# What are the limitations on the flux of syntactic dependencies? Evidence from UD treebanks 

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#### Abstract

The aim of this paper is to study some characteristics of dependency flux, that is the set of dependencies linking a word on the left with a word on the right in a given position. Based on an exploration of the whole set of UD treebanks ( 12 M word corpus), we show that what we have called the flux weight, which measures center embeddings, is less than 3 in $99.62 \%$ of the inter-word positions and is bounded by 6 , which could be due to shortterm memory limitations.


## 1 Introduction

It is generally recognized that speaker performance is limited by several factors and especially by short-term memory. Yngve (1960) was one of the first to take these limitations into account in language modeling, on the grounds that "although all languages have a grammar based on constituent structure, the sentences actually used in the spoken language have a depth that does not exceed a certain number equal or nearly equal to the span of immediate memory (presently assumed to be $7 \pm 2$ )." This $7 \pm 2$ bound refers to the famous paper by Miller (1956). Miller (1962) and Chomsky and Miller (1963) stated that center-embedded constructions are limited. Very few studies have been conducted, however, on limitations on the syntactic structure. Gibson (1998) stated that "memory cost is hypothesized to be quantified in terms of the number of syntactic categories that are necessary to complete the current input string as a grammatical sentence", as well as the length during which "a predicted category must be kept in memory before the prediction is satisfied". Muratu et al. (2001) verified on a 20 K word corpus of Japanese that the number of words on the left
of a position that can have a dependent on the right (which will be called the left span of flux here) was bounded by 10. Liu (2008), Liu et al. (2009), and Liu (2010) expressed Gibson's hypothesis in terms of dependency length and studied it on Chinese data and on treebanks of 20 different languages.

In this paper, we will study dependency flux, that is the set of dependencies linking a word on the left with a word on the right in a given interword position. The notion of dependency flux was introduced in Kahane (2001:67) and previously studied on corpora of written French (Jardonnet 2009) and spoken French (Botalla 2014). This new study (Yan 2017) was conducted on the whole series of dependency treebanks provided by the Universal Dependencies (UD) project (Nivre et al. 2016), comprising 12M words and 630 K sentences distributed in 70 treebanks of 50 languages. ${ }^{1}$ Several features of the flux were measured: size, left and right spans, weight and density. Weight, which measures center embeddings and nested constructions, has stable properties: it seems to be distributed quite similarly in each corpus and language, and it is less than 3 in the overwhelming majority of the inter-word positions ( $99.62 \%$ ) and it never exceeds 6 .

Dependency flux and its main characteristics are defined in Section 2 and studied on the UD treebanks in Section 3. A closer look at weight is proposed in Section 4.

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Figure 1. A UD dependency tree with three inter-word positions marked

## 2 Dependency flux and its characteristics

### 2.1 Definition and size

The dependency flux in a given inter-word position is the set of dependencies at this position, that is, linking a word on the left with a word on the right. In Fig. 1, the flux contains one dependency at position 1 , three at positions 2 and 3 .

The size of the flux is the number of dependencies belonging to it. The size of the flux is the most basic information about the flux. It is therefore a useful starting point for apprehending other concepts about flux.

Two dependencies are said to be concomitant if they belong to the same flux. The dependencies "with <case guerillas" and "clashed obl> fight" are concomitant at position 2.

The flux represents the set of pending syntactic relations that the speaker has to keep in mind after every word. One might expect it to be limited by the same boundary as that stated by Miller (1956) and not exceed $7 \pm 2$. We will see that this is not the case.

### 2.2 Spans and bouquets

Other characteristics of the flux can be considered. The left span (resp. right span) of the flux is the number of words on the left (resp. right) which are vertices of a dependency in the flux. For instance, the left span is 1 in position 1 (US), 2 in position 2 (clashed, with) and 3 in position 3 (clashed, in, a).

The left span in a given position corresponds to the number of words awaiting a governor or a dependent on the right of this position and the right span to the number of elements expected. In a transition-based parser (Bohnet \& Nivre 2012, Dyer et al. 2015), it is the minimal number of words that must be stored in the stack. ${ }^{2}$ Again,

2 In practice all the nodes that are likely to have a dependent on the right are stored in the stack in
one might expect the left span to be bounded due to short-term memory limitations, but it is not really the case. This can be illustrated by looking at what happens at position 3: the left span is 3 but the right span is only 1 ; all the words of the left span are linked to the same word (fight) on the right. This means that the information can be factorized and that the three words in the left span count more or less as one, which is their common target.

The flux configuration in position 3 is called a left-branching bouquet. A bouquet is a set of dependencies sharing the same vertex. When the common vertex is on the left, the bouquet is right-branching, and left-branching when the common vertex is on the right (Fig. 2).


Figure 2. Right-branching bouquet

### 2.3 Disjoint dependencies and weight

We would like to measure the flux modulo the bouquets. This measure will be called the weight of the flux.

A set of dependencies is said to be disjoint if the dependencies do not share any vertex (Fig. 3). The weight is the size of the largest disjoint subset of dependencies in the flux.


Figure 3. Disjoint dependencies
The weight of the flux is equal to 1 in position 3: it is not possible to find two disjoint dependencies. The weight is equal to 2 in position 2 because the subset \{ with <case guerrillas, clashed obl> fight $\}$ is disjoint but there is no disjoint subset with 3 elements.
arc-standard and arc-eager parsing strategies.

As we will see in the next section, the weight is clearly bounded. The weight measures more or less the center-embeddings: the fact that the dependency "with <case guerrillas" is disjoint from "clashed obl> fight" but concomitant means that the phrase with guerrillas headed by guerrillas is center-embedded in the phrase headed by clashed. ${ }^{3}$ In other words, the weight is likely to measure the cognitive cost of parsing. This is noticeable if we compare the flux in positions 2 and 3. We saw earlier that the sizes of the flux at these two positions are equal: both have a value of 3 . However, their weights are unequal: the weight at position 2 has a value of 2, whereas the weight at position 3 has a value of 1 . Position 3 is simpler than position 2, because, as said before, the three dependencies at position 3 have a common target and requires less cognitive space than the disjoint dependencies at position 2.

We hypothesize that dependencies forming bouquets are cognitively less costly than dependencies forming disjoint subsets. This hypothesis is supported by the fact that the flux weight is clearly bounded while the size is not. We suppose that information can be factorized in case of dependencies sharing a same vertex. It is quite intuitive with right-branching bouquet, when the common vertex is on the left: only this vertex must be stored to analyze the bouquet. We postulate that the complexity is quite similar in case of left-branching bouquet, when two words are waiting for the same target word, but it remains to be proved by further studies.

Another advantage of the weight on the size is that it smooths out some idiosyncrasies of the UD scheme. For instance, coordination is analyzed in UD with every conjunct depending on the first conjunct, forming potentially very extended right-branching bouquets.

To calculate the weight, we have to find the biggest subset of disjoint dependencies in the flux. We can start with any dependency $D$ in the flux with at least one vertex that is not shared with other dependencies in the flux (such a dependency exists because the structure is acyclic). Then we suppress all the dependencies that share a vertex with D and therefore cannot be disjoint from $D$. If the remaining flux is not empty we start over exactly the same process: choosing a dependency with at least one vertex that is not shared with other dependencies in the remaining
${ }^{3}$ In UD, prepositions are dependent on the noun they introduce. That is why the head of the PP with guerrillas is the noun in the dependency tree taken as an example here.
flux and deleting all the dependencies sharing a vertex with it. At the end we obtain one of the biggest sets of disjoint dependencies in the flux. This simple algorithm is linear in time.

## 2.4 $\mathrm{R} / \mathrm{L}$ ratio and density

Note that the size of the flux is higher than the left and right span, which are both higher than the weight. Some ratios can be interesting to study.

Head-initial languages, such as Standard Arabic or Welsh, have right-branching dependency trees, while head-final languages, such as Japanese, Korean, or Turkish, have left-branching dependency trees. In other words, head-initial languages should have an $R / L$ ratio (where R is the right span and $L$ is the left span) higher than 1 and head-final languages an $\mathrm{R} / \mathrm{L}$ ratio less than 1. Unfortunately, UD is not a very good resource to measure that due to some idiosyncrasies of the UD scheme, such as the right-branching analysis of coordination, which is particularly irrelevant for head-final languages.

The density of the flux is the W/S ratio, where W is the weight and S is the size. This ratio measures the proportion of bouquets in the flux: a disjoint flux, that is, a flux without bouquets, has a density of 1 . The more bouquets the flux has, the lower the density is. For instance, the density in position 1 is 1 , in position $2,2 / 3$, and in position $3,1 / 3$.

## 3 Results on UD

### 3.1 The UD corpus

We studied the flux on the whole collection of UD treebanks. The 70 dependency treebanks distributed by the UD project have all been corrected manually and they follow a common annotation scheme. Nevertheless, these treebanks were developed by different teams, who may have interpreted the guidelines differently and the coherence and quality of the different treebanks have not yet been verified. And as mentioned above, some of the decisions made for the UD annotation scheme are not very suitable for a study of flux. Despite the defects of this resource, however, it is the only available resource of this scale allowing a cross-linguistic study of 50 different languages.

### 3.2 List of measures

Table 1 gives the following measures of the flux for each UD treebank. Average values were
calculated on the values in each inter-word position.

- S-max: maximum size
- S-av: average size
- W-max: maximum weight
- W-av: average weight
- L-max: maximum left span
- R-max: maximum right span
- L-av: average left span
- R-ax: average right span
- R/L-av: average $\mathrm{R} / \mathrm{L}$ ratio
- D-av: density = average W/S ratio


### 3.3 Sizes

The maximum size varies from 8 for Kazakh, Sanskrit, Uyghur, and Vietnamese, to 97 for Ancient Greek. The average size ranges from 1.92 for Polish to 3.61 for Czech-CLTT. As said before, the highest sizes are due to the bouquetwise annotation of some constructions, such as coordination (conj), apposition (appos), flat (sic!) constructions (flat), and multiword expressions (fixed). We converted the annotations to obtain a string-analysis of these constructions, giving a maximum size between 6 for Sanskrit and 77 for Arabic-NYUAD and an average size between 1.89 for Polish and 3.44 for Persian. ${ }^{4}$ Further investigations are needed to understand what could cause excessive flux sizes.

### 3.4 Weights

Compared to the size, the weight is more stable. The maximum weight ranges from 3 (only for Sanskrit) to 6. In the whole UD database only one occurrence with a weight of 7 was found, for Czech-CLTT. Most of the fluxes with a maximum weight that we checked were due to erroneous analysis. The average weight varied from 1.18 for Polish and Slovak to 1.77 for CzechCLTT. Weight is studied in greater detail in the next section.

### 3.5 Spans

The left span is more stable among the various treebanks than the right span with values between 7 and 17 against values between 5 and 97. As expected, treebanks with the highest $\mathrm{R} / \mathrm{L}$ ratio are head-initial languages: 1.31 for Old Church Slavonic, 1.37 for Irish, 1.55 and 1.32 for Arabic, 1.22 for Indonesian and 1.23 for Gothic. The first
exception is the value of 1.36 for Czech-CLTT, but this small corpus of Czech is atypical, the other two Czech treebanks having R/L ratios of 1.03 and 1.00 . The second exception is that we have the value of 1.29 for Dutch-LassySmall, while the other Dutch treebank has an $\mathrm{R} / \mathrm{L}$ ratio of 0.92 for Dutch.

The results for head-final languages are not relevant, as forecasted. Japanese has an R/L ratio of 1.17 , Turkish, 1.04, and Korean 0.99 , while the minimum ratio is 0.77 for Persian. The average ratio on the whole database is 1.05 .

### 3.6 Densities

The density is quite stable with an average value between $57.00 \%$ for Persian and $72.20 \%$ for Polish, with $65.31 \%$ for the whole database. This means that about $2 / 3$ of dependencies in the flux form together disjoint sets and $1 / 3$ are additional dependencies forming bouquets with the 2 other thirds. In fact, many fluxes have a density of 1 with only one element, as the flux at position 1 in Fig. 1, and form disjoint fluxes consequently.

## 4 A closer look at weight

### 4.1 Distribution of weight

Table 2 shows the distribution of the value of the weight of the flux for the 70 treebanks. For each treebank and each value between 1 and 6 , we indicate the percentage of inter-word positions in the treebank with this value.

The first main result is that $99.62 \%$ of interword positions in the whole UD database have a weight less than (or equal to) 3 . Only $0.36 \%$ have a weight of $4,0.02 \%$, of 5 , and $0.00 \%$ of 6. For Polish, Sanskrit, Slovak and Vietnamese, $99.9 \%$ of positions have a weight less than 3 .

We have seen that some small corpora, such as Czech-CLLT, can have more exceptional values. If we put corpora with fewer than 1,000 sentences aside, Arabic, Chinese, and Korean are the three languages with more than $10 \%$ of positions with weight of 3 .

Positions with a flux weight of 1 account for $62.15 \%$ of positions in the whole database, and more than $80 \%$ of positions in Finnish-FTB, Polish, and Slovak.

[^1]|  | Tokens | Trees | S-max | S-av | W-max | W-av | L-max | R-max | L-av | R-av | R/L-av | D-av |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| UD_Ancient_Greek | 182030 | 12613 | 97 | 3,01 | 6 | 1,49 | 12 | 97 | 2,31 | 1,99 | 1,13 | 60,32\% |
| UD_Ancient_Greek-PROIEL | 198034 | 15865 | 31 | 2,89 | 6 | 1,49 | 12 | 29 | 2,19 | 1,99 | 1,14 | 61,96\% |
| UD_Arabic | 254120 | 6984 | 36 | 2,93 | 5 | 1,66 | 9 | 35 | 2,06 | 2,41 | 1,32 | 66,47\% |
| UD_Arabic-NYUAD | 738889 | 19738 | 78 | 3,12 | 6 | 1,66 | 12 | 78 | 1,95 | 2,74 | 1,55 | 64,65\% |
| UD_Basque | 97069 | 7194 | 13 | 2,25 | 5 | 1,36 | 9 | 11 | 1,86 | 1,63 | 1,05 | 70,68\% |
| UD_Belarusian | 6864 | 333 | 17 | 2,48 | 4 | 1,44 | 9 | 17 | 1,98 | 1,78 | 1,09 | 69,28\% |
| UD_Bulgarian | 140425 | 10022 | 14 | 2,24 | 5 | 1,28 | 9 | 14 | 1,90 | 1,50 | 0,97 | 67,67\% |
| UD_Catalan | 474069 | 14832 | 20 | 2,69 | 6 | 1,48 | 13 | 19 | 2,17 | 1,83 | 1,03 | 64,16\% |
| UD_Chinese | 111271 | 4497 | 27 | 3,24 | 6 | 1,65 | 14 | 25 | 2,77 | 1,86 | 0,84 | 61,28\% |
| UD_Coptic | 8519 | 320 | 9 | 2,74 | 4 | 1,43 | 8 | 8 | 2,23 | 1,74 | 1,00 | 60,08\% |
| UD_Croatian | 183816 | 8289 | 13 | 2,52 | 5 | 1,40 | 11 | 13 | 2,13 | 1,65 | 0,98 | 65,74\% |
| UD_Czech | 1332566 | 77765 | 56 | 2,43 | 6 | 1,37 | 17 | 56 | 2,03 | 1,63 | 1,00 | 67,23\% |
| UD_Czech-CAC | 483520 | 24081 | 47 | 2,50 | 6 | 1,39 | 11 | 47 | 2,04 | 1,71 | 1,03 | 66,49\% |
| UD_Czech-CLTT | 26781 | 814 | 28 | 3,61 | 7 | 1,77 | 10 | 24 | 2,36 | 2,83 | 1,36 | 62,24\% |
| UD_Danish | 90710 | 4947 | 16 | 2,61 | 4 | 1,34 | 16 | 12 | 2,20 | 1,61 | 0,97 | 63,32\% |
| UD_Dutch | 197925 | 13050 | 15 | 2,89 | 5 | 1,43 | 12 | 15 | 2,46 | 1,69 | 0,92 | 60,44\% |
| UD_Dutch-LassySmall | 91793 | 6841 | 29 | 2,74 | 4 | 1,33 | 10 | 29 | 2,06 | 1,87 | 1,21 | 61,32\% |
| UD_English | 229733 | 14545 | 18 | 2,58 | 6 | 1,35 | 13 | 17 | 2,19 | 1,58 | 0,92 | 63,01\% |
| UD_English-LinES | 67197 | 3650 | 25 | 2,54 | 5 | 1,35 | 10 | 24 | 2,13 | 1,61 | 0,95 | 63,89\% |
| UD_English-ParTUT | 38114 | 1590 | 15 | 2,63 | 5 | 1,39 | 9 | 14 | 2,26 | 1,60 | 0,89 | 62,79\% |
| UD_Estonian | 34628 | 3172 | 10 | 2,26 | 5 | 1,25 | 9 | 10 | 1,82 | 1,58 | 1,11 | 68,04\% |
| UD_Finnish | 180911 | 13581 | 33 | 2,31 | 6 | 1,31 | 10 | 33 | 1,89 | 1,63 | 1,06 | 68,53\% |
| UD_Finnish-FTB | 143326 | 16856 | 14 | 2,06 | 5 | 1,19 | 11 | 14 | 1,77 | 1,39 | 0,98 | 70,29\% |
| UD_French | 392230 | 16031 | 34 | 2,51 | 5 | 1,39 | 11 | 34 | 2,04 | 1,71 | 1,02 | 65,09\% |
| UD_French-ParTUT | 17927 | 620 | 11 | 2,70 | 5 | 1,44 | 11 | 10 | 2,31 | 1,68 | 0,91 | 62,86\% |
| UD_French-Sequoia | 60574 | 2643 | 31 | 2,63 | 5 | 1,44 | 12 | 31 | 2,15 | 1,75 | 1,00 | 64,58\% |
| UD_Galician | 109106 | 3139 | 15 | 2,56 | 5 | 1,41 | 11 | 15 | 2,04 | 1,80 | 1,08 | 64,54\% |
| UD_Galician-TreeGal | 15436 | 600 | 13 | 2,55 | 4 | 1,43 | 9 | 12 | 2,12 | 1,71 | 1,00 | 65,30\% |
| UD_German | 281974 | 14917 | 28 | 3,00 | 6 | 1,46 | 13 | 26 | 2,51 | 1,76 | 0,96 | 59,84\% |
| UD_Gothic | 45138 | 4372 | 21 | 2,53 | 4 | 1,38 | 10 | 20 | 1,87 | 1,91 | 1,23 | 65,96\% |
| UD_Greek | 51351 | 2065 | 13 | 2,51 | 5 | 1,41 | 10 | 9 | 2,12 | 1,65 | 0,95 | 65,57\% |
| UD_Hebrew | 149088 | 5725 | 62 | 2,56 | 5 | 1,48 | 11 | 61 | 2,01 | 1,86 | 1,11 | 66,99\% |
| UD_Hindi | 316274 | 14963 | 18 | 3,20 | 6 | 1,58 | 13 | 15 | 2,76 | 1,84 | 0,85 | 59,67\% |
| UD_Hungarian | 31584 | 1351 | 13 | 2,83 | 6 | 1,54 | 10 | 10 | 2,44 | 1,75 | 0,89 | 64,54\% |
| UD_Indonesian | 110143 | 5036 | 28 | 2,31 | 5 | 1,39 | 9 | 28 | 1,75 | 1,85 | 1,22 | 70,30\% |
| UD_Irish | 13826 | 566 | 18 | 2,88 | 5 | 1,56 | 7 | 18 | 1,94 | 2,34 | 1,37 | 64,95\% |
| UD_Italian | 282611 | 13402 | 35 | 2,50 | 5 | 1,39 | 10 | 34 | 2,10 | 1,65 | 0,96 | 65,69\% |
| UD_Italian-ParTUT | 42651 | 1590 | 14 | 2,59 | 5 | 1,43 | 9 | 14 | 2,20 | 1,66 | 0,93 | 64,46\% |
| UD_Japanese | 173458 | 7675 | 15 | 2,79 | 5 | 1,55 | 15 | 11 | 2,17 | 2,03 | 1,17 | 64,52\% |
| UD_Kazakh | 529 | 31 | 8 | 2,67 | 4 | 1,52 | 6 | 5 | 2,21 | 1,82 | 1,00 | 67,07\% |
| UD_Korean | 63426 | 5350 | 23 | 2,73 | 5 | 1,62 | 9 | 20 | 2,25 | 1,93 | 0,99 | 68,80\% |
| UD_Latin | 18184 | 1334 | 17 | 2,86 | 5 | 1,52 | 8 | 16 | 2,31 | 1,87 | 1,02 | 63,32\% |
| UD_Latin-ITTB | 280734 | 16508 | 11 | 2,67 | 6 | 1,46 | 10 | 10 | 2,30 | 1,65 | 0,89 | 64,10\% |
| UD_Latin-PROIEL | 159407 | 15324 | 28 | 2,77 | 6 | 1,47 | 14 | 28 | 2,15 | 1,91 | 1,12 | 64,14\% |
| UD_Latvian | 44795 | 3054 | 18 | 2,48 | 6 | 1,39 | 9 | 17 | 2,04 | 1,68 | 0,99 | 67,31\% |
| UD_Lithuanian | 5356 | 263 | 14 | 2,43 | 4 | 1,38 | 9 | 13 | 2,06 | 1,60 | 0,95 | 68,01\% |
| UD_Norwegian-Bokmaal | 280256 | 18106 | 38 | 2,44 | 5 | 1,30 | 11 | 38 | 2,08 | 1,54 | 0,96 | 64,18\% |
| UD_Norwegian-Nynorsk | 276580 | 16064 | 38 | 2,50 | 6 | 1,32 | 11 | 38 | 2,12 | 1,57 | 0,96 | 63,82\% |
| UD_Old_Church_Slavonic | 47532 | 5196 | 20 | 2,48 | 5 | 1,34 | 8 | 19 | 1,76 | 1,93 | 1,31 | 66,03\% |
| UD_Persian | 136896 | 5397 | 14 | 3,45 | 6 | 1,64 | 13 | 10 | 3,03 | 1,81 | 0,77 | 57,00\% |
| UD_Polish | 72763 | 7127 | 10 | 1,92 | 4 | 1,18 | 8 | 7 | 1,62 | 1,40 | 1,04 | 72,20\% |
| UD_Portuguese | 217591 | 8891 | 19 | 2,54 | 5 | 1,43 | 13 | 19 | 2,12 | 1,70 | 0,98 | 65,84\% |
| UD_Portuguese-BR | 287884 | 10874 | 38 | 2,54 | 5 | 1,45 | 10 | 38 | 2,05 | 1,77 | 1,04 | 66,46\% |
| UD_Romanian | 202187 | 8795 | 14 | 2,39 | 6 | 1,40 | 9 | 14 | 1,95 | 1,69 | 1,05 | 67,75\% |
| UD_Russian | 87841 | 4429 | 31 | 2,34 | 5 | 1,37 | 10 | 30 | 1,83 | 1,74 | 1,12 | 69,62\% |
| UD_Russian-SynTagRus | 988460 | 55398 | 18 | 2,34 | 6 | 1,37 | 10 | 17 | 1,94 | 1,63 | 1,01 | 68,64\% |
| UD_Sanskrit | 1206 | 190 | 8 | 2,23 | 3 | 1,29 | 6 | 5 | 2,05 | 1,39 | 0,82 | 68,76\% |
| UD_Slovak | 93015 | 9543 | 10 | 2,00 | 4 | 1,18 | 9 | 8 | 1,74 | 1,36 | 0,96 | 70,22\% |
| UD_Slovenian | 126593 | 7212 | 17 | 2,50 | 5 | 1,30 | 13 | 17 | 2,21 | 1,47 | 0,87 | 64,12\% |
| UD_Slovenian-SST | 19488 | 2137 | 14 | 2,77 | 4 | 1,33 | 12 | 8 | 2,34 | 1,62 | 0,94 | 60,51\% |
| UD_Spanish | 419587 | 15587 | 38 | 2,51 | 5 | 1,42 | 11 | 38 | 2,03 | 1,74 | 1,04 | 65,91\% |
| UD_Spanish-AnCora | 496953 | 15959 | 31 | 2,63 | 5 | 1,47 | 12 | 31 | 2,16 | 1,76 | 1,00 | 65,21\% |
| UD_Swedish | 76442 | 4807 | 31 | 2,58 | 5 | 1,32 | 10 | 31 | 2,07 | 1,68 | 1,04 | 62,95\% |
| UD_Swedish-LinES | 64787 | 3650 | 25 | 2,55 | 5 | 1,34 | 10 | 24 | 2,07 | 1,67 | 1,03 | 63,25\% |
| UD_Tamil | 9581 | 600 | 10 | 2,42 | 4 | 1,48 | 9 | 8 | 2,07 | 1,74 | 1,00 | 70,91\% |
| UD_Turkish | 48093 | 4660 | 13 | 2,44 | 6 | 1,48 | 9 | 13 | 2,00 | 1,77 | 1,04 | 71,20\% |
| UD_Ukrainian | 12846 | 863 | 11 | 2,19 | 4 | 1,27 | 8 | 9 | 1,85 | 1,49 | 0,98 | 69,22\% |
| UD_Urdu | 123271 | 4595 | 32 | 3,44 | 5 | 1,66 | 15 | 29 | 2,92 | 1,96 | 0,85 | 58,34\% |
| UD_Uyghur | 1662 | 100 | 8 | 2,93 | 5 | 1,73 | 7 | 6 | 2,75 | 1,80 | 0,77 | 67,31\% |
| UD_Vietnamese | 31799 | 2200 | 8 | 2,09 | 4 | 1,25 | 7 | 8 | 1,68 | 1,57 | 1,12 | 70,45\% |
| Total | 1E+007 | 630518 | 97 | 2,62 | 7 | 1,43 | 17 | 97 | 2,11 | 1,79 | 1,05 | 65,31\% |

Table 1: Size, weight, left and right spans, R/L ratio and density for the 70 UD treebanks available

|  | Tokens | Trees | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| UD_Ancient_Greek | 182030 | 12613 | 57.77\% | 35.79\% | 5.96\% | 0.45\% | 0.02\% | 0.00\% |
| UD_Ancient_Greek-PROIEL | 198034 | 15865 | 57.81\% | 35.97\% | 5.74\% | 0.46\% | 0.02\% | 0.00\% |
| UD_Arabic | 254120 | 6984 | 47.15\% | 41.10\% | 10.60\% | 1.10\% | 0.05\% | 0.00\% |
| UD_Arabic-NYUAD | 738889 | 19738 | 47.16\% | 40.86\% | 10.67\% | 1.23\% | 0.08\% | 0.00\% |
| UD_Basque | 97069 | 7194 | 67.85\% | 28.28\% | 3.66\% | 0.21\% | 0.01\% | 0.00\% |
| UD_Belarusian | 6864 | 333 | 62.43\% | 31.70\% | 5.37\% | 0.50\% | 0.00\% | 0.00\% |
| UD_Bulgarian | 140425 | 10022 | 73.86\% | 24.20\% | 1.87\% | 0.06\% | 0.00\% | 0.00\% |
| UD_Catalan | 474069 | 14832 | 57.82\% | 36.58\% | 5.30\% | 0.30\% | 0.01\% | 0.00\% |
| UD_Chinese | 111271 | 4497 | 49.73\% | 37.35\% | 10.91\% | 1.78\% | 0.22\% | 0.01\% |
| UD_Coptic | 8519 | 320 | 61.76\% | 33.74\% | 4.37\% | 0.13\% | 0.00\% | 0.00\% |
| UD_Croatian | 183816 | 8289 | 64.46\% | 31.70\% | 3.66\% | 0.17\% | 0.01\% | 0.00\% |
| UD_Czech | 1332566 | 77765 | 66.78\% | 29.61\% | 3.42\% | 0.17\% | 0.01\% | 0.00\% |
| UD_Czech-CAC | 483520 | 24081 | 65.16\% | 30.82\% | 3.80\% | 0.22\% | 0.01\% | 0.00\% |
| UD_Czech-CLTT | 26781 | 814 | 42.78\% | 41.74\% | 12.19\% | 2.71\% | 0.53\% | 0.05\% |
| UD_Danish | 90710 | 4947 | 69.13\% | 27.85\% | 2.90\% | 0.12\% | 0.00\% | 0.00\% |
| UD_Dutch | 197925 | 13050 | 63.41\% | 31.12\% | 5.00\% | 0.44\% | 0.02\% | 0.00\% |
| UD_Dutch-LassySmall | 91793 | 6841 | 70.30\% | 27.04\% | 2.50\% | 0.15\% | 0.00\% | 0.00\% |
| UD_English | 229733 | 14545 | 68.45\% | 28.08\% | 3.29\% | 0.17\% | 0.00\% | 0.00\% |
| UD_English-LinES | 67197 | 3650 | 68.40\% | 28.16\% | 3.20\% | 0.23\% | 0.01\% | 0.00\% |
| UD_English-ParTUT | 38114 | 1590 | 64.99\% | 31.09\% | 3.77\% | 0.15\% | 0.00\% | 0.00\% |
| UD_Estonian | 34628 | 3172 | 77.26\% | 20.37\% | 2.21\% | 0.15\% | 0.01\% | 0.00\% |
| UD_Finnish | 180911 | 13581 | 72.60\% | 23.79\% | 3.28\% | 0.30\% | 0.03\% | 0.00\% |
| UD_Finnish-FTB | 143326 | 16856 | 82.77\% | 15.91\% | 1.22\% | 0.10\% | 0.00\% | 0.00\% |
| UD_French | 392230 | 16031 | 64.31\% | 32.23\% | 3.27\% | 0.17\% | 0.01\% | 0.00\% |
| UD_French-ParTUT | 17927 | 620 | 60.66\% | 34.99\% | 4.05\% | 0.26\% | 0.03\% | 0.00\% |
| UD_French-Sequoia | 60574 | 2643 | 61.25\% | 33.76\% | 4.69\% | 0.29\% | 0.01\% | 0.00\% |
| UD_Galician | 109106 | 3139 | 62.78\% | 33.73\% | 3.34\% | 0.14\% | 0.00\% | 0.00\% |
| UD_Galician-TreeGal | 15436 | 600 | 61.98\% | 33.75\% | 4.02\% | 0.25\% | 0.00\% | 0.00\% |
| UD_German | 281974 | 14917 | 59.60\% | 35.60\% | 4.46\% | 0.33\% | 0.01\% | 0.00\% |
| UD_Gothic | 45138 | 4372 | 65.83\% | 30.51\% | 3.46\% | 0.21\% | 0.00\% | 0.00\% |
| UD_Greek | 51351 | 2065 | 62.49\% | 33.73\% | 3.59\% | 0.19\% | 0.00\% | 0.00\% |
| UD_Hebrew | 149088 | 5725 | 58.04\% | 36.56\% | 5.17\% | 0.23\% | 0.00\% | 0.00\% |
| UD_Hindi | 316274 | 14963 | 49.02\% | 44.76\% | 5.65\% | 0.54\% | 0.03\% | 0.00\% |
| UD_Hungarian | 31584 | 1351 | 56.04\% | 35.24\% | 7.58\% | 0.99\% | 0.14\% | 0.02\% |
| UD_Indonesian | 110143 | 5036 | 64.82\% | 31.38\% | 3.61\% | 0.18\% | 0.01\% | 0.00\% |
| UD_Irish | 13826 | 566 | 53.11\% | 38.57\% | 7.47\% | 0.82\% | 0.03\% | 0.00\% |
| UD_Italian | 282611 | 13402 | 64.93\% | 31.55\% | 3.37\% | 0.16\% | 0.01\% | 0.00\% |
| UD_Italian-ParTUT | 42651 | 1590 | 61.56\% | 34.48\% | 3.78\% | 0.17\% | 0.00\% | 0.00\% |
| UD_Japanese | 173458 | 7675 | 50.98\% | 42.82\% | 6.03\% | 0.17\% | 0.00\% | 0.00\% |
| UD_Kazakh | 529 | 31 | 55.27\% | 37.42\% | 6.88\% | 0.43\% | 0.00\% | 0.00\% |
| UD_Korean | 63426 | 5350 | 51.30\% | 37.10\% | 10.24\% | 1.28\% | 0.09\% | 0.00\% |
| UD_Latin | 18184 | 1334 | 56.34\% | 35.90\% | 7.01\% | 0.69\% | 0.06\% | 0.00\% |
| UD_Latin-ITTB | 280734 | 16508 | 60.44\% | 33.25\% | 5.85\% | 0.45\% | 0.02\% | 0.00\% |
| UD_Latin-PROIEL | 159407 | 15324 | 61.30\% | 31.41\% | 6.27\% | 0.92\% | 0.10\% | 0.00\% |
| UD_Latvian | 44795 | 3054 | 67.21\% | 27.51\% | 4.75\% | 0.48\% | 0.05\% | 0.01\% |
| UD_Lithuanian | 5356 | 263 | 66.76\% | 28.97\% | 4.07\% | 0.21\% | 0.00\% | 0.00\% |
| UD_Norwegian-Bokmaal | 280256 | 18106 | 72.73\% | 24.95\% | 2.23\% | 0.08\% | 0.00\% | 0.00\% |
| UD_Norwegian-Nynorsk | 276580 | 16064 | 70.73\% | 26.67\% | 2.50\% | 0.10\% | 0.00\% | 0.00\% |
| UD_Old_Church_Slavonic | 47532 | 5196 | 69.31\% | 27.41\% | 3.15\% | 0.13\% | 0.00\% | 0.00\% |
| UD_Persian | 136896 | 5397 | 45.75\% | 45.14\% | 8.52\% | 0.59\% | 0.01\% | 0.00\% |
| UD_Polish | 72763 | 7127 | 82.46\% | 16.96\% | 0.57\% | 0.00\% | 0.00\% | 0.00\% |
| UD_Portuguese | 217591 | 8891 | 61.69\% | 33.94\% | 4.16\% | 0.21\% | 0.01\% | 0.00\% |
| UD_Portuguese-BR | 287884 | 10874 | 60.06\% | 35.50\% | 4.24\% | 0.20\% | 0.01\% | 0.00\% |
| UD_Romanian | 202187 | 8795 | 64.42\% | 31.62\% | 3.74\% | 0.22\% | 0.00\% | 0.00\% |
| UD_Russian | 87841 | 4429 | 66.76\% | 29.75\% | 3.28\% | 0.21\% | 0.00\% | 0.00\% |
| UD_Russian-SynTagRus | 988460 | 55398 | 67.30\% | 29.04\% | 3.42\% | 0.23\% | 0.01\% | 0.00\% |
| UD_Sanskrit | 1206 | 190 | 71.95\% | 27.07\% | 0.98\% | 0.00\% | 0.00\% | 0.00\% |
| UD_Slovak | 93015 | 9543 | 83.09\% | 16.24\% | 0.66\% | 0.01\% | 0.00\% | 0.00\% |
| UD_Slovenian | 126593 | 7212 | 72.12\% | 25.49\% | 2.31\% | 0.08\% | 0.00\% | 0.00\% |
| UD_Slovenian-SST | 19488 | 2137 | 70.09\% | 26.59\% | 3.17\% | 0.15\% | 0.00\% | 0.00\% |
| UD_Spanish | 419587 | 15587 | 61.54\% | 34.75\% | 3.56\% | 0.15\% | 0.01\% | 0.00\% |
| UD_Spanish-AnCora | 496953 | 15959 | 58.20\% | 36.45\% | 5.10\% | 0.25\% | 0.00\% | 0.00\% |
| UD_Swedish | 76442 | 4807 | 70.77\% | 26.62\% | 2.50\% | 0.10\% | 0.01\% | 0.00\% |
| UD_Swedish-LinES | 64787 | 3650 | 69.32\% | 27.51\% | 3.03\% | 0.13\% | 0.00\% | 0.00\% |
| UD_Tamil | 9581 | 600 | 58.14\% | 36.18\% | 5.23\% | 0.45\% | 0.00\% | 0.00\% |
| UD_Turkish | 48093 | 4660 | 60.71\% | 31.69\% | 6.69\% | 0.85\% | 0.06\% | 0.00\% |
| UD_Ukrainian | 12846 | 863 | 74.84\% | 23.60\% | 1.49\% | 0.06\% | 0.00\% | 0.00\% |
| UD_Urdu | 123271 | 4595 | 44.94\% | 45.09\% | 8.82\% | 1.04\% | 0.11\% | 0.00\% |
| UD_Uyghur | 1662 | 100 | 43.87\% | 42.16\% | 11.50\% | 2.12\% | 0.34\% | 0.00\% |
| UD_Vietnamese | 31799 | 2200 | 76.10\% | 22.71\% | 1.18\% | 0.01\% | 0.00\% | 0.00\% |
| Total | $1.2 \mathrm{E}+07$ | 630518 | 62.15\% | 32.75\% | 4.71\% | 0.36\% | 0.02\% | 0.00\% |

Table 2: Percentage of inter-word positions for every possible value of the weight


Figure 4. A dependency tree from UD-English with weight 5

We do not have enough metadata to know if the differences between treebanks are due to differences between languages or to differences between genres. It is highly likely that some kinds of texts (e.g. legal texts, specification sheets) are much more complicated than others. For 16 languages, there are two or three treebanks and noticeable divergences are observed in only three cases (Finnish, Dutch, and again Czech-CLTT). At first sight variations between languages appear to be greater than variations between corpora in the same language, but this point needs further investigation.

### 4.2 Examples

The only example of English with weight 6 was erroneously annotated. We give here two examples with weight 5 . In all the examples, punctuation links (punct) have been removed and are not considered.
(1) I dont know how it is possible to make orange chicken, sesame chicken and kung pao
chicken as well as cheese puffs taste THAT bad but China Delight accomplished that. (en-udtrain.conllu sent_id = reviews-235423-0012)

Sentence (1) has a weight of 5 between kung and pao (Fig. 4). A set of five disjoint dependencies at this point is:

1: kung <compound pao
2: and $<\mathrm{cc}$ chicken $_{3}$
3: chicken ${ }_{1}$ con $j>$ puffs
4: make xcomp> taste
5: know conj> accomplished
(2) as an example they took payment for 5 out of 6 monthly plan premiums for a yearly policy and cancelled the contract for the remainder of the policy for reasons they stated was not receiving information on other licensed drivers in the household? (en-ud-train.conllu sent_id $=$ re-views-217359-0006)


Figure 5. Another dependency tree from UD-English with weight 5

Sentence（2）has two positions with weight 5 ．We consider the flux between out and of（Fig．5）．

1：out case＞ 6
2： $5<$ compound monthly
3：for＜case premiums
4：payment nmod＞policy
5：took con $j>$ cancelled
If we except the two small corpora of Czech and Uyghur，Chinese appears to be the language with the largest number of positions with a weight higher than 5 （ $0.23 \%$ ）．We will study an example with weight 6 ．
（3）一 級 抗體 對於 檢測 如
one level antibody for detect such＿as
癌症，糖尿 病，帕金森氏 症
cancer，diabetes disease，Parkinson＇s disease
和 阿爾茨海默氏 病 等 疾病 and Alzheimer＇s disease etc．disease

所 特有 的 生物 標記
that specifically＿have de（PART）biology marker
是非常有用的。
be very useful de（PART）．
（zh－ud－train．conllu id＝21）
＇Primary antibodies are useful for detecting biomarkers that diseases such as cancer，diabetes， Parkinson＇s disease，Alzheimer＇s disease，etc． specifically contain．＇

The weight 6 appears between the noun 阿爾茨海默 ‘Alzheimer’ and the case particle 氏（＇s）． This flux contains 9 dependencies and can be separated into 6 disjoint bouquets of dependen－ cies：
1：阿爾茨海默 ‘Alzheimer＇$<$ case：suff 氏
2：和＇and＇$<\mathrm{cc}$ 病 ‘disease’
3：癌症＇cancer＇conj＞病＇disease＇
癌症＇cancer acl＞等＇etc．＇
癌症＇cancer＇appos＞疾病＇disease＇
4：如＇such＿as＇＜csubj 特有＇specifically＿have＇
5：檢測 ‘detect’ obj＞疾病 ‘disease’
檢測＇detect＇xcomp＞有用‘useful＇
6：抗體‘antibody’＜nsubj 有用‘useful＇
The complexity of this Chinese sentence，com－ pared to its English translation，is in great part due to word order differences．

1．In Chinese，adverbs and adverbial modifiers are placed before the verb．As a result，有用 ＇useful＇is at the end of the sentence and the long adverbial modifier＇for detecting ．．．＇is between the subject and the verb．
2．Noun modifiers are placed before the noun and＇［diseases［such as cancer，diabetes，Parkin－ son＇s disease，and Alzheimer＇s disease，etc．］＇be－ comes＇［［such as cancer，diabetes，Parkinson＇s disease，and Alzheimer＇s disease，etc．］ diseases］＇）．


Figure 6．A dependency tree from UD－Chinese with weight 6
3. Relative clauses are also placed before the noun, which is a source of complexity discussed in Hsiao \& Gibson (2003): "A key word-order difference between Chinese and other Subject-Verb-Object languages is that Chinese relative clauses precede their head nouns. Because of this word order difference, the results follow from a resource-based theory of sentence complexity, according to which there is a storage cost associated with predicting syntactic heads in order to form a grammatical sentence."
In any case, [biomarkers [ (that are) specific to[ diseases [such as cancer, diabetes, Parkinson's disease, and Alzheimer's disease etc.]]]] becomes [ [[[such as cancer, diabetes, Parkinson's disease, and Alzheimer's disease etc.] disease] (that) specifically have] biomarkers].

## 5 Conclusion

We have studied different parameters concerning the dependency flux on a set of treebanks in 50 languages. We saw that the size, as well as the left and right spans, of the flux can vary considerably depending on the corpus and its language, and that they are not clearly bounded. Moreover, these values are quite heavily dependent on certain annotation choices. For instance the fact that UD proposes a bouquet-based analysis (rather than a string-based analysis) of coordination (and other similar constructions) significantly increases the size and the right span of the dependency flux.

Conversely, the dependency flux weight appears to be more homogeneous across languages and much less dependent on particular annotation choices (such as bouquet vs. string-based analysis of coordination). Weight measures what is traditionally called center embedding in con-stituency-based formalisms. We observe that weight is bounded by 5 except for very few positions (less than 1 position for 10,000 with weight of 6), which could be related to short-term memory limitations.

What now remains is to study all the data we have collected to determine, language after language, genre after genre, what are the most complex constructions and under which conditions they can appear. In particular, a comparison between weight and dependency distance (Liu 2010) is needed to determine how they are correlated and which one is the best predictor of the complexity. ${ }^{5}$

5 Fluxes with important weight or size tend to contain long dependencies and long dependencies to

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[^0]:    1 Our experiments have been done on UD v2 available in May 2017.

[^1]:    4 The maximum size for Arabic is due to a sentence with 385 words and 77 nominal modifier (nmod) relations depending on the $5^{\text {th }}$ word, which is likely to be a wrong analysis.

