

# Text Categorization using Feature Projections

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## Abstract

This paper proposes a new approach for text categorization, based on a feature projection technique. In our approach, training data are represented as the projections of training documents on each feature. The voting for a classification is processed on the basis of individual feature projections. The final classification of test documents is determined by a majority voting from the individual classifications of each feature. Our empirical results show that the proposed approach, *Text Categorization using Feature Projections* (TCFP), outperforms  $k$ -NN, Rocchio, and Naïve Bayes. Most of all, TCFP is about one hundred times faster than  $k$ -NN. Since TCFP algorithm is very simple, its implementation and training process can be done very easily. For these reasons, TCFP can be a useful classifier in the areas, which need a fast and high-performance text categorization task.

## Introduction

An issue of text categorization is to classify documents into a certain number of pre-defined categories. Text categorization is an active research area in information retrieval and machine learning. A wide range of supervised learning algorithms has been applied to this issue, using a training data set of categorized documents. The Naïve Bayes (McCalum et al., 1998; Ko et al., 2000), Nearest Neighbor (Yang et al., 2002), and Rocchio (Lewis et al., 1996) are well-known algorithms.

Among these learning algorithms, we focus

on the Nearest Neighbor algorithm. In particular, the  $k$ -Nearest Neighbor ( $k$ -NN) classifier in text categorization is one of the state-of-the-art methods including Support Vector Machine (SVM) and Boosting algorithms. Since the Nearest Neighbor algorithm is much simpler than the other algorithms, the  $k$ -NN classifier is intuitive and easy to understand, and it learns quickly. But the weak point of  $k$ -NN is too slow at running time. The main computation is the on-line scoring of all training documents, in order to find the  $k$  nearest neighbors of a test document. In order to reduce the scaling problem in on-line ranking, a number of techniques have been studied in the literature. Techniques such as *instance pruning technique* (Wilson et al., 2000) and *projection* (Akkus et al., 1996) are well known.

The *instance pruning technique* is one of the most straightforward ways to speed classification in a nearest neighbor system. It reduces time necessary and storage requirements by removing instances from the training set. A large number of such reduction techniques have been proposed, including the *Condensed Nearest Neighbor Rule* (Hart, 1968), *IB2* and *IB3* (Aha et al., 1991), and the *Typical Instance Based Learning* (Zhang, 1992). These and other reduction techniques were surveyed in depth in (Wilson et al., 1999), along with several new reduction techniques called *DROP1-DROP5*. Of these, *DROP4* had the best performance.

Another trial to overcome this problem exists on *feature projections*. Akkus and Guvenir presented a new approach to classification based on feature projections (Akkus et al., 1996). They called their resulting algorithm *k-Nearest Neighbor on Feature Projections* ( $k$ -NNFP). In

this approach, the classification knowledge is represented as the sets of projections of training data on each feature dimension. The classification of an instance is based on a voting by the  $k$  nearest neighbors of each feature in a test instance. The resulting system allowed the classification to be much faster than that of  $k$ -NN and its performance were comparable with  $k$ -NN.

In this paper, we present a particular implementation of text categorization using feature projections. When we applied the feature projection technique to text categorization, we found several problems caused by the special properties of text categorization problem. We describe these problems in detail and propose a new approach to solve them. The proposed system shows the better performance than  $k$ -NN and it is much faster than  $k$ -NN.

The rest of this paper is organized as follows. Section 1 simply presents  $k$ -NN and  $k$ -NNFP algorithm. Section 2 explains a new approach using feature projections. In section 3, we discuss empirical results in our experiments. Section 4 is devoted to an analysis of time complexity and strong points of the new proposed classifier. The final section presents conclusions.

## 1. $k$ -NN and $k$ -NNFP Algorithm

In this section, we simply describe  $k$ -NN and  $k$ -NNFP algorithm.

### 1.1 $k$ -NN Algorithm

As an instance-based classification method,  $k$ -NN has been known as an effective approach to a broad range of pattern recognition and text classification problems (Duda et al., 2001; Yang, 1994). In  $k$ -NN algorithm, a new input instance should belong to the same class as their  $k$  nearest neighbors in the training data set. After all the training data is stored in memory, a new input instance is classified with the class of  $k$  nearest neighbors among all stored training instances.

For the distance measure and the document representation, we use the conventional vector space model in text categorization; each document is represented as a vector of term

weights, and similarity between two documents is measured by the cosine value of the angle between the corresponding vectors (Yang et al., 2002).

Let a document  $d$  with  $n$  terms ( $t$ ) be represented as the feature vector:

$$\vec{d} = \langle w(t_1, \vec{d}), w(t_2, \vec{d}), \dots, w(t_n, \vec{d}) \rangle \quad (1)$$

We compute the weight vectors for each document using one of the conventional TF-IDF schemes (Salton et al., 1988). The weight of term  $t$  in document  $d$  is calculated as follows:

$$w(t, \vec{d}) = \frac{(1 + \log tf(t, \vec{d})) \times \log(N/n_t)}{\|\vec{d}\|} \quad (2)$$

where

- i)  $w(t, \vec{d})$  is the weight of term  $t$  in document  $\vec{d}$
- ii)  $tf(t, \vec{d})$  is the within-document Term Frequency (TF)
- iii)  $\log(N/n_t)$  is the Inverted Document Frequency (IDF)
- iv)  $N$  is the number of documents in the training set
- v)  $n_t$  is the number of training documents in which  $t$  occurs
- vi)  $\|\vec{d}\| = \sqrt{\sum_{t \in \vec{d}} w(t, \vec{d})^2}$  is the 2-norm of vector  $\vec{d}$

Given an arbitrary test document  $d$ , the  $k$ -NN classifier assigns a *relevance score* to each candidate category  $c_j$  using the following formula:

$$s(c_j, \vec{d}) = \sum_{\vec{d}' \in R_k(\vec{d}) \cap D_j} \cos(\vec{d}', \vec{d}) \quad (3)$$

where  $R_k(\vec{d})$  denotes a set of the  $k$  nearest neighbors of document  $d$  and  $D_j$  is a set of training documents in class  $c_j$ .

### 1.2 $k$ -Nearest Neighbor on Feature Projection ( $k$ -NNFP) Algorithm

The  $k$ -NNFP is a variant of  $k$ -NN method. The main difference is that instances are projected on their features in the  $n$ -dimensional space (see figure 1) and distance between two instances is calculated according to a single feature. The

distance between two instances  $d_i$  and  $d_j$  with regard to  $m$ -th feature  $t_m$  is  $dist_m(t_m(i), t_m(j))$  as follows:

$$dist_m(t_m(i), t_m(j)) = |w(t_m, \vec{d}_i) - w(t_m, \vec{d}_j)| \quad (4)$$

where  $t_m(i)$  denotes  $m$ -th feature  $t$  in a instance  $\vec{d}_i$ .

The classification on a feature is done according to votes of the  $k$ -nearest neighbors of that feature in a test instance. The final classification of the test instance is determined by a majority voting from individual classification of each feature. If there are  $n$  features, this method returns  $n \times k$  votes whereas  $k$ -NN method returns  $k$  votes.

## 2. A New Approach of Text Categorization on Feature Projections

First of all, we show an example of feature projections in text categorization for more easy understanding. We then enumerate the problems to be duly considered when the feature projection technique is applied to text categorization. Finally, we propose a new approach using feature projections to overcome these problems.

### 2.1 An Example of Feature Projections in Text Categorization

We give a simple example of the feature projections in text categorization. To simplify our description, we suppose that all documents have just two features ( $f_1$  and  $f_2$ ) and two categories ( $c_1$  and  $c_2$ ). The TF-IDF value by formula (2) is used as the weight of a feature. Each document is normalized as a unit vector and each category has three instances:  $c_1 = \{d_1, d_2, d_3\}$  and  $c_2 = \{d_4, d_5, d_6\}$ . Figure 1 shows how document vectors in conventional vector space are transformed into feature projections and stored on each feature dimension. The result of feature projections on a term (or feature) can be seen as a set of weights of documents for the term. Since a term with 0.0 weight is useless, the size of the set equals to the DF value of the term.

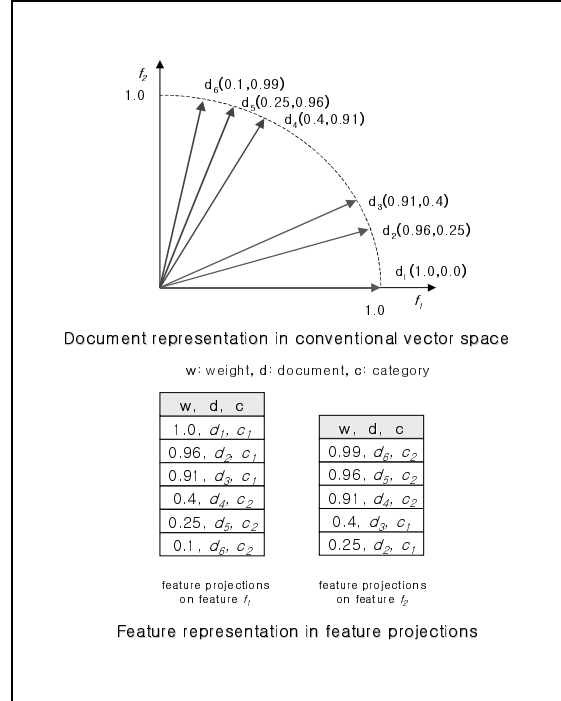


Figure 1. Feature representation on feature projections

### 2.2 Problems in Applying Feature Projections to Text Categorization

There are three problems: (1) the diversity of the Document Frequency (DF) values of terms, (2) the property of using TF-IDF value of a term as the weight of the feature, and (3) the lack of contextual information.

#### 2.2.1 The diversity of the Document Frequency values of terms

Table 1 shows a distribution of the DF values of the terms in **NewsGroup** data set. The numerical values of Table 1 are calculated from training data set with 16,000 documents and 10,000 features chosen by feature selection. The  $k$  in fourth column means the number of nearest neighbors selected in  $k$ -NNFP; the  $k$  in  $k$ -NNFP was set to 20 in our experiments.

Table 1. A distribution of the DF values of the terms in NewsGroup data set

Average DF	maximum DF	Minimum DF	The # of features DF < $k$ (20)
54.59	8,407	4	6,489

According to Table 1, more than a half of the features have the DF values less than  $k$  (20). This result is also explained by Zipf's law. The problem is that some features have the DF values less than  $k$  while other features have the DF values much greater than  $k$ . For a feature that has a DF value less than  $k$ , all the elements of the feature projections on the feature could and should participate for voting. In this case, the number of elements chosen for voting is less than  $k$ . For other features, only maximum  $k$  elements among the elements of the feature projections should be chosen for voting. Therefore, we need to normalize the voting ratio for each feature. As shown in formula (5), we use a proportional voting method to normalize the voting ratio.

### 2.2.2 The property of using TF-IDF value of a term as weight of a feature

The TF-IDF value of a term is their presumed value for identifying the content of a document (Salton et al., 1983). On feature projections, elements with a high TF-IDF value for a feature become more useful classification criterions for the feature than any elements with low TF-IDF values. Thus we use only elements with TF-IDF values above the average TF-IDF value for voting. The selected elements also participate for proportional voting with the same importance as TF-IDF value of each element. The voting ratio of each category  $c_j$  in a feature  $t_m(i)$  of a test document  $\vec{d}_i$  is calculated by the following formula:

$$r(c_j, t_m(i)) = \frac{\sum_{t_m(l) \in I_m} w(t_m, \vec{d}_l) \cdot y(c_j, t_m(l))}{\sum_{t_m(l) \in I_m} w(t_m, \vec{d}_l)} \quad (5)$$

In above formula,  $I_m$  denotes a set of elements selected for voting and  $y(c_j, t_m(l)) \in \{0,1\}$  is a function; if the category for a element  $t_m(l)$  is equal to  $c_j$ , the output value is 1. Otherwise, the output value is 0.

### 2.2.3 The lack of contextual information

Since each feature votes separately on feature projections, contextual information is missed. We use the idea of co-occurrence frequency for applying contextual information to our

algorithm.

To calculate a co-occurrence frequency value between two terms  $t_i$  and  $t_j$ , we count the number of documents that include both terms. It is separately calculated in each category of training data. Finally, the co-occurrence frequency value of two terms is obtained by a maximum value among co-occurrence frequency values in each category as follows:

$$co(t_i, t_j) = \max_{c_j} \{co(t_i, t_j, c_j)\} \quad (6)$$

where  $co(t_i, t_j)$  denotes a co-occurrence frequency value of  $t_i$  and  $t_j$ , and  $co(t_i, t_j, c_j)$  denotes a co-occurrence frequency value of  $t_i$  and  $t_j$  in a category  $c_j$ .

TF-IDF values of two terms  $t_i$  and  $t_j$ , which occur in a test document  $d$ , are modified by reflecting the co-occurrence frequency value. That is, the terms with a high co-occurrence frequency value and a low category frequency value could have higher term weights as follows:

$$tw(t_i, \vec{d}) = w(t_i, \vec{d}) \cdot \left( 1 + \left( \frac{1}{1 + \log(cf)} \right) \cdot \left( \frac{1 + \log(co(t_i, t_j))}{1 + \log(\max co(t_i, t_j))} \right) \right) \quad (7)$$

where i)  $tw(t_i, d)$  denotes a modified term weight assigned to term  $t_i$ , ii)  $cf$  denotes the category frequency, the number of categories in which  $t_i$  and  $t_j$  co-occur, and iii)  $\max co(t_i, t_j)$  is the maximum value among all co-occurrence frequency values.

Finally, in order to apply these improvements (formulae (5) and (7)) to our algorithm, we calculate the voting score of each category  $c_j$  in  $t_m$  of a test document  $\vec{d}_i$  as the following formula:

$$s(c_j, t_m(i)) = tw(t_m, \vec{d}_i) \cdot r(c_j, t_m(i)) \quad (8)$$

Here, since the modified TF-IDF value of a feature in a test document has to be also considered as an important factor, it is used for voting score instead of the simple voting value (1).

### 2.3 A New Text Categorization Algorithm using Feature Projections

A new text categorization algorithm using feature projections, named **TCFP**, is described in the following:

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test document:  $\vec{d} = \langle t_1, t_2, \dots, t_n \rangle$ , category set:
 $C = \{c_1, c_2, \dots, c_m\}$ 

begin
  for each category  $c_j$ 
    vote[ $c_j$ ] = 0
  for each feature  $t_i$ 
     $tw(t_i, d)$  is calculated by formula (7)

  /* majority voting */
  for each feature  $t_i$ 
    for each category  $c_j$ 
      vote[ $c_j$ ] = vote[ $c_j$ ] +  $tw(t_i, d) \times r(c_j, t_i)$ 
      by formula (8)

  for each category  $c_j$ 
    prediction =  $\arg \max_{c_j} vote[c_j]$ 

  return prediction
end

```

In training phase, our algorithm needs only a very simple process; the training documents are projected on their each feature and numerical values for the proportional voting (formula (5)) are calculated.

## 3. Empirical Evaluation

### 3.1 Data Sets and Experimental Settings

To test our proposed approach, we used two different data sets. For fair evaluation, we used the five-fold cross-validation method. Therefore, all results of our experiments are averages of five runs.

The **Newsgroups** data set, collected by Ken Lang, contains about 20,000 articles evenly divided among 20 UseNet discussion groups (McCalum et al., 1998). After removing words that occur only once or on a stop word list, the average vocabulary from five training data has 51,325 words (with no stemming). The second data set comes from the **WebKB** project at CMU (Yang et al., 2002). We use the four most populous entity-representing categories: **course**,

**faculty**, **project**, and **student**. The resulting data set consists of 4,198 pages with a vocabulary of 18,742 words. It is an uneven data set; the largest category has 1,641 pages and the smallest one has 503 pages.

We applied statistical feature selection at a preprocessing stage for each classifier, using a  $\chi^2$  statistics (Yang et al., 1997).

To compare TCFP to other algorithms for speeding classification, we implemented  $k$ -NNFP and  $k$ -NN with reduction. We used *DROP4* as reduction technique (Wilson et al., 1999). By *DROP4*, only 26% of the original training documents in both data sets was retained. The  $k$  in  $k$ -NNFP was set to 20 and the  $k$  in  $k$ -NN with reduction was set to 30. In addition, we implement other classifiers: Naive Bayes,  $k$ -NN, and Rocchio classifier. The  $k$  in  $k$ -NN was set to 30 and  $\alpha=16$  and  $\beta=4$  were used in Rocchio classifier.

As performance measures, we followed the standard definition of recall, precision, and  $F_1$  measure. For evaluating performance average across categories, we used the micro-averaging method.

### 3.2 Experimental Results

#### 3.2.1 Comparison of TCFP and $k$ -NN (and other algorithms for speeding classification)

Figure 2 and Table 2 show results from TCFP,  $k$ -NN,  $k$ -NN with reduction, and  $k$ -NNFP. In addition, we added other type of TCFP to our experiment. It was TCFP without contextual information (not using formula (7)).

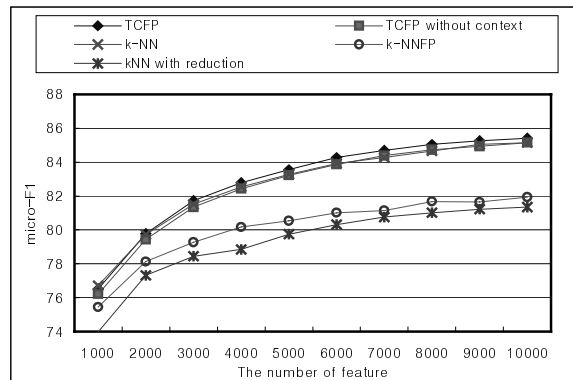


Figure 2. Comparison of TCFP,  $k$ -NN,  $k$ -NNFP, and  $k$ -NN with reduction

Table 2. The top micro-average  $F_1$  of each classifier

TCFP	TCFP without context	$k$ -NN	$k$ -NNFP	$k$ -NN with reduction
<b>85.41</b>	85.14	85.15	81.93	81.34

As a result, TCFP achieved the highest micro-average  $F_1$  score. Also, TCFP without contextual information presented the nearly same performance as  $k$ -NN. Although, over all vocabulary sizes, TCFP without contextual information achieved little lower performance than TCFP, it also can be useful classifier for its simplicity and the fast running time(see Table 5).

### 3.2.2 Comparison with other classifiers

The comparisons with other classifiers are shown in Figure 3 and Table 3. In this experiment, we used Naïve Bayes, and Rocchio classifier.

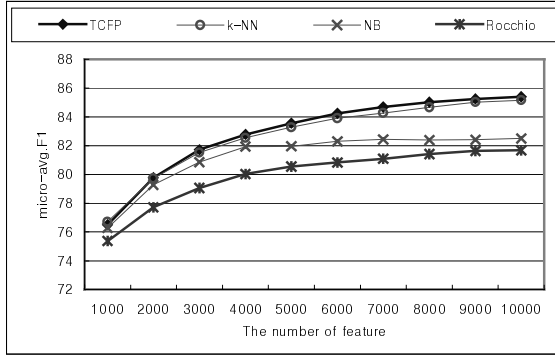


Figure 3. Comparison with other classifiers

Table 3. The top micro-average  $F_1$  of each classifier

TCFP	$k$ -NN	NB	Rocchio
<b>85.41</b>	85.15	82.51	81.68

The result shows that TCFP produced the higher performance than the other classifiers.

### 3.2.3 Comparison of performances in an uneven data set, WebKB.

In the above experiments, the **NewsGroup** data set, which is an evenly divided data set, was used. If we use an uneven data set, we can face a problem. The cause of the problem is that a category of the larger size has more voting candidates than a category of the smaller size.

We simply modified the majority voting score calculated in TCFP algorithm by the following formula:

$$vote[c_j] = vote[c_j] \cdot \left( \frac{\max\{num(d, c_i)\}}{num(d, c_j)} \right) \quad (9)$$

where  $num(d, c_j)$  denotes the number of training document in category  $c_j$ .

The results of the modified algorithm are shown in Table 4. As we can see in this table, the modified TCFP algorithm performed similarly on the uneven data set, **WebKB**; the modified **TCFP** algorithm achieved the highest score.

Table 4. The top micro-average  $F_1$  of each classifier

TCFP	$k$ -NN	NB	Rocchio	$k$ -NNFP	$k$ -NN with reduction
<b>86.6</b>	84.83	85.22	85.98	82.78	81.34

### 3.2.4 Run-time observation

Table 5 shows the average running times in CPU seconds for each classifier on the **NewsGroup** data. Note that we included only testing phase with 4,000 documents.

Table 5. Average running time of each classifier

TCFP without context	Rocchio	NB	TCFP	$k$ -NN with reduction	$k$ -NN
<b>0.69</b>	0.8	1.22	<b>1.38</b>	37.97	142.5

Since the computations depend on the vocabulary sizes, we calculated the above numerical value by averaging running times from 1,000 to 10,000 terms. In Table 5, the running time of TCFP is similar to other faster classifiers: Rocchio and Naïve Bayes. Also it is about one hundred times faster than that of  $k$ -NN. Note that TCFP without contextual information is the fastest classifier.

## 4. Discussions

First of all, time complexities between  $k$ -NN and TCFP are compared. Using the inverted-file indexing of training documents, the time complexity of  $k$ -NN is  $O(m^2ln)$  (Yang, 1994), where  $m$  is the number of unique words in the document,  $l$  is the number of training documents,

and  $n$  is the number of unique terms in the training collection. TCFP has the time complexity of  $O(m^2)$ . Even more, the time complexity of TCFP without contextual information is  $O(mc)$ , where  $c$  is the number of categories. That is, the classification of TCFP requires a simple calculation in proportion to the number of unique terms in the test document. On the other hand, in  $k$ -NN, a search in the whole training space must be done for each test document.

The other strong points of TCFP are the simplicity of algorithm and high-performance. Since the algorithm of TCFP is very simple like  $k$ -NN, TCFP can be implemented quite easily and its training phase can also be a simple process. In our experiments, we achieved the better performance than  $k$ -NN. We analyze that our algorithm is more robust from irrelevant features than  $k$ -NN. When a document contains irrelevant features, the angle of the document vector is changed in  $k$ -NN. In TCFP, however, the irrelevant features contribute to only voting of the features. Hence TCFP decreases the bad effect of the irrelevant features.

## Conclusions

In this paper, a new type of text categorization, TCFP, has been presented. This algorithm has been compared with  $k$ -NN and other classifiers. Since each feature in TCFP individually contributes to the classification process, TCFP is robust from irrelevant features. By the simplicity of TCFP algorithm, its implementation and training process can be done very easily. The experimental results show that, on the performance, TCFP is superior to Rocchio, Naïve Bayes, and  $k$ -NN. Moreover, it outperforms other classifiers for speeding classification such as  $k$ -NNFP and  $k$ -NN with reduction. In running time observation, TCFP is about one hundred times faster than  $k$ -NN. Therefore, we can use TCFP in the areas, which require a fast and high-performance text classifier.

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