

An Investigation of the (In)effectiveness of Counterfactually Augmented Data

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Abstract

While pretrained language models achieve excellent performance on natural language understanding benchmarks, they tend to rely on spurious correlations and generalize poorly to out-of-distribution (OOD) data. Recent work has explored using counterfactually-augmented data (CAD)—data generated by minimally perturbing examples to flip the ground-truth label—to identify robust features that are invariant under distribution shift. However, empirical results using CAD during training for OOD generalization have been mixed. To explain this discrepancy, through a toy theoretical example and empirical analysis on two crowdsourced CAD datasets, we show that: (a) while features perturbed in CAD are indeed robust features, it may prevent the model from learning *unperturbed* robust features; and (b) CAD may exacerbate existing spurious correlations in the data. Our results thus show that the lack of perturbation diversity limits CAD’s effectiveness on OOD generalization, calling for innovative crowdsourcing procedures to elicit diverse perturbation of examples.

1 Introduction

Large-scale datasets have enabled tremendous progress in natural language understanding (NLU) (Rajpurkar et al., 2016; Wang et al., 2019) with the rise of pretrained language models (Devlin et al., 2019; Peters et al., 2018). Despite this progress, there have been numerous works showing that models rely on spurious correlations in the datasets, i.e. heuristics that are effective on a specific dataset but do not hold in general (McCoy et al., 2019; Naik et al., 2018; Wang and Culotta, 2020). For example, BERT (Devlin et al., 2019) trained on MNLI (Williams et al., 2018) learns the spurious correlation between world overlap and entailment label.

A recent promising direction is to collect counterfactually-augmented data (CAD) by asking humans to minimally edit examples to flip their

ground-truth label (Kaushik et al., 2020). Figure 1 shows example edits for Natural Language Inference (NLI). Given interventions on *robust features* that “cause” the label to change, the model is expected to learn to disentangle the spurious and robust features.

Despite recent attempt to explain the efficacy of CAD by analyzing the underlying causal structure of the data (Kaushik et al., 2021), empirical results on out-of-distribution (OOD) generalization using CAD are mixed. Specifically, Huang et al. (2020) show that CAD does not improve OOD generalization for NLI; Khashabi et al. (2020) find that for question answering, CAD is helpful only when it is much cheaper to create than standard examples — but Bowman et al. (2020) report that the cost is actually similar per example.

In this work, we take a step towards bridging this gap between what theory suggests and what we observe in practice in regards to CAD. An intuitive example to illustrate our key observation is shown in Figure 1 (a), where the verb ‘eating’ is changed to ‘drinking’ to flip the label. While there are many other words that could have been changed to flip the label, given only these two examples, the model learns to use *only* the verbs (e.g. using a Naive Bayes model, all other words would have zero weights). As a result, this model would fail when evaluated on examples such as those in (b) where the quantifier ‘two’ is changed to ‘three’, while a model trained on the unaugmented data may learn to use the quantifiers.

First, we use a toy theoretical setting to formalize counterfactual augmentation, and demonstrate that with CAD, the model can learn to ignore the spurious features without explicitly intervening on them. However, we find that without perturbing all robust features to generate CAD, perturbations of one robust feature can prevent the model from learning other unperturbed robust features. Motivated by this, we set up an empirical analysis on

- Premise:** The lady is standing next to her two children who are eating a pizza.
Original Hypothesis: The two children near the lady are **eating** something. (Entailment)
Revised Hypothesis: The two children near the lady are **drinking** something. (Contradiction)
- (a)
- Premise:** The lady is standing next to her two children who are eating a pizza.
Original Hypothesis: The **two** children near the lady are eating something. (Entailment)
Revised Hypothesis: The **three** children near the lady are eating something. (Contradiction)
- (b)

Figure 1: Illustration of counterfactual examples in natural language inference. Augmenting examples like (a) hurts performance on examples like (b) where a different robust feature has been perturbed, since the first example encourages the model to exclusively focus on the highlighted words.

two crowdsourced CAD datasets collected for NLI and Question Answering (QA). In the empirical analysis, we identify the robust features by categorizing the edits into different *perturbation types* (Wu et al., 2021) (e.g. negating a sentence or changing the quantifiers), and show that models do not generalize well to unseen perturbation types, sometimes even performing worse than models trained on unaugmented data.

Our analysis of the relation between perturbation types and generalization can help explain other observations such as CAD being more beneficial in the low-data regime. With increasing data size, improvement from using CAD plateaus compared to unaugmented data, suggesting that the number of perturbation types in existing CAD datasets does not keep increasing.

Another consequence of the lack of diversity in edits is annotation artifacts, which may produce spurious correlations similar to what happens in standard crowdsourcing procedures. While CAD is intended to debias the dataset, surprisingly, we find that crowdsourced CAD for NLI exacerbates word overlap bias (McCoy et al., 2019) and negation bias (Gururangan et al., 2018a) observed in existing benchmarks.

In sum, we show that while CAD can help the model ignore spurious feature, its effectiveness in current CAD datasets is limited by the set of robust features that are perturbed. Furthermore, CAD may exacerbate spurious correlations in existing benchmarks. Our results highlight the importance of increasing the diversity of counterfactual perturbations during crowdsourcing: We need to elicit more diverse edits of examples that make models more robust to the complexity of language.

2 Toy Example: Analysis of a Linear Model

In this section, we use a toy setting with a linear Gaussian model and squared loss to formalize counterfactual augmentation and discuss the conditions required for its effectiveness. The toy example serves to motivate our empirical analysis in Section 3.

2.1 Learning under Spurious Correlation

We adopt the setting in Rosenfeld et al. (2021): each example consists of *robust features* $x_r \in \mathbb{R}^{d_r}$ whose joint distribution with the label is invariant during training and testing, and *spurious features* $x_s \in \mathbb{R}^{d_s}$ whose joint distribution with the label varies at test time. Here d_r and d_s denote the feature dimensions. We consider a binary classification setting where the label $y \in \{-1, 1\}$ is drawn from a uniform distribution, and both the robust and spurious features are drawn from Gaussian distributions. Specifically, an example $x = [x_r, x_s] \in \mathbb{R}^d$ is generated by the following process (where $d = d_r + d_s$):

$$y = \begin{cases} 1 & \text{w.p. } 0.5 \\ -1 & \text{otherwise} \end{cases} \quad (1)$$

$$x_r | y \sim \mathcal{N}(y\mu_r, \sigma_r^2 I), \quad (2)$$

$$x_s | y \sim \mathcal{N}(y\mu_s, \sigma_s^2 I), \quad (3)$$

where $\mu_r \in \mathbb{R}^{d_r}$; $\mu_s \in \mathbb{R}^{d_s}$; $\sigma_r, \sigma_s \in \mathbb{R}$; and I is the identity matrix.¹ The corresponding data distribution is denoted by \mathcal{D} . Note that the relation between y and the spurious features x_s depends on μ_s and σ_s , which may change at test time, thus relying on x_s may lead to poor OOD performance.

¹This model corresponds to the anti-causal setting (Scholkopf et al., 2012), i.e. the label causing the features. We adopt this setting since it is consistent with how most data is generated in tasks like NLI, sentiment analysis etc.

Intuitively, in this toy setting, a model trained with only access to examples from \mathcal{D} would not be able to differentiate between the spurious and robust features, since they play a similar role in the data generating process for \mathcal{D} . Formally, consider the setting with infinite samples from \mathcal{D} where we learn a linear model ($y = w^T x$ where $w \in \mathbb{R}^d$) by least square regression. Let $\hat{w} \in \mathbb{R}^d$ be the optimal solution on \mathcal{D} (without any counterfactual augmentation). The closed form solution is:

$$\begin{aligned} \text{Cov}(x, x)\hat{w} &= \text{Cov}(x, y) \\ \hat{w} &= \text{Cov}(x, x)^{-1}\mu \end{aligned} \quad (4)$$

where $\mu = [\mu_r, \mu_s] \in \mathbb{R}^d$ and $\text{Cov}(\cdot)$ denotes the covariance matrix:

$$\text{Cov}(x, x) = \begin{bmatrix} \Sigma_r & \mu_r \mu_s^T \\ \mu_s \mu_r^T & \Sigma_s \end{bmatrix}, \quad (5)$$

where Σ_r, Σ_s are covariance matrices of x_r and x_s respectively. This model relies on x_s whose relationship with the label y can vary at test time, thus it may have poor performance under distribution shift. A robust model w_{inv} that is invariant to spurious correlations would ignore x_s :

$$w_{\text{inv}} = [\Sigma_r^{-1}\mu_r, 0]. \quad (6)$$

2.2 Counterfactual Augmentation

The counterfactual data is generated by editing an example to flip its label. We model the perturbation by an *edit vector* z that translates x to change its label from y to $-y$ (i.e. from 1 to -1 or vice versa). For instance, the counterfactual example of a positive example $(x, +1)$ is $(x + z, -1)$. Specifically, we define the edit vector to be $z = [yz_r, yz_s] \in \mathbb{R}^d$, where $z_r \in \mathbb{R}^{d_r}$ and $z_s \in \mathbb{R}^{d_s}$ are the displacements for the robust and spurious features. Here, z is label-dependent so that examples with different labels are translated in opposite directions. Therefore, the counterfactual example $(x^c, -y)$ generated from (x, y) has the following distribution:

$$x_r^c \mid -y \sim \mathcal{N}(y(\mu_r + z_r), \sigma_r^2 I), \quad (7)$$

$$x_s^c \mid -y \sim \mathcal{N}(y(\mu_s + z_s), \sigma_s^2 I). \quad (8)$$

The model is then trained on the combined set of original examples x and counterfactual examples x^c , whose distribution is denoted by \mathcal{D}_c .

Optimal edits. Ideally, the counterfactual data should de-correlate x_s and y , thus it should only perturb the robust features x_r , i.e. $z = [yz_r, 0]$. To find the displacement z_r that moves x across the decision boundary, we maximize the log-likelihood of the flipped label under the data generating distribution \mathcal{D} :

$$\begin{aligned} z_r^* &= \arg \max_{z_r \in \mathbb{R}^{d_r}} \mathbb{E}_{(x,y) \sim \mathcal{D}} \log p(-y \mid x + [yz_r, 0]) \\ &= -2\mu_r. \end{aligned} \quad (9)$$

Intuitively, it moves the examples towards the mean of the opposite class along coordinates of the robust features.

Using the edits specified above, if the model trained on \mathcal{D}_c has optimal solution \hat{w}_c , we have:

$$\begin{aligned} \text{Cov}(x, x)\hat{w}_c &= \text{Cov}(x, y) \\ \hat{w}_c &= [\Sigma_r^{-1}\mu_r, 0] = w_{\text{inv}}. \end{aligned} \quad (10)$$

Thus, the optimal edits recover the robust model w_{inv} , demonstrating the effectiveness of CAD.

Incomplete edits. There is an important assumption made in the above result: we have assumed *all* robust features are edited. Suppose we have two sets of robust features x_{r1} and x_{r2} ,² then *not* editing x_{r2} would effectively make it appear spurious to the model and indistinguishable from x_s .

In practice, this happens when there are multiple robust features but only a few are perturbed during counterfactual augmentation (which can be common during data collection if workers rely on simple patterns to make the minimal edits). Considering the NLI example, if all entailment examples are flipped to non-entailment ones by inserting a negation word, then the model will only rely on negation to make predictions.

More formally, consider the case where the original examples $x = [x_{r1}, x_{r2}, x_s]$ and counterfactual examples are generated by incomplete edits $z = [z_{r1}, 0, 0]$ that perturb only x_{r1} . Using the same analysis above where z_{r1} is chosen by maximum likelihood estimation, let the model learned on the incompletely augmented data be denoted by \hat{w}_{inc} . We can then show that the error of the model trained from incomplete edits can be more than that of the model trained without any counterfactual augmentation under certain conditions. More formally, we have the following:

²We assume they are conditionally independent given the label.

Type	Definition	Example	# examples (NLI/BoolQ)
negation	<i>Change in negation modifier</i>	A dog is not fetching anything.	200/683
quantifier	<i>Change in words with numeral POS tags</i>	The lady has many → three children.	344/414
lexical	<i>Replace few words without changing the POS tags</i>	The boy is swimming → running .	1568/1737
insert	<i>Only insert words or short phrases</i>	The tall man is digging the ground.	1462/536
delete	<i>Only delete words or short phrases</i>	The lazy person just woke up.	562/44
resemantic	<i>Replace short phrases without affecting rest of the parsing tree</i>	The actor saw → had just met the director.	2760/1866

Table 1: Definition of the perturbation types and the corresponding number of examples in the NLI CAD dataset released by (Kaushik et al., 2020) and the BoolQ CAD dataset released by Khashabi et al. (2020). In the example edits, the deleted words are shown in red and the newly added words are shown in green.

Proposition 1. Define the error for a model as $\ell(w) = \mathbb{E}_{x \sim \mathcal{F}} [(w_{inv}^T x - w^T x)^2]$ where the distribution \mathcal{F} is the test distribution in which x_r and x_s are independent: $x_r | y \sim \mathcal{N}(y\mu_r, \sigma_r^2 I)$ and $x_s \sim \mathcal{N}(0, I)$.

Assuming all variables have unit variance (i.e. $\sigma_r = 1$ and $\sigma_s = 1$), $\|\mu_r\| = 1$, and $\|\mu_s\| = 1$, we get $\ell(\hat{w}_{inc}) > \ell(\hat{w})$ if $\|\mu_{r1}\|^2 < \frac{1+\sqrt{13}}{6} \approx 0.767$, where $\|\cdot\|$ denotes the Euclidean norm, and μ_{r1} is the mean of the perturbed robust feature r_1 .

Intuitively, this statement says that if the norm of the edited robust features (in the incomplete-edits model) is sufficiently small, then the test error for a model with counterfactual augmentation will be more than a model trained with no augmentation.

Proof Sketch. The proof mainly follows from algebra and using the fact that $\text{Cov}(x, x)^{-1}$ is a block matrix consisting of rank-one perturbations of the identity matrix. We refer the reader to Appendix A for the detailed proof. \square

Thus, Proposition 1 implies that perturbing only a small subset of robust features could perform worse than no augmentation, indicating the importance of diversity in CAD. Next, we show that the problem of incomplete edits is exhibited in real CAD too.

3 Diversity and Generalization in CAD

In this section, we test the following hypothesis based on the above analysis: models trained on CAD are limited to the specific robust features that are perturbed and may not learn other unperturbed robust features. We empirically analyze how augmenting counterfactual examples by perturbing one robust feature affects the performance on examples generated by perturbing other robust features.

3.1 Experiment Design

Perturbation types. Unlike the toy example, in NLU it is not easy to define robust features since they typically correspond to the semantics of the text (e.g. sentiment). Following Kaushik et al. (2021) and similar to our toy model, we define robust features as spans of text whose distribution with the label remains invariant, whereas spans of text whose dependence on the label can change during evaluation are defined as spurious features. We then use linguistically-inspired rules (Wu et al., 2021) to categorize the robust features into several *perturbation types*: negation, quantifier, lexical, insert, delete and resemantic. Table 1 gives the definitions of each type.

Train/test sets. Both the training sets and the test sets contain counterfactual examples generated by a particular perturbation type. To test the generalization from one perturbation type to another, we use two types of test sets: *aligned test sets* where examples are generated by the same perturbation type as the training data; and *unaligned test sets* where examples are generated by unseen perturbation types (e.g. training on examples from lexical and testing on negation).

3.2 Experimental Setup

Data. We experiment on two CAD datasets collected for SNLI (Kaushik et al., 2020) and BoolQ (Khashabi et al., 2020). The size of the paired data (seed examples and edited examples) for each perturbation type in the training dataset is given in Table 1. Since some types (e.g. delete) contain too few examples for training, we train on the top three largest perturbation types: lexical, insert, and resemantic for SNLI; and lexical, negation, and resemantic for BoolQ.

For SNLI, to control for dataset sizes across all

Train Data	lexical	insert	resemantic	quantifier	negation	delete
SNLI seed	75.16 _{0.32}	74.94 _{1.05}	76.77 _{0.74}	74.36 _{0.21}	69.25 _{2.09}	65.76 _{2.34}
lexical	79.70 _{2.07}	68.61 _{5.26}	71.46 _{3.07}	69.90 _{3.83}	66.00 _{2.99}	61.76 _{5.27}
insert	67.83 _{3.96}	79.30 _{0.39}	70.53 _{2.19}	66.31 _{3.10}	55.00 _{4.10}	69.75 _{2.43}
resemantic	77.14 _{2.12}	76.43 _{1.05}	75.31 _{1.10}	71.26 _{0.36}	66.75 _{1.69}	70.16 _{1.09}

Table 2: Accuracy of NLI CAD on both **aligned** and unaligned test sets. We report the mean and standard deviation across 5 random seeds. Each dataset has a total of 1400 examples. On average models perform worse on unaligned test sets (i.e. unseen perturbation types).

Train Data	lexical	negation	resemantic	quantifier	insert
BoolQ seed	65.79 _{2.11}	62.61 _{2.65}	68.97 _{1.83}	61.00 _{1.65}	57.11 _{0.67}
lexical	77.38 _{1.04}	64.32 _{2.18}	80.78 _{1.46}	70.75 _{2.03}	66.77 _{1.35}
negation	63.18 _{1.46}	72.91 _{2.31}	66.74 _{2.22}	61.75 _{2.44}	65.42 _{1.45}
resemantic	72.29 _{0.72}	64.92 _{1.56}	75.60 _{2.11}	70.00 _{2.85}	64.91 _{2.31}

Table 3: Accuracy of BoolQ CAD on both **aligned** and unaligned test sets. We report the mean and standard deviation across 5 random seeds. Each dataset has a total of 9427 examples. On average models perform worse on unaligned test sets (i.e. unseen perturbation types).

experiments, we use 700 seed examples and their corresponding 700 perturbations for each perturbation type. As a baseline (‘SNLI seed’), we subsample examples from SNLI to create a similar sized dataset for comparison.³

For BoolQ (Clark et al., 2019a), our initial experiments show that training on only CAD does not reach above random-guessing. Thus, we include all original training examples in BoolQ (Khashabi et al., 2020), and replace part of them with CAD for each perturbation type. This results in a training set of 9427 examples of which 683 are CAD for each perturbation type. The size 683 is chosen to match the the smallest CAD type for BoolQ. As a baseline (‘BoolQ seed’), we train on all the original training examples, consisting of 9427 examples. For both datasets, the training, dev and test sets are created from their respective splits in the CAD datasets. The size of the dev and test sets is reported in Appendix B.2.

Model. We use the Hugging Face implementation (Wolf et al., 2020) of RoBERTa (Liu et al., 2019) to fine-tune all our models. To account for the small dataset sizes, we run all our experiments with 5 different random seeds and report the mean and standard deviation. Details on hyperparameter tuning are reported in Appendix B.1.⁴

³We observe similar trends when using different subsets of the SNLI data. We report the mean and standard deviation across different subsets in Appendix B.3.

⁴Our code can be found at: <https://github.com/joshinh/investigation-cad>

3.3 Generalization to Unseen Perturbation Types

We discuss results for the main question in this section—how does adding CAD generated from one perturbation type affect performance on examples generated from other perturbation types? Table 2 and 3 show results for SNLI and BoolQ.

CAD performs well on aligned test sets. We see that on average models perform very well on the **aligned test sets** (same perturbation type as the training set), but do not always do well on unaligned test sets (unseen perturbation types), which is consistent with our analysis in Section 2. On SNLI, one exception is resemantic, which performs well on unseen perturbation types. We believe this is because it is a broad category (replacing any constituent) that covers other types such as lexical (replacing any word). Similarly, on BoolQ, lexical and resemantic both perform better than the baseline on some unaligned test sets (e.g. quantifier), but they perform much better on the aligned test sets.

CAD sometimes performs worse than the baseline on unaligned test sets. For example, on SNLI, training on insert does much worse than the seed baseline on lexical and resemantic, and SNLI seed performs best on quantifier and negation. On BoolQ, training on negation does slightly worse than the baseline on lexical and resemantic. This suggests that augmenting perturbations of one particular robust feature may reduce the model’s reliance on other robust features,

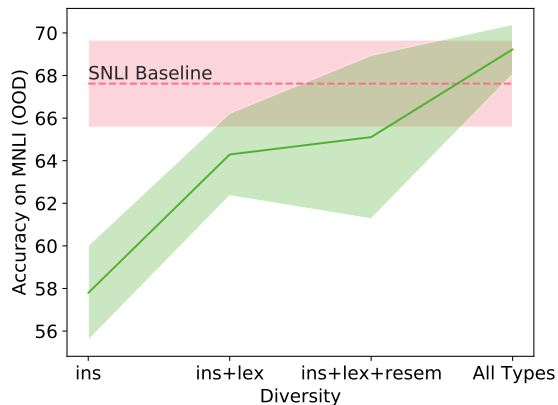


Figure 2: OOD accuracy (mean, std. deviation) on MNLI of models trained on SNLI CAD and SNLI seed (baseline) with increasing number of perturbation types and fixed training set size. More perturbation types in the training data leads to higher OOD accuracy.

that could have been learned without augmentation.

3.4 Generalization to Out-of-Distribution Data

In Section 3.3, we have seen that training on CAD generated by a single perturbation type does not generalize well to unseen perturbation types. However, in practice CAD contains many different perturbation types. Do they cover enough robust features to enable OOD generalization?

Increasing Diversity. We first verify that increasing the number of perturbed robust features leads to better OOD generalization. Specifically, we train models on subsets of SNLI CAD with increasing coverage of perturbation types and evaluate on MNLI as the OOD data. Starting with only insert, we add one perturbation type at a time until all types are included; the total number of examples are fixed throughout the process at 1400 (which includes 700 seed examples and the corresponding 700 perturbations).

Figure 2 shows the OOD accuracy on MNLI when trained on CAD and SNLI seed examples of the same size. We observe that as the number of perturbation types increases, models generalize better to OOD data despite fixed training data size. The result highlights the importance of collecting a diverse set of counterfactual examples, even if each perturbation type is present in a small amount.

A natural question to ask here is: If we continue to collect more counterfactual data, does it cover more perturbation types and hence lead to better OOD generalization? Thus we investigate the im-

	BERT	RoBERTa
SNLI seed	59.7 _{0.3}	73.8 _{1.2}
CAD	60.2 _{1.0}	70.0 _{1.1}

Table 4: Accuracy (mean and std. deviation across 5 runs) on MNLI of different pretrained models finetuned on SNLI seed and CAD. CAD seems to be less beneficial when using better pretrained models.

pact of training data size next.⁵

Role of Dataset Size. To better understand the role dataset size plays in OOD generalization, we plot the learning curve on SNLI CAD in Figure 3, where we gradually increase the amount of CAD for training. The baseline model is trained on SNLI seed examples of the same size, and all models are evaluated on MNLI (as the OOD dataset). We also conduct a similar experiment on BoolQ in Figure 4, where a subset of MultiRC (Khashabi et al., 2018) is used as the OOD dataset following Khashabi et al. (2020). Since the test set is unbalanced, we report F1 scores instead of accuracy in this case.

For SNLI, CAD is beneficial for OOD generalization only in low data settings (< 2000 examples). As the amount of data increases, the comparable SNLI baseline performs better and surpasses the performance of CAD. Similarly for BoolQ, we observe that CAD is comparable to the baseline in the low data setting (~ 1000 examples). Surprisingly, more CAD for BoolQ leads to worse OOD performance. We suspect this is due to overfitting to the specific perturbation types present in BoolQ CAD.

Intuitively, as we increase the amount of data, the diversity of robust features covered by the seed examples also increases. On the other hand, the benefit of CAD is restricted to the *perturbed* robust features. The plateaued performance of CAD (in the case of NLI) shows that the diversity of perturbations may not increase with the data size as fast as we would like, calling for better crowdsourcing protocols to elicit diverse edits from workers.

Role of Pretraining. Tu et al. (2020) show that larger pretrained models generalize better from minority examples. Therefore, in our case we would expect CAD to have limited benefit on larger pretrained models since they can already leverage the

⁵The results in Figure 2 when all perturbation types are included indicate that CAD performs better than the SNLI baseline. This is not in contradiction with the results found in Huang et al. (2020), since our models are trained on only a subset of CAD. This further motivates the study of how CAD data size affects generalization.

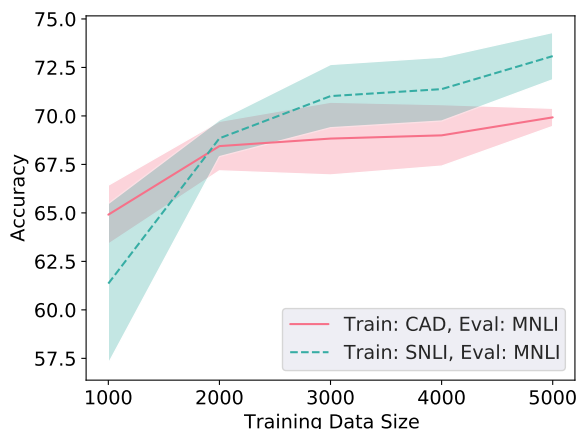


Figure 3: Accuracy on the OOD set (MNLI) for models trained on increasing amounts of NLI CAD. CAD is more beneficial in the low data regime, but its benefits taper off (compared to SNLI baseline of same size) as the dataset size increases.

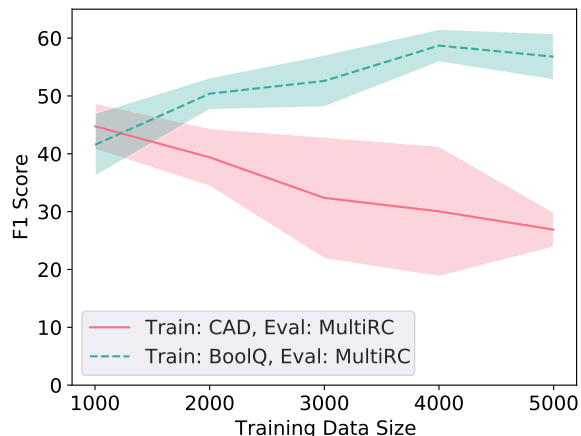


Figure 4: F1 score on the OOD set (MultiRC) for models trained on increasing amounts of QA CAD. CAD performs comparable to the baseline in the low data regime, but surprisingly performs worse with increasing dataset sizes, probably due to overfitting to a few perturbation types.

diverse (but scarce) robust features revealed by SNLI examples. We compare the results of BERT (Devlin et al., 2019) and RoBERTa (Liu et al., 2019) trained on SNLI CAD in Table 4 — both models are fine-tuned on the SNLI CAD dataset and are evaluated on the OOD set (MNLI). For the RoBERTa model (pretrained on more data), CAD no longer improves over the SNLI baseline, suggesting that current CAD datasets may not have much better coverage of robust features than what stronger pretrained models can already learn from benchmarks like SNLI.

4 CAD Exacerbates Existing Spurious Correlation

An artifact of underdiverse perturbations is the newly introduced spurious correlations. As an example, in the extreme case where all entailment examples are flipped to non-entailment by the negation operation in Table 1, the model would learn to exclusively rely on the existence of negation words to make predictions, which is clearly undesirable. In this section, we study the impact of CAD on two known spurious correlations in NLI benchmarks: word overlap bias (McCoy et al., 2019) and negation bias (Gururangan et al., 2018b).

Negation bias. We take examples where there is a presence of a negation word (i.e. "no", "not", "n't") in the hypothesis, and plot the fraction of examples in each class in both the seed and the

	Stress Test	MNLI subset
SNLI Seed	57.5 _{4.6}	63.3 _{3.8}
CAD	49.6 _{1.5}	55.7 _{4.2}

Table 5: Accuracy of models on challenge examples in the stress test and MNLI, where non-contradiction examples contain a negation word in the hypothesis. Models trained on CAD perform worse on both sets, implying that it exacerbates the negation bias.

corresponding CAD examples in Figure 5a. As expected, contradiction is the majority class in the seed group, but surprisingly, including CAD amplifies the fraction of contradiction examples! As a result, training on CAD leads to worse performance on challenge sets that counter the negation bias compared to training on seed examples of the same size. Specifically, we test on the ‘negation’ part of the Stress Tests (Naik et al., 2018)⁶ and challenge examples in the combined MNLI development set which contain negation words in the hypothesis but are not contradictions. Table 5 shows that models trained on CAD perform worse on both test sets, implying that they rely more on the negation bias.

Word-overlap bias. Similarly, in Figure 5b, we show that CAD amplifies the fraction of entailment examples among those with high word overlap (i.e. more than 90% of words in the hypoth-

⁶Synthetic examples where the phrase “and false is not true” is appended to the hypothesis of MNLI examples.

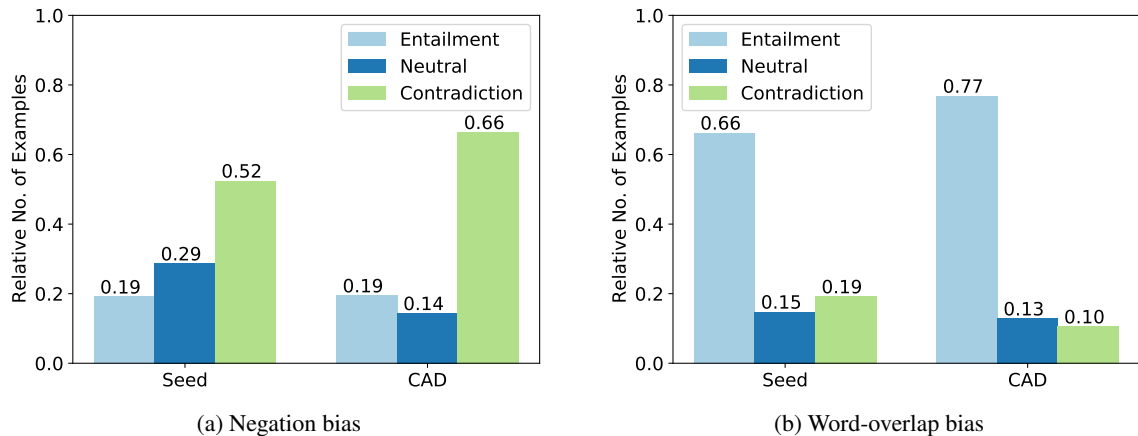


Figure 5: Fraction of entailment/neutral/contradiction examples in the SNLI seed set and CAD where (a) negation words are present in the hypothesis; (b) word overlap bias is observed. We observe that the distribution is more skewed in CAD compared to the seed examples, towards contradiction for the negation bias (a) and towards entailment for the word overlap bias (b).

esis are present in the premise). Models trained on SNLI and CAD both perform poorly (< 10% accuracy) on the non-entailment subset of HANS challenge set (McCoy et al., 2019), which exploits the word overlap bias.

Takeaway. This section reveals that in the process of creating CAD, we may inadvertently exacerbate existing spurious correlations. The fundamental challenge here is that perturbations of the robust features are only observed through word change in the sentence—it is hard to surface the underlying causal variables without introducing (additional) artifacts to the sentence form.

5 Related Work

Label-Preserving Data Augmentation. A common strategy to build more robust models is to augment existing datasets with examples similar to those from the target distribution. Min et al. (2020) improve accuracy on HANS challenge set (McCoy et al., 2019) by augmenting syntactically-rich examples. Jia and Liang (2016) and Andreas (2020) recombine examples to achieve better compositional generalization. There has also been a recent body of work using task-agnostic data augmentation by paraphrasing (Wei and Zou, 2019), back-translation (Sennrich et al., 2016) and masked language models (Ng et al., 2020). The main difference between these works and CAD is that the edits in these works are label-preserving whereas they are label-flipping in CAD—the former prevents models from being over-sensitive and the latter alleviates under-sensitivity to perturbations.

Label-Changing Data Augmentation. Lu et al. (2020) and Zmigrod et al. (2019) use rule-based CAD to mitigate gender stereotypes. Gardner et al. (2020) build similar contrast sets using expert edits for evaluation. In contrast, Kaushik et al. (2020) crowdsource minimal edits. Recently, Teney et al. (2020) also use CAD along with additional auxiliary training objectives and demonstrate improved OOD generalization.

Kaushik et al. (2021) analyze a similar toy model (linear Gaussian model) demonstrating the benefits of CAD, and showed that noising the edited spans hurts performance more than other spans. Our analysis complements theirs by showing that while spans identified by CAD are useful, a lack of diversity in these spans limit the effectiveness of CAD, thus better coverage of robust features could potentially lead to better OOD generalization.

Robust Learning Algorithms. Another direction of work has explored learning more robust models without using additional augmented data. These methods essentially rely on learning debiased representations—Wang et al. (2018) create a biased classifier and project its representation out of the model’s representation. Along similar lines, Belinkov et al. (2019) remove hypothesis-only bias in NLI models by adversarial training. He et al. (2019) and Clark et al. (2019b) correct the conditional distribution given a biased model. Utama et al. (2020) build on this to remove ‘unknown’ biases, assuming that a weak model learns a biased representations. More recently, Veitch et al. (2021) use ideas from causality to learn invariant predic-

tors from counterfactual examples. The main difference between these methods and CAD is that the former generally requires some prior knowledge of what spurious correlations models learn (e.g. by constructing a biased model or weak model), whereas CAD is a more general human-in-the-loop method that leverages humans’ knowledge of robust features.

6 Conclusion and Future Directions

In this work, we first analyzed CAD theoretically using a linear model and showed that models do not generalize to unperturbed robust features. We then empirically demonstrated this issue in two CAD datasets, where models do not generalize well to unseen perturbation types. We also showed that CAD amplifies existing spurious correlations, pointing out another concern. Given these results, a natural question is: How can we fix these problems and make CAD more useful for OOD generalization? We discuss a few directions which we think could be helpful:

- We can use generative models (Raffel et al., 2020; Lewis et al., 2020) to generate *diverse* minimal perturbations and then crowdsource labels for them (Wu et al., 2021). We can improve the diversity of the generations by masking different spans in the text to be in-filled, thus covering more robust features.
- An alternative to improving the crowdsourcing procedure is to devise better learning algorithms which mitigate the issues pointed out in this work. For example, given that we know the models do not always generalize well to unperturbed features, we can regularize the model to limit the reliance on the perturbed features.

We hope that this analysis spurs future work on CAD, making them more useful for OOD generalization.

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A Toy Example Proof

In this section, we give the proof for Proposition 1 for the toy example. For clarity, we also reproduce the statement of the proposition in this section:

Proposition 1. Define the error for a model as $\ell(w) = \mathbb{E}_{x \sim \mathcal{F}} [(w_{\text{inv}}^T x - w^T x)^2]$ where the distribution \mathcal{F} is the test distribution in which x_r and x_s are independent: $x_r | y \sim \mathcal{N}(y\mu_r, \sigma_r^2 I)$ and $x_s \sim \mathcal{N}(0, I)$.

Assuming all variables have unit variance (i.e. $\sigma_r = 1$ and $\sigma_s = 1$), $\|\mu_r\| = 1$, and $\|\mu_s\| = 1$, we get $\ell(\hat{w}_{\text{inc}}) > \ell(\hat{w})$ if $\|\mu_{r1}\|^2 < \frac{1+\sqrt{13}}{6} \approx 0.767$, where $\|\cdot\|$ denotes the Euclidean norm, and μ_{r1} is the mean of the perturbed robust feature r_1 .

Proof for Proposition 1. Given the definition of error we have,

$$\ell(\hat{w}) = \mathbb{E}_{x \sim \mathcal{F}} [(w_{\text{inv}}^T x - \hat{w}^T x)^2] \quad (11)$$

According to equation (6), we have $w_{\text{inv}} = [\Sigma_r^{-1} \mu_r, 0]$ where

$$\begin{aligned} \Sigma_r &= \text{Cov}(x_r, x_r) = \mathbb{E}_{x \sim \mathcal{D}} [x_r x_r^T] \\ &= \mathbb{E}_{y \sim \mathcal{D}} [\mathbb{E}_{x \sim \mathcal{D}} [x_r x_r^T | y]] \\ &= \mathbb{E}_{y \sim \mathcal{D}} [I + y^2 \mu_r \mu_r^T] \\ &= I + \mu_r \mu_r^T \end{aligned} \quad (12)$$

This gives us $\Sigma_r^{-1} = (I + \mu_r \mu_r^T)^{-1} = I - \alpha \mu_r \mu_r^T$ using the Sherman-Morrison formula since we have a rank-one perturbation of the identity matrix. Here $\alpha = \frac{1}{1 + \|\mu_r\|^2} = \frac{1}{2}$, giving $w_{\text{inv}} = [\frac{\mu_r}{2}, 0]$.

Now note that according to equation (4), $\hat{w} = M^{-1} \mu$ where M , the covariance matrix can be written as a block matrix as in equation (5). Hence we can formula for inverse of block matrix to get:

$$M^{-1} = \begin{bmatrix} I - \frac{1}{3} \mu_r \mu_r^T & -\frac{1}{3} \mu_r \mu_s^T \\ -\frac{1}{3} \mu_s \mu_r^T & I - \frac{1}{3} \mu_s \mu_s^T \end{bmatrix} \quad (13)$$

Note that we have not shown the actual plugging in the formula of block matrix inverse, and simplifying but it is to verify that $MM^{-1} = I$. Therefore, we get

$$\begin{aligned} \hat{w} &= M^{-1} \mu \\ &= \begin{bmatrix} I - \frac{1}{3} \mu_r \mu_r^T & -\frac{1}{3} \mu_r \mu_s^T \\ -\frac{1}{3} \mu_s \mu_r^T & I - \frac{1}{3} \mu_s \mu_s^T \end{bmatrix} \begin{bmatrix} \mu_r \\ \mu_s \end{bmatrix} \end{aligned} \quad (14)$$

$$= \frac{1}{3} \mu \quad (15)$$

since $\|\mu_r\| = 1$ and $\|\mu_s\| = 1$. Plugging all these back into equation (11), we get:

$$\begin{aligned} \ell(\hat{w}) &= \mathbb{E}_{x \sim \mathcal{F}} \left[\left(\frac{\mu_r^T x_r}{2} - \frac{\mu^T x}{3} \right)^2 \right] \\ &= \mathbb{E}_{x \sim \mathcal{F}} \left[\frac{\mu_r^T x_r x_r^T \mu_r}{4} + \frac{\mu^T x x^T \mu}{9} - \frac{\mu_r^T x_r x^T \mu}{3} \right] \end{aligned} \quad (16)$$

For the distribution \mathcal{F} we have, $\mathbb{E}_{x \sim \mathcal{F}} [x_r x_r^T] = I + \mu_r \mu_r^T$ (since x_r is distributed similarly in \mathcal{D} and \mathcal{F}), $\mathbb{E}_{x \sim \mathcal{F}} [x_r x^T] = [I + \mu_r \mu_r^T, 0]$ (since x_r and x_s are independent in \mathcal{F}) and $\mathbb{E}_{x \sim \mathcal{F}} [x x^T] = \begin{pmatrix} I + \mu_r \mu_r^T & 0 \\ 0 & I \end{pmatrix}$. Plugging all these back and again using $\|\mu_r\| = 1$, $\|\mu_s\| = 1$, we get

Test Set	Size (NLI)	Size (QA)
lexical	406	314
resemantic	640	332
negation	80	268
quantifier	206	80
insert	376	118
delete	250	-

Table 6: Size of the tests sets corresponding to the different perturbation types for both NLI and QA. For QA, the number of examples in delete were extremely small and hence we do not use that perturbation type for QA.

$$\begin{aligned}\ell(\hat{w}) &= \frac{1}{2} + \frac{2+1}{9} - \frac{2}{3} \\ &= \frac{1}{6}\end{aligned}\tag{17}$$

For the incomplete edits, we have $\hat{w}_{\text{inc}} = [\Sigma_{r1}^{-1} \mu_{r1}, 0]$ where $\Sigma_{r1}^{-1} = (I + \mu_{r1} \mu_{r1}^T)^{-1} = I - \gamma \mu_{r1} \mu_{r1}^T$, $\gamma = \frac{1}{1 + \|\mu_{r1}\|^2}$ using the Sherman-Morrison formula again, since we have a rank-one perturbation of the identity matrix. This gives $\hat{w}_{\text{inc}} = \frac{1}{1 + \|\mu_{r1}\|^2} [\mu_{r1}, 0]$. Note that $\mathbb{E}_{x \sim \mathcal{F}} [x_r x_r^T] = I + \mu_r \mu_r^T$, $\mathbb{E}_{x \sim \mathcal{F}} [x_{r1} x_{r1}^T] = I + \mu_{r1} \mu_{r1}^T$ and $\mathbb{E}_{x \sim \mathcal{F}} [x_r x_{r1}^T] = [I + \mu_{r1} \mu_{r1}^T, 0]^T$. Thus the error for incomplete edits is:

$$\begin{aligned}\ell(\hat{w}_{\text{inc}}) &= \mathbb{E}_{x \sim \mathcal{F}} \left[\frac{\mu_r^T x_r x_r^T \mu_r}{4} + \frac{\mu_{r1}^T x_{r1} x_{r1}^T \mu_{r1}}{(1 + \|\mu_{r1}\|^2)^2} - \frac{\mu_r^T x_r x_{r1}^T \mu_{r1}}{1 + \|\mu_{r1}\|^2} \right] \\ &= \frac{1}{2} + \frac{\|\mu_{r1}\|^2}{1 + \|\mu_{r1}\|^2} - \|\mu_{r1}\|^2\end{aligned}\tag{18}$$

Thus using equation (17) and (18), we get $\ell(\hat{w}_{\text{inc}}) > \ell(\hat{w})$ if $3\|\mu_{r1}\|^4 - \|\mu_{r1}\|^2 - 1 < 0$ which is exactly satisfied when $\|\mu_{r1}\|^2 < \frac{1 + \sqrt{13}}{6}$. □

B Additional Experiments & Results

Here, we report more details on the experiments as well as present some additional results.

B.1 Experiment Details

For NLI, models are trained for a maximum of 10 epochs, and for QA all models are trained for a maximum of 5 epochs (convergence is faster due to the larger dataset size). The best model is selected by performance on a held-out development set, that includes examples from the same perturbation type as in the training data.

B.2 Dataset Details

The size of the training datasets and how they are constructed are described in Section 3.2. Here, we give more details on the size of the various test sets used in the experiments. The size of the CAD datasets for the different perturbation types are given Table 6 for both NLI and QA. Note that all test sets contain paired counterfactual examples, i.e. the seed examples and their perturbations belonging to that specific perturbation type.

B.3 Accounting for small dataset sizes

The experiments in Section 3.2 were run for 5 different random initializations, and we report the mean and standard deviation across the random seeds. For completeness, we also report results when using different subsamples of the SNLI dataset. Table 7 shows the mean and standard deviation across 5 different subsamples, along with the rest of the results which were presented in Section 3.3. We observe that even though there is variance in results across the different subsamples, majority of the trends reported in 3.3 are consistent across the different subsamples — CAD performs well on aligned test sets, but does not necessarily generalize to unaligned test sets.

Train Data	All types	lexical	insert	resemantic	quantifier	negation	delete
SNLI seed	67.84 _{0.84}	75.16 _{0.32}	74.94 _{1.05}	76.77 _{0.74}	74.36 _{0.21}	69.25 _{2.09}	65.76 _{2.34}
SNLI seed (subsamples)	64.87 _{1.02}	75.06 _{1.89}	71.38 _{2.30}	73.84 _{1.60}	69.12 _{3.17}	66.75 _{2.87}	63.60 _{2.44}
lexical	70.44 _{1.07}	81.81 _{0.99}	74.04 _{1.04}	74.93 _{1.16}	72.42 _{1.58}	68.75 _{2.16}	67.04 _{3.00}
insert	66.00 _{1.41}	71.08 _{2.53}	78.98 _{1.58}	71.74 _{1.53}	68.15 _{0.88}	57.75 _{4.54}	68.80 _{2.71}
resemantic	70.80 _{1.68}	77.23 _{2.35}	76.59 _{1.12}	75.40 _{1.44}	70.77 _{1.04}	67.25 _{2.05}	70.40 _{1.54}

Table 7: Results for the different perturbation types in NLI with multiple subsamples of the dataset. (denotes *aligned test sets*). We observe that there is variance across different subsamples, but the majority of the trends reported in Section 3.3 still hold true.

Train Data	All types	lexical	insert	resemantic	quantifier	negation	delete
SNLI seed	71.41 _{0.40}	79.90 _{1.00}	78.08 _{0.49}	79.84 _{1.17}	75.92 _{1.17}	77.25 _{2.42}	70.88 _{0.68}
lexical	73.10 _{0.56}	83.54 _{0.91}	77.28 _{0.64}	80.81 _{0.47}	75.72 _{0.86}	78.00 _{1.69}	70.72 _{1.46}
insert	72.91 _{0.54}	80.39 _{0.88}	78.93 _{0.66}	80.56 _{0.76}	76.89 _{0.84}	77.25 _{2.66}	71.43 _{2.40}
resemantic	73.44 _{0.33}	81.23 _{0.64}	77.97 _{0.51}	81.06 _{0.49}	76.60 _{1.42}	75.75 _{2.03}	73.84 _{1.25}

Table 8: Results for the different perturbation types in NLI with larger dataset sizes, with 10% of the data being the perturbations (denotes *aligned test sets*).

To account for the small dataset sizes, we also ran an experiment using the NLI CAD dataset analogous to the QA setup—using a larger number of SNLI examples (7000) and replace a small percentage of them (10%) with perturbations of the corresponding perturbation type. We ensure that the original examples from which the perturbations were generated are also present in the dataset. Thus, all experiments will have much larger dataset sizes than before (7000 vs 1400), while still using counterfactual examples generated only by one specific perturbation type. The results for this experiment are reported in Table 8. We observe that CAD still performs best on aligned test sets but only marginally — this happens since a large fraction of the dataset (90%) is similar across all experiments. Although CAD performs worse on unaligned test sets than the aligned test sets, it does not necessarily perform worse than the SNLI baseline — this happens since the larger number of seed examples will implicitly regularize the model from overfitting to that specific perturbation type.