Monotonic Paraphrasing Improves Generalization of Language Model Prompting

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Abstract

Performance of large language models (LLMs) may vary with different prompts or instructions for even the same task. One commonly recognized factor for this phenomenon is the model's familiarity with the given prompt or instruction, which is typically estimated by its perplexity. However, finding the prompt with the lowest perplexity is challenging, given the enormous space of possible prompting phrases. In this paper, we propose monotonic paraphrasing (MONOPARA), an end-to-end decoding strategy that paraphrases given prompts or instructions into their lower perplexity counterparts based on an ensemble of a paraphrase LM for prompt (or instruction) rewriting, and a target LM (i.e. the prompt or instruction executor) that constrains the generation for lower perplexity. The ensemble decoding process can efficiently paraphrase the original prompt without altering its semantic meaning, while monotonically decreasing the perplexity of each generation as calculated by the target LM. We explore in detail both greedy and search-based decoding as two alternative decoding schemes of MONOPARA. Notably, MONOPARA does not require any training and can monotonically lower the perplexity of the paraphrased prompt or instruction, leading to improved performance of zero-shot LM prompting as evaluated on a wide selection of tasks. In addition, MONOPARA is also shown to effectively improve LMs' generalization on perturbed and unseen task instructions.¹

1 Introduction

Large language models (LLMs) have demonstrated remarkable proficiency in zero-shot decision making (Gonen et al., 2023; Schick and Schütze, 2021; Brown et al., 2020) and instruction following (Jiang et al., 2023; Köpf et al., 2023; Touvron et al., 2023b; Taori et al., 2023; Chiang et al., 2023; Ouyang et al., 2022). However, there can be significant variance in the performance of seemingly similar prompts (Zhao et al., 2021; Lu et al., 2022c; Webson and Pavlick, 2022; Gonen et al., 2023; Yan et al., 2024). Despite efforts of studies on prompting LMs (Shin et al., 2020; Li and Liang, 2021; Gao et al., 2021; Ding et al., 2022; Sanh et al., 2021; Kojima et al., 2022), it is still challenging to develop high-quality prompts that can induce better performance for varying tasks on evolving models in an effort-saving manner.

One consensus reached by recent studies is the inverse relationship between a prompt's perplexity and its task performance (Kumar et al., 2023; Gonen et al., 2023). This stems from the intuition that the frequency of a prompt (or an instruction)² appearing in the (pre-)training data positively influences the model's familiarity with it, thereby enhancing its capability to perform the described task (Iter et al., 2023; Gonen et al., 2023; Wang et al., 2023; Lee et al., 2023). As a result, existing attempts use specific criteria, especially perplexity for selecting prompts from a collection of candidates. For example, Gonen et al. (2023) builds a large prompt pool for each task and selects the one with the lowest perplexity. However, the performance of such rewrite-then-select methods (Jiang et al., 2020; Zhou et al., 2022; Gonen et al., 2023; Prasad et al., 2023) is limited by the size, quality, and even availability of the candidate pool. Searching the prompt with the lowest perplexity for a particular task remains challenging due to the vast expanse of potential prompts.

To address this challenge, we propose a novel progressive *end-to-end* prompt refining approach, namely monotonic paraphrasing (MONOPARA), that can *proactively* rewrite the given prompt into its low-perplexity counterpart without compromis-

¹Our code is available at https://github.com/ luka-group/MonoPara.

 $^{^{2}}$ We use the terms "prompt" and "instruction" interchangeably in this paper as they both refer to a natural language command for zero-shot inference.

ing its expressiveness of the task. During prompt (or instruction) refinement, MONOPARA conducts an ensemble decoding process of a paraphrasing model together with the target LM. The paraphrase model is instructed to rewrite the given prompt of a specific task, while the target model, which is later on used for task inference, provides a constraint that aims to lower the perplexity of the generation. MONOPARA iteratively decodes tokens based on the ensemble of these two models. Intuitively, the paraphrase model can genuinely paraphrase the original prompt without altering its semantic meaning and remain instructive for the given task, while the target model restricts the search space of paraphrased tokens to those with low perplexity, resulting in a task prompt that the target model is more familiar with.

Further. for the decoding process of MONOPARA, we explore two decoding schemes. In addition to greedy decoding ($\S2.3$) that iteratively generates the next token based on the weighted combination of predicted probabilities from both models, we also explored search-based decoding $(\S2.4)$. The search-based decoding scheme follows the look-ahead decoding paradigm (Lu et al., 2022b), which keeps several sequence candidates and maintains the one with the lowest perplexity scored by the target model. Compared to recent prompt refinement approaches (Gonen et al., 2023; Kumar et al., 2023; Shum et al., 2023), MONOPARA needs zero training effort and far less computational cost, and do not require the pre-existence of multiple prompt or instruction candidates (Gonen et al., 2023). We find that by an ensemble of two LMs, we are able to consistently decode lower perplexity prompts, which would, in turn, bring about better generalization of LMs on downstream tasks.

Our contributions are three-fold. First, we propose MONOPARA, a prompt refinement method that paraphrases prompts to be more familiar with the target model for boosted generalization and task performance. Second, we explore and compare two distinct decoding strategies that proactively refine prompts by monotonically lowering their perplexity and maintaining their expressiveness of the task. Third, we conduct experimentation for both prompt refinement for regular LMs and instruction refinement for instruction-tuned LMs to illustrate that monotonic paraphrasing improves the generalization of LM prompting.



Figure 1: Perplexity of x_{para} as the output paraphrase of P_{para} vs. as the input prompt of P_{tar} for the AG News dataset with Mistral 7B as both P_{para} and P_{tar} . Each point stands for a different prompt x_{para} . A lowperplexity paraphrase does not necessarily result in a low-perplexity prompt for the target model.

2 Monotonic Paraphrasing

We propose MONOPARA as an ensemble-based decoding method that can refine a given prompt by paraphrasing it into a low-perplexity counterpart. We first provide the intuition of MONOPARA in §2.1 and the basics of prompt paraphrasing in §2.2. Then, we formally define two decoding schemes of MONOPARA in §2.3 and §2.4.

2.1 Intuition and Methodology

Assume that the user wants to address a task specified by a given prompt x_{ori} using a target LM P_{tar} . MONOPARA seeks to refine the given prompt to its low-perplexity counterpart x_{para} (i.e. a more familiar prompt to P_{tar}), thereby enhancing model performance. However, simply paraphrasing the original prompt with a paraphrase model P_{para} does not necessarily result in a low-perplexity counterpart. This discrepancy arises from a mismatch between the perplexity of the output x_{para} from the paraphrase model and the perplexity observed when using x_{para} as the input prompt for the target model. As shown in Fig. 1, there is a lack of significant correlation between the perplexity of x_{para} as output in P_{para} and that of x_{para} as input in P_{tar} , even if we use the same model as the paraphrase and target model $(P_{para} = P_{tar})$. This observation indicates that the minimal perplexity of a paraphrased prompt could not be achieved by the paraphrase model alone.

Based on the above fact, the goal of MONOPARA is to take on the semantic hints from the paraphrase



Figure 2: Two explored decoding schemes of MONOPARA. Ensemble-based decoding (bottom) combines the token probabilities from the paraphrase model and the target model in each decoding step. Search-based decoding (top) further leverages look-ahead decoding to consider the potential future impact of current choices.

model while following the constraint of perplexity from the target model. Specifically, the paraphrase model generates paraphrases for a given prompt, while the target model constrains the paraphrase perplexity during the generation process. With an ensemble of these two models, we can leverage the strengths of both: the guided content generation capability of the paraphrase model and the lowperplexity prompt constraint of the target model. MONOPARA is thus able to produce paraphrases with lower perplexity by synergizing the benefits of both models.

2.2 Prompt Paraphrasing

We first introduce prompt paraphrasing without perplexity constraint. We consider using an LLM for prompt paraphrasing in a zero-shot manner, where the model is instructed to paraphrase the original prompt x_{ori} to a fluent and coherent counterpart x_{para} with a system prompt x_{sys} , such as the following one:

The System Prompt for Paraphrasing

Generate ONE paraphrase of the following sentence.

Specifically, we denote the input of the paraphrase model, including the concatenation of the system prompt x_{sys} and the original prompt x_{ori} that the model is instructed to rewrite, as $[x_{sys}, x_{ori}] = (x_1, \ldots, x_n)$, where x_i is a token in the vocabulary V. Suppose the decoder of a pre-trained autoregressive language model P_{para} generates continuations of length m as the requested paraphrase, denoted as

 $x_{para} = (x_{n+1}, \ldots, x_{n+m})$, based on the system prompt x_{sys} and original prompt x_{ori} . At decoding time, P_{para} iteratively decodes one token at a time by conditioning on the preceding context:

$$P_{para}(x_{para}|x_{sys}, x_{ori}) = \prod_{i=n+1}^{n+m} P_{para}(x_i|x_{< i}),$$

where $P_{para}(x_i|x_{< i})$ is the predicted next token probability.

2.3 Ensemble-based (Greedy) MONOPARA

To introduce perplexity constraint from the target model to the paraphrase model, here we introduce the ensemble-based greedy decoding for monotonic paraphrasing (as shown in the lower half of Fig. 2). Based on the intuition delivered in §2.1, MONOPARA decodes the paraphrase iteratively, and the next token is selected based on the combination of predicted probabilities from the two LMs:

$$\begin{aligned} x_{next} &= \underset{x_i \in V}{argmax} (\alpha \cdot \log P_{tar}(x_i | x_{gen}) \\ &+ (1 - \alpha) \cdot \log P_{para}(x_i | x_{sys}, x_{ori}, x_{gen})), \end{aligned}$$

where x_{gen} denotes the sequence of generated tokens, and α determines the coefficient between the two models (Alg. 1).

By combining the prediction probabilities of both models, the ensemble can navigate the complex landscape of language generation more effectively and precisely. The paraphrase model P_{para}

Algorithm 1	l Ensemble	e-based	Decoding
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Require: ▷ System prompt for paraphrase x_{sys} V \triangleright Vocabulary P_{tar}, P_{para} ▷ Target and paraphrase models ▷ Weighting factor

Ensure:

- x_{gen} ▷ Generated text sequence 1: Initialize $x_{qen} \leftarrow \emptyset$
- 2: $x_{next} \leftarrow \underset{x_i \in V}{argmax} P_{para}(x_i | x_{sys} \oplus x_{ori})$ \triangleright

Generate first token with P_{para}

- 3: $x_{gen} \leftarrow x_{gen} \oplus x_{next}$
- 4: while not end of sequence do
- Compute weighted log probabilities for 5: each $x_i \in V$:
- $score_{tar} \leftarrow \alpha \cdot \log P_{tar}(x_i | x_{gen})$ 6:
- $score_{para} \leftarrow (1-\alpha) \cdot \log P_{para}(x_i | x_{sys} \oplus$ 7: $x_{ori} \oplus x_{qen}$)
- $\begin{array}{l} x_{next} \leftarrow argmax \ (score_{tar} + score_{para}) \\ x_{gen} \leftarrow x_{gen} \oplus x_{next} \end{array}$ 8: 9:
- 10: end while
- 11: return x_{gen}

keeps the rewritten prompt (or instruction) remains with the original intent, while the target model P_{tar} evaluates the paraphrase's likelihood or confidence, up-weighting any generation samples that lead towards low-perplexity outcomes. Based on the ensemble, the next token is selected by maximizing the weighted sum of logarithmic probabilities from both models, considering both the instruction and the generated text thus far.

As a coefficient, α balances the contribution of each model, ensuring that the final output satisfies both semantic fidelity to the prompt intent and linguistic familiarity to the target model. Higher α increases the weight of the logarithmic probability derived from the target model P_{tar} and cuts down on the semantic hints for P_{para} , which raises the risk of sacrificing the semantic fidelity of the generation. Conversely, a lower α shifts the emphasis towards P_{para} , placing greater value on ensuring that the generated text closely follows the instructional context and semantic intent from P_{para} . In this case, the decoding process lacks the constraint of perplexity from P_{tar} and sacrifices the linguistic familiarity of the generated paraphrase for the target model.

2.4 Search-based MONOPARA

To further enhance the efficiency of decoding prompts of lower perplexity, we define the searchbased decoding strategy for MONOPARA (as shown in the upper half of Fig. 2). To take more steps of token generation into account and expand the search space, we leverage look-ahead decoding to search for the sequence that exhibits the lowest perplexity from an even broader candidate space. Following Lu et al. (2022a), each step of our searchbased decoding consists of (i) expanding a set of candidate next-tokens, (ii) scoring each candidate, and (iii) selecting the k best candidates (Alg. 2 in Appx. §A):

$$X'_{m} = \{ \mathbf{x}_{< m} \circ x_{m} | \mathbf{x}_{< m} \in X_{m-1}, x_{m} \in V \}, X_{m} = \underset{(x_{< m}, x_{m}) \in X'_{m}}{\arg topk} \{ f(\mathbf{x}_{< m}, x_{m}) \},$$

where x_m is a candidate predicted by paraphrase model, and $f(\cdot)$ is a scoring function that returns the perplexity of $x_{< m} \circ x_m$ evaluated by the target model:

$$f(\mathbf{x}_{< m}, x_m) = \left(\prod_{i=1}^m \frac{1}{P_{tar}(x_i | x_{< i})}\right)^{\frac{1}{m}}.$$
 (1)

Specifically, at each step m of the decoding process, the current set of sequences X_{m-1} is expanded by appending the most probable next-token x_m , predicted by the paraphrase model P_{para} , from vocabulary V to each sequence $x_{\leq m}$. This results in a temporary expanded set of candidate sequences X'_m . Each candidate sequence in X'_m is then evaluated by the scoring function $f(\cdot)$ shown in Eq. 1, which calculates the perplexity of a sequence by the target model P_{tar} . Since a paraphrase of lower perplexity is preferred, the k sequences with the best scores (i.e., lowest perplexity) are selected to form the set X_m , narrowing down the choices to the k most promising sequences for continuation.

In comparison to greedy decoding, this lookahead decoding mechanism evaluates a broader range of potential future impact from current choices (i.e., the selection of x_m), thereby allowing for a more informed and potentially more accurate selection of candidates.

3 **Experiment**

In this section, we demonstrate two distinct experimental settings for evaluation. In §3.1, we examine MONOPARA's effectiveness on prompt refinement

for eliciting better task performance. In §3.2, we evaluate MONOPARA's effect on enhancing model robustness and generalization under instruction perturbations.

3.1 Task I: Prompt Refinement

Task Description To inspect if monotonic paraphrasing can refine a prompt and elicit better performance on prompting an LLM as designed, we use SUPER-NATURALINSTRUCTION (SUP-NATINST for short, Wang et al., 2022). This benchmark consists of 1,616 diverse NLP tasks and their expertwritten prompts for evaluating the zero-shot generalizability of LLMs on a variety of NLP tasks. In SUP-NATINST, each task is paired up with an instruction that consists of the task definition for mapping an input text to a task output and several examples for demonstrating the desired or undesired output. To make our evaluation more challenging, we only use the task definition as a prompt for the target model to perform the task. During test time, the target model is prompted with a concatenation of SUP-NATINST task description (or its paraphrase), test sample, and multiple choices of answers. Since SUP-NATINST provides only one description of definition for each task, we use GPT4 (Achiam et al., 2023) to generate 4 more SUP-NATINST-like task descriptions for each involved task, which results in 5 prompts for each task in total.

Datasets Following Gonen et al. (2023), we choose 7 classification tasks from Huggingface Datasets³ to have a set of diverse tasks: (i) GLUE Cola (Warstadt et al., 2019) for grammatical acceptability discrimination; (ii) Newspop (Moniz and Torgo, 2018) for news classification; (iii) AG News (Zhang et al., 2015) for news classification; (iv) IMDB (Maas et al., 2011) for movie review sentiment analysis; (v) DBpedia (Lehmann et al., 2015) for topic classification; (vi) Emotion (Saravia et al., 2018) for tweet emotion classification; and (vii) Tweet Offensive (Barbieri et al., 2020) for offensive tweet discrimination. We sample 1,000 examples from each dataset for prompt evaluation. For these tasks, the prompt follows the input, and at the end of each prompt, we add the choices of classes following Gonen et al. (2023): "Choices: X, Y, Z. Answer: " as it helps with accuracy.

Evaluation Metrics To inspect whether monotonic paraphrasing can refine a prompt into its low-perplexity counterpart and further enhance the generalization of LLM prompting, we use PPL (perplexity), Acc (accuracy), and BS (BERTScore, Zhang* et al., 2020) for evaluation. (1) Perplexity. Following Gonen et al. (2023), we define the perplexity of the prompt as the perplexity of the full prompt sequence, including the input itself and the choices of labels. To avoid noise when computing perplexity, the prompts are instantiated with 1,000 random examples of the dataset (we keep the same selected examples for performance evaluation), and the perplexity is averaged across all instantiated prompts. The correlation between the perplexity of a standalone prompt and the average perplexity over instantiated ones is illustrated in Appx. §E. (2) BERTScore. As a paraphrasing scheme, MONOPARA is also evaluated by its performance in semantic alignment with the source sentence based on pre-trained BERT (Devlin et al., 2019). (3) Accuracy. To compute accuracy, for each test sample, we obtain the model's predicted probability of all classes and choose the highest ranking class as the prediction of the model. The accuracy is calculated over the 1,000 samples for each task.

Models We study two auto-regressive models, Mistral-7B⁴ (Jiang et al., 2023)and Starling-7B⁵ (Zhu et al., 2023a), for their significant ability in instruction following and paraphrasing. In this paper, we keep the paraphrase model **the same** as the target model. Please refer to Appx. §B for the results on Llama-3-8B⁶ (AI@Meta, 2024).

Baselines We compare our method with two baselines: SPELL (Gonen et al., 2023) and vanilla LLM-based paraphrasing (Para). Based on similar intuition that low perplexity and better performance exhibit strong correlation, SPELL (Selecting Prompts by Estimating LM Likelihood) ranks and selects the prompts with the lowest perplexity for a given task after creating a set of prompt candidates manually and expanding them to hundred-scale using automatic paraphrasing and back-translation. We use the prompt candidates

⁴https://huggingface.co/mistralai/ Mistral-7B-Instruct-v0.1

⁵https://huggingface.co/berkeley-nest/ Starling-LM-7B-alpha

⁶https://huggingface.co/meta-llama/ Meta-Llama-3-8B

³https://huggingface.co/docs/datasets/index

Methods	Metric	GLUE Cola	Newspop	AG News	IMDB	DBpedia	Emotion	Tweet Offensive
				Mistr	al 7B			
Ori.	Acc PPL	61.76 ± 2.93 15.72 ± 4.60		67.68 ± 3.47 12.74 ± 1.07	84.12 ± 4.89 16.41 ± 0.80	70.82 ± 2.27 8.10 ± 0.22	44.32 ± 1.57 16.48 ± 2.14	67.04 ± 0.95 19.25 ± 3.43
SPELL	Acc PPL	43.42 ± 1.16 8.24 ± 0.88	81.08 ± 7.2 15.05 ± 4.15	73.88 ± 3.18 15.99 ± 3.77	86.00 ± 0.81 15.76 ± 1.42	71.02 ± 1.70 25.36 ± 6.80		65.06 ± 1.04 14.31 ± 0.93
Para	Acc PPL BS	39.48 ± 8.19 78.01 ± 11.22 88.88 ± 0.74	76.72 ± 16.54 49.37 ± 7.81 87.47 ± 0.84	28.37 ± 2.58			$\begin{array}{c} 43.65 \pm 3.41 \\ 46.53 \pm 5.30 \\ 90.08 \pm 0.35 \end{array}$	65.04 ± 1.46 53.65 ± 1.92 89.93 ± 0.67
Mono-E	Acc PPL BS	63.96 ± 3.88 14.89 ± 2.75 93.03 ± 2.15	88.96 ± 3.04 8.33 ± 1.30 92.85 ± 2.35	10.07 ± 2.93	87.58 ± 3.27 13.05 ± 1.86 89.35 ± 2.60	$72.07 \pm 3.54 \\ 8.85 \pm 0.88 \\ 93.21 \pm 1.16$	13.67 ± 1.87	67.00 ± 1.21 14.11 ± 3.53 91.73 ± 1.32
Mono-S	Acc PPL BS	62.31 ± 6.17 15.85 ± 4.88 92.47 ± 2.00	11.95 ± 2.09	9.89 ± 1.31	16.38 ± 1.63	72.46 ± 3.00 8.63 ± 0.41 95.87 ± 1.20	15.03 ± 1.65	$65.66 \pm 2.43 \\ 18.35 \pm 4.07 \\ 91.62 \pm 2.48$
				Starli	ng 7B			
Ori.	Acc PPL	$55.18 \pm 12.43 \\ 16.38 \pm 4.18$		88.44 ± 1.18 12.10 ± 0.91		94.06 ± 0.37 8.11 ± 0.22	55.48 ± 0.91 17.90 ± 2.82	64.62 ± 0.18 20.41 ± 3.90
SPELL	Acc PPL	46.46 ± 6.70 44.96 ± 18.23	89.84 ± 0.91 54.60 ± 18.72			92.02 ± 0.64 28.66 ± 9.47		64.20 ± 0.17 33.56 ± 3.83
Para	Acc PPL BS		$\begin{array}{c} 82.67 \pm 19.63 \\ 54.41 \pm 8.80 \\ 88.35 \pm 0.51 \end{array}$	30.67 ± 2.81		26.56 ± 1.39	58.87 ± 4.44	64.44 ± 0.08 11.71 \pm 0.86 79.93 \pm 11.52
Mono-E	Acc PPL BS	69.62 ± 4.12 8.56 ± 1.00 93.00 ± 0.85	95.15 ± 0.59 10.12 ± 1.02 94.19 ± 0.94	8.52 ± 0.76	12.60 ± 1.57	94.05 ± 0.42 9.58 ± 0.86 93.23 ± 0.50	9.23 ± 0.97	$64.45 \pm 0.09 \\ 11.71 \pm 0.86 \\ 93.69 \pm 1.52$
Mono-S	Acc PPL BS	50.96 ± 11.52 14.05 ± 3.76 92.69 ± 0.99	12.55 ± 2.07		92.96 ± 4.78 16.44 ± 0.92 93.01 ± 1.25	$92.82 \pm 2.17 \\ 8.39 \pm 0.53 \\ 96.99 \pm 0.70$	16.28 ± 2.18	66.80 ± 1.22 20.17 ± 3.17 94.45 ± 1.43

Table 1: Results of Task I (Prompt Refinement). Ori. refers to the original prompts. Para refers to paraphrasing the original prompts without perplexity constraint. Mono-E refers to ensemble-based MONOPARA. Mono-S refers to search-based MONOPARA. The best accuracy for each task is in **bold**, while the lowest perplexity and the highest BERTScore for each task is in blue and orange respectively. The coefficient α is fixed as 0.5 for all the results.

provided by Gonen et al. (2023) and rank them by the perplexity w.r.t. the target model. Para paraphrases source prompts with greedy decoding (top-1 sampling) by directly prompting the target LLM with the instruction introduced in §2.2. Besides, we also implement reranking based on the prompt candidates generated by MONOPARA for a fair comparison with SPELL. The implementation details and results are discussed in Appx. §D.

Results As shown in Tab. 1, the two variants of MONOPARA successfully refine prompts to those with perplexities lower than the original ones, thereby enhancing model performance on 10 out of 14 scenarios (2 models, each on 7 datasets). Specifically, Mono-E (ensembled-based MONOPARA) improves the accuracy of Mistral-7B by an average of 2.64% and that of Starling-7B by an average of 1.85% on seven different datasets. In contrast,

directly paraphrasing the prompts without perplexity constraint (Para) results in prompts with higher perplexities than the original ones in 13 out of 14 scenarios, most of which lead to worse task performance. This highlights the importance of incorporating perplexity constraints when paraphrasing prompts. The correlation between task accuracy and prompt perplexity is analyzed in Appx. §C.

Besides, our method outperforms SPELL with consistently lower perplexity and superior task performance with the refined prompt. This superiority stems from the fact that, although SPELL explores a vast search space with hundred-scale prompt candidates, the candidates are searched in an ad hoc manner without an optimization goal, leading to inefficiencies in prompt rewriting or paraphrasing. In contrast, our method incorporates the perplexity constraint that leads to optimized target-model perplexity during one single refined prompt generation process, leading to both enhanced task performance and refinement efficiency.

Moreover, MONOPARA achieves superior performance in terms of both average prompt perplexity and BERTScore, indicating the synergistic role played by both the target model and the paraphrase model in prompt refinement. During decoding, the target model prioritizes achieving low perplexity, while the paraphrase model preserves the original prompt intent, resulting in a high BERTScore. We provide a detailed case study on BERTScore of Para and MONOPARA in Appx. §G to explain why MONOPARA outperforms Para on BERTScore. Specifically, Mono-E outperforms Mono-S in some cases since Mono-S involves the additional hyperparameter of beam size which we did not tune. Additionally, having additional token options at each decoding step may introduce more randomness, potentially affecting the overall performance. That being said, Mono-S mostly exhibits a higher BERTScore than the simpler method Mono-E, indicating better quality of paraphrasing.

3.2 Task II: Robustness Evaluation on Instruction Perturbation

We further evaluate MONOPARA's effectiveness in enhancing model robustness against various instruction perturbations at character, word, sentence, and semantic levels using PromptBench (Zhu et al., 2023b).

Task Description PromptBench introduces perturbation to task instructions of a diverse set of tasks, such as sentiment analysis, grammar correctness, duplicate sentence detection, and natural language inference. It includes character-level perturbations using DeepWordBug (Gao et al., 2018) to introduce typos, word-level using TextFooler (Jin et al., 2020) to replace words with contextually similar words, and semantic-level by using prompts following the linguistic behavior of different languages. For semantic-level perturbations, the adversary constructs prompts using various languages, such as Chinese, French, Arabic, Spanish, Japanese, and Korean, and then translates these prompts into English. By exploiting the nuances and idiosyncrasies of different languages during translation, it can introduce subtle ambiguities, grammatical errors, or inconsistencies in the input prompt. The perturbed prompt itself is still in English.



Figure 3: Model's average accuracy across 4 GLUE datasets, with each dataset having six instructions with perturbation added at character, word, and semantic levels. Mono-E has consistent improvement in accuracy across all types of perturbation compared to vanilla paraphrasing.

Datasets We select 4 GLUE tasks (Wang et al., 2018) from Huggingface Datasets for evaluation: (i) Cola, which is also used for Task I; (ii) SST-2 (Socher et al., 2013) for two-way sentiment classification; (iii) MNLI (Wang et al., 2018) for multigenre inference identification; and (iv) MRPC (Dolan and Brockett, 2005) for paraphrase identification. We adopt the same instruction format as that of Task I.

Model For this task, we use Alpaca⁷ (Taori et al., 2023), a model instruction-tuned from the LLaMA model (Touvron et al., 2023a) on the 52k self-instruct dataset. The paraphrase model is also the same as the target model.

Results As shown in Fig. 3, we compare the performance of original prompts, prompts paraphrased without perplexity constraint, and our method Mono-E. Across all kinds of instruction perturbations, our method achieves consistent accuracy improvement by up to 10.13%. This notable increase in performance demonstrates that MONOPARA not only refines prompts for improved task performance but also enhances model robustness against various instruction perturbations. We also show the model performance with unperturbed prompts and compare the degradation from perturbation in Appx. §F to show the robustness of Mono-E.

⁷https://huggingface.co/tloen/alpaca-lora-7b. We use a different language model for this task to demonstrate the robustness and versatility of our proposed method across various models.

	Content	BertScore	PPL
Ori Instruction	Read the provided excerpt and choose between 'positive' and 'negative' to describe its sentiment Iyk1IJt8yw:	-	78.12
Para	Determine the sentiment of the given excerpt as either positive or negative	81.26	44.29
$\alpha = 0.2$	Determine the sentiment of the given text by selecting either 'positive' or 'negative'.	86.18	24.90
Mono $\alpha = 0.5$	Determine the sentiment of the given text by classifying it as positive or negative.	80.22	16.27
$\alpha = 0.7$	Determine the remainder when 101 is divided by 10.\n A: 1	50.22	4.53

Table 2: Effect of coefficient α on Mono-E with Mistral-7B model.

3.3 Effect of Coefficient

We further analyze the effect of coefficient α between the target model and the paraphrase model in MONOPARA. Tab. 2 presents a case study of α on the ensemble-based decoding variant (Mono-E) with a prompt under character-level perturbation. Obviously, a larger value of α amplifies the influence of the target model, resulting in a stronger perplexity constraint and monotonically lower perplexity. Consequently, the impact of the paraphrase model is diminished, leading to a lower BERTScore. By adjusting α , the user can find a balanced point to achieve better prompts that strike a balance between semantic fidelity to the original prompt intent and linguistic familiarity to the target model. Detailed results and analysis are presented in Appx. §H and Tab. 9.

4 Related Work

Paraphrasing. Paraphrase generation has been a longstanding task in NLP. Since the era of deep learning, studies have adopted the universal paradigm of training sequence-to-sequence generation models based on abundant learning resources (Nema et al., 2017; Gupta et al., 2018; Li et al., 2018). While more recent works have leveraged more robust pre-trained language models that captured rich supervision signals from various sequence-to-sequence generation tasks (Raffel et al., 2020; Lewis et al., 2020) and achieving even more robust performance of paraphrasing with relatively limited end-task supervision (Sun et al., 2021; Meng et al., 2021; Bui et al., 2021). In addition to these advancements, a series of works have added auxiliary supervision signals such as syntactical guidance, lexical regularization, and cross-lingual supervision, to further improve the performance and controllability of paraphrasing in aspects such as syntactic structures, stylistic specification, or textual simplicity (Iyyer et al., 2018;

Li et al., 2019; Chen et al., 2019; Kumar et al., 2020; Goyal and Durrett, 2020; Hosking and Lapata, 2021; Chowdhury et al., 2022).

Different from existing paraphrasing techniques, this work conducts constrained decoding methods that seek to monotonically decrease the perplexity in the process of paraphrasing. This innovative approach serves as a general approach to rewrite and refine prompts or task instructions towards their more familiar counterparts for LMs, seeking to enhance the generalization of LM prompting without the need for any training effort.

Prompt Refinement. Prompt refinement has been actively explored in recent years with the aim of selecting, retrieving, or even generating prompts that lead to improved zero-shot performance of LM prompting. When an end-task objective is known, prior works on prompt refinement approaches often set the end-task performance as the objective, and leverage approaches such as gradient-based search, similar to continuous prompts but with projections onto a discrete vocabulary (Shin et al., 2020). Other works have explored edit-based enumeration (Prasad et al., 2023), reinforcement learning (Deng et al., 2022), and large language model continuation and filtering (Zhou et al., 2022). As for general-purpose LLMs, a dedicated prompt refinement approach may not assume the pre-existence of any specific end tasks. Hence, more recent works Iter et al. (2023); Gonen et al. (2023); Wang et al. (2023); Lee et al. (2023) explored the heuristic criterion based on the familiarity of the language model with the language contained in the prompt, as measured by its perplexity. Lower perplexity prompts are preferred as they are expected to perform better across a wide range of tasks.

While the last line of research has relieved the generic principle for improving zero-shot LLM prompting generalizability, these studies are largely limited to selecting among pre-existing prompts or multiple beam search samples. Our proposed monotonic paraphrasing approach, however, can proactively rewrite a prompt or task instruction into counterparts that better satisfy the above heuristic criterion, without the need of any pre-existing candidate prompts or any training effort.

Ensemble and Search-based Decoding. The proposed two decoding schemes of MONOPARA are connected to both ensemble decoding and searchbased decoding approaches in recent studies. Ensemble decoding has been previously proposed for purposes including debiasing (Li et al., 2023), controllable generation (Meng et al., 2022; Huang et al., 2023), and cross-modality data processing (Liu et al., 2023). Search-based decoding, on the other hand, is proposed to efficiently extend the search space of generation samples for satisfying specific constraints or criteria (Lu et al., 2022a; Wuebker et al., 2012; Lee and Berg-Kirkpatrick, 2022; Xu et al., 2023). Representative approaches include look-ahead (Lu et al., 2022a) and look-back (Xu et al., 2023) ones that search within the beam space towards different directions.

The explored decoding schemes in MONOPARA are inspired by both lines of studies on decoding approaches. Specifically, the first line is related to our design choice for composing the probabilities of both the paraphrasing and the target LMs in greedy generation. And our search-based decoding scheme is specifically inspired by the look-ahead decoding strategy in the second line of studies.

5 Conclusion

In this paper, we propose monotonic paraphrasing (MONOPARA) for automatically and iteratively generating low-perplexity prompts for given LLMs, which can lead to better task performance. Following the high-level idea of paraphrasing prompts with perplexity constraints from the target LLM, we design ensemble-based and search-based decoding strategies for efficient prompt refinement. Experiments on prompt variations of unseen tasks and instructions demonstrate the effectiveness of MONOPARA in reducing prompt perplexity while enhancing task performance and model robustness. Future work may apply MONOPARA on other scenarios, such as searching stealthy prompts for redteaming. Replacing perplexity with other criteria, such as complexity (Li et al., 2024), for different purposes of constrained generation is also a meaningful research direction.

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Limitations

The current investigation of MONOPARA has the following limitations. First, using the target model as the paraphrase model is a natural technical choice. However, examining other paraphrasing models, especially those customized for paraphrasing, may lead to better performance. Second, our proposed method can not be applied to black-box LLMs such as ChatGPT⁸, PaLM (Chowdhery et al., 2023), Claude⁹, etc. This limitation arises from the necessity of access to the decoding phase, which in turn comes with far less computational cost due to zero training, and does not require the pre-existence of multiple prompt or instruction candidates. Third, while we conduct experiments on a wide range of tasks, their original prompts and responses are relatively short. This actually limits the operational space of MONOPARA. Experiments on tasks with longer inputs and outputs may provide additional evidence of MONOPARA's effectiveness.

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⁸https://chat.openai.com

⁹https://www.anthropic.com/claude

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Appendices

A Algorithm for Search-based MONOPARA

Algorithm 2 Search-based Decoding

Require: V▷ Vocabulary P_{tar}, P_{para} > Target and paraphrase models $k \triangleright$ Number of candidate sequences to retain **Ensure:** ▷ Best generated sequence x_{best} 1: $X_0 \leftarrow \{\emptyset\}$ \triangleright Initialize with empty sequence 2: while not end do $m \leftarrow \text{current decoding step}$ 3: $X'_m \gets \emptyset$ 4: for each $\mathbf{x}_{< m} \in X_{m-1}$ do 5: for each $x_m \in V$ do 6: Append $x_{\leq m} \circ x_m$ to X'_m 7: 8: end for end for 9: Use P_{para} for k candidates for each $x_{< m}$ 10: $X_m \leftarrow arg \ topk \ \{f(\mathbf{x}_{< m}, x_m)\}$ 11: $(x_{< m}, x_m) \in X'_m$ Select k candidates with lowest perplexity $end \leftarrow$ If any sequence ends with EOS12: 13: end while 14: $x_{best} \leftarrow$ select the sequence from X_m with the lowest perplexity by P_{tar}

15: return x_{best}

B Results on Llama-3-8B

Results on Llama-3-8B are illustrated in Tab. 3.

C Correlation Between Accuracy and Perplexity

To illustrate the interplay between task accuracy and prompt perplexity, we calculate the Pearson and Spearman correlation for each task based on the results in Tab. 1. The results are shown in Tab. 4. Most tasks show a strong negative correlation between perplexity and accuracy on both models except AG News, which is also discovered by Gonen et al. (2023) that for some of the tasks, there is not a negative correlation between perplexity and accuracy. The paraphrasing may be more helpful for cases where the nuances of expression don't matter so much (or there's enough room for error), but in domains where precision of language is important, perhaps perplexity-based paraphrasing might not be as helpful. AG News is a four-class news classification task with labels of "World", "Business", "Sci/Tech", and "Sports", which are not as easy as other binary classification tasks. As a result, the precision of the instruction for AG News is important. Additionally, we can see that the accuracy of AG News is not affected much under different methods, indicating that the accuracy is not so dependent on the perplexity of the prompt as other tasks. This indicates that MONOPARA works best for tasks with high distinction among labels.

D Reranking for MONOPARA

D.1 Implementation Setting

We implemented reranking on top of the linear combination of P_{tar} and P_{para} under two settings: (1) the coefficient α equals 0.5, which is kept consistent with the results presented in Tab. 1 for direct comparison; (2) the coefficient is randomly selected from $[0.1, 0.2, \dots, 0.6]$ for a larger search space. In both cases, we allow sampling from the top 3 tokens at every decoding step for randomness.

For each task, we use the 5 prompts as the original prompts (the same setting as Tab. 1) and randomly generate 100 paraphrases with the linear combination of P_{tar} and P_{para} for every single original prompt. For the generated 100 paraphrases, we use the same scheme as is described in §3 to calculate the perplexity: each paraphrase is instantiated with 1,000 random test samples, and the perplexity is averaged across all the 1,000 instantiated prompts. For budget k, we select the first k paraphrases from the 100 candidates and choose the prompt with the lowest average instantiated perplexity to be tested on the task.

D.2 Analysis

For the reranking setting (1), with additional randomness when sampling paraphrases from the linear combination of P_{tar} and P_{para} , a large enough budget (i.e., 100 paraphrases) can consistently catch paraphrased prompts with lower perplexity which achieve better task performance (Tab. 5). However, with a small budget of 10 or even 50, reranking can hardly surpass Mono-E in either perplexity or task performance. The reason is that with randomness allowed, the paraphrase is no longer decoded greedily at each token, which undermines the constraint on the perplexity and leads to a large variation of the perplexity of the resulting paraphrase. This further affects the performance of

Methods	Metric	GLUE Cola	Newspop	AG News	Tweet Offensive
Ori.	Acc PPL	$54.82 \pm 1.73 \\ 9.42 \pm 5.08$	73.82 ± 4.57 17.72 ± 6.11	60.37 ± 7.59 13.64 ± 4.97	63.25 ± 0.95 23.64 ± 4.61
Para	Acc PPL	$\begin{vmatrix} 43.69 \pm 9.02 \\ 32.07 \pm 8.43 \end{vmatrix}$	68.45 ± 13.24 29.41 ± 8.17	64.85 ± 3.73 23.77 ± 4.32	64.22 ± 1.48 46.14 ± 9.24
SPELL	Acc PPL	$\begin{array}{c} 46.91 \pm 2.33 \\ 7.98 \pm 1.58 \end{array}$	71.67 ± 5.30 12.47 ± 3.76	66.93 ± 3.70 11.29 ± 2.79	64.73 ± 0.76 8.79 ± 1.93
Mono-E	Acc PPL	$58.35 \pm 2.61 \\ 6.64 \pm 0.95$	77.85 ± 4.01 9.17 ± 2.59	65.45 ± 2.11 8.29 ± 1.47	64.90 ± 0.59 6.40 ± 3.61

Table 3: Performance of Llama-3-8B.

Model	Metric	GLUE Cola	Newspop	AG News	IMDB	DBpedia	Emotion	Tweet Offensive
Mistral	Pearson	-0.62	-0.88	0.19	-0.04	-0.70	-0.57	-0.48
	Spearman	-0.30	-0.99	0.30	-0.30	-0.39	-0.70	-0.30
Starling	Pearson	-0.83	-0.69	0.16	-0.60	-0.70	-0.96	-0.05
	Spearman	-0.90	-0.49	0.3	-0.3	-0.70	-0.89	-0.15

Table 4: Pearson and Spearman correlation between task accuracy and prompt perplexity w.r.t. the target model. Results are calculated based on Tab. 1.

these paraphrased prompts, which in turn proves the correlation between perplexity and task accuracy. Generally, we can expect vanilla Mono-E and reranking to break even with a large budget of around 50 paraphrases.

The reranking setting (2) is not as effective as setting (1), where even a budget of 100 could not surpass the vanilla Mono-E. The reason is that although a large search space is allowed with randomness on the combination coefficient α , the constraint on perplexity while decoding is undermined even further. With more randomness for paraphrase sampling, the results of setting (2) also show a higher standard deviation than setting (1).

E Correlation Between Standalone and Instantiated Prompts

To bridge the intuition gap, we investigate the correlation between the standalone prompt and its instantiated prompts. We instantiate each task-specific prompt with 1,000 input instances and the perplexity used for correlation evaluation is averaged over 5 prompts for each task. As shown in Tab. 6, the Pearson correlation is high (close to 1.0) in most cases for different datasets despite slight noise for Emotion under greedy paraphrase of prompts. We can conclude that there is a high correlation between instantiated and standalone prompts. Thus, it is valid to use the perplexity of the standalone prompt optimized by P_{tar} to serve as the constraint.

F Unperturbed Accuracy for Task II

Tab. 7 shows the task performance of three perturbation methods (Alpaca's average accuracy across 4 GLUE datasets) and performance degradation compared with the unperturbed prompt (as shown in the brackets). We can witness a narrow performance gap between perturbed and unperturbed original prompts for Mono-E, which is more robust than directly using the given prompt (Ori) or the greedily paraphrased one (Para). The reason is that Mono-E largely mitigates the effect of adversarial perturbations on the prompts and successfully rewrites the given prompts (whether perturbed or unperturbed) into higher-quality versions.

G BERTScore of Para and MONOPARA

We provide a case study on the paraphrase results and the according BERTScore in Tab. 8. We could see that both Para and Mono-E largely preserve the semantic meaning of the original prompt. Further, Para tends to use new vocabulary for diversity, while Mono-E prefers words that are more familiar to the target model, which is often the same as

Method	Metric	GLUE Cola	Newspop	AG News	IMDB	DBpedia	Emotion	Tweet Offensive
Ori.	Acc PPL	61.76 ± 2.93 15.72 ± 4.60	85.28 ± 3.45 12.60 ± 2.40		84.12 ± 4.89 16.41 ± 0.80	70.82 ± 2.27 8.10 ± 0.22	44.32 ± 1.57 16.48 ± 2.14	67.04 ± 0.95 19.25 ± 3.43
Para	Acc PPL	39.48 ± 8.19 78.01 ± 11.22	76.72 ± 16.54 49.37 ± 7.81		86.60 ± 4.86 22.27 ± 0.98			65.04 ± 1.46 53.65 ± 1.92
Mono-E	Acc PPL	63.96 ± 3.88 14.89 ± 2.75	88.96 ± 3.04 8.33 ± 1.30	72.20 ± 3.87 10.07 ± 2.93				67.00 ± 1.21 14.11 ± 3.53
Rerank (1)								
Budget = 10	Acc PPL	62.20 ± 3.47 14.27 ± 2.69	86.14 ± 3.14 11.46 ± 1.99	69.31 ± 4.29 11.92 ± 3.97	85.02 ± 4.13 15.95 ± 2.83			66.12 ± 2.15 15.63 ± 3.57
Budget = 50	Acc PPL	63.84 ± 2.46 13.54 ± 3.16	85.86 ± 5.36 10.53 ± 2.85		86.52 ± 5.86 13.44 ± 2.22			67.74 ± 1.45 13.94 ± 3.86
Budget = 100	Acc PPL	$64.58 \pm 3.50 \\ 10.22 \pm 2.32$	89.82 ± 2.04 7.53 ± 1.82	$72.33 \pm 4.17 \\ 9.52 \pm 4.20$	87.61 ± 4.93 12.88 ± 3.01	$72.52 \pm 3.16 \\ 8.16 \pm 1.67$		68.5 ± 1.84 11.56 ± 4.44
Rerank (2)								
Budget = 10	Acc PPL	62.35 ± 4.77 15.63 ± 3.85	86.96 ± 4.61 12.27 ± 3.99		84.86 ± 4.71 16.43 ± 2.17			66.63 ± 4.53 18.87 ± 4.48
Budget = 50	Acc PPL	62.08 ± 3.97 14.42 ± 4.16	86.50 ± 5.10 10.24 ± 4.36		86.03 ± 5.24 14.33 ± 3.55			65.15 ± 5.03 18.53 ± 4.54
Budget = 100	Acc PPL	64.35 ± 4.91 11.67 ± 4.37	87.82 ± 4.48 8.93 ± 3.15		86.64 ± 5.16 13.47 ± 3.84			67.80 ± 8.95 16.65 ± 3.53

Table 5: Reranking for ensemble-based MONOPARA. The best results of each task are **bolded** and the second-best are *italicized*.

	Newspop	IMDB	DBpedia	Emotion	Tweet
Ori	0.949	0.952	0.895	0.839	0.974
Para	0.813	0.951	0.835	0.645	0.871
Mono-E	0.956	0.895	0.927	0.931	0.968

Table 6: Pearson correlation between the perplexity of standalone prompt and its instantiated prompts. Pearson correlation is high (close to 1.0) in most cases, indicating a high correlation.

	Ori	Para	Mono-E
Un.	56.67	58.31	65.94
Cha.	51.03 (-9.95%)	53.62 (-8.04%)	65.81 (-0.20%)
Word	52.41 (-7.51%)	57.39 (-1.58%)	67.23 (+1.96%)
Sem.	49.42 (-12.79%)	54.22 (-7.01%)	64.35 (-2.4%)

Table 7: Performance degradation of Alpaca model compared with the unperturbed prompt. *Un.*, *Cha.*, and *Sem.* are short for unperturbed, character, and semantic, respectively, referring to different prompt perturbation methods.

in the original prompt. This might be the reason why Para results in lower BertScore compared to Mono-E and Mono-S.

H Ablation Study on Alpha Value

We provide results with various alpha values in Tab. 9, which illustrates the impact of alpha values on model accuracy and paraphrase perplexity across various datasets on the Mistral-7B model. With the increase of α value, the perplexity (PPL) of the paraphrase monotonically goes down due to the design and motivation of our method. Given the low perplexity, we compare the task accuracy of various alpha values. For $\alpha = 0.4$ or 0.6, the model shows outstanding performance on some of the datasets. But increasing alpha to 0.7 results in a nonsensical prompt though the perplexity is super low. From the results we can also see that the performance just corrupted with this nonsensical prompt. The setting of α should seek a balance between lower perplexity and the preservation of the original semantics. As a result, alpha = 0.5(Mono-E) offers a balanced and reliable performance, making it a suitable default choice.

	Content	BertScore
Ori Prompt	In this task, you are presented with a short article. Your objective is to classify the article according to its category using the following labels: World, Sports, Business, Sci/Tech. Tag the text as "World" if it involves information about global events or issues. Mark it as "Sports" if it deals with sports-related content. Label it "Business" if it pertains to business affairs, markets, or economics. Assign "Sci/Tech" if it covers scientific or technological developments.	_
Para	In this assignment , you are given a brief article. Your goal is to categorize the article based on its topic using these tags: World, Sports, Business, Sci/Tech. Identify it as "World" if it discusses international events or matters. Designate it as "Sports" if it focuses on athletic content. Categorize it as "Business" if it concerns commercial activities, markets, or the economy. Label it "Sci/Tech" if it reports on advancements in science or technology.	86.02
Mono-E	In your task you will have an input which consists of a single article. You have to sort this article according to its category using a list which consists of 4 categories: "World", "Sci/tech", "Business", or "Sports". You should mark it with the appropriate label based on the content. The article should be labeled with the "Sports" category, when its topic deals with sports. When the article is about business, you need to mark it as a 'business' label. If you are talking about science and tech developments then label the content with "Sci/Tech", if it is a world-related issue or event then label it with "World".	89.63

Table 8: Case study on the paraphrase results and BERTScore. Para tends to use new vocabulary for diversity, while Mono-E prefers words that are more familiar to the target model, which is often the same as in the original prompt.

Method	Metric	GLUE Cola	Newspop	AG News	IMDB	DBpedia	Emotion	Tweet
Ori.	Acc	61.76 ± 2.93	85.28 ± 3.45	67.68 ± 3.47	84.12 ± 4.89	70.82 ± 2.27	44.32 ± 1.57	67.04 ± 0.95
	PPL	15.72 ± 4.60	12.60 ± 2.40	12.74 ± 1.07	16.41 ± 0.80	8.10 ± 0.22	16.48 ± 2.14	19.25 ± 3.43
Para	Acc	39.48 ± 8.19	76.72 ± 16.54	71.60 ± 2.70	86.60 ± 4.86	70.22 ± 5.71	43.65 ± 3.41	65.04 ± 1.46
	PPL	78.01 ± 11.22	49.37 ± 7.81	28.37 ± 2.58	22.27 ± 0.98	28.34 ± 1.36	46.53 ± 5.30	53.65 ± 1.92
Mono-E	Acc	63.96 ± 3.88	88.96 ± 3.04	72.20 ± 3.87	87.58 ± 3.27	72.07 ± 3.54	47.76 ± 3.72	67.00 ± 1.21
	PPL	14.89 ± 2.75	8.33 ± 1.30	10.07 ± 2.93	13.05 ± 1.86	8.85 ± 0.88	13.67 ± 1.87	14.11 ± 3.53
$\alpha = 0.1$	Acc	60.80 ± 4.28	84.98 ± 3.41	69.09 ± 4.01	85.52 ± 1.72	70.42 ± 3.66	44.80 ± 2.31	65.56 ± 5.07
	PPL	15.61 ± 2.51	12.32 ± 1.01	12.03 ± 2.96	15.70 ± 1.85	9.61 ± 0.61	16.16 ± 1.11	18.49 ± 2.84
$\alpha = 0.2$	Acc	61.80 ± 5.63	85.32 ± 3.56	71.49 ± 4.32	85.08 ± 4.97	70.54 ± 5.23	44.04 ± 2.44	66.80 ± 5.19
	PPL	15.22 ± 2.06	11.56 ± 1.27	11.68 ± 3.25	15.30 ± 1.55	9.23 ± 0.79	15.71 ± 0.20	16.92 ± 2.68
$\alpha = 0.3$	Acc	61.54 ± 5.85	86.72 ± 4.94	72.4 ± 2.77	86.68 ± 4.21	71.90 ± 3.91	44.96 ± 2.67	67.56 ± 3.59
	PPL	15.18 ± 2.84	10.21 ± 1.22	11.06 ± 2.74	14.42 ± 1.05	8.95 ± 0.75	15.21 ± 1.04	15.87 ± 3.61
$\alpha = 0.4$	Acc	62.72 ± 4.37	89.44 ± 3.08	71.31 ± 2.27	87.86 ± 3.37	72.18 ± 3.44	45.58 ± 1.55	67.70 ± 1.60
	PPL	14.93 ± 2.91	9.16 ± 0.57	10.39 ± 3.56	13.81 ± 2.60	9.04 ± 1.18	14.35 ± 0.90	15.18 ± 3.72
$\alpha = 0.6$	Acc	64.30 ± 6.63	90.86 ± 3.24	71.66 ± 10.09	87.74 ± 4.04	71.36 ± 6.25	47.12 ± 1.66	66.26 ± 3.24
	PPL	11.49 ± 1.00	7.53 ± 0.68	9.38 ± 0.88	12.15 \pm 2.47	7.11 ± 1.08	13.12 ± 0.79	13.29 ± 2.58
$\alpha = 0.7$	Acc PPL	$\begin{array}{c} 41.50 \pm 13.68 \\ 8.80 \pm 0.42 \end{array}$	54.52 ± 22.29 3.84 ± 0.91	50.56 ± 21.95 3.43 ± 0.36	$\begin{array}{c} 64.84 \pm 16.01 \\ 4.99 \pm 0.28 \end{array}$	$\begin{array}{c} 48.12 \pm 16.26 \\ 2.34 \pm 0.25 \end{array}$	38.62 ± 1.59 4.28 ± 0.55	59.34 ± 7.75 6.58 ± 1.40

Table 9: Results with varying α values for Mono-E on Mistral-7B. The best accuracy for each task is in **bold**. For $\alpha = 0.4$ or 0.6, the model shows outstanding performance on most of the datasets. But increasing alpha to 0.7 results in a nonsensical prompt though the perplexity is super low, leading to corrupted task performance.