# **Dirichlet Processes for Joint Learning of Morphology and PoS Tags**

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### Abstract

This paper presents a joint model for learning morphology and part-of-speech (PoS) tags simultaneously. The proposed method adopts a finite mixture model that groups words having similar contextual features thereby assigning the same PoS tag to those words. While learning PoS tags, words are analysed morphologically by exploiting similar morphological features of the learned PoS tags. The results show that morphology and PoS tags can be learned jointly in a fully unsupervised setting.

#### 1 Introduction

The morphology of a word is an important indicator that determines its PoS tag, meanwhile the PoS tag of a word helps in identifying the correct morphological segmentation of the word. This relationship between morphology and syntax has been beneficial in both morphology learning with the exploitation of the syntactic features and in PoS tagging with the adoption of morphological features.

There has been a number of research that have performed PoS tagging by making use of morphological information (Clark (2003), Hasan and Ng (2009), Abend et al. (2010), Christodoulopoulos et al. (2011), etc.). There has been also a number of other research that have performed morphological segmentation by adopting syntactic information (Hu et al. (2005), Can and Manandhar (2009), Lee et al. (2011), etc.). However, there is a small number of research that combines two tasks in a single framework.

Sirts and Alumäe (2012) share a similar goal

with us in joining PoS tagging and morphological segmentation in a single framework. They use hierarchical Dirichlet process for infinite HMMs to induce both PoS tags and morphological segmentation. Their model is type-based, whereas our model is token based. In our model, we use finite mixture models for PoS tagging and Dirichlet processes for segmentation.

#### 2 **Model Definition**

The generative story of the model goes as follows:

- 1. Draw a PoS tag  $c_i$ .
- 2. Generate a word  $w_i$  that belongs to  $c_i$ .
- 3. Generate the context  $c_{i-1,i+1}$  of the word  $w_i$ from  $c_i$ .
- 4. From the possible splits of  $w_i$ , generate a suffix  $m_i$  conditioned on  $c_i$ , such that  $w_i =$  $s_i + m_i$ , where  $s_i$  denotes the stem.

The generative story is summarised as follows:

$$p(c_{i}, c_{i-1,i+1}, w_{i}, s, m) = p(c_{i})p(c_{i-1,i+1}|c_{i})$$
  
$$p(w_{i}|c_{i})p(m|c_{i})p(s)$$

#### 2.1 PoS Tagging

The model adopts a finite mixture model for PoS tagging (see Figure 1). Each mixture component represents a PoS tag that shares a set of features with other members in the same component. Each mixture component  $c_i$  consists of 1. a distribution over contexts and 2. a distribution over words. Each context is a PoS tag pair  $\langle c_{i-1}, c_{i+1} \rangle$ where the previous word  $w_{i-1}$  belongs to  $c_{i-1}$  and the following word  $w_{i+1}$  belongs to  $c_{i+1}$ . We employ a token-based approach for PoS tagging due to the significance of the context. The model is



Figure 1: The complete joint model.

defined formally as follows:

$$c_i \sim Mult(\phi)$$
 (1)

$$\phi \sim Dir(\pi)$$
 (2)

$$w_i | c_i \sim Mult(\theta_w)$$
 (3)

$$\theta_w \sim Dir(\kappa)$$
 (4)

$$C_{i-1,i+1}|C_i \sim Mult(\theta_{c,c'}) \tag{5}$$

$$\theta_{c,c'} \sim Dir(\beta)$$
 (6)

Class indicators  $c_i$  are drawn from a Multinomial distribution with parameters  $\phi$  (which have a Dirichlet prior distribution with hyperparameters  $\pi$ ). Each  $c_i$  involves a set of words  $w_i$  drawn from a Multinomial distribution with parameters  $\theta_w$  (which have a Dirichlet prior distribution with hyperparameters  $\kappa$ ). Each  $c_i$  also involves a distribution over contexts  $c_{i-1,i+1}$  drawn from a Multinomial distribution with parameters:  $\theta_{c,c'}$  (which have a prior distribution with hyperparameters  $\beta$ ).

#### 2.2 Morphology Learning

We model morphology using a Dirichlet process (DP) in order to split each word into a stem and a suffix (see Figure 1). Stems are generated by  $DP(\gamma_s, H_s)$  with concentration parameter  $\gamma_s$  and base distribution  $H_s$ , whereas suffixes are generated by  $DP(\gamma_m, H_m)$  with concentration parameter  $\gamma_m$  and base distribution  $H_m$ . Hence, the model is defined formally as follows:

$$s_i \sim DP(\gamma_s, H_s)$$
  
 $m_i | c_i \sim DP(\gamma_m, H_m)$ 

Base distributions are length priors that favour shorter morphs (Creutz and Lagus, 2005):

$$H_x(x_i) = p(c_{ij})^{|x_i|}$$
 (7)

where  $x_i$  is a morph and  $|x_i|$  is the length of  $x_i$  in letters. Each character has a probability of  $p(c_{ij})$ , where characters are assumed to be distributed uniformly in the alphabet. We also assume that each morph ends with a special character; i.e. end of morph marker.

Here,  $DP(\gamma_s, H_s)$  is a global Dirichlet process where stems may belong to any PoS tag, whereas  $DP(\gamma_m, H_m)$  is defined locally for each PoS tag. The reason is that stems are shared amongst different PoS tags. However, words belonging to the same PoS tag usually have similar endings, thereby leading to local distributions.

# **3** Inference

In our model, we assign values to the hyperparameters  $\pi, \kappa, \beta, \gamma_s, \gamma_m$  empirically, and we integrate out the parameters  $\phi, \theta_w, \theta_{c,c'}$  by using the Multinomial-Dirichlet conjugacy.

We use Gibbs sampling to infer POS tags, stems and suffixes. We perform inference in two steps: 1. a PoS tag is sampled for the word, 2. a stem and a suffix are sampled for the word.

#### 3.1 Inferring PoS tags

Each word's PoS tag is sampled subject to its context. Let a word be  $w_i$  and imagine that it occurs in context  $\langle w_{i-1}, w_{i+1} \rangle$  where  $w_{i-1}$  belongs to  $c_{i-1}$  and  $w_{i+1}$  belongs to  $c_{i+1}$ . We define the sampling probability of  $c_i$  for  $w_i$  as follows:

$$\begin{aligned} p(c_i| < w_{i-1}, w_{i+1} >, w_i) &\propto \quad p(< w_{i-1}, w_{i+1} >, w_i|c_i)p(c_i) \\ &\propto \quad p(w_i|c_i)p(< w_{i-1}, w_{i+1} > |c_i) \\ &p(c_i) \end{aligned}$$

We also assume that  $\langle w_{i-1}, w_{i+1} \rangle$  and  $w_i$  are independent since it is possible to remove  $w_i$  from  $\langle w_{i-1}, w_{i+1} \rangle$  and insert another word instead.

In order to calculate  $p(w_i|c_i)$ ,  $w_i$  is removed from the corpus:

$$p(w_i|c_i^{-w_i},\kappa) = \frac{n_{w_i,c_i^{-w_i}} + \kappa}{N_{c_i}^{-w_i} + W_{c_i^{-w_i}}\alpha}$$
(8)

where  $c_i^{-w_i}$  denotes the mixture component  $c_i$  that excludes  $w_i$ ,  $n_{w_i,c_i^{-w_i}}$  is the number of the wordtag pairs  $\langle w_i, c_i \rangle$ ,  $N_{c_i}^{-w_i}$  is the number of word



Figure 2: Many-to-1 accuracy scores obtained from corpora of size 24K, 36K, 48K, 60K, 72K, 84K, 96K, 120K, and 250K.

tokens having the PoS tag  $c_i$ ,  $W_{c_i^{-w_i}}$  is the number of word types that are tagged with  $c_i$ .  $p(c_i)$  is computed as follows:

$$p(c_i|\mathbf{c}^{-w_i}, \pi) = \frac{n_{c_i^{-w_i}} + \pi}{N^{-w_i} + K\pi}$$
(9)

where  $N^{-w_i}$  denotes the number of word tokens in the model excluding  $w_i$ , K is the number of class indicators (i.e. number of PoS tags).

In order to mitigate the sparsity within the context probabilities, we use the approximation introduced by Clark (2000):

$$p(\langle w_{i-1}, w_{i+1} \rangle | c_i) = p(\langle c_{i-1}, c_{i+1} \rangle | c_i)$$
(10)  
$$p(w_{i-1} | c_{i-1}) p(w_{i+1} | c_{i+1})$$

where,  $p(\langle c_{i-1}, c_{i+1} \rangle | c_i)$  is computed such that:

$$p(\langle c_{i-1}, c_{i+1} \rangle | c_x, c_y, c_z, c_i, \beta) = \frac{n_{c_{i-1}, c_i, c_{i+1}} + \beta}{k_{c_i} + L\beta}$$
(11)

Here,  $c_x$  is  $c_i^{-\langle c_{i-1}, c_{i+1} \rangle}$ ,  $c_y$  is  $c_{i-1}^{-\langle c_{i-2}, c_i \rangle}$ ,  $c_z$  is  $c_{i+1}^{-\langle c_i, c_{i+2} \rangle}$ ,  $k_{c_i}$  is the number of contexts in  $c_i$ , and L denotes the possible number of different contexts in the model (i.e. K \* K).

#### 3.2 Inferring Morphology

Two latent variables are inferred for morphology: stems and suffixes. The sampling probability for morphology is defined as follows:

$$p(w_i = s_i + m_i | \mathbf{s}^{-i}, \mathbf{m}_{c_i}^{-i}) = p(s_i | \mathbf{s}^{-i}) p(m_i | \mathbf{m}_{c_i}^{-i})$$
(12)

where  $\mathbf{s}^{-i}$  is the set of stems excluding  $s_i$ ,  $\mathbf{m}_{c_i}^{-i}$  is the set of suffixes assigned with  $c_i$  excluding  $m_i$ . The conditional probability of a stem is:

$$p(s_i|\mathbf{s}^{-i}, \gamma_s, H_s) = \frac{f^{s^{-i}} + \gamma_s H_s(s_i)}{T^{s^{-i}} + M^{s^{-i}} \gamma_s}$$
(13)



Figure 3: Variation of Information (VI) obtained from corpora of size 24K, 36K, 48K, 60K, 72K, 84K, 96K, 120K and 250K.

where  $f^{s^{-i}}$  is the frequency of the stem type  $s_i$  already generated,  $T^{s^{-i}}$  is the number of all stems in the model, and  $M^{s^{-i}}$  is the number of stem types generated excluding  $s_i$ . Similarly, the conditional probability of a suffix is computed as follows:

$$p(m_i | \mathbf{m}_{c_i}^{-m_i}, \gamma_m) = \frac{f_{c_i}^{m^{-i}} + \gamma_m H_m(m_i)}{T_{c_i}^{m^{-i}} + M^{m^{-i}} \gamma_m} \quad (14)$$

where  $f_{c_i}^{m^{-i}}$  is the frequency of the suffix type  $m_i$ already generated in  $c_i$ ,  $T_{c_i}^{m^{-i}}$  is the number of all suffixes assigned with PoS tag  $c_i$ , and  $M^{m^{-i}}$  is the number of suffix types already generated excluding  $m_i$ .

In the algorithm, initially each word is assigned a PoS tag and split randomly. The algorithm goes through each word by sampling a PoS tag, a stem, and a suffix. All constituents of the respective word (tag, stem, suffix, context, contexts of adjacent words) are removed from the model beforehand. This process is repeated for a number of iterations until a convergence is ensured.

# **4** Experiments & Evaluation

We used small portions of the Penn WSJ treebank (Marcus et al., 1993) for the experiments. We manually set the hyperparameters and concentration parameters for each experiment:  $\pi = 10^{-6}, \beta = 10^{-6}, \kappa = 10^{-6}, \gamma_s = 10^{-6}, \gamma_m = 10^{-6}$ . These values were set empirically through several experiments. We also inserted a special character at the end of each sentence and assigned it a distinct PoS tag. No other words could be assigned this tag.

#### 4.1 PoS Tagging Results

In our experiments we fixed the number of PoS tags to 45, which is the number of PoS tags in

	V-measure	Many-to-one
Christ.1 <sup>1</sup>	48.6	57.8
Joint	41.11	59.67
Clark <sup>2</sup>	63.8	68.8
Christ.2 (Best Pub.) <sup>3</sup>	67.7	72.0
<sup>1</sup> Christodoulopoulos	s et al. (2011)	
<sup>2</sup> Clark (2003)		
3 Chainta davida and	+ - 1 (2010)	

<sup>o</sup> Christodoulopoulos et al. (2010)

Table 1: PoS tagging scores.

	missing	extra	wrong	correct
Joint	0.72%	28.55%	10.13%	60.60%
Morfessor	15.07%	7.23%	10.22%	67.48%

Table 2: Morphological segmentation scores.

Penn WSJ treebank. We applied many-to-one accuracy by assigning each result tag a gold standard tag having the highest frequency among the words assigned with this result tag (see Figure 2). Second, we applied one-to-one accuracy which have similar results with many-to-one scores.

We also measured the variation of information (VI) (Rosenberg and Hirschberg, 2007) (see Figure 3). Although there is not a smooth decrement in VI measure, it improves with the larger datasets in average<sup>1</sup>.

Results show that determiners, modal verbs, prepositions, pronouns, conjunctions, and numbers are discovered generally correctly. The most common error type is due the confusion of nouns and adjectives. Normally, nouns are distributed over several PoS tags. Verbs and adverbs are also generally confused and spread over different tags.

We report our results with a comparison to other systems in Table 1 by using a dataset of 250K words. We use a small portion of Penn WSJ treebank for the comparison. The dataset involves 250K words where the number of word types is 20957. The other systems are also tested on a small portion of WSJ involving 16850 word types, which is reported in Christodoulopoulos et al. (2011).

Our system outperforms Christodoulopoulos et al. (2011) with the many-to-one evaluation, whereas Christodoulopoulos et al. (2011) perform better than our system based on V-measure evaluation. It should be noted that Clark (2003) and Christodoulopoulos et al. (2010) are both type-based.



Figure 4: Confusion matrix shows the correlation between found morphs and true morphs. The shades reflect the number of matchings.

### 4.2 Morphological Segmentation Results

We performed the evaluation of morphological segmentation on verbs. We adopted some heuristics that strip off common verb endings such as *-ed, -d, -ing, -s, -es* from verbs in order to build the gold standard. Irregular verbs are introduced exceptionally and left as they are.

The results obtained from the 96K setting were used for the evaluation. We ran Morfessor Baseline (Creutz and Lagus, 2002; Creutz and Lagus, 2005; Creutz and Lagus, 2007) on the verbs in the same dataset. Table 2 gives the scores where missing types refers to the case that gold standard suggests a suffix but no suffix is identified in the results, extra suffixes means that gold standard does not identify any suffixes but the results contain suffixes, wrong suffixes implies that both gold standard and results identify suffixes but they are not the same, and correct types means that both gold standard and results contain suffixes and they match. Our model identifies 12257 suffix types, whereas Morfessor Baseline identifies 2309 due to undersegmentation. In addition, confusion matrix that depicts the result morphs against true morphs is given in Figure 4.

# 5 Conclusion

We proposed a model that jointly learns PoS tags and morphology. The results show that learning PoS tags and morphology can be performed cooperatively.

<sup>&</sup>lt;sup>1</sup>Although, Figure 3 shows that results for 36k words are better than results for 48k words, this could be due to the particular choice of training sets we used.

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