

# Compare, Compress and Propagate: Enhancing Neural Architectures with Alignment Factorization for Natural Language Inference

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## Abstract

This paper presents a new deep learning architecture for Natural Language Inference (NLI). Firstly, we introduce a new architecture where alignment pairs are compared, compressed and then propagated to upper layers for enhanced representation learning. Secondly, we adopt factorization layers for efficient and expressive compression of alignment vectors into scalar features, which are then used to augment the base word representations. The design of our approach is aimed to be conceptually simple, compact and yet powerful. We conduct experiments on three popular benchmarks, SNLI, MultiNLI and SciTail, achieving competitive performance on all. A lightweight parameterization of our model also enjoys a  $\approx 3$  times reduction in parameter size compared to the existing state-of-the-art models, e.g., ESIM and DIIN, while maintaining competitive performance. Additionally, visual analysis shows that our propagated features are highly interpretable.

## 1 Introduction

Natural Language Inference (NLI) is a pivotal and fundamental task in language understanding and artificial intelligence. More concretely, given a premise and hypothesis, NLI aims to detect whether the latter *entails* or *contradicts* the former. As such, NLI is also commonly known as Recognizing Textual Entailment (RTE). NLI is known to be a significantly challenging task for machines whose success often depends on a wide repertoire of reasoning techniques.

In recent years, we observe a steep improvement in NLI systems, largely contributed by the release of the largest publicly available corpus for NLI - the Stanford Natural Language Inference (SNLI) corpus (Bowman et al., 2015) which comprises 570K hand labeled sentence pairs. This has

improved the feasibility of training complex neural models, given the fact that neural models often require a relatively large amount of training data.

Highly competitive neural models for NLI are mostly based on soft-attention alignments, popularized by (Parikh et al., 2016; Rocktäschel et al., 2015). The key idea is to learn an alignment of sub-phrases in both sentences and learn to compare the relationship between them. Standard feed-forward neural networks are commonly used to model similarity between aligned (decomposed) sub-phrases and then aggregated into the final prediction layers.

Alignment between sentences has become a staple technique in NLI research and many recent state-of-the-art models such as the Enhanced Sequential Inference Model (ESIM) (Chen et al., 2017b) also incorporate the alignment strategy. The difference here is that ESIM considers a non-parameterized comparison scheme, i.e., *concatenating* the subtraction and element-wise product of aligned sub-phrases, along with two original sub-phrases, into the final comparison vector. A bidirectional LSTM is then used to aggregate the compared alignment vectors.

This paper presents a new neural model for NLI. There are several new novel components in our work. Firstly, we propose a *compare, compress and propagate* (ComProp) architecture where compressed alignment features are propagated to upper layers (such as a RNN-based encoder) for enhancing representation learning. Secondly, in order to achieve an efficient propagation of alignment features, we propose alignment factorization layers to reduce each alignment vector to a single scalar valued feature. Each scalar valued feature is used to augment the base word representation, allowing the subsequent RNN encoder layers to benefit from not only global but also cross sentence information.

There are several major advantages to our proposed architecture. Firstly, our model is relatively compact, i.e., we compress alignment feature vectors and augment them to word representations instead. This is to avoid large alignment (or match) vectors being propagated across the network. As a result, our model is more parameter efficient compared to ESIM since the width of the middle layers of the network is now much smaller. To the best of our knowledge, this is the first work that explicitly employs such a paradigm.

Secondly, the explicit usage of compression enables improved interpretability since each alignment pair is compressed to a scalar and hence, can be easily visualised. Previous models such as ESIM use subtractive operations on alignment vectors, edging on the intuition that these vectors represent contradiction. Our model is capable of visually demonstrating this phenomena. As such, our design choice enables a new way of deriving insight from neural NLI models.

Thirdly, the alignment factorization layer is expressive and powerful, combining ideas from standard machine learning literature (Rendle, 2010) with modern neural NLI models. The factorization layer tries to decompose the alignment vector (constructed from the variations of  $a - b$ ,  $a \odot b$  and  $[a; b]$ ), learning higher-order feature interactions between each compared alignment. In other words, it models the second-order (pairwise) interactions between *each* feature in *every* alignment vector using factorized parameters, allowing more expressive comparison to be made over traditional fully-connected layers (FC). Moreover, factorization-based models are also known to be able to model low-rank structure and reduce risks of overfitting. The effectiveness of the factorization alignment over alternative baselines such as feed-forward neural networks is confirmed by early experiments.

The major contributions of this work are summarized as follows:

- We introduce a *Compare, Compress and Propagate* (ComProp) architecture for NLI. The key idea is to use the myriad of generated comparison vectors for augmentation of the base word representation instead of simply aggregating them for prediction. Subsequently, a standard compositional encoder can then be used to learn representations from the augmented word representations. We

show that we are able to derive meaningful insight from visualizing these augmented features.

- For the first time, we adopt expressive factorization layers to model the relationships between soft-aligned sub-phrases of sentence pairs. Empirical experiments confirm the effectiveness of this new layer over standard fully connected layers.
- Overall, we propose a new neural model - CAFE (ComProp Alignment-Factorized Encoders) for NLI. Our model achieves state-of-the-art performance on SNLI, MultiNLI and the new SciTail dataset, outperforming existing state-of-the-art models such as ESIM. Ablation studies confirm the effectiveness of each proposed component in our model.

## 2 Related Work

Natural language inference (or textual entailment recognition) is a long standing problem in NLP research, typically carried out on smaller datasets using traditional methods (Maccartney, 2009; Dagan et al., 2006; MacCartney and Manning, 2008; Iftene and Balahur-Dobrescu, 2007).

The relatively recent creation of 570K human annotated sentence pairs (Bowman et al., 2015) have spurred on many recent works that use neural networks for NLI. Many advanced neural architectures have been proposed for the NLI task, with most exploiting some variants of neural attention which learn to pay attention to important segments in a sentence (Parikh et al., 2016; Chen et al., 2017b; Wang and Jiang, 2016b; Rocktäschel et al., 2015; Yu and Munkhdalai, 2017a).

Amongst the myriad of neural architectures proposed for NLI, the ESIM (Chen et al., 2017b) model is one of the best performing models. The ESIM, primarily motivated by soft subphrase alignment in (Parikh et al., 2016), learns alignments between BiLSTM encoded representations and aggregates them with another BiLSTM layer. The authors also propose the usage of subtractive composition, claiming that this helps model contradictions amongst alignments.

Compare-Aggregate models are also highly popular in NLI tasks. While this term was coined by (Wang and Jiang, 2016a), many prior NLI models follow this design (Wang et al., 2017; Parikh

et al., 2016; Gong et al., 2017; Chen et al., 2017b). The key idea is to aggregate matching features and pass them through a dense layer for prediction. (Wang et al., 2017) proposed BiMPPM, which adopts multi-perspective cosine matching across sequence pairs. (Wang and Jiang, 2016a) proposed a one-way attention and convolutional aggregation layer. (Gong et al., 2017) learns representations with highway layers and adopts ResNet for learning features over an interaction matrix.

There are several other notable models for NLI. For instance, models that leverage directional self-attention (Shen et al., 2017) or Gumbel-Softmax (Choi et al., 2017). DGEM is a graph based attention model which was proposed together with a new entailment challenge dataset, SciTail (Khot et al., 2018). Pretraining have been known to also be highly useful in the NLI task. For instance, contextualized vectors learned from machine translation (McCann et al., 2017) (CoVe) or language modeling (Peters et al., 2018) (ELMo) have shown to be able to improve performance when integrated with existing NLI models.

Our work compares and compresses alignment pairs using factorization layers which leverages the rich history of standard machine learning literature. Our factorization layers incorporate highly expressive factorization machines (FMs) (Rendle, 2010) into neural NLI models. In standard machine learning tasks, FMs remain a very competitive choice for learning feature interactions (Xiao et al., 2017) for both standard classification and regression problems. Intuitively, FMs are adept at handling data sparsity (typically interactions) by using factorized parameters to approximate a feature matching matrix. This makes it suitable in our model architecture since feature interaction between subphrase alignment pairs is typically very sparse as well.

A recent work (Beutel et al., 2018) reports an interesting empirical study pertaining to the ability of standard FC layers and their ability to model ‘cross features’ (or multiplicative features). Their overall finding suggests that while standard ReLU FC layers are able to approximate 2-way or 3-way features, they are extremely inefficient in doing so (requiring either very wide or deep layers). This further motivates the usage of FMs in this work and is well aligned with our empirical results, i.e., strong competitive performance with reasonably small parameterization.

### 3 Our Proposed Model

In this section, we provide a layer-by-layer description of our model architecture. Our model accepts two sentences as an input, i.e.,  $P$  (premise) and  $H$  (hypothesis). Figure 1 illustrates a high-level overview of our proposed model architecture.

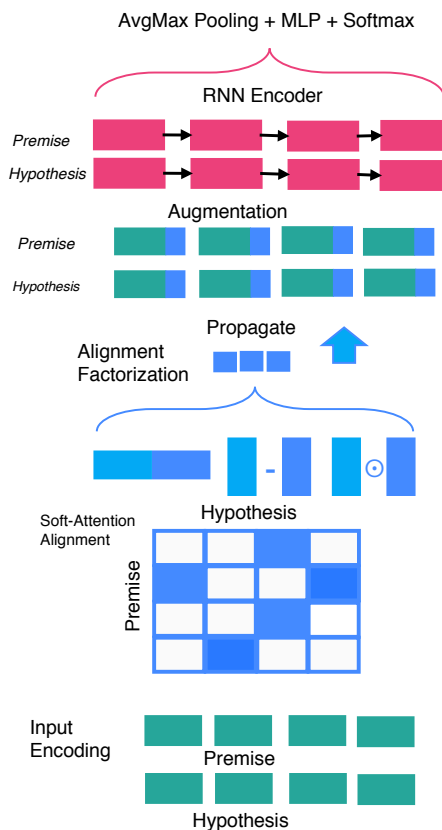


Figure 1: High level overview of our proposed architecture (*best viewed in color*). Alignment vectors are compressed and then propagated to upper representation learning layers (RNN encoders). Intra-attention is omitted in this diagram due to the lack of space.

#### 3.1 Input Encoding Layer

This layer aims to learn a  $k$ -dimensional representation for each word. Following (Gong et al., 2017), we learn feature-rich word representations by concatenating word embeddings, character embeddings and syntactic (part-of-speech tag) embeddings (provided in the datasets). Character representations are learned using a convolutional encoder with max pooling function and is commonly used in many relevant literature (Wang et al., 2017; Chen et al., 2017c).

**Highway Encoder** Subsequently, we pass each concatenated word vector into a two layer highway network (Srivastava et al., 2015) in order to

learn a  $k$ -dimensional representation. Highway networks are gated projection layers which learn adaptively control how much information is being carried to the next layer. Our strategy is similar to (Parikh et al., 2016) which trains the projection layer in place of tuning the embedding matrix. The usage of highway layers over standard projection layers is empirically motivated. However, an intuition would be that the gates in this layer adapt to learn the relative importance of each word to the NLI task. Let  $H(\cdot)$  and  $T(\cdot)$  be single layered affine transforms with ReLU and sigmoid activation functions respectively. A single highway network layer is defined as:

$$y = H(x, W_H) \cdot T(x, W_T) + C \cdot x \quad (1)$$

where  $C = (1 - T(x, W_T))$  and  $W_H, W_T \in \mathbb{R}^{r \times d}$ . Notably, the dimensions of the affine transform might be different from the size of the input vector. In this case, an additional nonlinear transform is used to project  $x$  to the same dimensionality. The output of this layer is  $\bar{P} \in \mathbb{R}^{k \times \ell_P}$  (premise) and  $\bar{H} \in \mathbb{R}^{k \times \ell_H}$  (hypothesis), with each word converted to a  $r$ -dimensional vector.

### 3.2 Soft-Attention Alignment Layer

This layer describes two soft-attention alignment techniques that are used in our model.

**Inter-Attention Alignment Layer** This layer learns an alignment of sub-phrases between  $\bar{P}$  and  $\bar{H}$ . Let  $F(\cdot)$  be a standard projection layer with ReLU activation function. The alignment matrix of two sequences is defined as follows:

$$e_{ij} = F(\bar{p}_i)^\top \cdot F(\bar{h}_j) \quad (2)$$

where  $E \in \mathbb{R}^{\ell_p \times \ell_h}$  and  $\bar{p}_i, \bar{h}_j$  are the  $i$ -th and  $j$ -th word in the premise and hypothesis respectively.

$$\beta_i = \sum_{j=1}^{\ell_p} \frac{\exp(e_{ij})}{\sum_{k=1}^{\ell_p} \exp(e_{ik})} \bar{p}_j \quad (3)$$

$$\alpha_j = \sum_{i=1}^{\ell_h} \frac{\exp(e_{ij})}{\sum_{k=1}^{\ell_h} \exp(e_{kj})} \bar{h}_i \quad (4)$$

where  $\beta_i$  is the sub-phrase in  $\bar{P}$  that is softly aligned to  $h_i$ . Intuitively,  $\beta_i$  is a weighted sum across  $\{p_j\}_{j=1}^{\ell_p}$ , selecting the most relevant parts of  $\bar{P}$  to represent  $h_i$ .

**Intra-Attention Alignment Layer** This layer learns a *self-alignment* of sentences and is applied to both  $\bar{P}$  and  $\bar{H}$  independently. For the sake of brevity, let  $\bar{S}$  represent either  $\bar{P}$  or  $\bar{H}$ , the intra-attention alignment is computed as:

$$s'_i = \sum_{j=1}^{\ell_p} \frac{\exp(f_{ij})}{\sum_{k=1}^{\ell_p} \exp(f_{ik})} \bar{s}_j \quad (5)$$

where  $f_{ij} = G(\bar{s}_i)^\top \cdot G(\bar{s}_j)$  and  $G(\cdot)$  is a non-linear projection layer with ReLU activation function. The intra-attention layer models similarity of each word with respect to the entire sentence, capturing long distance dependencies and ‘global’ context of the entire sentence.

### 3.3 Alignment Factorization Layer

This layer aims to learn a scalar valued feature for each comparison between aligned sub-phrases. Firstly, we introduce our factorization operation, which lives at the core of our neural model.

**Factorization Operation** Given an input vector  $x$ , the factorization operation (Rendle, 2010) is defined as:

$$Z(x) = w_0 + \sum_{i=1}^n w_i x_i + \sum_{i=1}^n \sum_{j=i+1}^n \langle v_i, v_j \rangle x_i x_j \quad (6)$$

where  $Z(x)$  is a scalar valued output,  $\langle \cdot, \cdot \rangle$  is the dot product between two vectors and  $w_0$  is the global bias. Factorization machines model low-rank structure within the matching vector producing a scalar feature. The parameters of this layer are  $w_0 \in \mathbb{R}, w \in \mathbb{R}^r$  and  $v \in \mathbb{R}^{r \times k}$ . The first term  $\sum_{i=1}^n w_i x_i$  is simply a linear term. The second term  $\sum_{i=1}^n \sum_{j=i+1}^n \langle v_i, v_j \rangle x_i x_j$  captures all pairwise interactions in  $x$  (the input vector) using the factorization of matrix  $v$ .

**Inter-Alignment Factorization** This operation compares the alignment between inter-attention aligned representations, i.e.,  $(\beta_i, h_i)$  and  $(\alpha_j, p_j)$ . Let  $(a, b)$  represent an alignment pair, we apply the following operations:

$$y_c = Z([a; b]); y_s = Z(a - b); y_m = Z(a \odot b) \quad (7)$$

where  $y_c, y_s, y_m \in \mathbb{R}, Z(\cdot)$  is the factorization operation,  $[ \cdot ; \cdot ]$  is the concatenation operator and  $\odot$  is the element-wise multiplication. The intuition of

modeling subtraction is targeted at capturing contradiction. However, instead of simply concatenating the extra comparison vectors, we compress them using the factorization operation. Finally, for each alignment pair, we obtain three scalar-valued features which map precisely to a word in the sequence.

**Intra-Alignment Factorization** Next, for each sequence, we also apply alignment factorization on the intra-aligned sentences. Let  $(s, s')$  represent an *intra-aligned* pair from either the premise or hypothesis, we compute the following operations:

$$v_c = Z([s; s']); v_s = Z(s - s'); v_m = Z(s \odot s') \quad (8)$$

where  $v_c, v_s, v_m \in \mathbb{R}$  and  $Z(\cdot)$  is the factorization operation. Applying alignment factorization to intra-aligned representations produces another three scalar-valued features which are mapped to each word in the sequence. Note that each of the *six* factorization operations has its own parameters but shares them amongst all words in the sentences.

### 3.4 Propagation and Augmentation

Finally, the *six* factorized features are then aggregated<sup>1</sup> via concatenation to form a final feature vector that is propagated to upper representation learning layers via augmentation of the word representation  $\bar{P}$  or  $\bar{H}$ .

$$u_i = [s_i; f_{intra}^i; f_{inter}^i] \quad (9)$$

where  $s_i$  is  $i$ -th word in  $\bar{P}$  or  $\bar{H}$ , and  $f_{intra}^i$  and  $f_{inter}^i$  are the intra-aligned  $[v_c; v_s; v_m]$  and inter-aligned  $[y_c; y_s; y_m]$  features for the  $i$ -th word in the sequence respectively. Intuitively,  $f_{intra}^i$  augments each word with global knowledge of the sentence and  $f_{inter}^i$  augments each word with cross-sentence knowledge via inter-attention.

### 3.5 Sequential Encoder Layer

For each sentence, the augmented word representations  $u_1, u_2, \dots, u_\ell$  are then passed into a sequential encoder layer. We adopt a standard vanilla LSTM encoder.

$$h_i = LSTM(u, i), \forall i \in [1, \dots, \ell] \quad (10)$$

<sup>1</sup>Following (Parikh et al., 2016), we may also concatenate the intra-aligned vector to  $u_i$  which we found to have speed up convergence.

where  $\ell$  represents the maximum length of the sequence. Notably, the parameters of the LSTM are *siamese* in nature, sharing weights between both premise and hypothesis. We do not use a bidirectional LSTM encoder, as we found that it did not lead to any improvements on the held-out set. A logical explanation would be because our word representations are already augmented with global (intra-attention) information. As such, modeling in the reverse direction is unnecessary, resulting in some computational savings.

**Pooling Layer** Next, to learn an overall representation of each sentence, we apply a pooling function across all hidden outputs of the sequential encoder. The pooling function is a concatenation of temporal max and average (avg) pooling.

$$x = [\max([h_1, \dots, h_\ell]); \text{avg}([h_1, \dots, h_\ell])] \quad (11)$$

where  $x$  is a final  $2k$ -dimensional representation of the sentence (premise or hypothesis). We also experimented with *sum* and *avg* standalone poolings and found *sum* pooling to be relatively competitive.

### 3.6 Prediction Layer

Finally, given a fixed dimensional representation of the premise  $x_p$  and hypothesis  $x_h$ , we pass their concatenation into a two-layer  $h$ -dimensional highway network. Since the highway network has been already defined earlier, we omit the technical details here. The final prediction layer of our model is computed as follows:

$$y_{out} = H_2(H_1([x_p; x_h; x_p \odot x_h; x_p - x_h])) \quad (12)$$

where  $H_1(\cdot), H_2(\cdot)$  are highway network layers with ReLU activation. The output is then passed into a final linear softmax layer.

$$y_{pred} = \text{softmax}(W_F \cdot y_{out} + b_F) \quad (13)$$

where  $W_F \in \mathbb{R}^{h \times 3}$  and  $b_F \in \mathbb{R}^3$ . The network is then trained using standard multi-class cross entropy loss with L2 regularization.

## 4 Experiments

In this section, we describe our experimental setup and report our experimental results.

Model	Params	Train	Test
<b>Single Model (w/o Cross Sentence Attention)</b>			
300D Gumbel TreeLSTM (Choi et al., 2017)	2.9M	91.2	85.6
300D DISAN (Shen et al., 2017)	2.4M	91.1	85.6
300D Residual Stacked Encoders (Nie and Bansal, 2017)	9.7M	89.8	85.7
600D Gumbel TreeLSTM (Choi et al., 2017)	10M	93.1	<b>86.0</b>
300D CAFE (w/o CA)	3.7M	87.3	<u>85.9</u>
<b>Single Models</b>			
100D LSTM with attention (Rocktäschel et al., 2015)	250K	85.3	83.5
300D mLSTM (Wang and Jiang, 2016b)	1.9M	92.0	86.1
450D LSTMN + deep att. fusion (Cheng et al., 2016)	3.4M	88.5	86.3
200D DecompAtt + Intra-Att (Parikh et al., 2016)	580K	90.5	86.8
300D NTI-SLSTM-LSTM (Yu and Munkhdalai, 2017b)	3.2M	88.5	87.3
300D re-read LSTM (Sha et al., 2016)	2.0M	90.7	87.5
BiMPM (Wang et al., 2017)	1.6M	90.9	87.5
448D DIIN (Gong et al., 2017)	4.4M	91.2	88.0
600D ESIM (Chen et al., 2017b)	4.3M	92.6	88.0
150D CAFE (SUM+2x200D MLP)	750K	88.2	87.7
200D CAFE (SUM+2x400D MLP)	1.4M	89.4	88.1
300D CAFE (SUM+2x600D MLP)	3.5M	89.2	<u>88.3</u>
300D CAFE (AVGMAX+300D HN)	4.7M	89.8	<b>88.5</b>
<b>Ensemble Models</b>			
600D ESIM + 300D Tree-LSTM (Chen et al., 2017b)	7.7M	93.5	88.6
BiMPM (Wang et al., 2017)	6.4M	93.2	88.8
448D DIIN (Gong et al., 2017)	17.0M	92.3	88.9
300D CAFE (Ensemble)	17.5M	92.5	<b>89.3</b>
<b>External Resource Models</b>			
BiAttentive Classification + CoVe + Char (McCann et al., 2017)	22M	88.5	88.1
KIM (Chen et al., 2017a)	4.3M	94.1	88.6
ESIM + ELMo (Peters et al., 2018)	8.0M	91.6	88.7
200D CAFE (AVGMAX + 200D MLP) + ELMo	1.4M	89.5	<b>89.0</b>

Table 1: Performance comparison of all published models on the SNLI benchmark.

#### 4.1 Experimental Setup

To ascertain the effectiveness of our models, we use the SNLI (Bowman et al., 2015) and MultiNLI (Williams et al., 2017) benchmarks which are standard and highly competitive benchmarks for the NLI task. We also include the newly released SciTail dataset (Khot et al., 2018) which is a binary entailment classification task constructed from science questions. Notably, SciTail is known to be a difficult dataset for NLI, made evident by the low accuracy scores even though it is binary in nature.

**SNLI** The state-of-the-art competitors on this dataset are the BiMPM (Wang et al., 2017), ESIM (Chen et al., 2017b) and DIIN (Gong et al., 2017). We compare against competitors across three settings. The first setting disallows cross sentence at-

tention. In the second setting, cross sentence is allowed. The last (third) setting is a comparison between model ensembles while the first two settings only comprise single models. Note that we consider the 1st setting to be relatively less important (since our focus is not on the encoder itself) but still report the results for completeness.

**MultiNLI** We compare on two test sets (*matched* and *mismatched*) which represent in-domain and out-domain performance. The main competitor on this dataset is the ESIM model, a powerful state-of-the-art SNLI baseline. We also compare with ESIM + Read (Weissenborn, 2017).

**SciTail** This dataset only has one official setting. We compare against the reported results of ESIM (Chen et al., 2017b) and DecompAtt (Parikh et al.,

2016) in the original paper. We also compare with DGEM, the new model proposed in (Khot et al., 2018).

Across all experiments and in the spirit of fair comparison, we only compare with works that (1) do not use extra training data and (2) do not use external resources (such as external knowledge bases, etc.). However, for the sake of completeness, we still report their scores<sup>2</sup> (McCann et al., 2017; Chen et al., 2017a; Peters et al., 2018).

## 4.2 Implementation Details

We implement our model in TensorFlow (Abadi et al., 2015) and train them on Nvidia P100 GPUs. We use the Adam optimizer (Kingma and Ba, 2014) with an initial learning rate of 0.0003. L2 regularization is set to  $10^{-6}$ . Dropout with a keep probability of 0.8 is applied after each fully-connected, recurrent or highway layer. The batch size is tuned amongst {128, 256, 512}. The number of latent factors  $k$  for the factorization layer is tuned amongst {5, 10, 50, 100, 150}. The size of the hidden layers of the highway network layers are set to 300. All parameters are initialized with xavier initialization. Word embeddings are pre-loaded with 300d GloVe embeddings (Pennington et al., 2014) and fixed during training. Sequence lengths are padded to batch-wise maximum. The batch order is (randomly) sorted within buckets following (Parikh et al., 2016).

## 4.3 Experimental Results

Table 1 reports our results on the SNLI benchmark. On the cross sentence (single model setting), the performance of our proposed CAFE model is extremely competitive. We report the test accuracy of CAFE at different extents of parameterization, i.e., varying the size of the LSTM encoder, width of the pre-softmax hidden layers and final pooling layer. CAFE obtains 88.5% accuracy on the SNLI test set, an extremely competitive score on the extremely popular benchmark. Notably, competitive results can be also achieved with a much smaller parameterization. For example, CAFE also achieves 88.3% and 88.1% test accuracy with only 3.5M and 1.5M parameters

<sup>2</sup>Additionally, we added ELMo (Peters et al., 2018) to our CAFE model at the embedding layer. We report CAFE + ELMo under external resource models. This was done post review after EMNLP. Due to resource constraints, we did not train CAFE + ELMo ensembles but a single run (and single model) of CAFE + ELMo already achieves 89.0 score on SNLI.

respectively. This outperforms the state-of-the-art ESIM and DIIN models with only a fraction of the parameter cost. At 88.1%, our model has about three times less parameters than ESIM/DIIN (i.e., 1.4M versus 4.3M/4.4M). Moreover, our lightweight adaptation achieves 87.7% with only 750K parameters, which makes it extremely performant amongst models having the same amount of parameters such as the decomposable attention model (86.8%).

Finally, an ensemble of 5 CAFE models achieves 89.3% test accuracy, the best test scores on the SNLI benchmark to date<sup>3</sup>. Overall, we believe that the good performance of our CAFE can be attributed to (1) the effectiveness of the ComProp architecture (i.e., providing word representations with global and local knowledge for better representation learning) and (2) the expressiveness of alignment factorization layers that are used to decompose and compare word alignments. More details are given at the ablation study. Finally, we emphasize that CAFE is also relatively lightweight, efficient and fast to train given its performance. A single run on SNLI takes approximately 5 minutes per epoch with a batch size of 256. Overall, a single run takes  $\approx$  3 hours to get to convergence.

Model	MultiNLI		SciTail
	Match	Mismatch	-
Majority	36.5	35.6	60.3
NGRAM <sup>#</sup>	-	-	70.6
CBOW <sup>b</sup>	65.2	64.8	-
BiLSTM <sup>b</sup>	69.8	69.4	-
ESIM <sup>#,b</sup>	72.4	72.1	70.6
DecompAtt <sup>#</sup> -	-	-	72.3
DGEM <sup>#</sup>	-	-	70.8
DGEM + Edge <sup>#</sup>	-	-	77.3
ESIM <sup>†</sup>	76.3	75.8	-
ESIM + Read <sup>†</sup>	77.8	77.0	-
CAFE	78.7	77.9	<b>83.3</b>
CAFE Ensemble	<b>80.2</b>	<b>79.0</b>	-

Table 2: Performance comparison (accuracy) on MultiNLI and SciTail. Models with †, # and b are reported from (Weissenborn, 2017), (Khot et al., 2018) and (Williams et al., 2017) respectively.

Table 2 reports our results on the MultiNLI and SciTail datasets. On MultiNLI, CAFE significantly outperforms ESIM, a strong state-of-the-art model on both settings. We also outperform the ESIM + Read model (Weissenborn, 2017). An ensemble of CAFE models achieve competitive re-

<sup>3</sup>As of 22nd May 2018, the deadline of the EMNLP submission.

sult on the MultiNLI dataset. On SciTail, our proposed CAFE model achieves state-of-the-art performance. The performance gain over strong baselines such as DecompAtt and ESIM are  $\approx 10\%$  –  $13\%$  in terms of accuracy. CAFE also outperforms DGEM, which uses a graph-based attention for improved performance, by a significant margin of  $5\%$ . As such, empirical results demonstrate the effectiveness of our proposed CAFE model on the challenging SciTail dataset.

#### 4.4 Ablation Study

	Match	Mismatch
Original Model	79.0	78.9
(1a) Rm FM for 1L-FC	77.7	77.9
(1b) Rm FM for 1L-FC (ReLU)	77.3	77.5
(1c) Rm FM for 2L-FC (ReLU)	76.6	76.4
(2) Remove Char Embed	78.1	78.3
(3) Remove Syn Embed	78.3	78.4
(4) Remove Inter Att	75.2	75.6
(5) Replace HW Pred. with FC	77.7	77.9
(6) Replace HW Enc. with FC	78.7	78.7
(7) Remove Sub Feat	77.9	78.3
(8) Remove Mul Feat	78.7	78.6
(9) Remove Concat Feat	77.9	77.6
(10) Add Bi-directional	78.3	78.4

Table 3: Ablation study on MultiNLI development sets. HW stands for Highway.

Table 3 reports ablation studies on the MultiNLI development sets. In (1), we replaced all FM functions with regular full-connected (FC) layers in order to observe the effect of **FM versus FC**. More specifically, we experimented with several FC configurations as follows: (a) 1-layer linear, (b) 1-layer ReLU (c) 2-layer ReLU. The 1-layer linear setting performs the best and is therefore reported in Table 3. Using ReLU seems to be worse than nonlinear FC layers. Overall, the best combination (option a) still experienced a decline in performance in both development sets.

In (2-3), we explore the utility of using character and syntactic embeddings, which we found to have helped CAFE marginally. In (4), we remove the inter-attention alignment features, which naturally impact the model performance significantly. In (5-6), we explore the effectiveness of the highway layers (in prediction layers and encoding layers) by replacing them to FC layers. We observe that both highway layers have marginally helped the overall performance. Finally, in (7-9), we remove the alignment features based on their composition type. We observe that the *Sub* and *Concat* compositions were more important than the *Mul*

composition. However, removing any of the three will result in some performance degradation. Finally, in (10), we replace the LSTM encoder with a BiLSTM, observing that adding bi-directionality did not improve performance for our model.

#### 4.5 Linguistic Error Analysis

We perform a linguistic error analysis using the supplementary annotations provided by the MultiNLI dataset. We compare against the model outputs of the ESIM model across 13 categories of linguistic phenomena (Williams et al., 2017). Table 4 reports the result of our error analysis. We observe that our CAFE model generally outperforms ESIM on *most categories*.

	Matched		Mismatched	
	ESIM	CAFE	ESIM	CAFE
Conditional	100	70	60	<b>85</b>
Word overlap	50	<b>82</b>	62	<b>87</b>
Negation	<b>76</b>	<b>76</b>	71	<b>80</b>
Antonym	67	<b>82</b>	58	<b>80</b>
Long Sentence	75	<b>79</b>	69	<b>77</b>
Tense Difference	73	<b>82</b>	79	<b>89</b>
Active/Passive	88	<b>100</b>	<b>91</b>	90
Paraphrase	<b>89</b>	88	84	<b>95</b>
Quantity/Time	33	<b>53</b>	54	<b>62</b>
Coreference	<b>83</b>	80	75	<b>83</b>
Quantifier	69	<b>75</b>	72	<b>80</b>
Modal	78	<b>81</b>	76	<b>81</b>
Belief	65	<b>77</b>	67	<b>83</b>

Table 4: Linguistic Error Analysis on MultiNLI dataset.

On the mismatched setting, CAFE outperforms ESIM in 12 out of 13 categories, losing only in one percentage point in *Active/Passive* category. On the matched setting, CAFE is outperformed by ESIM very marginally on coreference and paraphrase categories. Despite generally achieving much superior results, we noticed that CAFE performs poorly on *conditionals*<sup>4</sup> on the matched setting. Measuring the absolute ability of CAFE, we find that CAFE performs extremely well in handling linguistic patterns of *paraphrase detection* and *active/passive*. This is likely to be attributed by the alignment strategy that CAFE and ESIM both exploits.

#### 4.6 Interpreting and Visualizing with CAFE

Finally, we also observed that the propagated features are highly interpretable, giving insights to the inner workings of the CAFE model. Figure 2 shows a visualization of the feature values from an example in the SNLI test set. The ground

<sup>4</sup>This only accounts for 5% of samples.



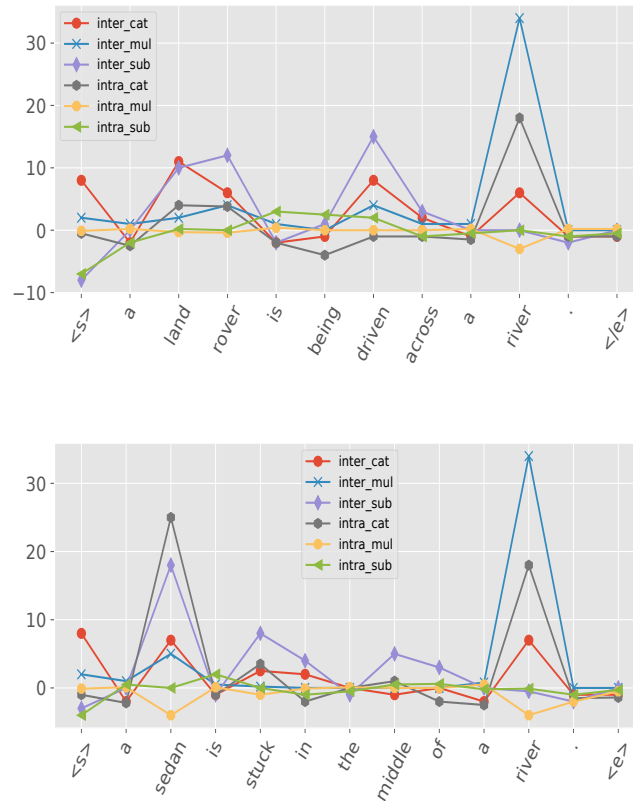


Figure 2: Visualization of *six* Propagated Features (*Best viewed in color*). Legend is denoted by {inter,intra} followed by the operations *mul*, *sub* or *cat* (concat).

truth is *contradiction*. Based on the above example we make several observations. Firstly, *inter\_mul* features mostly capture identical words (or semantically similar words), i.e., *inter\_mul* features for ‘river’ spikes in both sentences. Secondly, *inter\_sub* spikes on conflicting words that might cause contradiction, e.g., ‘sedan’ and ‘land rover’ are not the same vehicle. Another interesting observation is that we notice the *inter\_sub* features for *driven* and *stuck* spiking. This also validates the observation of (Chen et al., 2017b), which shows what the *sub* vector in the ESIM model is looking out for contradictory information. However, our architecture allows the inspection of these vectors since they are compressed via factorization, leading to larger extents of explainability - a quality that neural models inherently lack. We also observed that intra-attention (e.g., *intra\_cat*) features seem to capture the more important words in the sentence (‘river’, ‘sedan’, ‘land rover’).

## 5 Conclusion

We proposed a new neural architecture, CAFE for NLI. CAFE achieves very competitive performance on three benchmark datasets. Extensive ablation studies confirm the effectiveness of FM layers over FC layers. Qualitatively, we show how different compositional operators (e.g., *sub* and *mul*) behave in NLI task and shed light on why subtractive composition helps in other models such as ESIM.

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