Element-wise Bilinear Interaction for Sentence Matching

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Abstract

When we build a neural network model predicting the relationship between two sentences, the most general and intuitive approach is to use a Siamese architecture, where the sentence vectors obtained from a shared encoder is given as input to a classifier. For the classifier to work effectively, it is important to extract appropriate features from the two vectors and feed them as input. There exist several previous works that suggest heuristicbased function for matching sentence vectors, however it cannot be said that the heuristics tailored for a specific task generalize to In this work, we propose a other tasks. new matching function, ElBiS, that learns to model element-wise interaction between two vectors. From experiments, we empirically demonstrate that the proposed ElBiS matching function outperforms the concatenation-based or heuristic-based matching functions on natural language inference and paraphrase identification, while maintaining the fused representation compact.

1 Introduction

Identifying the relationship between two sentences is a key component for various natural language processing tasks such as paraphrase identification, semantic relatedness prediction, textual entailment recognition, etc. The most general and intuitive approach to these problems would be to encode each sentence using a sentence encoder network and feed the encoded vectors to a classifier network.¹

For a model to predict the relationship correctly, it is important for the input to the classifier to contain appropriate information. The most naïve method is to concatenate the two vectors and delegate the role of extracting features to subsequent network components. However, despite the theoretical fact that even a single-hidden layer feedforward network can approximate any arbitrary function (Cybenko, 1989; Hornik, 1991), the space of network parameters is too large, and it is helpful to narrow down the search space by directly giving information about interaction to the classifier model, as empirically proven in previous works built for various tasks (Ji and Eisenstein, 2013; Mou et al., 2016; Xiong et al., 2016, to name but a few).

In this paper, we propose a matching function which learns from data to fuse two sentence vectors and extract useful features. Unlike bilinear pooling methods designed for matching vectors from heterogeneous domain (e.g. image and text), our proposed method utilizes element-wise bilinear interaction between vectors rather than interdimensional interaction. In §3, we will describe the intuition and assumption behind the restriction of interaction.

This paper is organized as follows. In $\S2$, we briefly introduce previous work related to our objective. The detailed explanation of the proposed model is given in $\S3$, and we show its effectiveness in extracting compact yet powerful features in $\S4$. $\S5$ concludes the paper.

2 Related Work

As stated above, matching sentences is a common component in various tasks in natural language processing. Ji and Eisenstein (2013) empirically prove that the use of element-wise multiplication and absolute difference as matching function substantially improve performance on paraphrase identification, and Tai et al. (2015) apply the same matching scheme to the semantic related-

¹ The encoded vectors can also be fed into a regression network, however in this work we focus only on classification.

ness prediction task. Mou et al. (2016) show that using the element-wise multiplication and difference along with the concatenation of sentence vectors yields good performance in natural language inference, despite redundant components such as concatenation and element-wise difference. Yogatama et al. (2017) and Chen et al. (2017) use modified versions of the heuristics proposed by Mou et al. (2016) in natural language inference.

However, to the best of our knowledge, there exists little work on a method that adaptively learns to extract features from two sentence vectors encoded by a shared encoder. Though not directly related to our work's focus, there exist approaches to fuse vectors from a homogeneous space using exact or approximate bilinear form (Socher et al., 2013; Lin et al., 2015; Wu et al., 2016; Krause et al., 2016).

There have been several works for extracting features from two heterogeneous vectors. Wu et al. (2013) use a bilinear model to match queries and documents from different domains. Also, approximate bilinear matching techniques such as multimodal compact bilinear pooling (MCB; Fukui et al., 2016), low-rank bilinear pooling (MLB; Kim et al., 2017), and factorized bilinear pooling (MFB; Yu et al., 2017) are successfully applied in visual question answering (VQA) tasks, outperforming heuristic feature functions (Xiong et al., 2016; Agrawal et al., 2017).

MCB approximate the full bilinear matching using Count Sketch (Charikar et al., 2002) algorithm, MLB and MFB decompose a third-order tensor into multiple weight matrices, and MUTAN (Ben-younes et al., 2017) use Tucker decomposition to parameterize bilinear interactions. Although these bilinear pooling methods give significant performance improvement in the context of VQA, we found that they do not help matching sentences encoded by a shared encoder.

3 Proposed Method: ElBiS

As pointed out by previous works on sentence matching (Ji and Eisenstein, 2013; Mou et al., 2016), heuristic matching functions bring substantial gain in performance over the simple concatenation of sentence vectors. However, we believe that there could be other important interaction that simple heuristics miss, and the optimal heuristic could differ from task to task. In this section, we propose a general matching function that learns to extract compact and effective features from data.

Let $\mathbf{a} = (a_1, \dots, a_d) \in \mathbb{R}^d$ and $\mathbf{b} = (b_1, \dots, b_d) \in \mathbb{R}^d$ be sentence vectors obtained from a encoder network.² And let us define $\mathbf{G} \in \mathbb{R}^{d \times 3}$ as a matrix constructed by stacking three vectors $\mathbf{a}, \mathbf{b}, \vec{\mathbf{1}} \in \mathbb{R}^d$ where $\vec{\mathbf{1}}$ is the vector of all ones, and denote the *i*-th row of \mathbf{G} by \mathbf{g}_i .

Then the result of applying our proposed matching function, $\mathbf{r} = (r_1, \cdots, r_d) \in \mathbb{R}^d$, is defined by

$$r_i = \phi\left(\mathbf{g}_i^\top \mathbf{W}_i \mathbf{g}_i\right),\tag{1}$$

where $\mathbf{W}_i \in \mathbb{R}^{3\times 3}, i \in \{1, \dots, d\}$ is a matrix of trainable parameters and $\phi(\cdot)$ an activation function (tanh in our experiments).

Due to its use of bilinear form, it can model every quadratic relation between a_i and b_i , i.e. can represent every linear combination of $\{a_i^2, b_i^2, a_i b_i, a_i, b_i, 1\}$. This means that the proposed method is able to express frequently used element-wise heuristics such as element-wise sum, multiplication, subtraction, etc., in addition to other possible relations.³

Further, to consider multiple types of elementwise interaction, we use a set of M weight matrices per dimension. That is, for each \mathbf{g}_i , we get M scalar outputs (r_i^1, \dots, r_i^M) by applying Eq. 1 using a set of separate weight matrices $(\mathbf{W}_i^1, \dots, \mathbf{W}_i^M)$:

$$r_i^m = \phi\left(\mathbf{g}_i^\top \mathbf{W}_i^m \mathbf{g}_i\right). \tag{2}$$

Implementation-wise, we vertically stack G for M times to construct $\tilde{\mathbf{G}} \in \mathbb{R}^{Md \times 3}$, and use each row $\tilde{\mathbf{g}}_i$ as input to Eq. 1. As a result, the resulting output \mathbf{r} becomes a Md-dimensional vector:

$$r_i = \phi\left(\tilde{\mathbf{g}}_i^\top \mathbf{W}_i \tilde{\mathbf{g}}_i\right),\tag{3}$$

where $\mathbf{W}_i \in \mathbb{R}^{3\times 3}, i \in \{1, \dots, Md\}$. Eq. 1 is the special case of Eq. 2 and 3 where M = 1. We call our proposed element-wise bilinear matching function *ElBiS* (Element-wise Bilinear Sentence Matching).

Note that our element-wise matching requires only $M \times 3 \times 3 \times d$ parameters, the number of

² Throughout this paper, we assume a *d*-dimensional vector is equivalent to the corresponding $d \times 1$ matrix.

³ Though a bilinear form cannot represent the absolute difference between inputs, note that $(a_i - b_i)^2 = a_i^2 - 2a_ib_i + b_i^2$ can alternatively represent commutative difference. Yogatama et al. (2017) use this quadratic form instead of the absolute difference.

which is substantially less than that of full bilinear matching, Md^3 . For example, in the case of d = 300 and Md = 1200 (the frequently used set of hyperparameters in NLI), the full bilinear matching needs 108 million parameters, while the element-wise matching needs only 10,800 parameters.

Why element-wise? In the scenario we are focusing on, sentence vectors are computed from a Siamese network, and thus it can be said that the vectors are in the same semantic space. Therefore, the effect of considering interdimensional interaction is less significant than that of multimodal pooling (e.g. matching a text and a image vector), so we decided to model more powerful interaction within the same dimension instead. We also would like to remark that our preliminary experiments, where MFB (Yu et al., 2017) or MLB (Kim et al., 2017) was adopted as matching function, were not successful.

4 Experiments

We evalute our proposed ElBiS model on the natural language inference and paraphrase identification task. Implementation for experiments will be made public.

4.1 Natural Language Inference

Natural language inference (NLI), also called recognizing textual entailment (RTE), is a task whose objective is to predict the relationship between a premise and a hypothesis sentence. We conduct experiments using Stanford Natural Language Inference Corpus (SNLI; Bowman et al., 2015), one of the most famous dataset for the NLI task. The SNLI dataset consists of roughly 570k premisehypothesis pairs, each of which is annotated with a label (entailment, contradiction, or neutral).

For sentence encoder, we choose the encoder based on long short-term memory (LSTM; Hochreiter and Schmidhuber, 1997) architecture as baseline model, which is similar to that of Bowman et al. (2015) and Bowman et al. (2016). It consists of a single layer unidirectional LSTM network that reads a sentence from left to right, and the last hidden state is used as the sentence vector. We also conduct experiments using a more elaborated encoder model, Gumbel Tree-LSTM (Choi et al., 2018). As a classifier network, we use an MLP with a single hidden layer. In experiments

Matching Fn.	# Params.	Acc. (%)
Concat	1.34M	81.6
Heuristic	1.96M	83.9
ElBiS $(M = 1)$	1.04M	84.4
ElBiS $(M = 2)$	1.35M	84.5
ElBiS $(M = 3)$	1.66M	85.0
ElBiS ($M = 4$)	1.97M	84.6

Table 1: Results on the SNLI task using LSTM-based sentence encoders.

Matching Fn.	# Params.	Acc. (%)
Concat	2.25M	82.4
Heuristic	2.86M	84.6
ElBiS $(M = 1)$	1.94M	84.8
ElBiS ($M = 2$)	2.25M	85.6
ElBiS ($M = 3$)	2.56M	85.9
ElBiS ($M = 4$)	2.87M	85.6

Table 2: Results on the SNLI task using Gumbel Tree-LSTM-based sentence encoders.

with heuristic matching we use the heuristic features proposed by Mou et al. (2016) and adopted in many works on the NLI task: $[a; b; a-b; a \odot b]$, where a and b are encoded sentence vectors. For more detailed experimental settings, we refer readers to §A.1.

Table 1 and 2 contain results on the SNLI task. We can see that models that adopt the proposed ElBiS matching function extract powerful features leading to a performance gain, while keeping similar or less number of parameters. Also, though not directly related to our main contribution, we found that, with elaborated initialization and regularization, simple LSTM models (even the one with the heuristic matching function) achieve competitive performance with those of state-of-the-art models.⁴

4.2 Paraphrase Identification

Another popular task on identifying relationship between a sentence pair is paraphrase identification (PI). The objective of the PI task is to predict whether a given sentence pair has the same meaning or not. To correctly identify the paraphrase relationship, an input to a classifier should contain the semantic similarity and difference between sentences.

For evaluation of paraphrase identification, we

⁴https://nlp.stanford.edu/projects/ snli

Matching Fn.	# Params.	Acc. (%)
Concat	1.34M	85.0
Heuristic	1.34M	87.0
ElBiS $(M = 1)$	1.04M	86.7
ElBiS ($M = 2$)	1.35M	87.3
ElBiS ($M = 3$)	1.66M	87.1

Table 3: Results on the PI task using LSTM-based sentence encoders.

use Quora Question Pairs dataset⁵. The dataset contains 400k question pairs, each of which is annotated with a label indicating whether the questions of the pair have the same meaning. To our knowledge, the Quora dataset is the largest available dataset of paraphrase identification. We used the same training, development, test splits as the ones used in Wang et al. (2017).

For experiments with heuristic matching, we used the function proposed by Ji and Eisenstein (2013), which is shown by the authors to be effective in matching vectors in latent space compared to simple concatenation. It is composed of the element-wise product and absolute difference between two vectors: $[\mathbf{a} \odot \mathbf{b}; |\mathbf{a} - \mathbf{b}|]$, where \mathbf{a} and \mathbf{b} are encoded sentence vectors.

Similar to NLI experiments, we use a single layer unidirectional LSTM network as sentence encoder, and we state detailed settings in §A.2. The results on the PI task is listed in Table 3. Again we can see that the models armed with the ElBiS matching function discover parsimonious and effective interaction between vectors.

5 Conclusion and Discussion

In this work, we propose ElBiS, a general method of fusing information from two sentence vectors. Our method does not rely on heuristic knowledge constructed for a specific task, and adaptively learns from data the element-wise connections between vectors from data. From experiments, we demonstrated that the proposed method outperforms or matches the performance of commonly used concatenation-based or heuristic-based feature functions, while maintaining the fused representation compact.

Although the main focus of this work is about sentence matching, the notion of element-wise bilinear interaction could be applied beyond sentence matching. For example, many models that specialize in NLI have components where the heuristic matching function is used, e.g. in computing intra-sentence or inter-sentence attention weights. It could be interesting future work to replace these components with our proposed matching function.

One of the main drawback of our proposed method is that, due to its improved expressiveness, it makes a model overfit easily. When evaluated on small datasets such as Sentences Involving Compositional Knowledge dataset (SICK; Marelli et al., 2014) and Microsoft Research Paraphrase Corpus (MSRP; Dolan and Brockett, 2005), we observed performance degradation, partly due to overfitting. Similarly, we observed that increasing the number of interaction types M does not guarantee consistent performance gain. We conjecture that these could be alleviated by applying regularization techniques that control the sparsity of interaction, but we leave it as future work.

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⁵https://data.quora.com/

First-Quora-Dataset-Release-Question-Pairs

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A Experimental Settings

A.1 Natural Language Inference

For all experiments, we used the Adam (Kingma and Ba, 2015) optimizer with a learning rate 0.001 and halved the learning rate when there is no improvement in accuracy for one epoch. Each model is trained for 10 epochs, and the checkpoint with the highest validation accuracy is chosen as final model. Sentences longer than 25 words are trimmed to have the maximum length of 25 words, and batch size of 64 is used for training.

For all experiments, we set the dimensionality of sentence vectors to 300. 300-dimensional GloVe (Pennington et al., 2014) vectors trained on 840 billion tokens⁶ were used as word embeddings and not updated during training. The number of hidden units of the single-hidden layer MLP is set to 1024.

Dropout (Srivastava et al., 2014) is applied to word embeddings and the input and the output of the MLP. The dropout probability is selected from $\{0.10, 0.15, 0.20\}$. Batch normalization (Ioffe and Szegedy, 2015) is applied to the input and the output of the MLP.

Recurrent weight matrices are orthogonally initialized (Saxe et al., 2014), and the final linear projection matrix is initialized by sampling from Uniform(-0.005, 0.005). All other weights are initialized following the scheme of He et al. (2015).

A.2 Paraphrase Identification

For PI experiments, we used the same architecture and training procedures as NLI experiments, except the final projection matrix and heuristic matching function. Also, we found that the PI task is more sensitive to hyperparameters than NLI, so we apply different dropout probabilities to the encoder network and to the classifier network. Both values are selected from $\{0.10, 0.15, 0.20\}$. Each model is trained for 15 epochs, and the checkpoint with the highest validation accuracy is chosen as final model.

⁶http://nlp.stanford.edu/data/glove. 840B.300d.zip