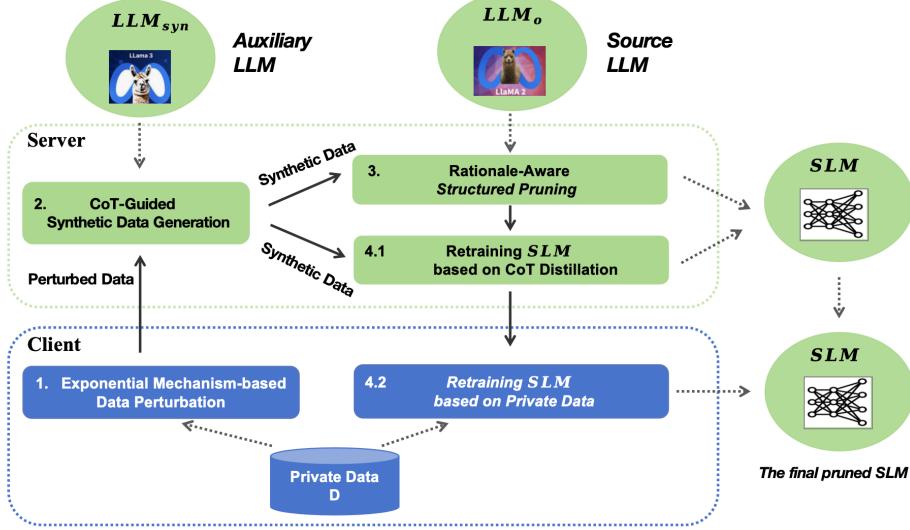


Figure 1: The overview of our proposed **PPC-GPT**. The PPC-GPT comprises four key components: (1) The *Exponential Mechanism-based Data Perturbation*, which perturbs the client’s data to ensure privacy; (2) The *CoT-Guided Synthetic Data Generation*, responsible for creating new synthetic data and rationales based on the perturbed data; (3) The *Rationale-Aware Structured Pruning*, a process that prunes original LLM_o to obtain the target smaller *SLM*; (4) The *Retraining SLM*, where the target *SLM* is retrained using both synthetic and original private data to restore accuracy.

where the sensitivity Δu is defined as:

$$\Delta u = \max_{x, x' \in X, y \in Y} |u(x, y) - u(x', y)| \quad (3)$$

2.2 Differential Privacy Synthetic Data

A practical approach to generating private synthetic data involves training a language model, such as LLaMA2-7B (Touvron et al., 2023), on private data using DP through DP-SGD (Song et al., 2013; Bassily et al., 2014; Abadi et al., 2016). Subsequently, the DP model is sampled repeatedly to produce synthetic data (Mattern et al., 2022; Yue et al., 2023; Kurakin et al., 2023). Research conducted by (Mattern et al., 2022; Yue et al., 2023; Kurakin et al., 2023) demonstrates that training downstream models on DP synthetic data achieves performance comparable to training directly on real data with DP, thereby underscoring the high quality of the synthetic data.

However, a significant challenge arises because cutting-edge LLMs, like GPT-4, do not offer model weights, making DP fine-tuning impractical. Even for open-source LLMs, such as LLaMA3-70B (Dubey et al., 2024), the process is resource-intensive. Meanwhile, these DP fine-tuning methods inherently rely on a trusted server to gather data from data owners for model training (Chen et al., 2023), significantly limiting their applicability in scenarios where such trusted servers are not

available, as is the case in our research context. In the context of this work, we operate within a client-server architecture where fine-tuning the LLM on the server is not an option.

2.3 Model Pruning

Model pruning, initially proposed by (LeCun et al., 1989) and subsequently enhanced by (Han et al., 2015), stands as a resilient and efficient strategy for mitigating model redundancy and attaining compression. This methodology branches into two primary techniques: *unstructured pruning* and *structured pruning*.

Unstructured pruning (Dong et al., 2017; Lee et al., 2019; Wang et al., 2020; Sun et al., 2024; Frantar and Alistarh, 2023) can obtain highly compressed models by directly pruning neurons, disregarding the model’s internal architecture, which also causes unstructured sparsity and hard deployment. A more pragmatic and structured option is structured pruning. *Structured pruning* targets organized patterns for removal, encompassing entire layers (Jha et al., 2023), attention heads within Multi-Head Attention (MHA) mechanisms (Michel et al., 2019), hidden sizes in Feedforward Neural Networks (FFN) (Nova et al., 2023), as well as hybrid configurations (Kurtić et al., 2024). In recent times, there has been a surge in structured pruning research tailored specifically for LLMs. For ex-

ample, ShortGPT (Men et al., 2024), LaCo (Yang et al., 2024), and Shortened LLaMA (Kim et al., 2024) concentrate solely on pruning depth (i.e., layer-wise). LLM-Pruner (Ma et al., 2023) eliminates coupled structures in relation to network width while preserving the layer count. Sheared-LLaMA (Xia et al., 2024) introduces a mask learning phase that is designed to pinpoint prunable components in both network width and depth. Our work falls in the category of structured pruning of LLMs.

3 Problem Formulation

Given an LLM f_θ with parameters θ , which represents the original LLM that requires pruning, and a task-specific dataset \mathcal{D} containing private data, our objective is to develop a target smaller, task-specific compressed SLM f_ϕ parameterized by ϕ . To achieve this, we seek to find the optimal pruning strategy \mathcal{P} and retraining approach \mathcal{R} . The objective can be formulated as follows:

$$\begin{aligned} & \min_{\mathcal{P}, \mathcal{R}} \mathcal{L}(\phi; \theta, \mathcal{D}) \\ \text{s.t. } & |\phi| \ll |\theta| \quad \text{and} \quad \mathcal{L}_p(\mathcal{D}) < \delta \end{aligned} \quad (4)$$

where $\mathcal{L}(\phi; \theta, \mathcal{D})$ is the loss function measuring the performance of the compressed SLM on the task-specific dataset. $|\phi|$ and $|\theta|$ denote the number of parameters in the compressed and original models, respectively. $\mathcal{L}_p(\mathcal{D})$ is the privacy loss incurred due to the perturbation of the data to ensure differential privacy.

Our goal is to find the optimal pruning strategy \mathcal{P} and retraining approach \mathcal{R} that minimizes the overall loss, taking into account both the performance of the compressed SLM and the privacy protection of the task-specific data in the client. We assume the server to be *semi-honest*, meaning it may attempt to extract the client's private data from the information it receives.

4 The Proposed PPC-GPT Framework

In this section, we introduce PPC-GPT, a unified privacy-preserving federated framework for compressing LLMs into task-specific SLMs. We illustrate the PPC-GPT architecture in Figure 1. As detailed in Algorithm 1, our framework comprises four key modules that work in concert:

- *Exponential Mechanism-based Data Perturbation*: Ensures privacy protection through exponential mechanism.

Algorithm 1 PPC-GPT

Require: Private dataset $\mathcal{D} = \{(x_i, y_i)\}_{i=1}^N$, LLM_{syn} for synthetic data generation, Original $LLM_o f_\theta$ that requires pruning, Privacy budget ϵ

Ensure: Task-specific SLM f_ϕ with privacy guarantees

- 1: **Phase 1: Exponential Mechanism-based Data Perturbation**
- 2: Apply Exponential Mechanism \mathcal{M} to \mathcal{D} with budget ϵ
- 3: Generate $\mathcal{D}_p = \{(x_i^p)\}_{i=1}^N$ according to Eq.(5)
- 4: **Phase 2: CoT-guided Synthetic Data Generation**
- 5: Server's LLM_{syn} processes \mathcal{D}_p to generate synthetic data
- 6: Generate $\mathcal{D}_s = \{(x_i^s, (y_i^s, r_i^s))\}_{i=1}^{N_s}$
- 7: **Phase 3: Rationale-Aware Structured Pruning**
- 8: Calculate Block Influence scores using \mathcal{D}_s according to Eq.(7)
- 9: Identify redundant layers based on BI values
- 10: Obtain pruned model structure f_ϕ where $|\phi| \ll |\theta|$
- 11: **Phase 4: Retraining SLM via Two-Stage Knowledge Distillation**
- 12: Server performs CoT distillation using \mathcal{D}_s according to Eq.(8), (9), (10)
- 13: Client fine-tunes with private data \mathcal{D} according to Eq.(11)
- 14: **return** Compressed task-specific SLM f_ϕ

- *CoT-guided Synthetic Data Generation*: Creates high-quality synthetic data and rationales.
- *Rationale-Aware Structured Pruning*: Leverages synthetic data and rationales for model compression.
- *Retraining SLM*: Optimizes the compressed model through two-stage knowledge distillation.

We elaborate on these modules in Section 4.1, 4.2, 4.3 and 4.4, respectively. Through this integrated approach, PPC-GPT effectively addresses the challenges of privacy-preserving LLM compression while maintaining task-specific performance.

4.1 Exponential Mechanism-based Data Perturbation

We utilize an exponential mechanism (McSherry and Talwar, 2007; Yue et al., 2021; Chen et al., 2023) to perturb the local private data $\mathcal{D} = \{(x_i, y_i)\}_{i=1}^N$, which satisfies the criteria for the ϵ -DP. For detailed information about the exponential mechanism, please refer to Section 2.1. We denote the perturbed dataset as $\mathcal{D}_p = \{(x_i^p)\}_{i=1}^N$, where x_i^p signifies an perturbed input based on the original local private dataset \mathcal{D} .

The Exponential Mechanism \mathcal{M} is defined as a randomized algorithm that, given the original local private dataset \mathcal{D} , outputs the perturbed dataset \mathcal{D}_p with probability proportional to the exponential of the utility score (in this work, we use cosine similarity as the utility function):

$$\mathcal{M}(\mathcal{D}) = \mathcal{D}_p \quad \text{with prob} \propto \exp\left(\frac{\epsilon \cdot u(\mathcal{D}, \mathcal{D}_p)}{2 \Delta u}\right) \quad (5)$$

4.2 CoT-guided Synthetic Data Generation

When the server-side LLM_{syn} receives the perturbed data \mathcal{D}_p , the server initiates a procedure where LLM_{syn} generates fresh synthetic data along with their corresponding rationales based on these perturbed data. We denote the synthetic dataset as $\mathcal{D}_s = \{(x_i^s, (y_i^s, r_i^s))\}_{i=1}^{N_s}$, where x_i^s signifies an input, y_i^s signifies the corresponding expected output label, r_i^s signifies the desired rationale, and N_s represents the sample size of synthetic data.

As illustrated in Figure 2, we introduce a simple and efficient method for generating synthetic data, utilizing prompt engineering techniques and CoT technology:

1. **Question Generation.** We prompt LLM_{syn} to create a new question, starting from a perturbed question. To enhance the validity of these new created questions, we enforce three guidelines within the prompt: (1) the new question needs to conform to common knowledge, (2) it must be solvable on its own, independent of the original question, and (3) it should not contain any answer responses. Furthermore, we establish specific formatting standards for both questions and answers, customized to suit the needs of various datasets (Li et al., 2024).

2. **Answer Generation.** We instruct LLM_{syn} to generate a CoT response for every newly created question. For consistency, we request LLM_{syn} to generate answers to the same question three times and check for agreement. If the answers differ, we reject the synthetic data.

3. **Rationale Generation.** We request LLM_{syn} to generate rationales for each synthetic data using the CoT prompting technique.

The generated synthetic data and their rationales are then employed for model pruning and retraining on the server-side.

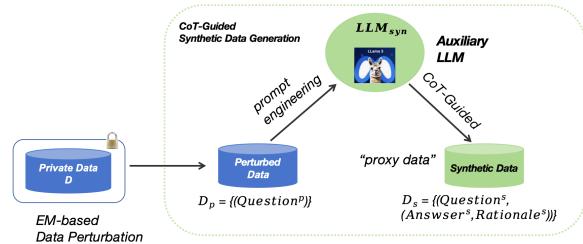


Figure 2: CoT-Guided Synthetic Data Generation.

4.3 Rationale-Aware Structured Pruning

LLMs exhibit layer-wise redundancy, with deeper layers often showing higher levels of functional overlap. To identify and remove redundant layers effectively, we need a quantitative metric that can assess each layer's contribution to the model's performance. This intrinsic metric should evaluate both the layer's individual importance and its interaction with other layers in maintaining the model's overall functionality.

To quantify the impact of each layer, we use a novel metric termed "Block Influence" (BI), which is proposed in the ShortGPT (Men et al., 2024). This metric is grounded in the hypothesis that a transformer block's significance is directly proportional to the extent it modifies the hidden states. Mathematically, the BI score for the i^{th} block is computed as:

$$BI_i = 1 - \mathbb{E}_{X,t} \left[\frac{X_{i,t}^T X_{i+1,t}}{\|X_{i,t}\|_2 \|X_{i+1,t}\|_2} \right], \quad (6)$$

where X_i denotes the input to the i^{th} layer, and $X_{i,t}$ represents the t^{th} row of X_i .

On the server, we utilize the synthetic dataset \mathcal{D}_s , as described in Section 4.2, to compute the BI

score for each layer of the LLM_o model, denoted as f_{θ_o} . This model represents the original LLM that requires pruning.

The original BI method (Men et al., 2024) relies solely on input and task label information, processed through a single forward pass: $f_{\theta}(x_i^s) \rightarrow y_i^s$. **We further extend the BI computation to encompass two distinct facets of influence:** $f_{\theta}(x_i^s) \rightarrow y_i^s$ and $f_{\theta}(x_i^s) \rightarrow r_i^s$. This enhancement not only facilitates the prediction of task labels but also enables the generation of corresponding rationales based on the inputs. **Our novel BI score is determined as follows:**

$$BI_i = BI_{Label,i} + BI_{Rationale,i} \quad (7)$$

where $BI_{Label,i}$ and $BI_{Rationale,i}$ signify the influences pertaining to label predictions and rationale generation, respectively.

A higher BI score indicates greater layer importance in the model architecture. As illustrated in Figure 3, we leverage these BI scores to guide our pruning strategy: layers are arranged in ascending order based on their BI scores, and those with lower scores are systematically removed to obtain the pruned model structure SLM f_{ϕ} .

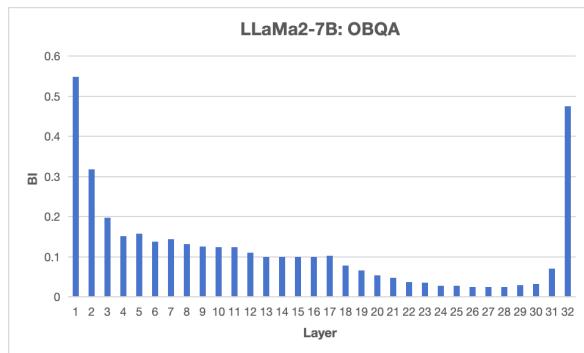


Figure 3: Layer Importance Example: The significance of each layer, as indicated by the BI (Block Influence) value of LLaMA2-7B on the OBQA dataset, based on the PPC-GPT framework.

4.4 Retraining

We employ the term "retraining" to designate the process of performance recovery subsequent to pruning. In this section, retraining is divided into two stages: (1) *Server-side Retraining*, and (2) *Client-side Retraining*.

Server-side Retraining. On the server side, we utilize the synthetic dataset \mathcal{D}_s , as described in Section 4.2, to retrain the pruned model SLM f_{ϕ} . **We propose CoT knowledge distillation, guided by**

rationales generated by LLM_{syn} , to enhance the performance of SLM f_{ϕ} . Formally, we conceptualize the learning process with rationales as a *multi-task learning* problem (Zhang and Yang, 2021; Wei et al., 2022; Hsieh et al., 2023). Specifically, we train the model $f_{\phi}(x_i^s) \rightarrow (y_i^s, r_i^s)$ to achieve not only the prediction of task labels but also the generation of corresponding rationales based on textual inputs. This multi-task training ensures that our model produces not only accurate predictions but also insightful justifications for its decisions, thereby enhancing the model's transparency and explainability. The multi-task learning objective can be formulated as follows:

$$\mathcal{L} = \mathcal{L}_{Label} + \mathcal{L}_{Rationale} \quad (8)$$

where \mathcal{L}_{Label} represents the label prediction loss:

$$\mathcal{L}_{Label}(\phi; \mathcal{D}_s) = \mathbb{E}_{(x^s, y^s) \sim \mathcal{D}_s} \ell_{CE}(f_{\phi}(x^s), y^s) \quad (9)$$

and $\mathcal{L}_{Rationale}$ represents the rationale generation loss:

$$\mathcal{L}_{Rationale}(\phi; \mathcal{D}_s) = \mathbb{E}_{(x^s, r^s) \sim \mathcal{D}_s} \ell_{CE}(f_{\phi}(x^s), r^s) \quad (10)$$

where ℓ_{CE} denotes the cross-entropy loss.

Client-side Retraining. On the client side, we utilize local private data \mathcal{D} to further retrain the pruned model, SLM f_{ϕ} , once it has been received from the server. **Our work encompasses conventional training, leveraging ground truth labels to further enhance the performance of SLM f_{ϕ} .** Formally, the label prediction loss for this dataset \mathcal{D} is formulated as follows:

$$\mathcal{L}_{Label}(\phi; \mathcal{D}) = \mathbb{E}_{(x, y) \sim \mathcal{D}} \ell_{CE}(f_{\phi}(x), y) \quad (11)$$

5 Experiments

5.1 Setup

We have devised a scenario to assess the performance of the PPC-GPT framework across various text generation tasks. This setup employs a client-server architecture, where the server hosts an *auxiliary LLM* for synthetic data generation, denoted as LLM_{syn} . Specifically, we have selected LLaMA3-70B (Dubey et al., 2024) for this purpose. For model pruning, we utilize LLaMA2-7B (Touvron et al., 2023) and OPT-6.7B (Zhang et al., 2022) as the source models, denoted as LLM_o . In the default setting, the privacy budget $\epsilon = 3$, and the synthetic data ratio is 8.

Datasets and Evaluation Metrics. We conduct a comparative evaluation of PPC-GPT on QA datasets. Specifically, we include CommonsenseQA (CQA) (Talmor et al., 2019), OpenBookQA (OBQA) (Mihaylov et al., 2018), ARC-C (Clark et al., 2018), ARC-E (Clark et al., 2018), FiQA-SA (Maia et al., 2018). For these datasets, we primarily use **Accuracy** as the evaluation metric. It’s worth noting that in our experiments, all methods undergo zero-shot evaluation and we use the *lm-evaluation-harness* package (Gao et al., 2023).

Baselines. To evaluate the performance of our PPC-GPT framework, we conducted a comparative analysis against the following baselines:

- DenseSFT, where the client independently fine-tunes LLM_o using its private dataset.
- Plain-C, where the client independently prunes LLM_o using its private dataset (suppose the client can deploy LLM_o) and subsequently fine-tunes the pruned model.
- DP-Instruct-C (Yu et al., 2024), where the client finetunes generator (e.g., LLaMA2-1.3B) with DP-SGD and using synthetic datasets generated from generator to prune LLM_o and subsequently fine-tunes the pruned model with the private dataset.

5.2 Main Results

In our experiments, we extensively evaluated the performance of the proposed PPC-GPT framework across various text generation tasks. Notably, given that current structured pruning methods typically reduce parameters by no more than 30%, we conducted experiments with approximately 30% of the parameters pruned. Additional experiments exploring different parameter reduction proportions will be discussed in Section 5.3.5.

As shown in Table 1, the results highlight the effectiveness of PPC-GPT in compressing LLMs into task-specific SLMs while prioritizing data privacy protection, when compared to other baseline approaches. PPC-GPT outperforms the DP-Instruct-C method, which utilizes DP-SGD for privacy protection during model compression. Furthermore, PPC-GPT even surpasses the Plain-C method, which directly compresses the model using private data. Additionally, when compared to DenseSFT, the compressed model in PPC-GPT even outperforms the raw model on some datasets. Specifically, taking LLaMA2-7B for an example,

in the LLaMA2-7B model, PPC-GPT outperforms the DP-Instruct-C method by 0.4%, 5.2%, 5%, 15.1%, and 1.8% on the CQA, OBQA, ARC-E, ARC-C, and FiQA-SA datasets, respectively. Similarly, PPC-GPT exceeds the Plain-C method by 0.7%, 2%, 4.5%, 8.2%, and 1.6% on the respective datasets.

5.3 Ablation Study

5.3.1 Impact of Different Privacy Budgets

In this section, we explore the impact of privacy budgets on the performance of PPC-GPT. Table 2 presents PPC-GPT’s performance across a range of privacy budgets ($\epsilon = 1, 3, 5, 10$). Notably, when juxtaposed with Table 1, it becomes apparent that even with a privacy budget of $\epsilon = 1$, PPC-GPT outperforms the Plain-C method by 1.7% and 3.4% on the OBQA and ARC-E datasets, respectively, within the LLaMA2-7B model. Similarly, PPC-GPT exceeds it by 14% and 14.4% in the OPT-6.7B model. As the privacy budget ϵ increases, PPC-GPT’s performance demonstrates a significant improvement, highlighting its proficiency and adaptability in achieving a balance between privacy and utility.

5.3.2 Impact of Different Synthetic Data

In this section, we explore the impact of synthetic data on PPC-GPT’s performance, considering two dimensions: the synthetic data ratio and the inclusion of rationales in synthetic data.

Synthetic Data Ratio. Table 3 presents the performance of PPC-GPT across various synthetic data ratios (ratio = 1, 2, 4, 8). As the ratio of synthetic data increases, PPC-GPT’s performance exhibits a substantial improvement, highlighting the crucial role of the synthetic data ratio and indicating that a higher amount of synthetic data results in further improvements. Specifically, PPC-GPT with the synthetic data ratio of 8 outperforms the ratio of 1 by 1.7% and 4.1% on the OBQA and ARC-E datasets, respectively, within the LLaMA2-7B model. Similarly, with the OPT-6.7B model, it exceeds the ratio of 1 by 4.2% and 7.6%.

Synthetic Data Rationales. We undertake an analysis to investigate the effects of rationales on PPC-GPT’s performance. Table 4 compares PPC-GPT’s performance between synthetic data with and without rationales (PPC-GPT w/ rationales and PPC-GPT w/o rationales). The findings demonstrate that PPC-GPT exhibits superior performance when the rationales of synthetic data is utilized,

Model	Method	Ratio (%)	DataSets				
			CQA	OBQA	ARC-E	ARC-C	FiQA-SA
LLaMA2-7B	DenseSFT	0	81.6 \pm 0.54	80.3 \pm 0.50	82.9 \pm 0.18	60.0 \pm 0.42	68.9 \pm 1.66
	Plain-C	30	77.6 \pm 0.14	77.9 \pm 0.16	79.7 \pm 0.29	54.0 \pm 0.82	71.1 \pm 1.37
	DP-Instruct-C	30	77.9 \pm 0.62	74.7 \pm 1.32	79.2 \pm 0.33	47.1 \pm 4.10	70.9 \pm 0.83
	PPC-GPT	30	78.3 \pm 0.41	79.9 \pm 0.57	84.2 \pm 0.33	62.2 \pm 0.61	72.7 \pm 0.54
OPT-6.7B	DenseSFT	0	75.4 \pm 0.64	60.0 \pm 0.99	65.8 \pm 0.70	31.4 \pm 0.86	70.0 \pm 1.09
	Plain-C	30	47.4 \pm 1.12	36.5 \pm 1.48	40.2 \pm 0.89	27.6 \pm 0.37	52.4 \pm 1.37
	DP-Instruct-C	30	58.7 \pm 2.04	39.7 \pm 1.04	44.5 \pm 2.53	28.6 \pm 1.72	54.5 \pm 1.67
	PPC-GPT	30	65.6 \pm 0.95	52.1 \pm 0.96	57.3 \pm 0.16	36.0 \pm 0.59	64.9 \pm 1.26

Table 1: Performance Comparison of Compression Methods on LLMs.

Model	Datasets	Stage	Privacy Budget(ϵ)			
			1	3	5	10
LLaMA2	OBQA	S	65.4	67.1	67.9	69.4
		C	79.6	79.9	80.1	79.8
	ARC-E	S	78.8	80.4	79.9	79.5
		C	83.1	84.2	84.4	83.4
OPT	OBQA	S	35.7	36.3	36.1	38.8
		C	50.5	52.1	52.4	53.5
	ARC-E	S	49.1	50.4	49.3	50.5
		C	54.6	57.3	55.5	55.3

Table 2: Comparison of PPC-GPT’s performance across **different privacy budgets ϵ** . S denotes the performance of target SLM on the server-side, while C represents the performance of target SLM on the client-side.

as compared to when it is absent. Specifically, PPC-GPT w/ rationales outperforms PPC-GPT w/o rationales by 0.8% and 0.9% on the OBQA and ARC-E datasets, respectively, within the LLaMA2-7B model. Similarly, with the OPT-6.7B model, PPC-GPT w/ rationales exceeds PPC-GPT w/o rationales by 7% and 9.1%.

5.3.3 Impact of Server-Side Retraining

In this section, we explore the impact of server-side retraining on the performance of PPC-GPT. Table 5 presents a comparison of PPC-GPT’s performance with and without server-side retraining. The findings demonstrate that PPC-GPT exhibits superior performance when server-side retraining is utilized, as compared to when it is absent. Specifically, PPC-GPT w/ server-side retraining outperforms PPC-GPT w/o server-side retraining by 2% and 4.5% on the OBQA and ARC-E datasets, respectively, within the LLaMA2-7B model. Similarly,

Model	Datasets	Stage	Synthetic Data Ratio			
			1	2	4	8
LLaMA2	OBQA	S	62.3	64.6	64.6	67.1
		C	78.2	78.3	78.5	79.9
	ARC-E	S	73.5	75.5	77.9	80.4
		C	80.1	80.8	82.3	84.2
OPT	OBQA	S	32.9	34.7	36.9	36.3
		C	47.9	50.2	51.5	52.1
	ARC-E	S	40.4	43.9	47.5	50.4
		C	49.7	52.3	54.9	57.3

Table 3: Comparison of PPC-GPT’s performance across **different synthetic data ratio**.

with the OPT-6.7B model, PPC-GPT w/ server-side retraining exceeds PPC-GPT w/o server-side retraining by 15.1% and 15.7%.

5.3.4 Impact of Different Importance Metric

In this section, we explore the impact of different important metrics on PPC-GPT’s performance:

Seq: The importance is directly correlated with the sequence order, where the shallower layers hold greater importance.

BI: BI mentioned in previous section 4.3.

Table 6 presents PPC-GPT’s performance across different important metrics. The findings demonstrate that PPC-GPT with BI exhibits superior performance than PPC-GPT with Seq.

5.3.5 Impact of Different Model Pruning Ratio

In this section, we explore the impact of different model pruning ratio on PPC-GPT’s performance. Table 7 presents the performance of PPC-GPT across different model pruning ratios (namely, 0%,

Model	Datasets	Stage	Rationales	
			w/	w/o
LLaMA2	OBQA	S	67.1	65.9
		C	79.9	79.1
	ARC-E	S	80.4	77.9
		C	84.2	83.3
OPT	OBQA	S	36.3	31.1
		C	52.1	45.1
	ARC-E	S	50.4	43.2
		C	57.3	48.2

Table 4: Comparison of PPC-GPT’s performance: with vs. without **rationales**.

Model	Dataset	Server:Retraining	
		w/	w/o
LLaMA2	OBQA	79.9	77.9
	ARC-E	84.2	79.7
OPT	OBQA	52.1	37.0
	ARC-E	57.3	41.6

Table 5: Comparison of PPC-GPT’s performance: with vs. without **server-side retraining**.

30%, 50%, and 70%). As the pruning ratio increases, the performance of PPC-GPT exhibits a decline.

6 Conclusions

In this paper, we introduced PPC-GPT, a novel federated framework for compressing LLMs into task-specific SLMs while preserving privacy. Our framework integrates four key components: exponential mechanism-based data perturbation, CoT-guided synthetic data generation, rationale-aware structured pruning, and CoT-based knowledge distillation. Experiments demonstrate that PPC-GPT effectively compresses LLMs while maintaining comparable performance and ensuring privacy protection. This work provides a practical solution for deploying LLMs in resource-constrained, privacy-sensitive scenarios.

Limitations

While PPC-GPT shows promising results in compressing LLMs into task-specific SLMs while ensuring data privacy, it has several limitations. Firstly, PPC-GPT relies on an auxiliary LLM with robust CoT capabilities to generate high-quality

Model	Datasets	Stage	Important	
			BI	Seq
LLaMA2	OBQA	S	67.1	66.5
		C	79.9	79.9
	ARC-E	S	80.4	80.0
		C	84.2	83.9
OPT	OBQA	S	36.3	34.7
		C	52.1	48.3
	ARC-E	S	50.4	43.7
		C	57.3	51.7

Table 6: Comparison of PPC-GPT’s performance across **different importance metrics**.

Model	Ratio (%)	DataSets	
		OBQA	ARC-E
LLaMA2	0	80.3	82.9
	30	79.9	84.2
	50	74.4	76.8
	70	35.3	37.4
OPT	0	60.0	65.8
	30	52.1	57.3
	50	36.1	38.3
	70	30.9	33.2

Table 7: Comparison of PPC-GPT’s performance across **different pruning ratios**.

synthetic data and rationales. These synthetic data are crucial for guiding the structured pruning and retraining processes of both the source LLM (the model slated for compression) and the target SLM (the compressed model). If the auxiliary LLM lacks sophisticated CoT reasoning abilities, the quality and diversity of the generated synthetic data may be compromised, which in turn could adversely affect the performance of the compressed SLMs. This limitation underscores the importance of selecting or pre-training an auxiliary LLM with strong CoT capabilities when deploying PPC-GPT. However, it’s important to note that the source LLM (the model slated for compression) does not necessarily require CoT capabilities. Furthermore, as observed in our experiments, the performance of PPC-GPT tends to degrade with higher pruning ratios. This indicates that optimizing the pruning strategy to strike a better balance between model size and performance remains an open challenge.

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A Privacy Analysis of PPC-GPT

Our privacy protection strategy in PPC-GPT is grounded in rigorous theoretical foundations and validated through comprehensive empirical studies. The framework implements a theoretically-sound differential privacy (DP) mechanism that operates at the token-level feature space, completely eliminating the need for raw data transmission. Specifically, we adopt the exponential mechanism, which provides formal ϵ -DP guarantees and has been extensively analyzed in privacy-preserving NLP literature (Yue et al., 2021; Chen et al., 2023; Tong et al., 2025). The theoretical privacy guarantees of this mechanism are well-established, allowing us to focus on its practical implementation and performance optimization rather than re-establishing its privacy properties.

B Implementation Details

B.1 Hyperparameter Settings

During the training process, we specifically configured the parameters. Specifically, we set the batch size to 32 and utilized the AdamW optimizer. The maximum number of training steps varied between 300 and 6400. Additionally, we established a learning rate of 5e-5. For the input and target lengths,

we set the maximum question length to 64 and the maximum target length to 128. For the LoRA configuration of LLaMA2, we set the LoRA alpha to 32 and the LoRA rank to 8. In contrast, for the OPT model, we configured the LoRA alpha to 64 and the LoRA rank to 32. The Lora dropout for both models was set to 0.1.

B.2 Data Splitting

For the datasets, all splits (training, validation, and test) were downloaded from HuggingFace (Lhoest et al., 2021).

B.3 Dataset Licenses

All the datasets were downloaded from HuggingFace (Lhoest et al., 2021) and under Apache License, Version 2.0.

B.4 Machine Configuration

The experiments were conducted on machines equipped with 4 and 8 Nvidia V100 32G.