

# Automated essay scoring with string kernels and word embeddings

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# Highlights

- We propose to combine string kernels (low-level character) n-gram features) and word embeddings (high-level semantic features) for automated essay scoring (AED)
- TOK, string kernels have never been used for AED
- TOK, this is the first successful attempt to combine string kernels and word embeddings
- Using a shallow approach, we surpass recent deep learning approaches [Dong et al, EMNLP 2016; Dong et al, CONLL 2017;Tay et al, AAAI 2018]

# **Fusion and learning method**

- We combine HISK and BOSWE in the dual (kernel) form, by simply summing up the two corresponding kernel matrices
- Note: summing up kernel matrices is equivalent to feature vector concatenation in the primal Hilbert space
- We employ  $\nu$ -Support Vector Regression ( $\nu$ -SVR) in order to automatically predict the score for an essay

#### Data set

Prompt	Number of Essays	Score Range
1	1783	2-12

#### String kernels

• We use the histogram intersection string kernel (HISK), which is formally defined as follows:

$$x^{\cap}(x, y) = \sum_{v \in \Sigma^n} \min\{\operatorname{num}_v(x), \operatorname{num}_v(y)\},$$

where  $x, y \in \Sigma^*$  are two strings over an alphabet  $\Sigma$ , num<sub>v</sub>(x) is the number of occurrences of n-gram v as a substring in x, and *n* is the length of *v*.

• We then normalize the kernel as follows:

$$\hat{k}^{\cap}(x,y) = \frac{k^{\cap}(x,y)}{\sqrt{k^{\cap}(x,x)\cdot k^{\cap}(y,y)}}$$

### **Bag-of-Super-Word-Embeddings**



2	1800	1-6
3	1726	0-3
4	1726	0-3
5	1772	0-4
6	1805	0-4
7	1569	0-30
8	723	0-60
		1

Table: The number of essays and the score ranges for the 8 different prompts in the Automated Student Assessment Prize (ASAP) data set.

### **In-domain results**

Method	1	2	3	4	5	6	7	8	Overall
Human	0.721	0.814	0.769	0.851	0.753	0.776	0.721	0.629	0.754
[Phandi et al, EMNLP 2015]	0.761	0.606	0.621	0.742	0.784	0.775	0.730	0.617	0.705
[Dong et al, EMNLP 2016]	-	-	-	-	-	-	-	-	0.734
[Dong et al, CONLL 2017]	0.822	0.682	0.672	0.814	0.803	0.811	0.801	0.705	0.764
[Tay et al, AAAI 2018]	0.832	0.684	0.695	0.788	0.815	0.810	0.800	0.697	0.764
HISK and $\nu$ -SVR	0.836	0.724	0.677	0.821	0.830	0.828	0.801	0.726	0.780
BOSWE and $\nu$ -SVR	0.788	0.689	0.667	0.809	0.824	0.824	0.766	0.679	0.756
HISK+BOSWE and $\nu$ -SVR	0.845	0.729	0.684	0.829	0.833	0.830	0.804	0.729	0.785

Table: In-domain automatic essay scoring results of our approach versus several state-of-the-art methods. Results are reported in terms of the quadratic weighted kappa (QWK) measure, using 5-fold cross-validation. The best QWK score (among the machine learning

systems) for each prompt is highlighted with blue.

### **Cross-domain results**

						- 100
Source→Target		_	$n_t = 10$	$n_t = 25$	$n_t = 50$	$n_t = 100$
1→2	[Phandi et al, EMNLP 2015]	0.434	0.463	0.457	0.492	0.510
	[Dong et al, EMNLP 2016]	-	0.546	0.569	0.563	0.559
	HISK and $\nu$ -SVR	0.440	0.586	0.637	0.652	0.657
	BOSWE and $\nu$ -SVR	0.398	0.474	0.478	0.492	0.506
	HISK+BOSWE and $\nu$ -SVR	0.542	0.584	0.632	0.657	0.661
3→4	[Phandi et al, EMNLP 2015]	0.522	0.593	0.609	0.618	0.646
	[Dong et al, EMNLP 2016]	-	0.628	0.656	0.659	0.662
	HISK and $\nu$ -SVR	0.703	0.716	0.724	0.742	0.751
	BOSWE and $\nu$ -SVR	0.615	0.640	0.716	0.728	0.727
	HISK+BOSWE and $\nu$ -SVR	0.701	0.713	0.737	0.754	0.779
5→6	[Phandi et al, EMNLP 2015]	0.187	0.539	0.662	0.680	0.713
	[Dong et al, EMNLP 2016]	-	0.647	0.700	0.714	0.750
	HISK and $\nu$ -SVR	0.715	0.726	0.754	0.757	0.781
	BOSWE and $\nu$ -SVR	0.617	0.623	0.644	0.650	0.692
	HISK+BOSWE and $\nu$ -SVR	0.728	0.734	0.764	0.771	0.788
7→8	[Phandi et al, EMNLP 2015]	0.171	0.586	0.607	0.613	0.621
	[Dong et al, EMNLP 2016]	-	0.570	0.590	0.568	0.587
	HISK and $\nu$ -SVR	0.486	0.604	0.617	0.626	0.639
	BOSWE and $\nu$ -SVR	0.419	0.526	0.577	0.582	0.591
	HISK+BOSWE and $\nu$ -SVR	0.522	0.606	0.637	0.638	0.649

Figure: Each word in the collection of documents is represented as word vector using a pre-trained word embeddings model. The word vectors are then clustered in order to obtain relevant semantic clusters of words. As in the standard bag-of-visual-words model, the clustering is done by k-means. Every embedded word in the collection of documents is then assigned to the nearest cluster centroid (the nearest super word vector). Put together, the super word vectors generate a vocabulary (codebook) that can further be used to represent each document as a *bag-of-super-word-embeddings* (BOSWE). After building the representation, we employ a kernel method to train the model for our task.

Table: Corss-domain automatic essay scoring results of our approach versus two state-of-the-art methods. Results are reported in terms of the quadratic weighted kappa (QWK) measure, using the same evaluation procedure as [Phandi et al, EMNLP 2015; Dong et al, EMNLP 2016]. The best QWK scores for each source  $\rightarrow$  target domain pair are highlighted with blue.

# Conclusion

- The in-domain and the cross-domain comparative results indicate that string kernels, both alone and in combination with word embeddings, attain the best performance on the automatic essay scoring task
- Our shallow approach attains better results than recent deep learning methods [Dong et al, EMNLP 2016; Dong et al, CONLL 2017; Tay et al, AAAI 2018]

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