# Zero-Shot Cross-Lingual Dependency Parsing through Contextual Embedding Transformation

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### Abstract

Linear embedding transformation has been shown to be effective for zero-shot crosslingual transfer tasks and achieve surprisingly promising results. However, cross-lingual embedding space mapping is usually studied in static word-level embeddings, where a space transformation is derived by aligning representations of translation pairs that are referred from dictionaries. We move further from this line and investigate a contextual embedding alignment approach which is sense-level and dictionary-free. To enhance the quality of the mapping, we also provide a deep view of properties of contextual embeddings, i.e., the anisotropy problem and its solution. Experiments on zero-shot dependency parsing through the concept-shared space built by our embedding transformation substantially outperform state-of-the-art methods using multilingual embeddings.

### 1 Introduction

Cross-lingual embedding space alignment (Mikolov et al., 2013b; Artetxe et al., 2016; Xing et al., 2015; Conneau et al., 2018) recently has been attracted a lot of attention because cross-lingual model transfer is effectively facilitated by shared semantic spaces in NLP tasks, e.g., named entity recognition (Xie et al., 2018), part-of-speech tagging (Hsu et al., 2019), and dependency parsing (Schuster et al., 2019), where dependency paring is scoped out in this paper. Compared with the delexicalized parsers (McDonald et al., 2011), multilingual word embeddings have been demonstrated to significantly improve the performance of zero-shot dependency parsing by bridging the lexical feature gap (Guo et al., 2015).

With the remarkable development of monolingual contextual pre-trained models (Peters et al., 2018; Devlin et al., 2019; Radford et al., 2019), which dramatically outperform static word embeddings (Mikolov et al., 2013a; Pennington et al., 2014; Bojanowski et al., 2017) in broad NLP applications, increasing number of researchers have started focusing on contextual representation alignment for cross-lingual dependency parsing (Schuster et al., 2019; Wang et al., 2019). Moreover, with the appearance of multilingual pre-trained models, such as Multilingual BERT (mBERT) (Devlin et al., 2019), zero-shot dependency parsing becomes easier by utilizing the large vocabulary of the multilingual models (Kondratyuk and Straka, 2019).

Our approach is most similar to Schuster et al. (2019), which maps a target language space into a source language space through a linear transformation to realize zero-shot transfer in dependency parsing. Typically, a transformation is usually derived by word-level embedding alignment, while we explore a sense-level embedding alignment method to map bilingual spaces more precisely, where sense-level representations are split from multi-sense word-level embeddings. Furthermore, our mapping approach is dictionary-free which utilizes the silver token pairs from parallel corpora and eliminates the necessity of gold dictionaries. The experimental results of zero-shot dependency parsing demonstrate that two parser evaluation scores (UAS and LAS) of sense-level mapping are always better than of word-level one. Moreover, we also notice the anisotropy problem (Ethayarajh, 2019) (defined in Section 3.2) in contextual embeddings, which potentially deteriorate the performance of the zero-shot transfer task. We significantly mitigate this drawback by leveraging a prepossessing step, iterative normalization (IN) (Zhang et al., 2019), which is originally used for improving the performance of static embedding mapping on the bilingual dictionary induction task.

Zero-shot dependency parsing experiments are conducted on *Universal Dependencies treebank* 



Figure 1: The target tokens (left, blue) and the source tokens (right, black) are aligned by *Fast Align*, so their contextual embeddings can be aligned as well.

v2.6 (Zeman et al., 2020), which shows that our results obtain a substantial gain compared with state-of-the-art methods using multilingual fastText and mBERT <sup>1</sup>.

## 2 Linear Cross-lingual Space Alignment

Let denote  $X \in \mathbb{R}^{d \times N}$  as the word embedding matrix for a target language <sup>2</sup>, and Y as the word embedding matrix for a source language. For each column of the target embedding matrix  $x_i \in \mathbb{R}^d$ , it has one source embedding vector  $y_i \in \mathbb{R}^d$  corresponding to a source word translated from the target word *i*. We aim to derive a linear transformation matrix  $\hat{W}$  used for mapping from the target language space to the source language space. This can be learned by minimizing the Frobenius norm:

$$\hat{W} = \underset{W \in \mathbb{R}^{d \times d}}{\arg\min} \|WX - Y\|_F$$
(1)

Furthermore, Xing et al. (2015) show that the quality of space alignment is successfully improved with the orthogonal restriction, i.e,  $W^T W = I$ . Thus, the problem can be solved by Procrustes approach (Schönemann, 1966):

$$\hat{W} = \underset{W \in \mathbb{O}^{d \times d}}{\arg\min} \|WX - Y\|_F = UV^T$$
s.t.  $U\Sigma V^T = \operatorname{svd}(YX^T)$ 
(2)

where  $\mathbb{O}^{d \times d}$  is the set of orthogonal matrices.

#### 3 Method

#### 3.1 Contextual Embedding Transformation

An unsupervised bidirectional word alignment algorithm based on *IBM Model 2* (Brown et al., 1993), *Fast Align* (Dyer et al., 2013), is first applied to a parallel corpus to derive silver aligned token pairs. We then respectively feed the parallel corpus to the BERTs of the target and the source languages and extract the outputs as contextual embeddings. As shown in Figure 1, *Fast Align* bridges "links" between silver token pairs, and between the embeddings of the token pairs as well. Thus, for each target type, a collection of its contextual embeddings can be obtained, as well as a collection of contextual embeddings of its aligned source tokens. Vectors are normalized to satisfy the orthogonal condition.

Motivated by the assumption that multiple senses of a type can construct multiple distinct clusters in its collection (Schuster et al., 2019), we derive several sense-level (cluster-level) embeddings for a type by averaging vectors in each cluster. This splits the representations of multi-sense words and helps the anchor-driven space mapping in a finer resolution. To find clusters, we utilize k-means to cluster contextual embeddings in the vector collection of each type, and adaptively find the optimal k by an elbow-based method Satopaa et al. (2011). Contextual vectors are only clustered in the target side to obtain sense-level embeddings, while the aligned sense-level embeddings in the source side can also be simultaneously derived because embeddings have been already "linked" by Fast Align. We next build a sense embedding matrix  $X_s$  for the target language by putting the senselevel embeddings in each column, and meanwhile construct a column-wise aligned sense embedding matrix  $Y_s$  in the source side. Finally, we obtain the optimal linear mapping  $\hat{W}$  from  $X_s$  to  $Y_s$  by Equation 2. Pseudo code of transformation method is in Appendix A.

<sup>&</sup>lt;sup>1</sup>Code is available at: https://github.com/ felixxu/ZeroShot-CrossLing-Parsing.

<sup>&</sup>lt;sup>2</sup>Different from usual settings, we use x-related symbols for target data and y-related ones for source data.



Figure 2: (a) Spanish vectors (purple arrows) cannot well fit to English vectors (pink arrows) by a linear transformation because they gather in different degrees of cones (different angles between vectors), where dash lines are mapped vectors. (b) After iterative normalization, Spanish and English vectors are uniformly distributed (same angles between vectors). They can be perfectly fit after mapping now.

#### 3.2 Anisotropy in Embedding Spaces

Our findings show that contextual embeddings always hold anisotropic property, i.e., they are not uniformly distributed in the space and gather toward a narrow range of orientations. Importantly, degrees of anisotropy across languages are various, which undermines the quality of cross-lingual mappings. A toy example of how the anisotropy affect mappings is illustrated in Figure 2a. One metric for anisotropy is to calculate the average cosine similarity distance of randomly selected vectors. The higher the distance is, the narrower directions vectors point to. Note that the distance for an isotropic space is 0. To mitigate this problem, we introduce iterative normalization. For each token i, the embedding vector  $x_i$  is forced to be zero-mean firstly in each iteration:

$$x_{i} = x_{i} - \frac{1}{N} \sum_{i=1}^{N} x_{i}$$
(3)

and then normalize it to a fixed length:

$$x_i = \frac{x_i}{\|x_i\|_2}$$
(4)

The two steps are repeated until convergence. N is the total number of embeddings. The iterative preprocessing enforces the space to be uniformally distributed, and relative angles between vectors across languages to be more similar (Figure 2b).

#### 3.3 Zero-shot Transfer

A parser is first trained on a source language treebank, where outputs of a frozen BERT are used as embeddings. To apply the pre-trained parser to the



Figure 3: The workflow of how zero-shot transfer processes in our model architecture.

target languages, we first replace the source BERT with the target BERT. Then, iterative normalization is operated to enforce contextual embeddings in a near-isotropic space. At last, we map the embeddings to the source language space. Specifically, for each target token *i*, its contextual representation  $x_i$  is mapped by  $\hat{W}x_i$ . The processing of zero-shot dependency parsing is visualized in Figure 3. Note that the space of pre-trained model has already fit to be near-isotropic by utilizing iterative normalization during training.

#### **4** Experiment

Our parser is the deep biaffine model from Dozat and Manning (2016) where hyperparameters are almost unchanged. The settings of all hyperparameters are listed in Appendix B. English is set as the source language and other languages are targets. In our experiments, we select 6 target languages from 4 language families for which we have offthe-shelf monolingual pre-trained BERT models (base-size). We train the parsing model only in the English treebank, and directly evaluate zero-shot transfer performance on the target languages.

## 4.1 Baseline

**Aligned fastText:** Our first baseline is multilingual fastText aligned by the RCSLS method (Joulin et al., 2018; Bojanowski et al., 2017) which is straightforwardly employed to the embedding layer for the corresponding language.

lang (treebank)	en (ewt)		es (gsd)		pt (gsd)		ro (rrt)		pl (lfg)		<b>fi</b> ( <i>tdt</i> )		<b>el</b> ( <i>gdt</i> )	
	UAS	LAS	UAS	LAS	UAS	LAS	UAS	LAS	UAS	LAS	UAS	LAS	UAS	LAS
aligned fastText	88.55	86.36	73.57	65.13	72.41	60.69	60.27	46.79	75.88	59.48	62.32	40.78	71.51	61.46
mBERT uncased	93.45	91.52	82.11	72.51	80.89	68.90	72.08	56.91	85.27	69.76	72.76	49.64	81.72	68.35
mBERT cased	93.32	91.34	82.83	74.08	80.80	68.68	70.76	56.04	83.77	68.01	71.82	48.84	78.24	65.92
word-level	93.70	01.79	82.43	73.86	79.77	67.35	71.13	57.28	84.58	69.53	74.65	51.06	82.29	69.88
sense-level	95.70	<u>91.78</u>	82.55	73.92	80.34	67.80	71.46	57.57	84.71	69.56	74.81	51.14	82.33	70.10
word-level + IN	94.21	92.01	83.70	75.14	81.48	69.04	74.65	59.68	84.32	70.45	75.07	51.75	83.76	71.11
sense-level + IN	74.21 9.	92.01	83.91	75.39	81.99	69.49	74.78	59.83	84.57	70.52	75.31	51.99	84.05	71.26

Table 1: UAS and LAS of zero-shot evaluation for various languages on test files. The highest scores are bolded and the second highest scores are underlined. Language families are split by dash lines. lang = language, en = English, es = Spanish, pt = Portuguese, ro = Romanian, pl = Polish, fi = Finnish, el = Greek.



Figure 4: (a) Discrepancy of anisotropic degrees for all tested language pairs, where scores of anisotropic degree are calculated by the mean cosine similarity between 1000 randomly selected vectors in their language spaces. (b) The isotropic degrees basically decrease to 0 at the first iteration and converge afterwards.

**mBERT:** We compare our approach with both uncased and cased version of mBERT. Outputs of mBERT are directly used for the embedding layer.

#### 4.2 Settings

Following the analysis that top layers of BERT contain more semantic information (Jawahar et al., 2019), our contextual representation are normalized mean vector of the last 4 layers of BERT. The parallel corpora used to extract contextual embeddings are obtained from *ParaCrawl v6.0*<sup>3</sup>. For each language pairs, we select 1M parallel sentences whose length is shorter than 150. Since some noisy alignments are produced during *Fast Align*, we only take one-to-one token alignment into consideration. The dataset used for cross-lingual dependency parsing is the *Universal Dependencies treebank v2.6*<sup>4</sup> (Zeman et al., 2020).

We store up to 10K contextual vectors extracted from BERT for non-OOV tokens <sup>5</sup>. Vectors in the collection of a target type are clustered to derive sense-level embeddings only if the token occurs more than 100 times. Otherwise, the representation for the token is the basic word-level embedding, i.e., the mean vector of its vector collection. Experiments of word-level embedding alignment are also conducted to compare with sense-level results.

## 4.3 Iterative Normalization Preprocessing

Forcing contextual embedding vectors in  $X_s$  and  $Y_s$  to be zero-mean is straightforward. Nevertheless, it is difficult to look for the universal mean vector of contextual embeddings when we train the English parser, because we do not have such an exact mean vector for all possible contextual embeddings. Thus, to successfully implement IN for pre-training the parser, we calculate the approximate universal mean vector by averaging all contextual vectors of every occurrence of tokens from the given training dataset in each iteration. IN runs for 5 iterations, which is sufficient for convergence.

## 5 Discussion

## 5.1 Why Contextual Embedding Mapping?

**Compare with Previous Methods:** Overall results are shown in Table 1. In the first place, our contextual-aware embedding mapping (row 4 - 7)

<sup>&</sup>lt;sup>3</sup>www.paracrawl.eu

<sup>&</sup>lt;sup>4</sup>https://lindat.mff.cuni.cz/ repository/xmlui/handle/11234/1-3226

<sup>&</sup>lt;sup>5</sup>We do not use the composition of subword vectors to approximately represent OOV tokens, because our preliminary results show this hurts the mapping.

exceeds the aligned fastText (row 1) by a large margin. Moreover, our sense-level mapping without IN preprocessing outperforms uncased and cased mBERT by 0.67% and 1.42% on LAS on average, and mapping with preprocessing further outperforms them by 2.07% and 2.82% on average.

**Dictionary-free Mapping:** Typically, aligned embeddings take a static dictionary as reference but high-quality manual dictionaries are still rare (Ruder et al., 2019). Our mapping skips the wordlevel alignment in dictionaries, and directly aligns the embeddings from parallel corpora which offers a large scope of token alignments.

**Sense-level Mapping:** Different from static embeddings whose words only have one unique representation, our contextual embeddings also take advantage of multiple representations for multi-sense words to improve the quality of anchor-driven mapping. In Table 1, the performance of sense-level mapping always surpasses word-level mapping.

## 5.2 Effect of Iterative Normalization

Figure 4a illustrates the various degrees of anisotropy among different language pairs. As we expect, the anisotropic degree for English (pink, right) is basically constant, but there is large discrepancy between other target languages (blue, left). After IN preprocessing, all language spaces are approximately isotropic, where their scores of anisotropy dramatically reduce near to zero. One example of how the anisotropic degree drops down in each iteration of IN for the Spanish-English pair is illustrated in Figure 4b. IN assists the aligned embeddings in building more similar relative angles across embeddings in different language spaces. As shown in Table 1, this preprocessing improves an absolute gain of 1.37% for word-level mapping and 1.40% for sense-level mapping on average.

## 6 Conclusion

We proposed a linear, dictionary-free and senselevel contextual mapping approach by exploiting parallel corpus which has shown promising results and substantial improvement compared with multilingual fastText and mBERT in the zero-shot dependency parsing task. We also revealed that various degrees of anisotropy hurts the performance of mapping, and introduced iterative normalization to alleviate it by enforcing contextual embeddings to be uniformly distributed, which also has indicated the benefits of isotropy.

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# A Pseudo Code of Contextual Embedding Transformation

Pseudo Code is shown in Alogirthm 1.

# **B** Hyperparamters

Here we list all hyperparamters for our pre-trained parser in Table 2.

Hyperparameters	Value			
Batch size	128			
Arc representation dim	500			
Tag representation dim	100			
Dropout	0.3			
LSTM hidden size	500			
LSTM # layers	3			
Pos tag embedding dim	100			
Grad norm	5			
# epochs	200			
Patience	25			
Optimizer	Dense Sparse ADAM			
Learning rate	0.0008			
Encoding Layer	<b>Bi-LSTM</b>			

Table 2: Hyperparameters for deep biaffine dependencyparser training.

# **C** pre-trained Monolingual BERTs

In Table 3, we list the names of pre-trained monolingual BERTs from huggingface <sup>6</sup> that we used in our experiments.

Language	Model name
mbert uncased	bert-base-multilingual-uncased
mbert cased	bert-base-multilingual-cased
en	bert-base-uncased
es	dccuchile/bert-base-spanish-wwm-uncased
pt	neuralmind/bert-base-portuguese-cased
ro	dumitrescustefan/bert-base-romanian-uncased-v1
pl	dkleczek/bert-base-polish-uncased-v1
fi	bert-base-finnish-uncased-v1
el	nlpaueb/bert-base-greek-uncased-v1

Table 3: Names of Pre-trained BERT models.

<sup>&</sup>lt;sup>6</sup>https://huggingface.co/models

#### Algorithm 1 Contextual Embedding Transformation

**Require:** Target Corpus  $\mathcal{X}$ , source Corpus  $\mathcal{Y}$ , target pre-trained BERT  $\mathcal{B}_x$ , source pre-trained BERT  $\mathcal{B}_y$ , where  $\mathcal{X}$  is the translation corpus of  $\mathcal{Y}$ 

```
1: function CONTEXTUAL-TRANSFORMATION(\mathcal{X}, \mathcal{Y}, \mathcal{B}_x, \mathcal{B}_y)
 2:
           # Part 1: Collect embeddings
 3:
          \mathcal{I} \leftarrow \text{FAST-ALIGN}(\mathcal{X}, \mathcal{Y}) \triangleright \mathcal{I} is an index-aligned corpus, where each line is composed of index pairs of aligned tokens
     for each parallel sentence.
 4:
           Initialize C \leftarrow Empty Hash Map
          for index i in LENGTH(\mathcal{X}) do

X \leftarrow \mathcal{X}[i], Y \leftarrow \mathcal{Y}[i], I \leftarrow \mathcal{I}[i]

E_X \leftarrow \mathcal{B}_x(X)

E_Y \leftarrow \mathcal{B}_y(Y)
 5:
                                                                                                                               ▷ number of sentences in the corpus
 6:
 7:
                                                                                                                               ▷ Contextual embeddings of tokens:
 8:
 9:
                for index j in LENGTH(X) do
                                                                                                                                \triangleright number of tokens in the sentence
10:
                     x \leftarrow X[j], e_x \leftarrow E_X[j]
                     e_y \leftarrow E_Y[I(j)] \triangleright Find the aligned embedding by looking at I, where I(j) is the index of aligned source token.
C[x].append((e_x, e_y))
11:
12:
13:
                 end for
           end for
14:
15:
16:
           # Part 2: Obtain aligned sense-level embeddings
17:
           Initialize Empty matrix X_s, Y_s
           for target type x in C.keys() do
18:
19:
                c_x \leftarrow \text{all target embeddings } \mathbf{e}_x \text{ in } \mathcal{C}[x]
                 c_y \leftarrow \text{all target embeddings } \mathbf{e}_y \text{ in } \mathcal{C}[x]
20:
21:
                 k \leftarrow \text{ELBOW-BASED}(c_x)
                                                                                                                                  ▷ Find optimal number of clusters
22:
                 for Subcluster c_{x_i} in K-MEANS(k, c_x) do
                      Get subcluster c_{y_i} due to aligned pair ((e_x, e_y)) in \mathcal{C}[x]
23:
                      mean_x \leftarrow mean \text{ vector of } c_{x_i}
24:
25:
                     mean_y \leftarrow mean \ vector \ of \ c_{y_i}
26:
                      Put mean_x in X_s as a column
                     Put mean_y in Y_s as a column
27:
28:
                end for
29:
           end for
30:
           # Part 3: Derive embedding transformation U\Sigma V^T = \operatorname{svd}(YX^T)
31:
32:
           \hat{W} = UV^T
33:
34:
           return \hat{W}
35: end function
```