# On Knowledge Distillation from Complex Networks for Response Prediction

Siddhartha Arora<sup>1,2</sup> and Mitesh M. Khapra<sup>1,2</sup> and Harish G. Ramaswamy<sup>1,2</sup>

<sup>1</sup>Department of Computer Science and Engineering, Indian Institute of Technology Madras

<sup>2</sup>Robert Bosch Centre for Data Science and AI (RBC-DSAI),

Indian Institute of Technology Madras

{sidarora,miteshk,hariguru}@cse.iitm.ac.in

# Abstract

Recent advances in Question Answering have lead to the development of very complex models which compute rich representations for query and documents by capturing all pairwise interactions between query and document words. This makes these models expensive in space and time, and in practice one has to restrict the length of the documents that can be fed to these models. Such models have also been recently employed for the task of predicting dialog responses from available background documents (e.g., Holl-E dataset). However, here the documents are longer, thereby rendering these complex models infeasible except in select restricted settings. In order to overcome this, we use standard simple models which do not capture all pairwise interactions, but learn to emulate certain characteristics of a complex teacher network. Specifically, we first investigate the conicity of representations learned by a complex model and observe that it is significantly lower than that of simpler models. Based on this insight, we modify the simple architecture to mimic this characteristic. We go further by using knowledge distillation approaches, where the simple model acts as a student and learns to match the output from the complex teacher network. We experiment with the Holl-E dialog data set and show that by mimicking characteristics and matching outputs from a teacher, even a simple network can give improved performance.

# 1 Introduction

The advent of large scale datasets for QA has lead to the development of increasing complex neural models with specialized components for (i) encoding the query (ii) encoding the document(s) (iii) capturing interactions between document and query words and (iv) generating/extracting the correct answer span from the given document (Seo et al., 2016; Hu et al., 2017; Yu et al., 2018). While these models give state-of-the-art performance on a variety of datasets, they have very high space and time complexity. This is a concern, and in practice, it is often the case that one has to resort to restricting the maximum length of the input document such that the model can run with reasonable resources (say, a single 12GB Tesla K80 GPU).

Such complex span prediction models are also being adapted for other NLP tasks such as dialog response prediction (Moghe et al., 2018), which is the focus of this work. In particular, we refer to the Holl-E dataset where the task is to extract the next response from a document which is relevant to the conversation (see Figure 1). This setup is very similar to QA wherein the input is {context, document} as opposed to {query, document} and the correct response span needs to be extracted from the given document. Given this similarity, it is natural to adopt existing QA models (Seo et al., 2016; Yu et al., 2018) for this task. However, the documents in Holl-E dataset are longer, and the authors specifically report that they were unable to run these models when the entire document was given as input. Hence, they report results only in constrained oracle settings where the document is trimmed such that the response still lies in the shortened document. The above situation suggests that there is clearly a trade-off needed. On one hand, we want to harness the power of these complex models to achieve better performance and on the other hand we want to be able to run them with reasonable compute resources without arbitrarily trimming the input document.

This trade-off situation naturally leads to the following question: *Is it possible to build a simple model, with low memory and compute requirements, that copy desirable characteristics from complex models?* To answer this, we start with a relatively simple model with very basic components for encoding query, document and capturing interactions. Once these interactions are cap-

**Source Doc:** ...comes in. As soon as the door is open, the Bride's fist crashes into Vernita's face. A savage fight follows, first with fists, then with knives.... The fight pauses ... At this point Vernita is introduced as a member of the Deadly Vipers, codename Copperhead. ...

Sample Conversation:
Prober (S1): Which is your favourite character in this?
Responder (S2): My favorite character was Copperhead because she was kicking butt.
Prober (S3): Oh my goodness I agree, because the fight with Vernita was the best in the whole movie.
Responder (S4): It's starts off action packed because as soon as the door is open, the Bride's fist crashes into Vernita's face. A savage fight follows, first with fists, then with knives.
Prober (S5): And it gets better when we find out they are both assassins.
Responder (S6): And a group of them, Vernita is introduced as a member of the Deadly Vipers, codename Copperhead.

Figure 1: Sample Conversation from the Holl-E Dataset. Note that the underlined responses directly correspond to spans in the background document.

tured, the model computes a final representation which is then fed to a decoder to predict the correct span in the document. This recipe is very similar to BiDAF (Seo et al., 2016), QANeT (Yu et al., 2018) but the main difference is that these models use much more complex encoder and interaction components to arrive at the final representation. As expected, the performance of this model is poor when compared to BiDAF, QANeT. The aim now is to improve the performance of this model by carefully analysing or learning from complex models. Given that the complex model differs in the manner in which the final representation is computed, one hypothesis is that it learns richer final representations than the simple model. Indeed, on investigation, we found that the final representations learned by complex models are diverse for different inputs (context, document pairs) as compared to the simple model. Based on this insight, we propose a modification to the simple model which increases the diversity of the embeddings, thereby improving the performance.

While this insight obtained by manual investigation is useful, there is clearly scope for learning by exploring other characteristics of the model. One principled way of doing this is to use knowledge distillation (Hinton et al., 2015) where the simple model acts as a student and learns to mimic the probability distributions predicted by a teacher. In other words, instead of simply maximizing the log likelihood of the training data, the simple model now gets additional signals from the teacher which act as hints while training.

Our experiments, using the *Holl-E* dataset show that by (i) improving the conicity (Chandrahas et al., 2018) of the representations learned by the simple model and (ii) mimicking the outputs of the complex teacher model the simple model can give improved performance with fewer compute and memory requirements. In particular, when compared to a standalone simple model the student model shows an improvement of 3.4% (compare SAM-mul-train (LD) and SAM-add-topk (LD) entries in Table 2 and Table 3 respectively).

## 2 Related Work

Over the past few years neural sequence prediction models which take a question as input and predict the corresponding answer span in a given document have evolved rapidly. Such models have also been adapted for dialog response prediction in the context of the *Holl-E* dataset (Moghe et al., 2018). These models typically differ in the components used for capturing interactions between query and document, capturing interactions between sentences in a document and refining the query/document representation over multiple passes (Shen et al., 2017; Dhingra et al., 2017; Sordoni et al., 2016).

In particular, a co-attention network which computes the importance of every query word w.r.t. every document word and the importance of every document word w.r.t. every query word is an important component in most state of the art models (Hermann et al., 2015; Kadlec et al., 2016; Cao et al., 2016; Xiong et al., 2016; Seo et al., 2016; Gong and Bowman, 2017; Dhingra et al., 2017; Wang et al., 2017; Shen et al., 2017; Trischler et al., 2016; Group and Asia, 2017; Tan et al., 2017; Sordoni et al., 2016). Similarly, some models (Group and Asia, 2017; Seo et al., 2016; Hu et al., 2017) contain a self-attention network which computes the importance of every document word w.r.t. every other document word. In general, the most successful models (for example, BiDAF (Seo et al., 2016), QANeT (Yu et al., 2018)) use a combination of these components which capture all pairwise interactions and are thus computationally very expensive. As a result, in practice, these models are not suitable for longer documents.

We now quickly review existing works which use the idea of knowledge distillation to build compact models (Cheng et al., 2017). For example, Ba and Caruana (2014); Hinton et al. (2015); Lopez-Paz et al. (2016); Chen et al. (2017) train a shallow student network using soft targets (or class probabilities) generated by an expensive teacher instead of the hard targets present in the training data. Romero et al. (2015) extend this idea to train a student model using the intermediate representations learned by the teacher model which act as additional hints. This idea of Knowledge Distillation has also been tried in the context of pruning networks for multiple object detection (Chen et al., 2017), speech recognition (Wong and Gales, 2016). In the context of reading comprehension or span prediction, Hu et al. (2018) have very recently shown that we can distill knowledge from an ensemble of models into a single model. However, unlike our work, the single model itself is a complex model (Hu et al., 2017) containing an expensive self attention network and a RL agent. To the best of our knowledge, ours is the first work which tries to build a simple span prediction model by distilling knowledge from a complex model.

#### 3 Models For Response Prediction

We view a conversation as sequence of utterances by a *prober* and a *responder*. The response prediction (RP) model aims to predict the utterance by the responder based on a source document, when given the query (prober's most recent utterance) and the history (past utterance by the prober and responder). See Figure 1 for an example.

We denote the lengths of source document, query, prober history and responder history as T, I, J, K. The LSTMs/GRUs used all have the same number of cells, denoted by d. In particular, the document length T is of the order of a few thousands and the query/history lengths I, J, Kare of the order of a few hundreds. Contrast this with QA tasks, where T is only of the order of a few hundreds, and the query length (I + J + K) is of the order of a few tens.

## 3.1 BiDAF for RP

BiDAF (Seo et al., 2016) is an extremely popular model used for span prediction in reading comprehension based question answering problems. We can frame the problem of response prediction as one of question answering by concatenating the query, prober history, and responder history into a single "question". BiDAF has proven to be hugely successful in QA tasks, but has a large number of parameters (about 2.5 million) and consumes a large amount of computational space and time during training and prediction.

We use the BiDAF model as a guiding post while constructing our model, and in particular focus on the so called *query to context attention*, which is a vector (denoted by  $\tilde{\mathbf{h}}$ ) that indicates the weighted sum of the most important words in the source document, with respect to the query and histories.

#### 3.2 QANeT for RP

QANeT (Yu et al., 2018) is another recent model used for span prediction in QA tasks and specifically targets better space and time efficiency than BiDAF. Despite this, it still has a large number of parameters (about 1.3 million) and still consumes a large amount of computational space and time during training and prediction. The QANeT model can also be modified for response prediction in a similar manner to BiDAF.

#### 3.3 Simple Attention Model for RP

We now describe the simple attention model that we aim to learn. In a fashion similar to that of BiDAF and QANeT architectures, the simple model also operates in 3 distinct layers. See Figure 2 for an overview into the model.

# 3.3.1 Word Embedding Layer

The words from the source document, the utterances by the prober and the responder are all encoded using standard GloVe embeddings (Pennington et al., 2014).

#### 3.3.2 Contextual Embedding Layer

In the next layer we encode the query (prober's most recent utterance) using a BiGRU/BiLSTM, and encode the previous utterances of the prober and responder in a query sensitive manner.

**Query Encoder:** Embedded query words are passed through BiGRU where final state  $q_I \in \mathbb{R}^{2d}$  acts as query representation.

Query Sensitive History Summariser: The history of the prober and responder are passed through a BiGRU to get context sensitive vectors  $\mathbf{h}_{j}^{\mathrm{P}} \in \mathbb{R}^{2d}$  and  $\mathbf{h}_{k}^{\mathrm{R}} \in \mathbb{R}^{2d}$  for  $j \in [J]$  and  $k \in [K]$ .

These vectors are combined to get vectors  $\mathbf{h}^{P}$ and  $\mathbf{h}^{R}$ . This process of combining uses the query representation  $\mathbf{q}_{I}$ , and hence  $\mathbf{h}^{P}$  and  $\mathbf{h}^{R}$  can



Figure 2: A Simple Attention Model with (1) Query Encoder, Prober History Encoder, Responder History Encoder, and Document Encoder (2) Query to Prober History Attention, Query to Responder History Attention, and Query & histories to Document Attention (3) Training Labels and Teacher Distribution.

be viewed as query-aware representations of the prober and responder history. The equations for  $\mathbf{h}^{P}$  are given below. The vector  $\mathbf{h}^{R}$  is also calculated in a similar manner.

$$e_j = \operatorname{mul}^{W^{\mathsf{P}}}(\mathbf{h}_j^{\mathsf{P}}, \mathbf{q}_I)$$
$$\boldsymbol{\alpha} = \operatorname{softmax}(\mathbf{e})$$
$$\mathbf{h}^{\mathsf{P}} = \sum_j \alpha_j \mathbf{h}_j^{\mathsf{P}}$$

where  $\operatorname{mul}^{W}(\mathbf{v}_{0}, \mathbf{v}_{1}) = \mathbf{v}_{0}^{\top} W \mathbf{v}_{1}$  is a parameterized multiplicative way of capturing the interaction between two vectors.

### 3.3.3 Span Prediction Layer

The source document is finally used in this layer to predict the start and end indices of the response. The GloVe embedded words of the source document are passed through a BiGRU to get context sensitive vectors  $\mathbf{u}_t \in \mathbb{R}^{2d}$ , for all  $t \in [T]$ . Each index t gets a score  $s_t$  based on the interaction between  $\mathbf{u}_t$  and the query/history vectors  $\mathbf{q}_I$ ,  $\mathbf{h}^P$ ,  $\mathbf{h}^R$ . The scores  $s_t$  are normalized by a softmax and is taken to be the prediction of the starting word index.

$$s_t = ext{mul}^{W^{ ext{strt}}}(\mathbf{u}_t, \mathbf{q}_I, \mathbf{h}^{\mathsf{P}}, \mathbf{h}^{\mathsf{R}})$$
  
 $\boldsymbol{\alpha} = ext{softmax}(\mathbf{s})$ 

where  $\operatorname{mul}^{W}(\mathbf{u}_{0}, \ldots, \mathbf{u}_{a}) = \mathbf{u}_{0}^{\top} \left( \sum_{i=1}^{a} W^{i} \mathbf{u}_{i} \right)$ A similar method is used for the prediction of the ending word index as well.

# 4 Bridging The Gap Between Simple and Complex Models

We performed several experiments on the Holl-E dataset and observed that the complex models (QANeT and BiDAF) perform better than the simple attention model described in Section 3.3. However, they take significantly more time and memory for training and inference. In fact, for the examples with longer source documents, both BiDAF and QANeT run into memory issues when training. During prediction, the memory issues in QANeT and BiDAF can be sidestepped by breaking the source document into multiple chunks and taking the highest scoring span.

In the rest of this section we study several approaches to nudge the simple attention model to take parameters that make it have similar behaviour as the complex models, and check if the so nudged model demonstrates better performance on the Holl-E dataset.

## 4.1 Diversity of Embeddings

We observed that for the simple attention model, the response predictions at different points in the



Figure 3: Conicity (*i.e.*, average cosine similarity of vectors with the mean of all the vectors) of two sets of vectors with standard deviation 0.1 (red) and 1.3 (blue)

same conversation are often the same, even though the "right response" is different in those points. For example, consider the conversation in Figure 1. We expect the trained model to be such that

$$\operatorname{Pred}_{\operatorname{span}}(SD, S_1, S_2, S_3) = \operatorname{span}_{SD}(S_4)$$

where SD is the source document, and  $S_i$  are the the utterances in the conversation. Similarly, we expect the trained model to be such that

 $\operatorname{Pred}_\operatorname{span}(SD, S_3, S_4, S_5) = \operatorname{span}_{SD}(S_6)$ 

However we often find that our simple model predicts the same span for both the cases above, which is wrong (unless  $S_4$  and  $S_6$  are the same.)

We hypothesize this as being due to the context sensitive embeddings of the history not depending strongly on the query, and hence the span prediction model picks up most information from the source document. To support this point of view we measured the diversity of the context-to-query vectors h of the BiDAF model for several examples grouped by conversation. In more detail we computed the conicity (Chandrahas et al., 2018) of vectors  $\mathbf{h}(SD, S_1, S_2, S_3), \mathbf{h}(SD, S_3, S_4, S_5), \dots$ for every conversation in the test set and averaged it over all conversations. (See Figure 3 for an overview on conicity). This average conicity was observed to be about 0.6 (see Table 6), which, according to Chandrahas et al. (2018), is low (low conicity implies high diversity).

We observe similar behaviour for QANeT as well. The average conicity of the row sums of the *similarity matrix* grouped by conversation was also observed to be about 0.6 (see Table 6).

On the other hand, for our simple attention model, the average conicity of the vectors  $\mathbf{h}^{R}$  and  $\mathbf{h}^{P}$ , when computed in a similar fashion as mentioned above were generally high (about 0.8) (see Table 6).

Based on these observations we hypothesize that decreasing the conicity of the vectors  $\mathbf{h}^{R}$  and  $\mathbf{h}^{P}$  would improve the performance of the simple attention model. In particular, we propose to change the multiplicative method of combining vectors into an additive method instead.

In particular we propose to replace the function mul in our simple model with the function add defined as follows:

$$\operatorname{add}^{W}(\mathbf{v}_{0},\mathbf{v}_{1},\ldots,\mathbf{v}_{a}) = \mathbf{w}^{\top} \tanh\left(\sum_{i=0}^{a} W^{i} \mathbf{v}_{i}\right)$$

where the vector  $\mathbf{w}$  and the matrices  $W^i$  parameterize the mode of combining the input vectors. This is motivated by Chandrahas et al. (2018) who show that using additive model in embedding of entities in knowledge graphs gives consistently better diversity than using multiplicative models.

## 4.2 Standard Knowledge Distillation from Complex Models

While borrowing high level ideas from complex models, like increasing diversity of the learned representation can help to some extent, one can push this further to distill the learned complex model (Hinton et al., 2015) into the simple attention model. To achieve this, we train a teacher model (BiDAF or QANeT) on the training set and use it to make predictions on the same training set. The simple attention model would minimise the sum of two loss functions: 1) Cross entropy loss of the predicted start and end indices with the train labels of the start and end indices, 2) KL-divergence of the predicted start and end indices from the teacher prediction of the same. The loss on a single training sample is given below

$$D(\mathbf{p}_{b}^{T}||\mathbf{p}_{b}^{S}) + D(\mathbf{y}_{b}||\mathbf{p}_{b}^{S}) + D(\mathbf{p}_{e}^{T}||\mathbf{p}_{e}^{S}) + D(\mathbf{y}_{e}||\mathbf{p}_{e}^{S})$$
(1)

where D denotes the KL divergence,  $\mathbf{p}_b^T, \mathbf{p}_e^T$  denote the predicted begin index and end index distribution of the teacher model, and  $\mathbf{p}_b^S, \mathbf{p}_e^S$  denote the predicted begin and end index distribution of the student model and  $\mathbf{y}_b, \mathbf{y}_S$  denote the true begin and end index in one-hot vector form.

#### **4.3** Top-*k* Based Knowledge Distillation

Another variant of knowledge distillation is as follows. We do not view the teacher predicted distribution for all indices with importance and just take the top few predicted indices. In particular the loss on a single training sample is given below

$$D(\widetilde{\mathbf{p}}_{b}^{T}||\widetilde{\mathbf{p}}_{b}^{S}) + D(\mathbf{y}_{b}||\mathbf{p}_{b}^{S}) + D(\widetilde{\mathbf{p}}_{e}^{T}||\widetilde{\mathbf{p}}_{e}^{S}) + D(\mathbf{y}_{e}||\mathbf{p}_{e}^{S})$$
(2)

where  $\widetilde{\mathbf{p}}_{b}^{T}, \widetilde{\mathbf{p}}_{e}^{T}$  gives just the (normalised) probability of the top-k predictions of teacher model on the begin and end indices. Similarly  $\widetilde{\mathbf{p}}_{b}^{S}, \widetilde{\mathbf{p}}_{e}^{S}$  gives the student predictions for the begin and end indices restricted to the top-k entries given by the teacher model.

## 4.4 Other Knowledge Distillation Approaches

As the teacher model is already trained, and the main objective in knowledge distillation is to have the student model mimic the teacher model, there is no need to restrict the objective terms 1 and 3 in equation 1 to only the training data. Hence by hallucinating conversations and documents we can get more terms in the objective and has an effect similar to data augmentation.

Another possible way to take advantage of teacher models is to extract more information than simply the predicted spans for each training example from the teacher models. In particular one easy way to extract piece of information is the gradient of the model output with respect to the input for the teacher model. The so called Sobolev training (Czarnecki et al., 2017) exploits this information and adds two more extra terms to the objective in (1).

$$||\nabla \mathbf{p}_b^T - \nabla \mathbf{p}_b^S||^2 + ||\nabla \mathbf{p}_e^T - \nabla \mathbf{p}_e^S||^2$$

The gradients are all taken with respect to the model input, which would be the source document, the query and the histories.

### 5 Experiments

In this section, we describe the setup used for our experiments and discuss the results.

#### 5.1 Experiment Setup

We perform experiments using the Holl-E conversation dataset (Moghe et al., 2018) which contains crowdsourced conversations from the movie domain. Every conversation in this dataset is associated with background knowledge comprising of plot details (from Wikipedia), reviews and comments (from Reddit). Every alternate utterance in the conversation is generated by copying and/or modifying sentences from this unstructured background knowledge. We refer the reader again to Figure 1 for a sample from this dataset.

We use the same train, test and validation splits as provided by the authors of the original paper (Moghe et al., 2018). For each chat in the training data, the authors construct training triplets of the form {document, context, response} where the number of train, test and validations triplets are 34486, 4388 and 4318 respectively. The context contains (i) the query (the prober's most recent utterance) and (ii) the history (past 2 utterances by the prober and the responder) as described earlier. The task then is to train a model which can predict the response given the document and the context. At test time, the model is shown document, context and predicts the response.

As mentioned earlier, the authors of Holl-E found that BiDAF and QANeT run into memory issues when evaluated on their dataset. Hence, they propose two setups (i) long document (LD) setup and (ii) short document (SD) setup. In the long document setup, the authors do not trim the document from which the response needs to be predicted. In the short document setup, the authors trim the document to 256 words such that the span containing the response is contained in the trimmed document. This enables them to evaluate BiDAF and QANeT on the trimmed document. We also report experiments using both the LD and SD setup.

As mentioned above complex models (BiDAF and QANeT) face memory issues on training set with long documents. So for all situations where we need predictions from complex models for long documents, we use a BiDAF/QANeT model trained on short document examples, and the prediction on the long document is made by splitting the long documents into chunks and feeding it to the trained BiDAF/QANeT model. The final predicted span is the largest scoring span across all chunks.

For all models, we considered the following hyperparameters and tuned them using the validation set. We tried batch sizes of 32 and 64 and the following GRU sizes: 64, 100, 128. We experimented with 1, 2 and 3 layers of GRU. We used pre-trained publicly available Glove word embeddings  $^1$  of 100 dimensions. The best performance

https://nlp.stanford.edu/projects/
glove/

	SAM, SD	SAM, LD	BiDAF, SD	BiDAF, LD	QANeT, SD	QANeT, LD
Memory	540MB	1.3GB	11GB	11GB	3GB	3GB
Time	30 secs	43 sec	347 secs	710 secs	90 secs	150 secs

Table 1: 'Inference' Memory and Time usage for different models. Here SAM, SD and LD refers to Simple Attention Model, short document and long document respectively.

Model	LD	SD
SAM-mul-train	36.49	40.08
SAM-add-train	36.96	41.30
BiDAF	38.30*	45.54
QANeT	38.10*	47.67

Table 2: Performance (F1 Scores) of different baseline models on SD (short document) and LD (long document) test set.

was with the batch size of 32, 2 layers of GRU with hidden size 64. We used Adam (Kingma and Ba, 2014) optimizer with initial learning rate set to 0.001,  $\beta_1 = 0.9$ ,  $\beta_2 = 0.999$ . We performed L2 weight decay with decay rate set to 0.001.

## 5.2 Model Variant Details

The models that we experiment with are listed below:

1. **SAM-add-Train** : The simple attention model with additive interactions and no teacher terms in the objective (Only terms 2 and 4 in Eqn. (1)).

2. **SAM-add-Teach** : The simple attention model with additive interactions and only knowledge distillation terms in the objective (Only terms 1 and 3 in Eqn. (1)).

3. **SAM-add** : The simple attention model with additive interactions and both knowledge distillation terms and training data terms in the objective (all terms in 1).

4. **SAM-add-topk** : The simple attention model with additive interactions and knowledge distillation applied to the top-k indices and training data terms in the objective (all terms in 2).

5. **SAM-add-aug** : The SAM-add model, where the teacher terms are evaluated on hallucinated data in addition to training data. The hallucinated data are derived from the original training set by reordering the words in the source document, query and histories.

6. **SAM-add-grad** : The SAM-add model, with extra terms in the loss penalising the deviation of the gradient of the simple model from the gradient

Model Details	BiDAF	QANeT
SAM-mul	36.50	37.03
SAM-add	37.14	37.28
SAM-add-topk	37.29	37.73
SAM-add-aug	37.17	37.01
SAM-add-ensemble	37.30	
SAM-add-both	36.80	

Table 3: F1 Scores for different variants of simpleattention model on long documents test set.

of the teacher model.

7. **SAM-add-both** : Same as the SAM-add model, but has 6 terms instead of the 4 terms in Equation 1. The extra two terms arise from using **both** QANeT and BiDAF instead of just one.

8. **SAM-add-ensemble** : Same as the SAM-add model, but the teacher predictions  $\mathbf{p}^{T}$  are set as the average of the QANeT and BiDAF predictions.

All the "add" models above also have a "mul" variant where the additive interaction add is replaced by a multiplicative interaction mul.

### 5.3 Results and Discussion

The F1-scores of the various models we train are given in Table 2, Table 3 and Table 4. A summary of the space and time complexity of prediction with the simple model and the complex models is given in Table 1. The training times and parameter counts of the models are given in Table 5 We draw several conclusions and inferences from these results and make some comments below.

**Efficient Training with Simple Model:** From Table 5, we observe that simple attention model has 5 to 10 times less parameters than QANeT and BiDAF. The training time of the simple model is also significantly lesser than that of the complex models.

**Efficient Prediction with Simple Model:** From Table 1, we observe that the simple model takes significantly less memory and time during prediction as well. The complex models run out of memory on the large document test set, but a prediction can still be made with a trained BiDAF or QANeT

Model Details	BiDAF	QANeT
SAM-add-teach	20.23	-
SAM-mul	40.81	40.76
SAM-add	42.05	41.89
SAM-add-topk	41.71	42.01
SAM-add-aug	41.65	41.62
SAM-add-ensemble	41.74	
SAM-add-both	42.32	
SAM-add-grad	41.37	41.72

Table 4: F1 Scores for different variants of simpleattention model on short document test set.

model by splitting the source document into manageable chunks.

**Conicity of Multiplicative models vs Additive Models:** As noted before we use two distinct methods to capture the interaction between a group of vectors : an additive mechanism add, and a multiplicative mechanism mul. As mentioned earlier, an additive model for capturing interactions has been hypothesized to increase diversity. This is true in our case as well: the conicity of the  $h^P$  and  $h^R$  vectors goes down from about 0.8 to 0.7 (compare SAM-mul and SAM-add entries in Table 6) when using the additive model instead of the multiplicative model.

**F1 scores of Multiplicative models vs Additive Models:** In addition to improving diversity, using the additive model add instead of the multiplicative model mul increases F1-scores all across the board. We have not reported scores for certain multiplicative variants because their performance is significantly worse.

**F1 scores of Simple Model with Knowledge Distillation:** We observe that using a teacher model for knowledge distillation using the objective in (1) almost always improves the performance of the simple model.

**Importance of training labels:** The objective in knowledge distillation (Equation (1)) involves both the training labels and the teacher predicted distribution. Even though the teacher predicted distribution also incorporates the training data, removing the training data term from the objective of knowledge distillation worsens performance significantly.

**Top-**k **Distillation:** The knowledge distillation approach based on top-k predicted indices results in the best simple model for long document exam-

	SAM	BiDAF	QANeT
Parameters	0.25 M	2.5 M	1.3 M
Train Time	307 secs	5880 secs	2213 secs

Table 5:Comparison of parameters (in Million) andtraining time (seconds) per epoch for different models.

Model	Conicity
Complex Models	0.6
SAM-mul	0.8
SAM-add	0.7

Table 6: Comparison of conicity between variants of simple-attention model and complex models.

ples (see Table 3). The value of k was chosen to be 50 for the short document case and it is 20 for the long document case.

Add-Both Knowledge Distillation: Learning from multiple teachers could lead to better performance hence we trained the student model with two teachers (BiDAF+QANeT). Here the objective function of student is to minimize KL Divergence between predictions for both teachers. We achieved best results with this technique on short document (SD) test set.

**Data Augmentation and Gradient Distillation:** While the data augmentation and gradient distillation methods hold a lot of promise, in the experiments that we conducted, we did not see a significant improvement.

**QANET Teachers vs BiDAF Teachers:** Using either QANET or BiDAF as a teacher doesn't seem to make any difference in the performance of the student models (compare the two columns in Table 3 and 4).

## 6 Conclusion

In this work, we address the trade-off between simple models on one hand which have low memory and compute requirements and complex models on the other hand which give better performance but are computationally expensive. We propose a middle ground by training a simple model to mimic the characteristics of a complex model. In particular, we make observations from a complex model which learns very diverse representations for different inputs and suitably modify the simple model to learn similar diverse representations. We go further, by using knowledge distillation techniques to improve the simple model by training it to match the outputs from the complex model. We experimented with the Holl-E conversation dataset and showed that by mimicking characteristics of the teacher a simple model can give improved performance.

#### Acknowledgements

We thank Department of Computer Science and Engineering, and Robert Bosch Center for Data Sciences and Artificial Intelligence, IIT Madras (RBC-DSAI) for providing us with adequate compute resources. Lastly, we thank Ananya Sai and Shweta Bhardwaj for valuable discussions and reviewing intial drafts of this paper.

#### References

- Jimmy Ba and Rich Caruana. 2014. Do deep nets really need to be deep? In *Advances in Neural Information Processing Systems 27*, pages 2654–2662.
- Ziqiang Cao, Wenjie Li, Sujian Li, Furu Wei, and Yanran Li. 2016. Attsum: Joint learning of focusing and summarization with neural attention. In *COLING*, pages 547–556. ACL.
- Chandrahas, Aditya Sharma, and Partha P. Talukdar. 2018. Towards understanding the geometry of knowledge graph embeddings. In *Proceedings of the 56th Annual Meeting of the Association for Computational Linguistics, ACL 2018, Melbourne, Australia, July 15-20, 2018, Volume 1: Long Papers,* pages 122–131.
- Guobin Chen, Wongun Choi, Xiang Yu, Tony Han, and Manmohan Chandraker. 2017. Learning efficient object detection models with knowledge distillation. In I. Guyon, U. V. Luxburg, S. Bengio, H. Wallach, R. Fergus, S. Vishwanathan, and R. Garnett, editors, *Advances in Neural Information Processing Systems* 30, pages 742–751. Curran Associates, Inc.
- Yu Cheng, Duo Wang, Pan Zhou, and Tao Zhang. 2017. A survey of model compression and acceleration for deep neural networks. *CoRR*, abs/1710.09282.
- Wojciech Marian Czarnecki, Simon Osindero, Max Jaderberg, Grzegorz Swirszcz, and Razvan Pascanu. 2017. Sobolev training for neural networks. *CoRR*, abs/1706.04859.
- Bhuwan Dhingra, Hanxiao Liu, Zhilin Yang, William W. Cohen, and Ruslan Salakhutdinov. 2017. Gated-attention readers for text comprehension. In Proceedings of the 55th Annual Meeting of the Association for Computational Linguistics, ACL 2017, Vancouver, Canada, July 30 - August 4, Volume 1: Long Papers, pages 1832–1846.
- Yichen Gong and Samuel R. Bowman. 2017. Ruminating reader: Reasoning with gated multi-hop attention. *CoRR*, abs/1704.07415.

- Natural Language Computing Group and Microsoft Research Asia. 2017. R-net: Machine reading comprehension with self-matching networks. *ACL*, abs/1606.02245.
- Karl Moritz Hermann, Tomás Kociský, Edward Grefenstette, Lasse Espeholt, Will Kay, Mustafa Suleyman, and Phil Blunsom. 2015. Teaching machines to read and comprehend. In Advances in Neural Information Processing Systems 28: Annual Conference on Neural Information Processing Systems 2015, December 7-12, 2015, Montreal, Quebec, Canada, pages 1693–1701.
- Geoffrey Hinton, Oriol Vinyals, and Jeffrey Dean. 2015. Distilling the knowledge in a neural network. In *NIPS Deep Learning and Representation Learning Workshop*.
- Minghao Hu, Yuxing Peng, and Xipeng Qiu. 2017. Mnemonic reader for machine comprehension. *CoRR*, abs/1705.02798.
- Minghao Hu, Yuxing Peng, Furu Wei, Zhen Huang, Dongsheng Li, Nan Yang, and Ming Zhou. 2018. Attention-guided answer distillation for machine reading comprehension. In *EMNLP*, pages 2077– 2086. Association for Computational Linguistics.
- Rudolf Kadlec, Martin Schmid, Ondrej Bajgar, and Jan Kleindienst. 2016. Text understanding with the attention sum reader network. In Proceedings of the 54th Annual Meeting of the Association for Computational Linguistics, ACL 2016, August 7-12, 2016, Berlin, Germany, Volume 1: Long Papers.
- Diederik P. Kingma and Jimmy Ba. 2014. Adam: A method for stochastic optimization. *CoRR*, abs/1412.6980.
- D. Lopez-Paz, B. Schölkopf, L. Bottou, and V. Vapnik. 2016. Unifying distillation and privileged information. In *International Conference on Learning Representations*.
- Nikita Moghe, Siddhartha Arora, Suman Banerjee, and Mitesh M. Khapra. 2018. Towards exploiting background knowledge for building conversation systems. In Proceedings of the 2018 Conference on Empirical Methods in Natural Language Processing, Brussels, Belgium, October 31 - November 4, 2018, pages 2322–2332.
- Jeffrey Pennington, Richard Socher, and Christopher D. Manning. 2014. Glove: Global vectors for word representation. In Proceedings of the 2014 Conference on Empirical Methods in Natural Language Processing, EMNLP 2014, October 25-29, 2014, Doha, Qatar, A meeting of SIGDAT, a Special Interest Group of the ACL, pages 1532–1543.
- Adriana Romero, Nicolas Ballas, Samira Ebrahimi Kahou, Antoine Chassang, Carlo Gatta, and Yoshua Bengio. 2015. Fitnets: Hints for thin deep nets. In *In Proceedings of ICLR*.

- Min Joon Seo, Aniruddha Kembhavi, Ali Farhadi, and Hannaneh Hajishirzi. 2016. Bidirectional attention flow for machine comprehension. *CoRR*, abs/1611.01603.
- Yelong Shen, Po-Sen Huang, Jianfeng Gao, and Weizhu Chen. 2017. ReasoNet: Learning to Stop Reading in Machine Comprehension. In *KDD*, pages 1047–1055. ACM.
- Alessandro Sordoni, Phillip Bachman, and Yoshua Bengio. 2016. Iterative alternating neural attention for machine reading. *CoRR*, abs/1606.02245.
- Chuanqi Tan, Furu Wei, Nan Yang, Weifeng Lv, and Ming Zhou. 2017. S-net: From answer extraction to answer generation for machine reading comprehension. *CoRR*, abs/1706.04815.
- Adam Trischler, Zheng Ye, Xingdi Yuan, Philip Bachman, Alessandro Sordoni, and Kaheer Suleman. 2016. Natural language comprehension with the epireader. In *EMNLP*, pages 128–137. The Association for Computational Linguistics.
- Wenhui Wang, Nan Yang, Furu Wei, Baobao Chang, and Ming Zhou. 2017. Gated self-matching networks for reading comprehension and question answering. In Proceedings of the 55th Annual Meeting of the Association for Computational Linguistics, ACL 2017, Vancouver, Canada, July 30 - August 4, Volume 1: Long Papers, pages 189–198.
- Jeremy H. M. Wong and Mark J. F. Gales. 2016. Sequence student-teacher training of deep neural networks. In Interspeech 2016, 17th Annual Conference of the International Speech Communication Association, San Francisco, CA, USA, September 8-12, 2016, pages 2761–2765.
- Caiming Xiong, Victor Zhong, and Richard Socher. 2016. Dynamic coattention networks for question answering. *CoRR*, abs/1611.01604.
- Adams Wei Yu, David Dohan, Minh-Thang Luong, Rui Zhao, Kai Chen, Mohammad Norouzi, and Quoc V. Le. 2018. QANet: Combining Local Convolution with Global Self-Attention for Reading Comprehension. *CoRR*, abs/1804.09541.